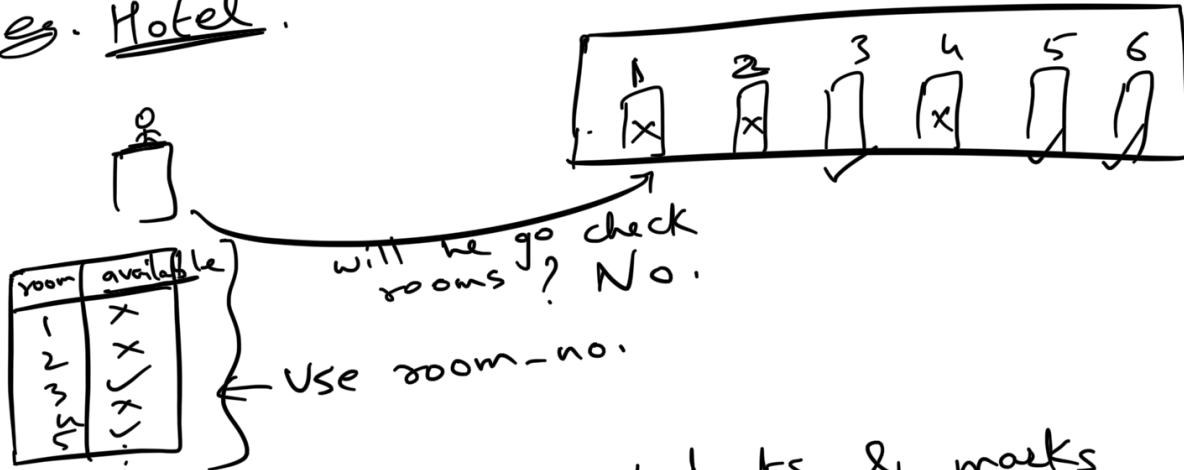


Introduction to Hashing

eg. Hotel.



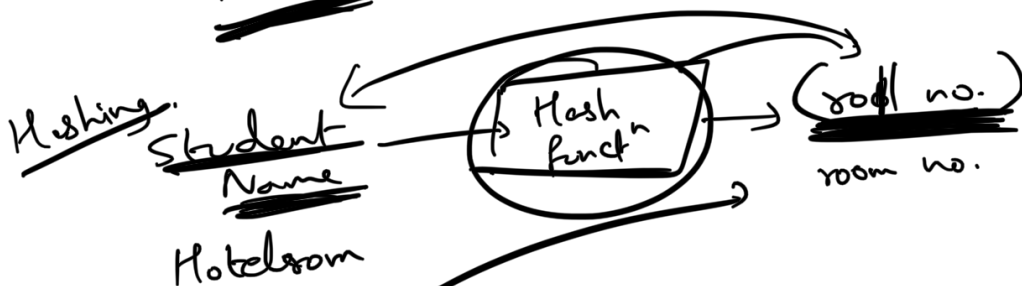
School → 200 students & marks

storing names & finding names is too

Roll-no. → sorted order

Map → String (Name) → int (Roll no.)

Hashing!



HashMap (Key, value)

Key → room-no

value → marks, available?

linear a num in

eg Q. Find how many range [1, 500] occurred before.

→ 1, 19, 2, 5, 19, 2, 19, 8 etc. ↓
 → 0, 0, 0, 0, 1, 1, 2, 0

Count[500]

Count[i] → how many i has occurred

Count[i]++

int a[500]

a[i]++
 a[19]++
 a[2]++ a[5]++ a[19]++

Now, nos → [1, 100] → 10 numbers.
 memory → [10]

