



**GRADIENT**  
KOŁO NAUKOWE



# **Warsztaty Sztucznej Inteligencji**

**Środa 18:00 EA AUD 2**

**10.11.2021** - Wprowadzenie do uczenia maszynowego 1

**24.11.2021** - Wprowadzenie do uczenia maszynowego 2

**01.12.2021** - Wprowadzenie do uczenia głębokiego

**08.12.2021** - Wizja komputerowa

**15.12.2021** - Sieci rekurencyjne i ich zastosowania

**05.01.2021** - Uczenie ze wzmacnieniem

**12.01.2021** - Implementacja uczenia maszynowego

**19.01.2021** - Modele ML w środowisku produkcyjnym

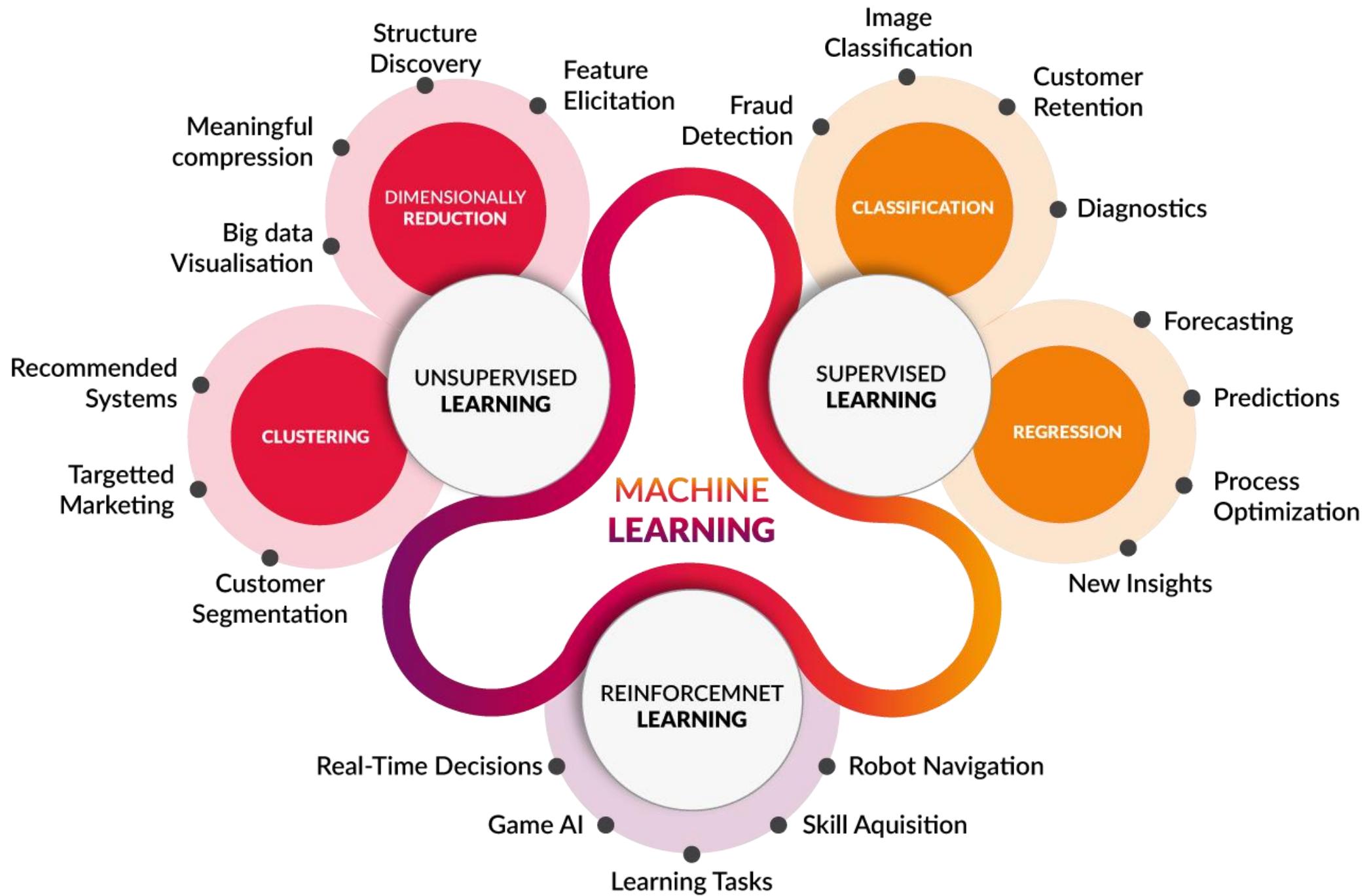
**Sukces jest progresywną realizacją  
wartościowej idei w ramach  
cierpliwego wymiaru czasu**



# Agenda

- 1 **Rodzaje uczenia maszynowego (5min)**
- 2 **Zastosowanie regresji wielorakiej (10min)**
- 3 **Budowa drzewa klasyfikującego (20 min)**
- 4 **Pytania rekrutacyjne + QUIZ (15min)**





