

# Capstone Exercise

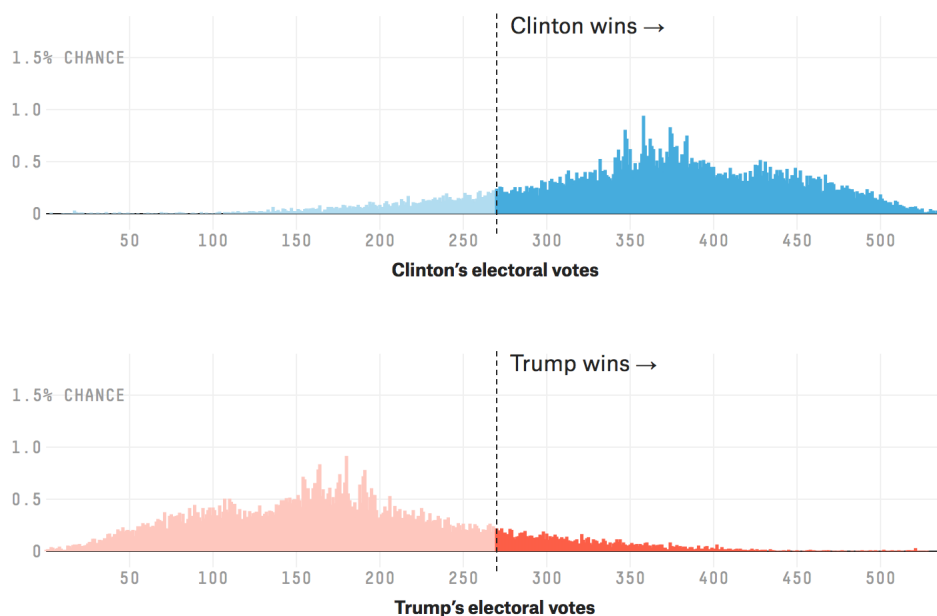
August 9, 2016

## Motivation

Nate Silver, who used Bayesian models to accurately predict Barack Obama's 2008 election is at it again in 2016 ([official methods link](#))! His model results in the below estimates, which, by this point, should look pretty familiar.

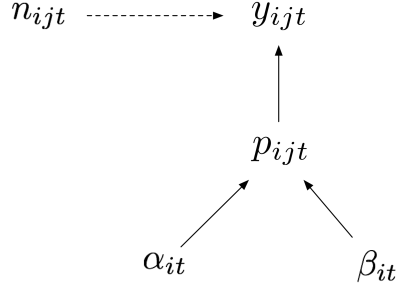
### What to expect from the Electoral College

In each of our simulations, we forecast the states and note the number of electoral votes each candidate wins. That gives us a distribution for each candidate, where the tallest bar is the outcome that occurred most frequently.



## Problem

1. Write out the DAG and joint distribution for this problem.



where  $y$  is the number of votes for Hillary Clinton, in the  $j^{th}$  poll, in week  $t$ , in the  $i^{th}$  state.

$$[\boldsymbol{\alpha}, \boldsymbol{\beta}, \mathbf{p} \mid \mathbf{y}] \propto \prod_{i=1}^{51} \prod_{j=1}^{N_j} \prod_{t=1}^T [y_{ijt} \mid p_{ijt}] [p_{ijt} \mid \alpha_{it}, \beta_{it}] [\alpha_{it}] [\beta_{it}]$$

2. How would you decide who wins each state? Who wins the national vote? Remember candidates must accumulate 270 of 538 state-level electoral votes to win the election.

$$\phi_{it} = \frac{\alpha_{it}}{\alpha_{it} + \beta_{it}}$$

$$V_{it} = \text{binomial}(N_{it}, \phi_{it})$$

where  $N_{it}$  is the number of likely voters in the  $i^{th}$  state and the  $t^{th}$  week.

$$\text{if } V_{it} > \frac{N_{it}}{2} \text{ then } Z_{it} = 1 \text{ else } Z_{it} = 0$$

$$E_t = Z_{it} \times \text{the number of electoral votes} = \sum_{i=1}^{51} E_{it}$$

$$H = 1 \text{ if } E_{it} \geq 270, \text{ then Clinton wins.}$$

$$H = 0 \text{ if } E_{it} < 270, \text{ then Trump wins.}$$

3. As the election season progresses, there is more and more information to use to inform priors. Think about how might you incorporate a weight,  $w$ , for each of the priors. We will discuss this as a group.

$$\alpha_{it} = \sum_{j=1}^J w_{ij} a_{ijt-1}$$

$$\beta_{it} = \sum_{j=1}^J w_{ij} b_{ijt-1}$$