a[]
 0
 1
 2
 3
 4
 5
 6
 7
 8
 9

58, 31, 27, 50, 9, 27

HF → n % 10

58 % 10 → 8
 31 % 10 → 1
 27 → 7
 50 → 0
 9 → 9
 2 % 10 → 2

38 → 8
 28 → 8
 58 → 8

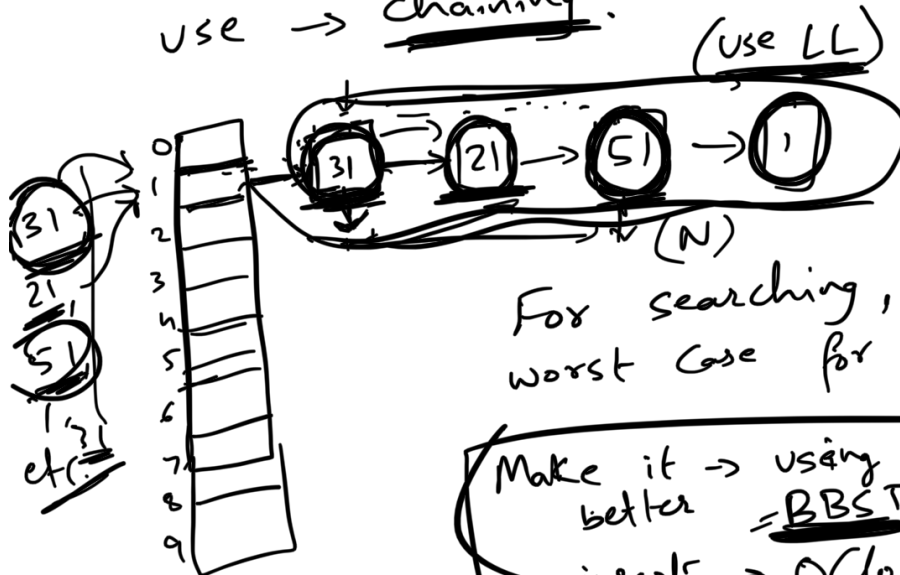
7
 27
 97

depends on

K Collision! \rightarrow separate hash fⁿ & memory.

$\frac{n \% K}{m \% K}$

To avoid collision,
use \rightarrow chaining.

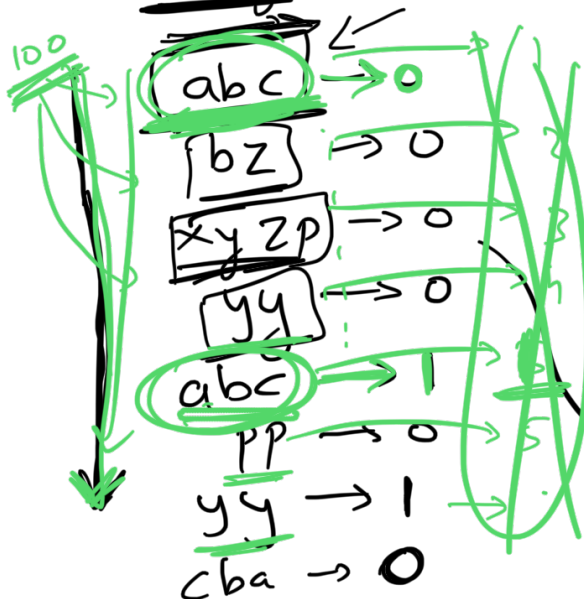


- separate d
- Linear pro
etc.

For searching,
worst case for N elem $\rightarrow O(N)$

Make it \rightarrow using
better BST etc.
insert $\rightarrow O(\log N)$
searching $\rightarrow O(\log N)$

egQ. Given random strings, for every
string check if it has already occurred or not



Right now, array is the only
knowledge we have

$f(\text{string}) \rightarrow \text{int } [0 \rightarrow 1]$
 $a[10^6]$

① hash functions

① Add ascii values of string.

$$\left(\sum_{i=0}^m s[i] \right) \% 10^6 \text{ collision} \rightarrow \text{abc}$$

lots of collisions

$$\text{Z} \rightarrow 26$$

$$\text{ay} \rightarrow 1+25 \rightarrow 26$$

$$\text{cba} \rightarrow 3+2+1$$

$$\text{cab} \rightarrow 3+1+2$$

$$\text{abc} \rightarrow 6$$

$$\text{abc} \Rightarrow 6$$

$$\text{ba} \rightarrow 3$$

$$\text{ba} \Rightarrow 3$$

$$\text{bac} \rightarrow 2+1+3=6$$



$\rightarrow \text{abc}$
 $\rightarrow \text{bac}$
 $\rightarrow \text{cab}$
 $\rightarrow \text{cba}$

anagrams

aacd
 daaca

an

②

$$\text{abc} \rightarrow (a \times 1 + b \times 10 + c \times 100 \text{ etc.}) \% 10^6$$

$$\text{bac} \rightarrow (b \times 1 + a \times 10 + c \times 100 \text{ etc.})$$

multiply by power of 10 index.