# MACHINE LEARNING

## REINFORCEMENT LEARNING

Real-Time Decisions

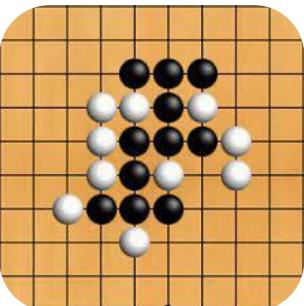
Game AI

Robot Navigation

Skill Aquisition

Learning Tasks

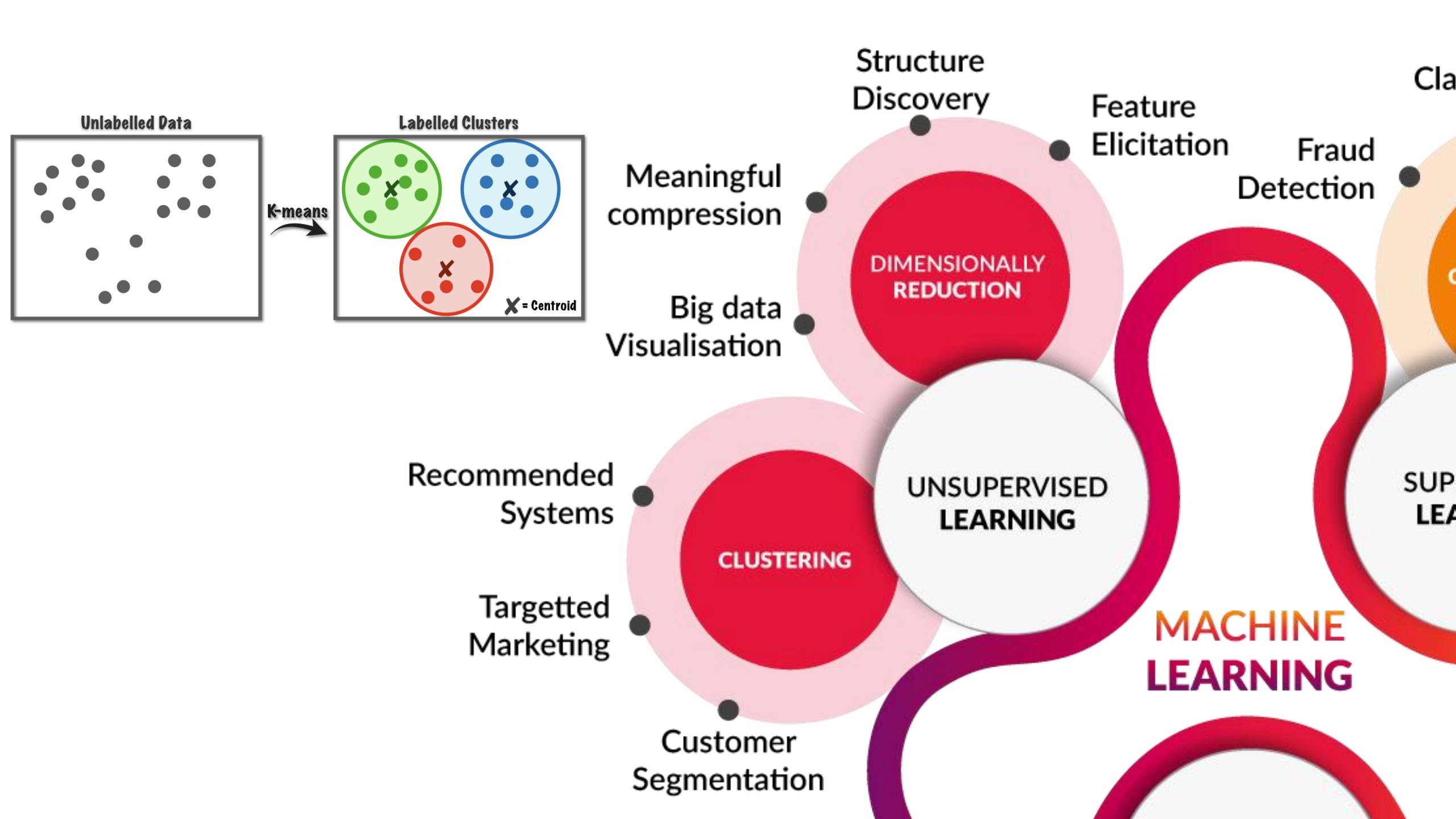
FlappyBird



Customer Segmentation

New Insights

Process Optimization



Feature  
Elicitation

Fraud  
Detection

Image  
Classification

CLASSIFICATION

SUPERVISED  
LEARNING

REGRESSION

New Insights

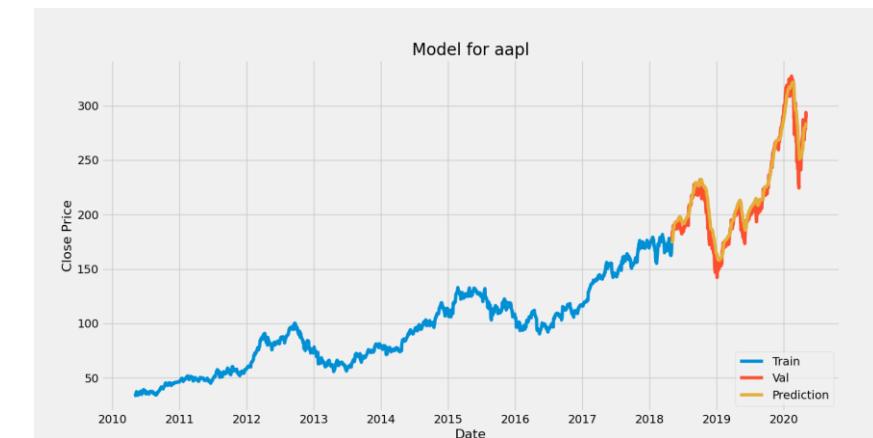
Customer  
Retention

Diagnostics

Forecasting

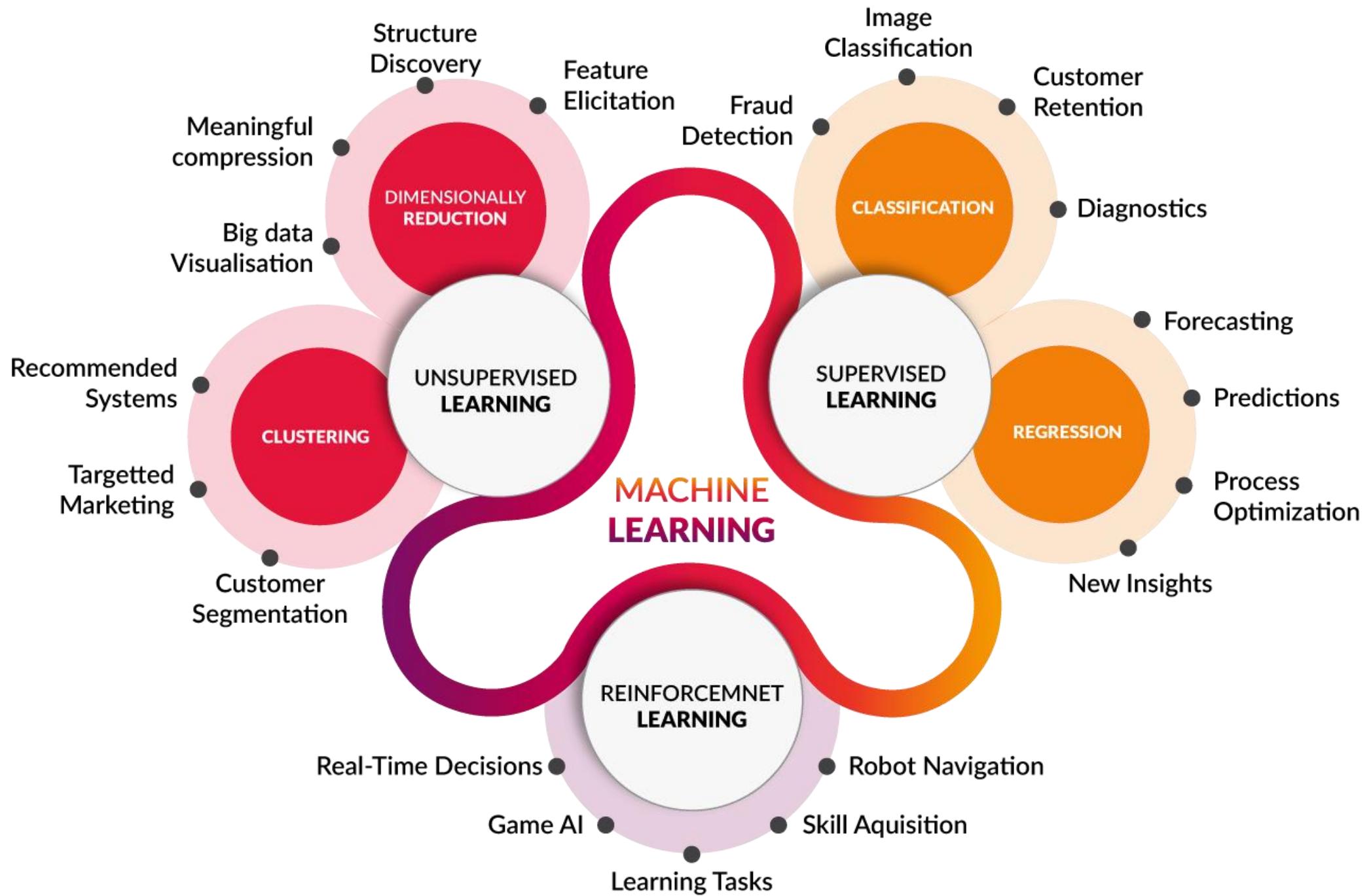
Predictions

Process  
Optimization



MACHINE  
LEARNING

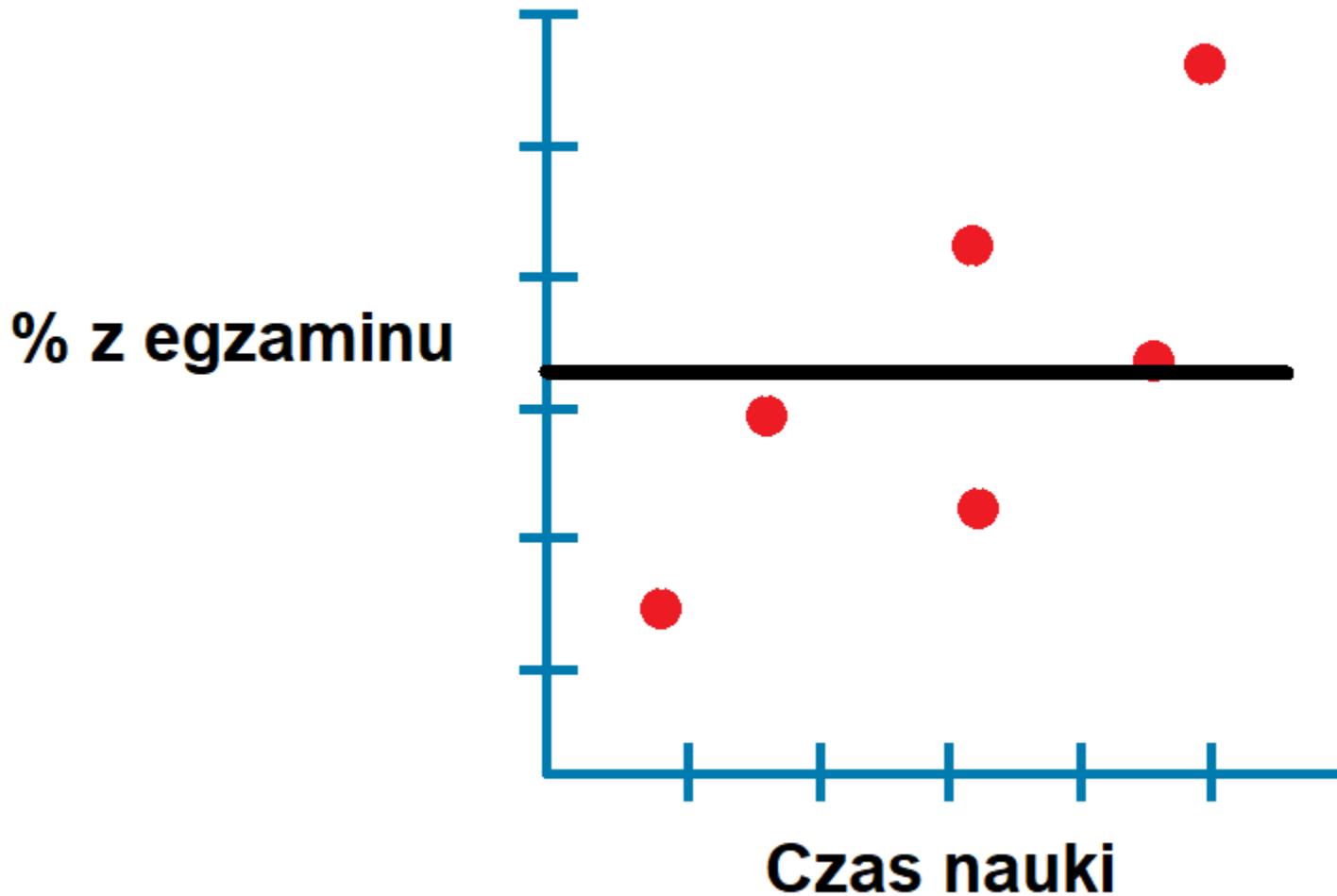
kNN



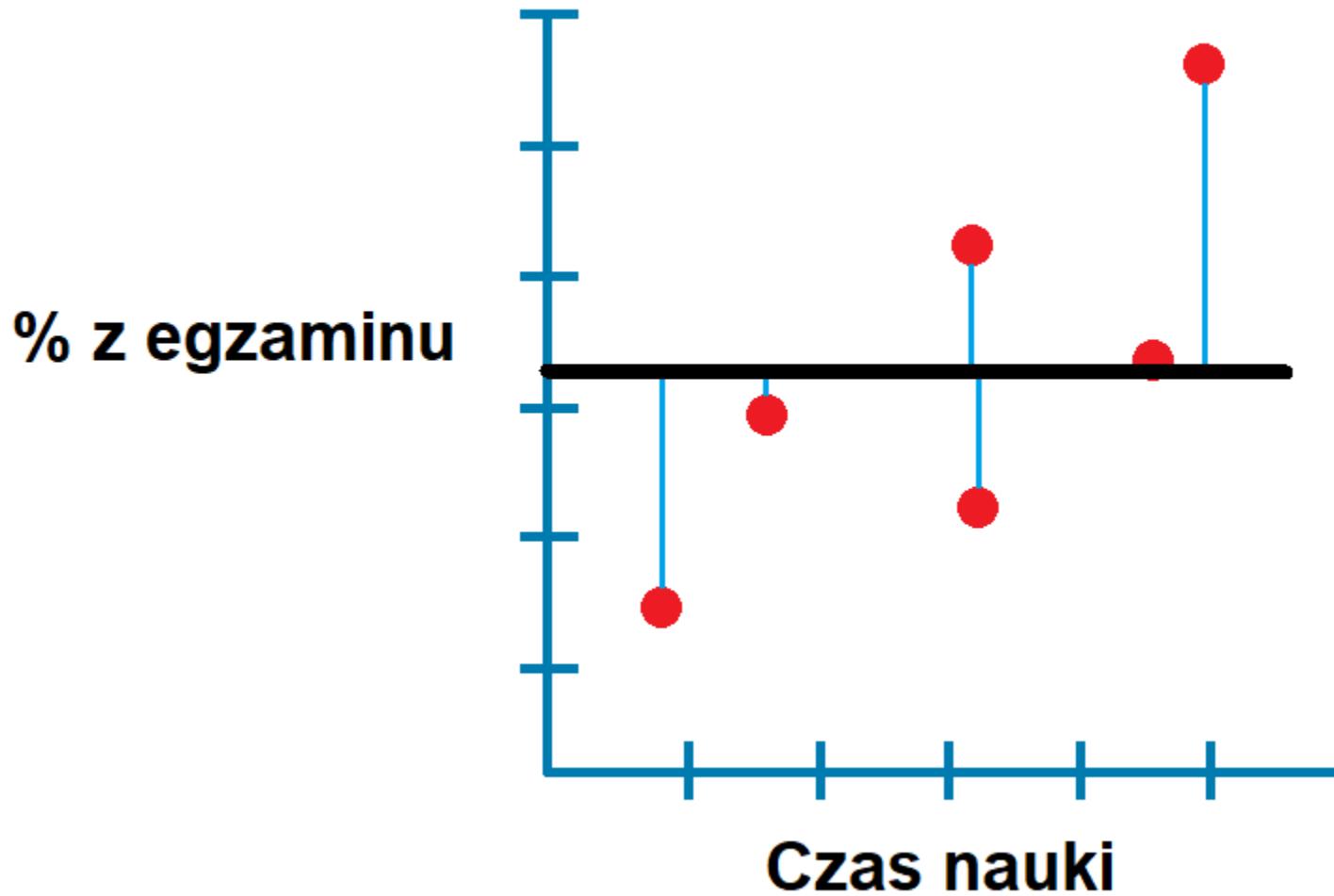
# Z poprzedniego wykładu

- Hipoteza
- Funkcja kosztu
- Gradient

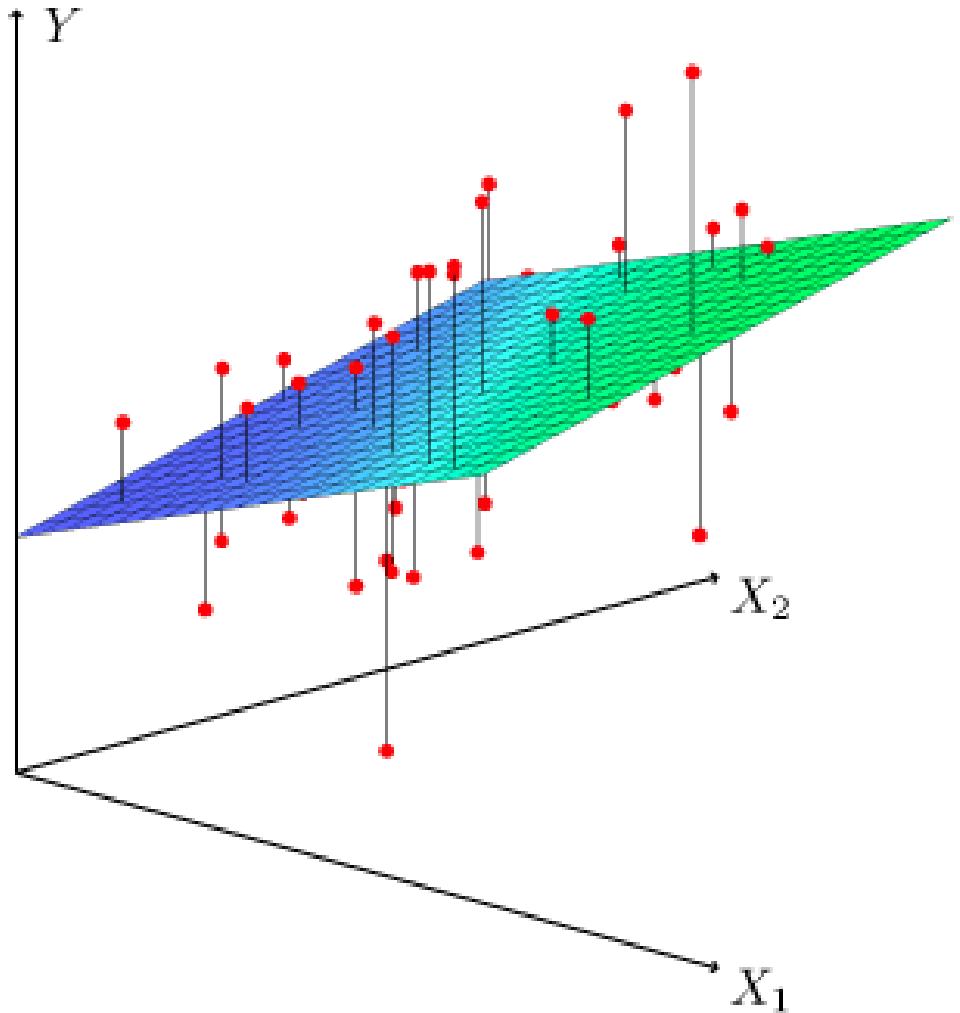
# Regresja liniowa



# Regresja liniowa



# Regresja wieloraka

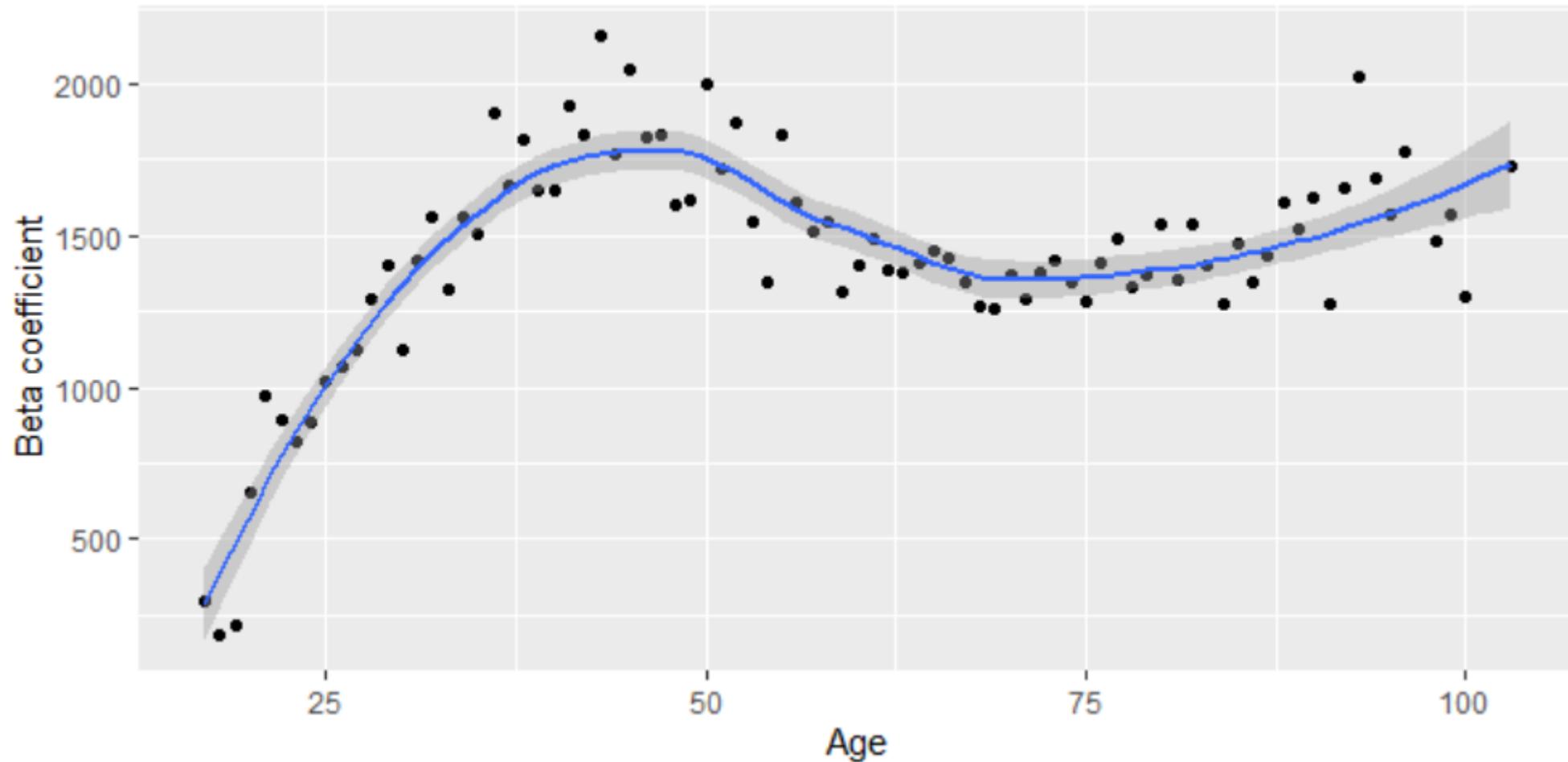


$$Y = aX_1 + bX_2 + c$$

```
lm(income~sex, data=extract, weights=waga)
```