$$\text{abc x y p q a z n}$$

\downarrow
 10^1

\downarrow
 10^6

$$a \times 1 + b \times 2 + c \times 3$$

and hash f^n , $\rightarrow (a \times p^n) + (b \times p^n)$

For govt research says → use prime no. to ensure uniform distributⁿ & less collision

$$+ (C \times p^L) \text{ etc.}$$

Rabin-Karp algorithm

a → 1
b → 2
c → 3

abc → $(1 \times 7 + 2 \times 7^2 + 3 \times 7^3) \% 10$

cba → $(3 \times 7 + 2 \times 7^2 + 1 \times 7^3) \% 10$

di

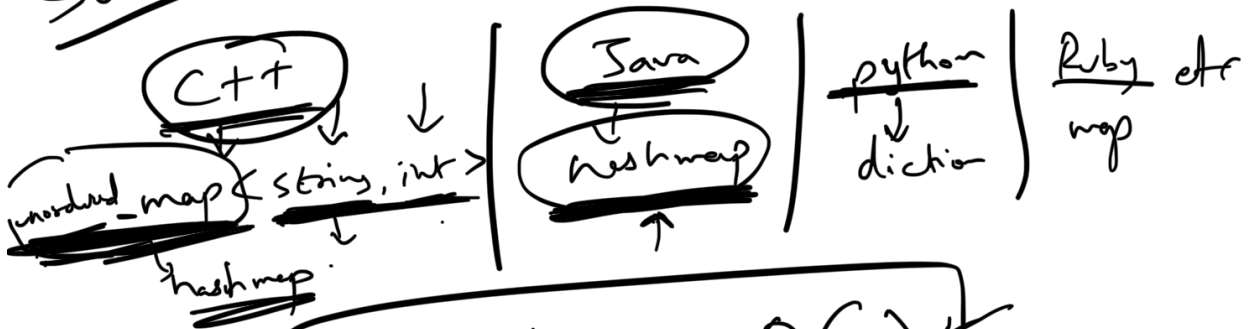
Another encryption, md5 hash

Requirement

pass

hashcode

Summary



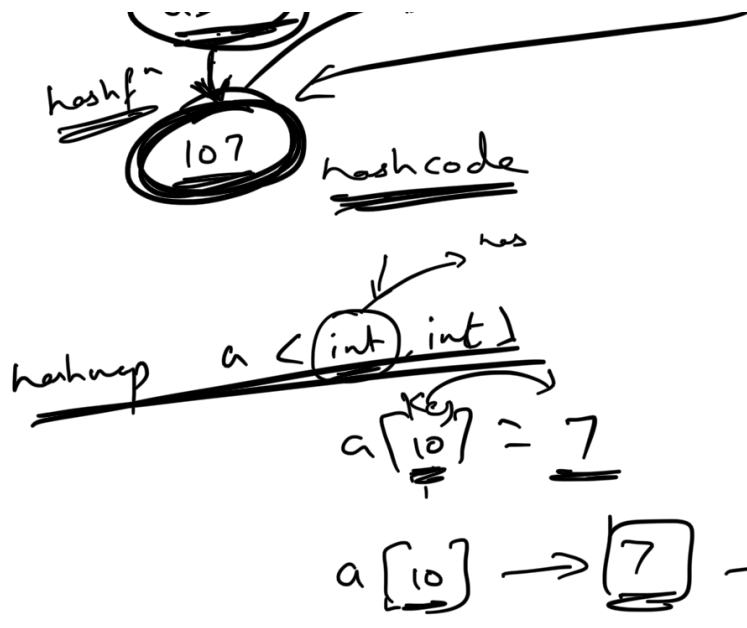
For good hash fⁿ

average-time → O(1)

map < string, int >

abc → 5

a[abc] = 5



Q.1 Given array, find freq. of every

a = (2, 7, 5, 2, 3, 5, 7, 2) ← N

use

hashmap < (a[i], freq)

un. map < int, int >

2 → 3

7 → 2

3 → 1

5 → 2

[2, 2, 2, 2, 2]

2 → 5

T.C ⇒ O(N)

S.C ⇒ O(N)

for (i = 0; i < n; i++)

{

if (HM.contains a[i]) → O(1)

HM[a[i]]++ → O(1)

else

HM[a[i]] = 1 → O(1)

add freq

for (Array)

print a[i] → HM[a[i]]

print freq

[1, 2, 7, 5, 13, 100, 200, 201, ... N]

$HM[] \rightarrow \text{freq.}$

$Has[] \rightarrow \text{value}$

Q.2 Given array, return 1st non-repeating element.

$a = [20, 1, 2, 10, 20, 1, 3, 2]$

any

insert into HM.
for(-freq.)

check 1st for($i=0; i < n$)
check HM $\rightarrow 1$
return $a[i]$.

20	2
1	2
2	2
10	1
3	1

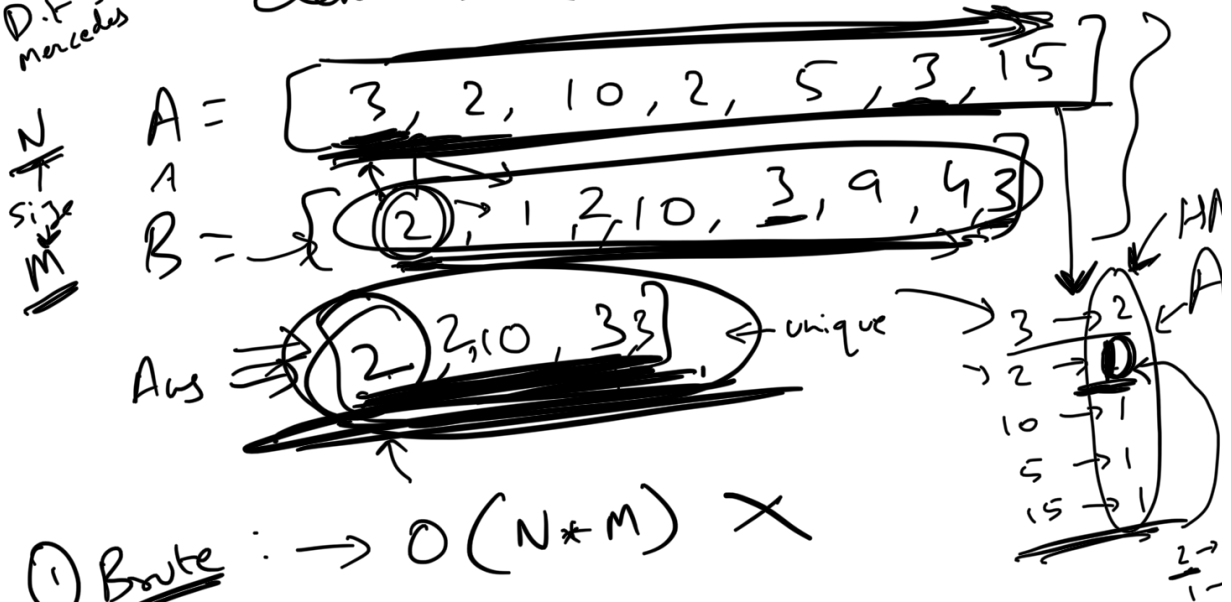
insert {
for($i=0; i < n; i++$)
{
HM[$a[i]$]++;
}
}
 $\Rightarrow O(N)$

check {
for($i=0; i < n; i++$)
{
if (HM[$a[i]$] == 1)
{
return $a[i]$;
}
}
}
 $\Rightarrow O(N)$

$\therefore C \Rightarrow O(N)$
 $S.C \Rightarrow O(N)$

Q.3
D.F Shaw
mercedes

Given 2 arrays, find the common elements (intersection)



① Brute : $\rightarrow O(N * M)$ X

② Use $\left(\begin{array}{l} \text{sort A} \\ + \\ \text{Binary Search} \\ \text{for B in A} \end{array} \right) \Rightarrow O(N \log N)$
 $\Rightarrow O(M \log N)$
 $\Rightarrow O((N+M) \log N)$

③ Use hashmap for A.