<b>Coefficients:</b>	$\Delta R^2$	<b>Estimate</b>	<b>Std. Error</b>	<b>t value</b>	<b>P-Value</b>
Step 1	0.04				<0.001
(Intercept)		1749.59	16.15	108.32	<0.001
Gender		580.51	23.26	24.96	<0.001

# Wiek jako czynnik



```
lm(income~sex+ageabove16upto40+age40flag+ageafter40+age60plusflag+
+height_ms+height_fs, data=extract, weights=waga)
```

<b>Coefficients:</b>	$\Delta R^2$	<b>Estimate</b>	<b>Std. Error</b>	<b>t value</b>	<b>P-Value</b>
Step 2 with age and height	0.09				<0.001
(Intercept)		758.10	55.88	13.57	<0.001
Gender		533.56	22.76	23.44	<0.001
Height (men)		28.28	2.39	11.81	<0.001
Height (women)		12.73	2.62	4.87	<0.001
Age between 16 and 40		70.74	3.35	21.14	<0.001
Age 40-60 (Flag)		1546.49	67.24	23.00	<0.001
Age between 40 and 60		-36.06	3.24	-11.81	<0.001
Age after 60 (Flag)		755.10	59.03	12.79	<0.001

```
lm(income~sex+ageabove16upto40+age40flag+ageafter40+age60plusflag
 + height_ms+ height_fs+relevel(education, ref = " without")
 + relevel(class, ref = " village"), data=extract, weights=waga)
```