Search elements from 2nd array in HM

$\Rightarrow O(N+M)$

$\Rightarrow O(N)$

S.C $\Rightarrow O(N)$

Q.4 Given an array, check if there

FB etc. exist a pair $a[i]$ & $a[j]$ & $i \neq j$
 such that $a[i] + a[j] = k$. (k is g)

eg $a = [7, 4, 10, 2, 5, 16, 3]$ & $k = 9$
 $7 + 2 = 9$
 $4, 5$
 return True

True $\leftarrow [5, 7, 9, 5, 8] \leftarrow k = 10$
False $\leftarrow [5, 7, 9, 4, 8] \leftarrow k = 10$
 $k - 5 \Rightarrow 5$

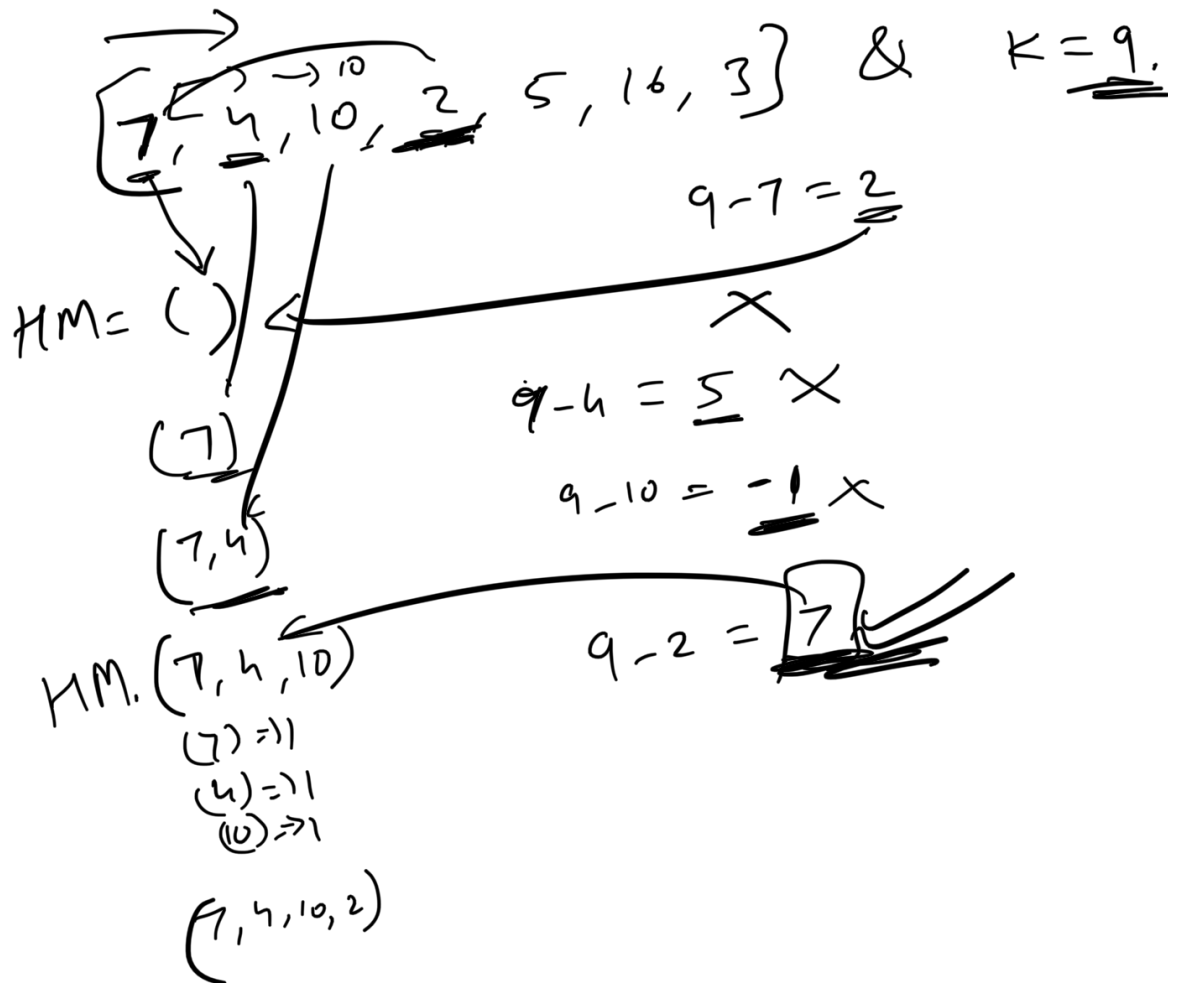
① Brute \rightarrow 2 loop
 $i = 0 \rightarrow N-1$
 $j = i+1 \rightarrow N$
 $T.C \Rightarrow O(N^2)$
 $S.C \Rightarrow O(1)$

② Sort & use B.S. $\Rightarrow O(N \log N)$ X

③ $a[i]$ \leftarrow $a[j] = k - a[i]$
 \underline{k}
 $a[i] + a[i] = k$

mark k in $a[i]$ & $k - a[i]$

Use H.M, to ~~check~~
is present
& then add $a[j]$



False $\leftarrow \{5, 4, 9, 7, 8\}$ $K = \underline{10}$.