Step 3 with education and class	0.25				<0.001
(Intercept)		65.27	118.95	0.55	.584
Gender		671.34	21.23	31.62	<0.001
Age between 16 and 40		52.70	3.28	16.07	<0.001
Age 41-60 (Flag)		1447.85	65.53	22.10	<0.001
Age between 41 and 60		-28.91	65.53	-9.76	<0.001
Age after 60 (Flag)		825.23	59.25	13.93	<0.001
Height (men)		17.33	2.19	7.90	<0.001
Height (woman)		0.05	2.40	0.019	0.985
PhD		2739.23	157.07	17.44	<0.001
Master		1430.77	109.60	13.05	<0.001
Bachelor		917.71	115.82	7.92	<0.001
Postsecondary		594.42	120.06	4.95	<0.001
Vocational		504.80	108.11	4.67	<0.001
Secondary		498.22	111.79	4.46	<0.001
Basic vocational		128.28	107.45	1.19	.233
Middle school		311.28	144.44	2.16	.031
Primary		-28.59	108.25	-0.26	.792
City bigger than 500 thou.		671.10	36.27	18.50	<0.001
City between 200 and 500 thou.		316.06	37.80	8.36	<0.001
City between 100 and 200 thou.		257.96	41.44	6.23	<0.001
City between 20 and 100 thou.		149.93	28.94	5.18	<0.001
City less than 20 thou.		206.68	34.37	0.01	<0.001

Age between 16 and 40	52.70	3.28	16.07	<0.001
Age 41-60 (Flag)	1447.85	65.53	22.10	<0.001
Age between 41 and 60	-28.91	65.53	-9.76	<0.001
Age after 60 (Flag)	825.23	59.25	13.93	<0.001
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Master	1430.77	109.60	13.05	<0.001
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City bigger than 500 thou.	671.10	36.27	18.50	<0.001
City between 200 and 500 thou.	316.06	37.80	8.36	<0.001
City between 100 and 200 thou.	257.96	41.44	6.23	<0.001
City between 20 and 100 thou.	149.93	28.94	5.18	<0.001
City less than 20 thou.	206.68	34.37	0.01	<0.001

*Income* = 65.27 + 671.34(*Gender*) + 52.70(*Age 16-40*) + 1447.85(*Age 41-60 Flag*) - 28.91(*Age 40-60*) + 825.23(*Age after 60 Flag*) + 17.33(*Height men*) + 0.05(*Height woman*) + 2739.23(*PhD*) + 1430.77(*Master*) + 917.71(*Bachelor*) + 594.42(*Postsecondary*) + 504.80(*Vocational*) + 498.22(*Secondary*) + 128.28(*Basic vocational*) + 311.28(*Middle school*) - 28.59(*Primary*) + 671.10(*City more than 500 thou.*) + 316.06(*City 200 – 500 thou.*) + 257.96(*City 100-200 thou.*) + 149.93(*City 20-100 thou.*) + 206.68(*City less than 20 thou.*),

# Drzewa decyzyjne

Osoba uczęszcza na  
warsztaty Gradientu

Fałsz

Żyje, ale  
co to za życie

Prawda

Dokształca się samemu

Fałsz

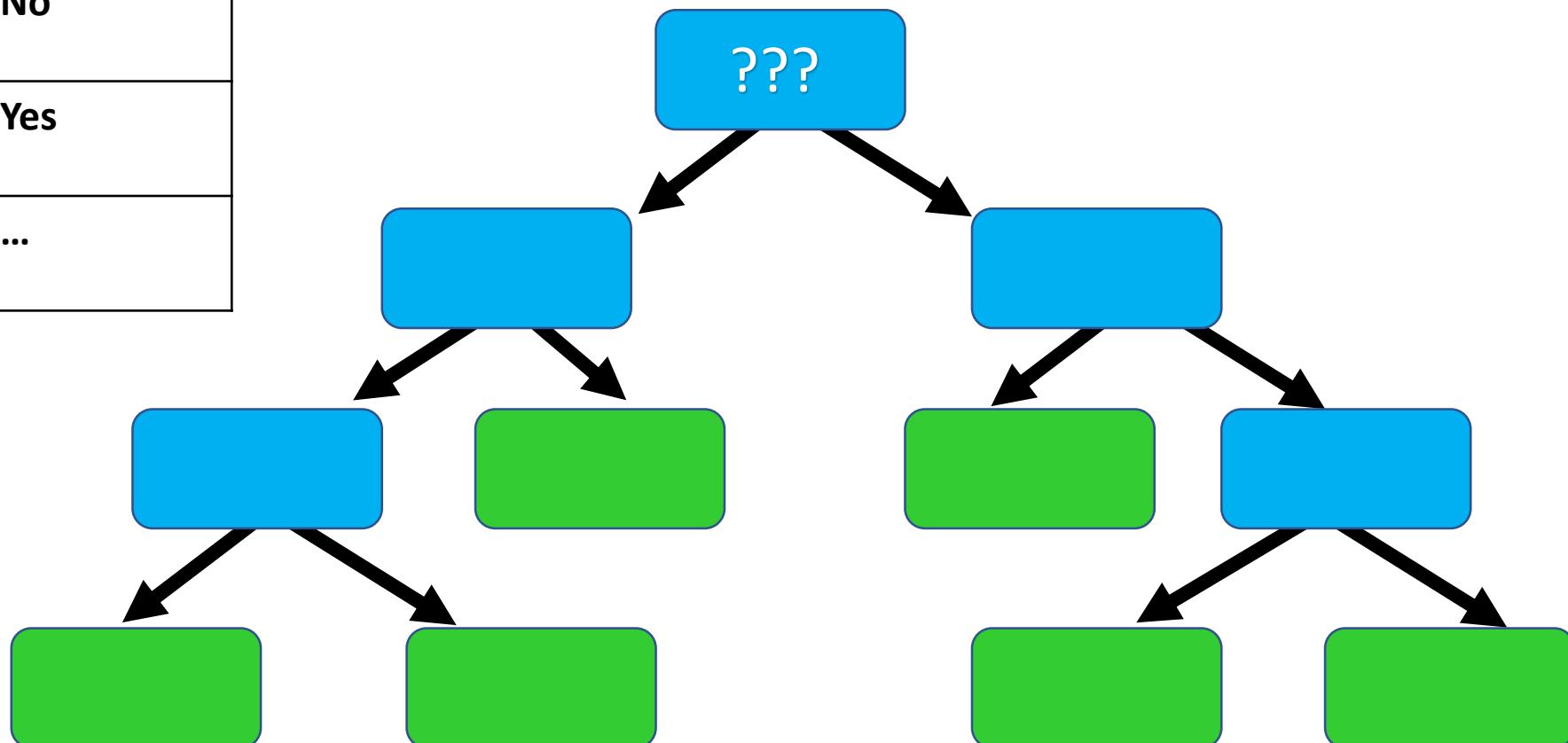
Mogło być  
lepiej

Prawda

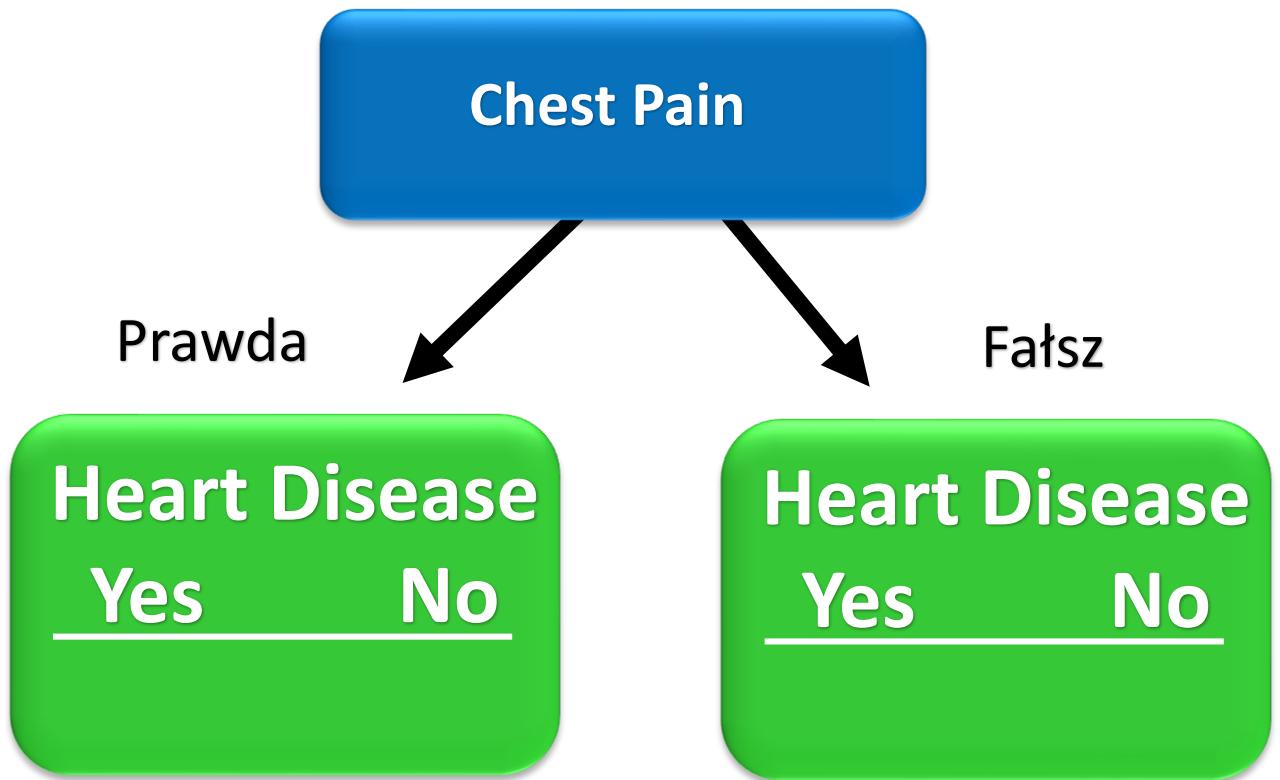
Jesteś Kozak!

Chest Pain	Good Blood Ciculation	Blocked Arteries	Heart Disease
No	No	No	No
Yes	Yes	Yes	Yes
Yes	Yes	No	No
Yes	No	Nan	Yes
...	...	...	...

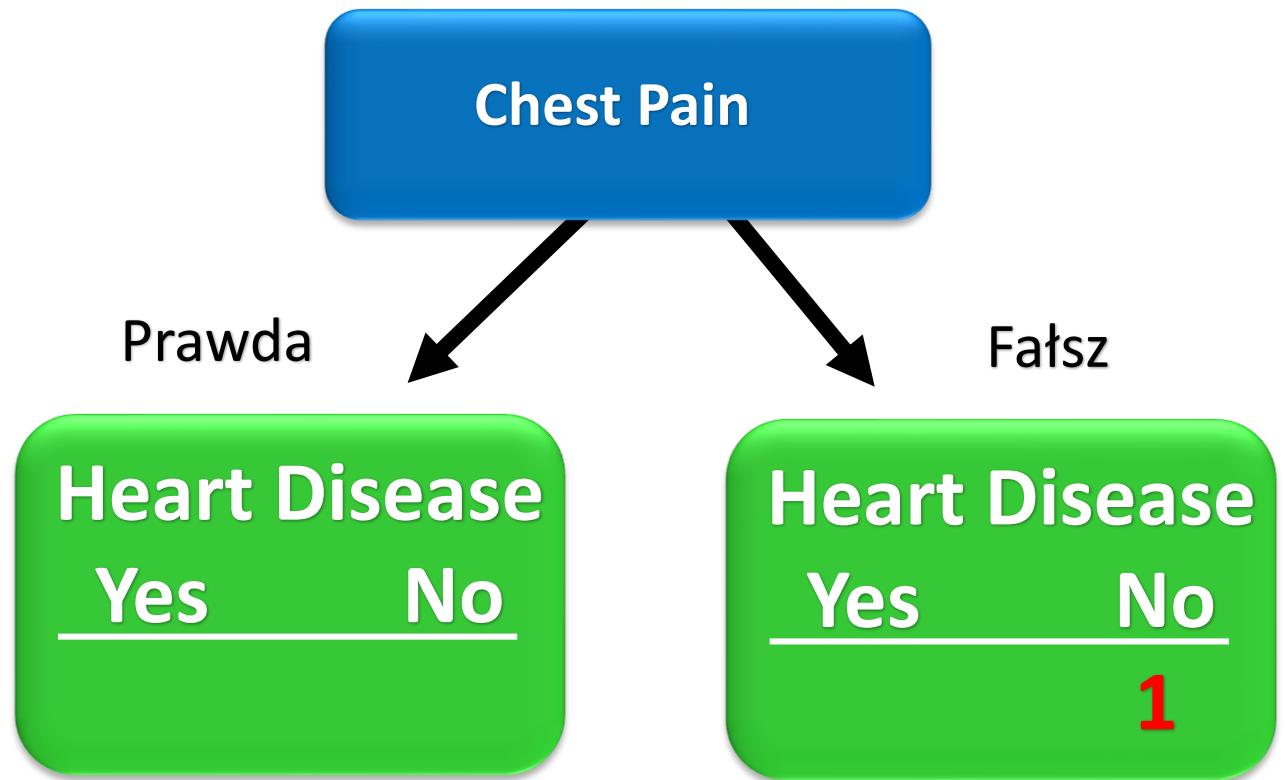
Co powinno być „root node”?



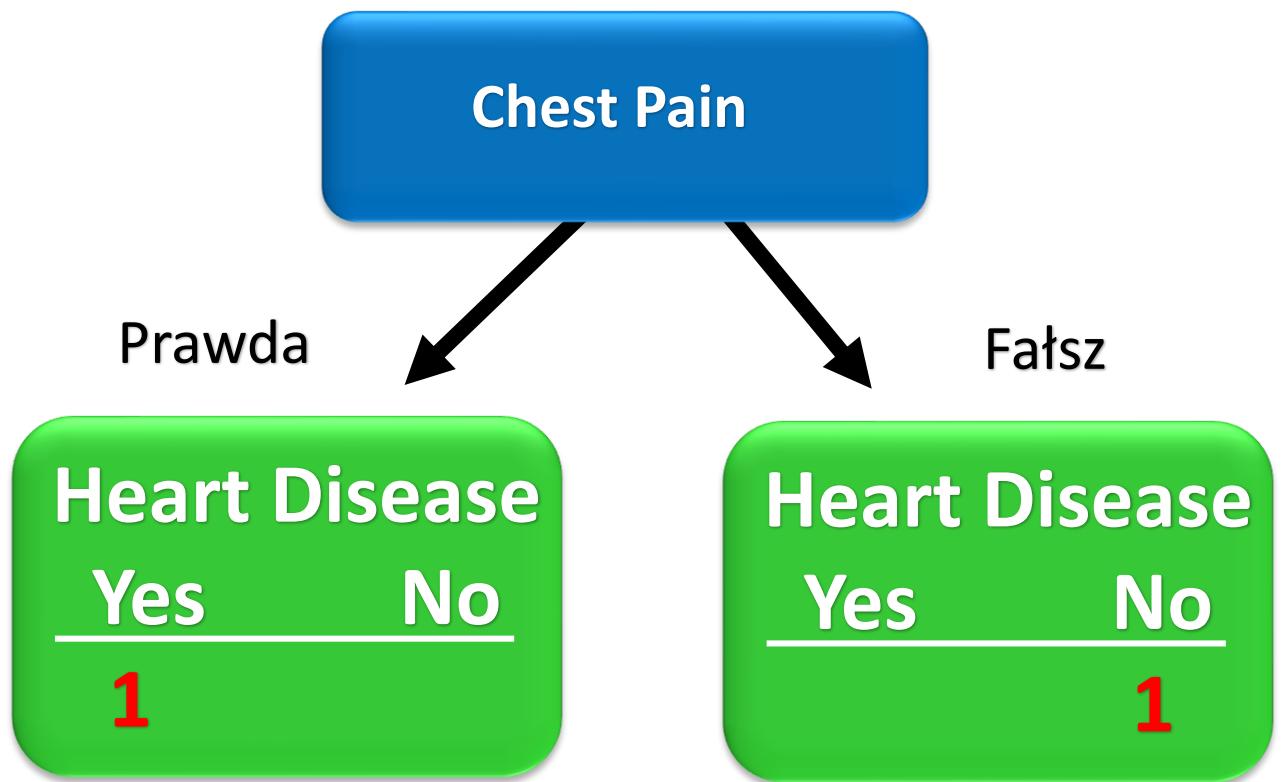
Chest Pain	Good Blood Ciculation	Blocked Arteries	Heart Disease
No	No	No	No
Yes	Yes	Yes	Yes
Yes	Yes	No	No
Yes	No	Nan	Yes
...	...	...	...



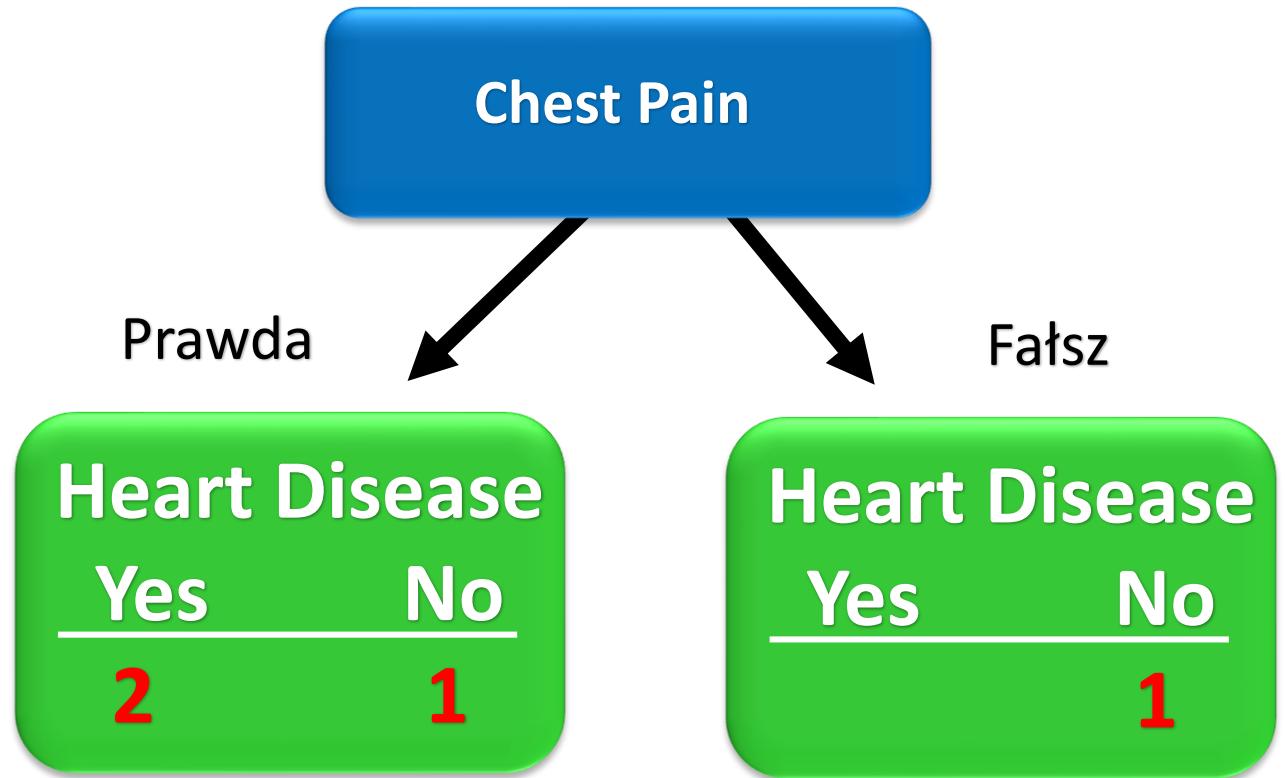
Chest Pain	Good Blood Circulation	Blocked Arteries	Heart Disease
No	No	No	No
Yes	Yes	Yes	Yes
Yes	Yes	No	No
Yes	No	Nan	Yes
...	...	...	...