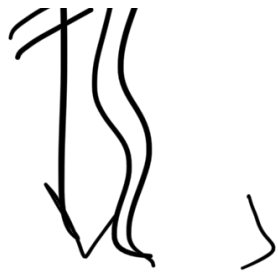
True $\leftarrow \{5, 4, 9, 5, 7, 8\}$ $K = 10$

$10 - 5 = \underline{5}$

```

for (i = 0; i < n; i++)
{
    if (HM contains  $K - a[i]$ )
        return true
}

```



else HM[a[i]]++;

T.C \Rightarrow $O(N)$

S.C \Rightarrow $O(N)$

Q.5 Find if pair $A[i] \wedge A[j] \in K$
exists. $i \neq j$

$[3, 1, 5, 9]$

$K = 2$

$3 \wedge 1 = 2 \rightarrow$ True

a	b	\wedge
1	1	0
1	0	1
0	1	1
0	0	0

$A[i]$

$A[j] = ? \Rightarrow K \wedge A[i]$

$(3) \quad 1 \wedge 2 = 3$



$3 \wedge 3 \Rightarrow 0$



$00 \rightarrow 0$ HM()

10
11
N

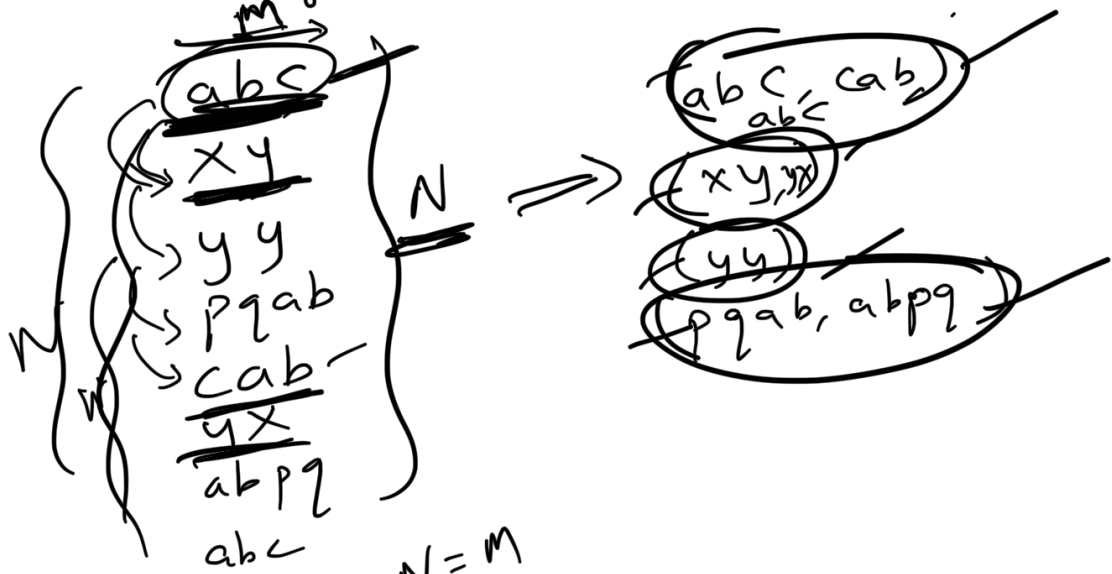
$O(N)$

$5 \rightarrow 10$
 $3 \rightarrow 01$
 $5 \wedge 3 = 6$ 11

H.W.
m b. Given N strings, group all the

Q.

anagrams together.



$$\underline{\underline{N = M}}$$

$$\underline{\underline{N * M}}$$

$$N = \underline{\underline{10^5}}$$

$$\text{length} \rightarrow \underline{\underline{10^5}}$$

hashCode()

$$\underline{\underline{10^{10}}}$$