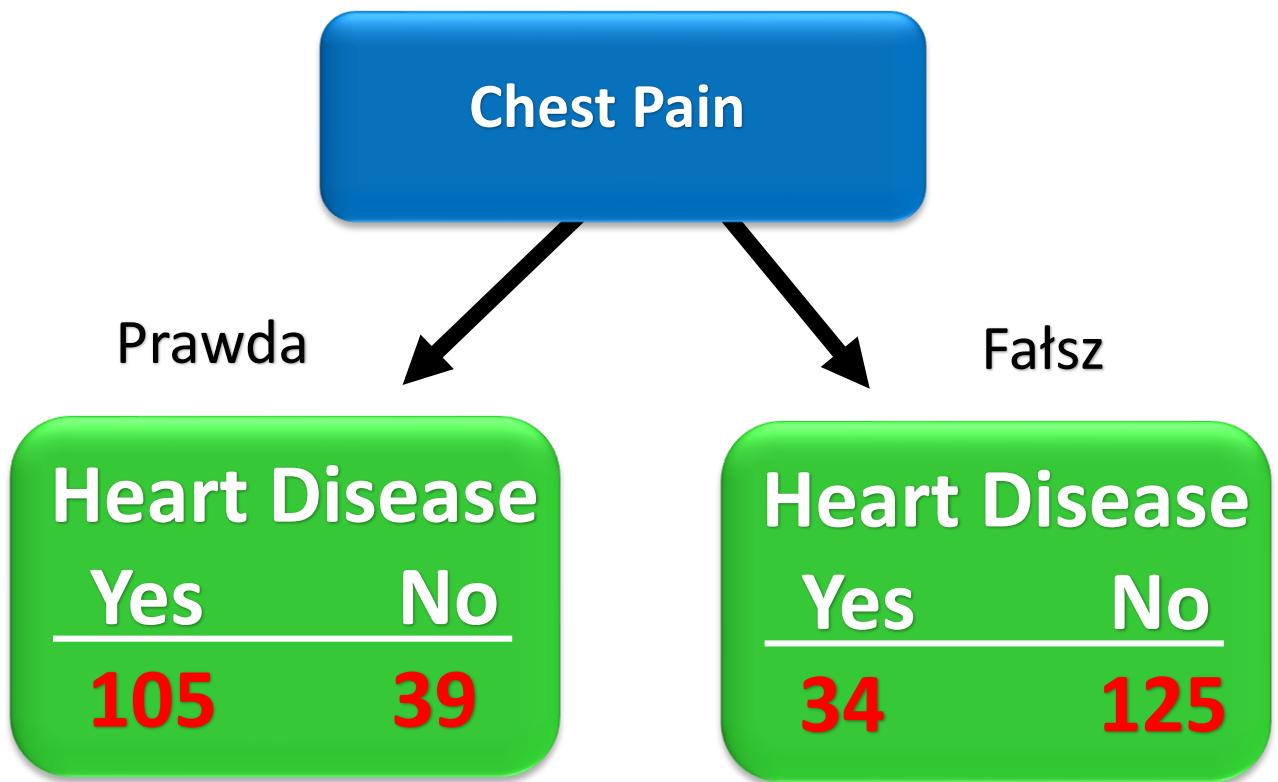
Chest Pain	Good Blood Circulation	Blocked Arteries	Heart Disease
No	No	No	No
Yes	Yes	Yes	Yes
Yes	Yes	No	No
Yes	No	Nan	Yes
...	...	...	...



Chest Pain	Good Blood Circulation	Blocked Arteries	Heart Disease
No	No	No	No
Yes	Yes	Yes	Yes
Yes	Yes	No	No
Yes	No	Nan	Yes
...	...	...	...

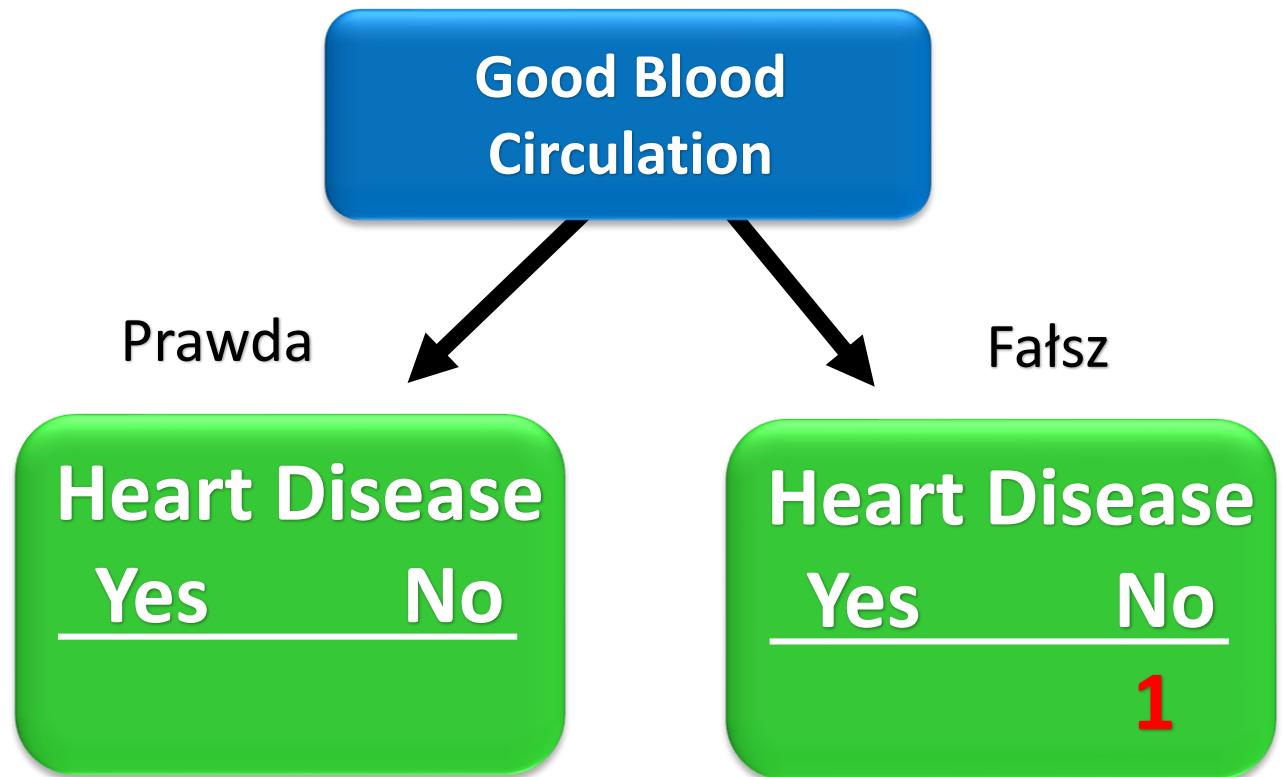


Chest Pain	Good Blood Circulation	Blocked Arteries	Heart Disease
No	No	No	No
Yes	Yes	Yes	Yes
Yes	Yes	No	No
Yes	No	Nan	Yes
...	...	...	...

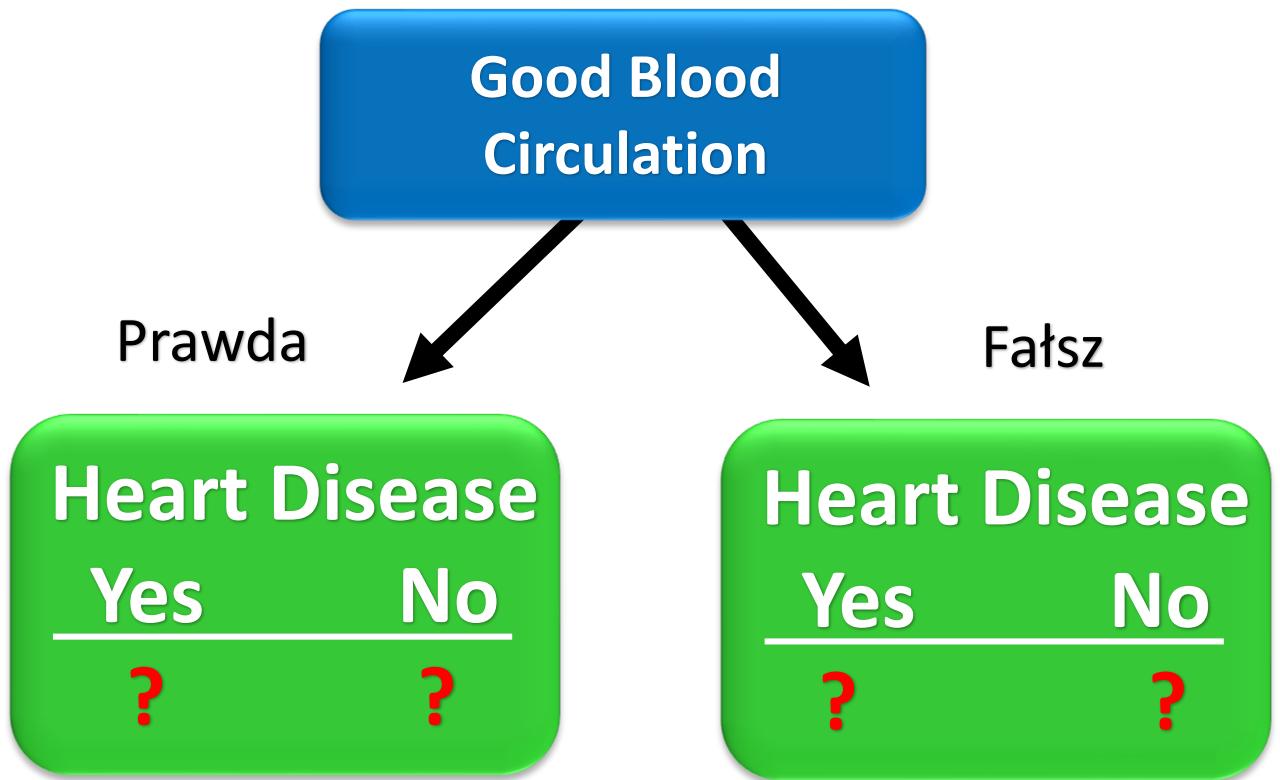


Chest Pain	Good Blood Circulation	Blocked Arteries	Heart Disease
No	No	No	No
Yes	Yes	Yes	Yes
Yes	Yes	No	No
Yes	No	Nan	Yes
...	...	...	...

Chest Pain	Good Blood Ciculation	Blocked Arteries	Heart Disease
No	No	No	No
Yes	Yes	Yes	Yes
Yes	Yes	No	No
Yes	No	Nan	Yes
...	...	...	...

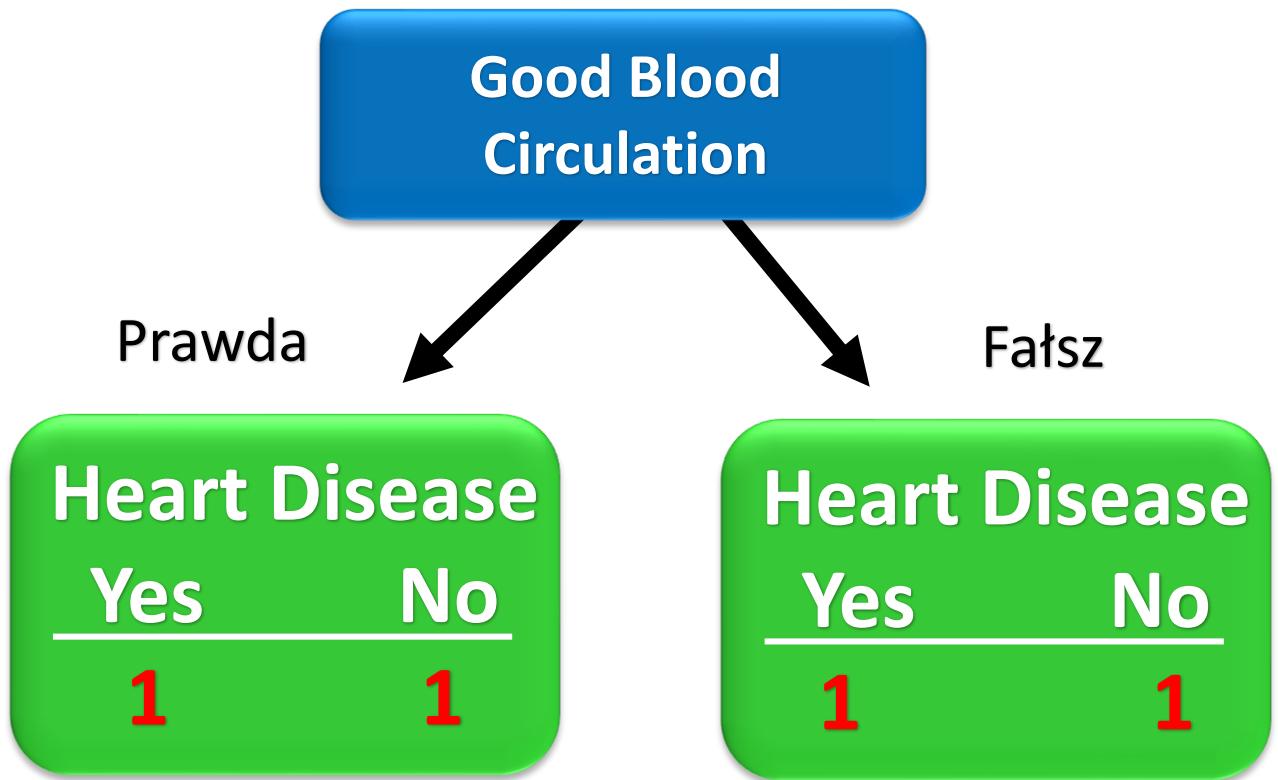


Chest Pain	Good Blood Circulation	Blocked Arteries	Heart Disease
No	No	No	No
Yes	Yes	Yes	Yes
Yes	Yes	No	No
Yes	No	Nan	Yes
...	...	...	...

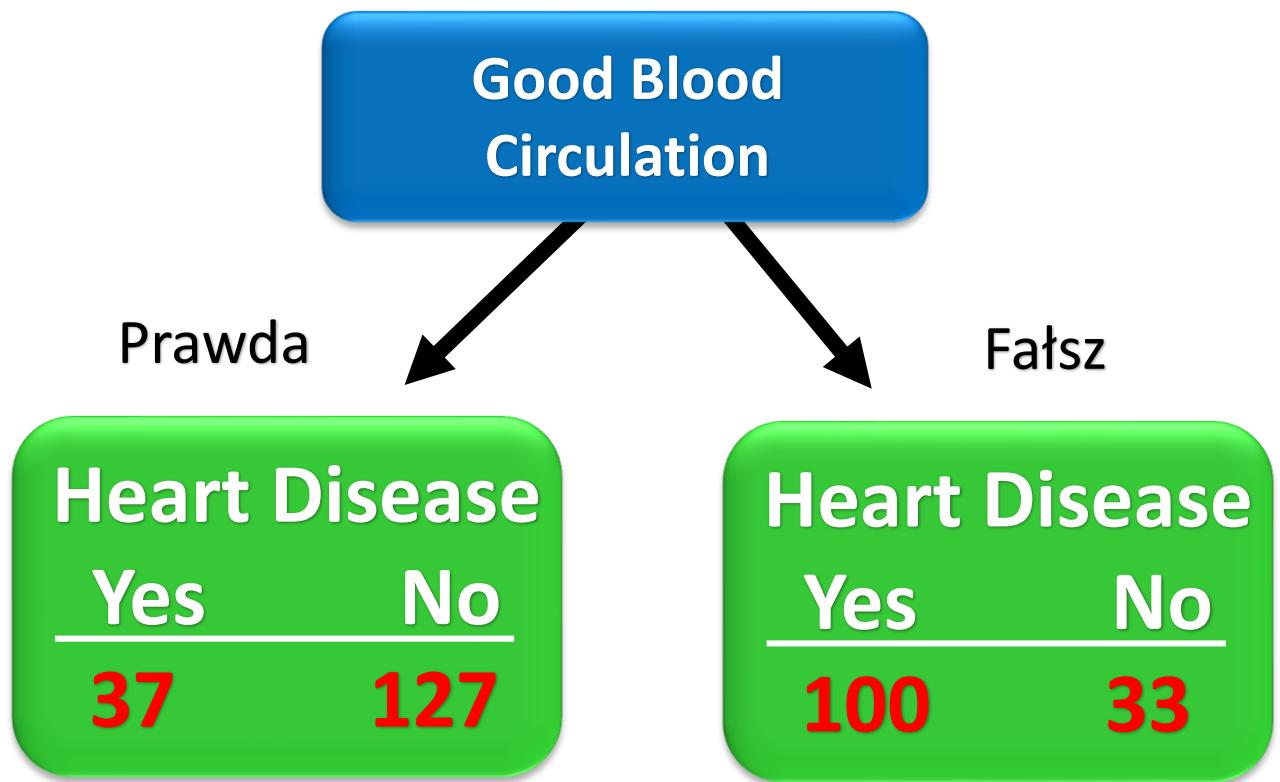


# Pytanie kontrolne!

Chest Pain	Good Blood Circulation	Blocked Arteries	Heart Disease
No	No	No	No
Yes	Yes	Yes	Yes
Yes	Yes	No	No
Yes	No	Nan	Yes
...	...	...	...



Chest Pain	Good Blood Circulation	Blocked Arteries	Heart Disease
No	No	No	No
Yes	Yes	Yes	Yes
Yes	Yes	No	No
Yes	No	Nan	Yes
...	...	...	...



Chest Pain	Good Blood Circulation	Blocked Arteries	Heart Disease
No	No	No	No
Yes	Yes	Yes	Yes
Yes	Yes	No	No
Yes	No	Nan	Yes
...	...	...	...

Blocked Arteries

Prawda

Fałsz

Heart Disease

Yes      No

1

Heart Disease

Yes      No

2

Chest Pain	Good Blood Circulation	Blocked Arteries	Heart Disease
No	No	No	No
Yes	Yes	Yes	Yes
Yes	Yes	No	No
Yes	No	NA	Yes
...	...	...	

NA vs NaN

Pytanie kontrolne!

Blocked Arteries

Prawda

Fałsz

Heart Disease

Yes      No

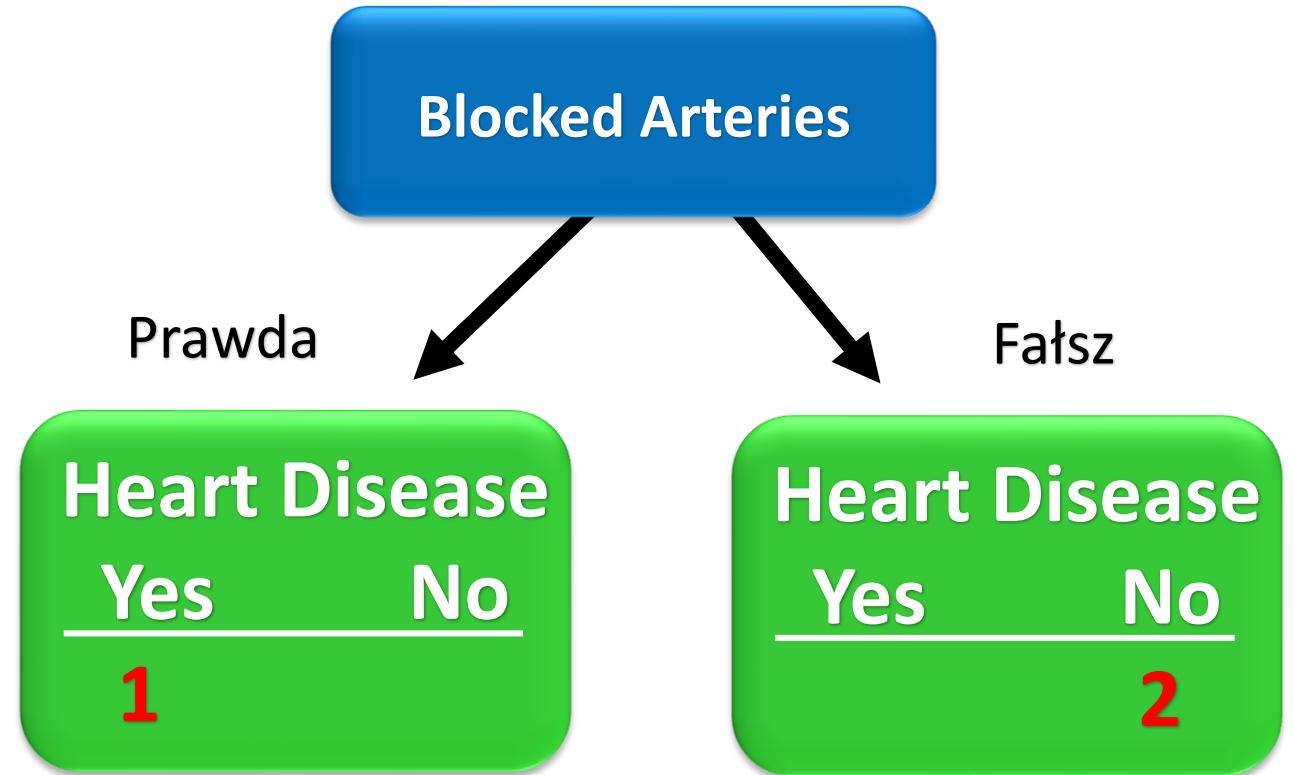
1

Heart Disease

Yes      No

2

Chest Pain	Good Blood Circulation	Blocked Arteries	Heart Disease
No	No	No	No
Yes	Yes	Yes	Yes
Yes	Yes	No	No
Yes	No	NA	Yes
...	...	...	...



# Dealing with missing data



Skip



Chest Pain	Good Blood Circulation	Blocked Arteries	Heart Disease
No	No	No	No
Yes	Yes	Yes	Yes
Yes	Yes	No	No
Yes	No	NA	Yes
...	...	...	...

Blocked Arteries

Prawda

Fałsz

Heart Disease

Yes      No

92      31

Heart Disease

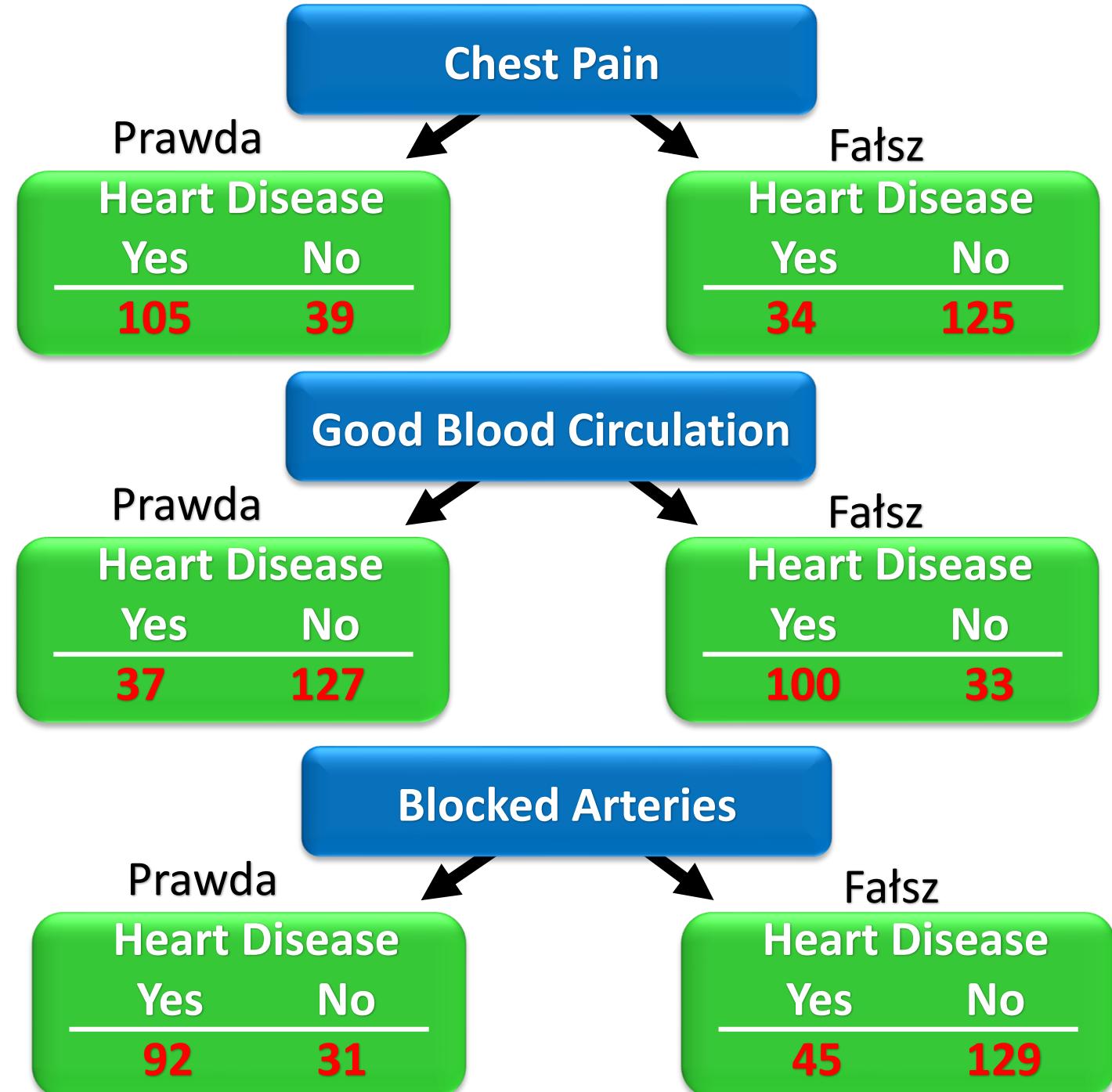
Yes      No

45      129

Idealnie by było...  
100% vs 0%

Jest nieczysto  
„impure”

Jak zmierzyć  
Impurity?



$$\text{gini}(S) = 1 - \sum p_j^2$$

*S – zbiór przykładów należących do n klas*

*p<sub>j</sub> – względna częstotliwość występowania klasy j w S*

Chest Pain

Prawda

Heart Disease

Yes No

**105 39**

Fałsz

Heart Disease

Yes No

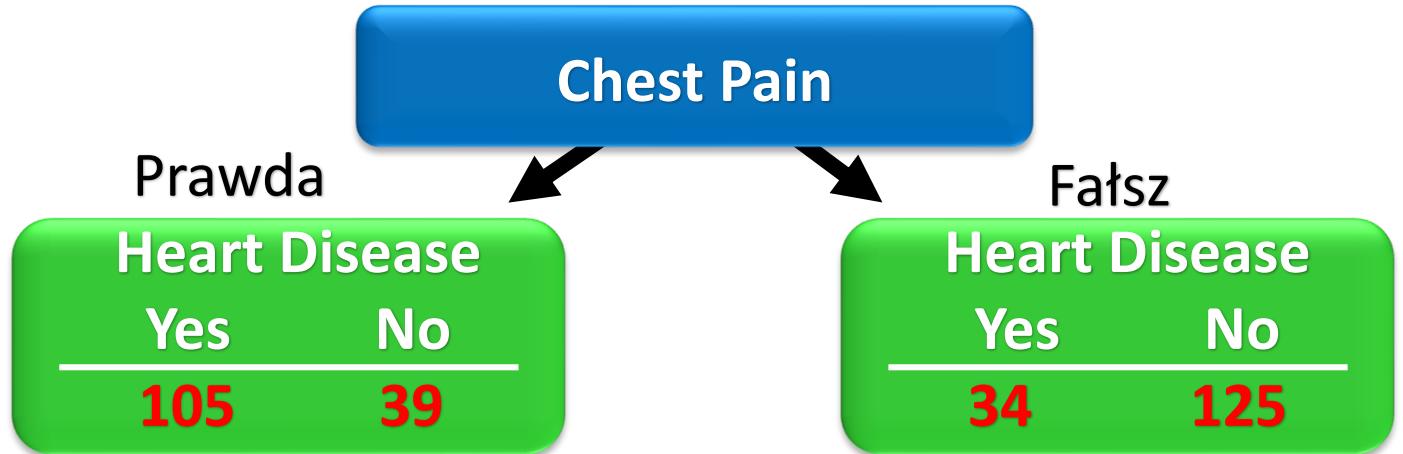
**34 125**

$$\text{Gini} = 1 - (p_{\text{yes}})^2 - (p_{\text{no}})^2$$

$$\text{Gini}_1 = 1 - \left(\frac{105}{105 + 39}\right)^2 - \left(\frac{39}{105 + 39}\right)^2 = 0.395$$

$$\text{Gini}_2 = 1 - \left(\frac{34}{34 + 125}\right)^2 - \left(\frac{125}{34 + 125}\right)^2 = 0.336$$

$$\text{Gini} = 1 - (p_{\text{yes}})^2 - (p_{\text{no}})^2$$



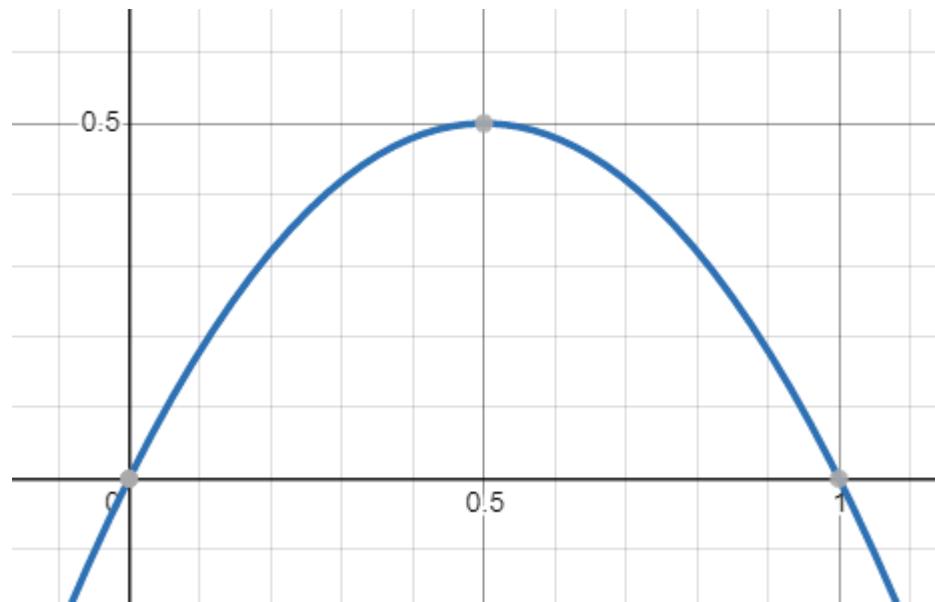
0.395

0.336

Gini całkowite = średnia ważona

$$\text{Gini}_C = \frac{144*0.395 + 159*0.336}{144 + 159} = 0.364$$

$$Gini = 1 - (p_{yes})^2 - (p_{no})^2$$



$Gini_{CP} = 0.364$

Chest Pain

Prawda

Heart Disease

Yes

No

105

39

Fałsz

Heart Disease

Yes

No

34

125

$Gini_{GBC} = 0.360$



Good Blood Circulation

Prawda

Heart Disease

Yes

No

37

127

Fałsz

Heart Disease

Yes

No

100

33

$Gini_{BA} = 0.381$

Blocked Arteries

Prawda

Heart Disease

Yes

No

92

31

Fałsz

Heart Disease

Yes

No

45

129

Chest Pain

Heart Disease	
Yes	No
13	98

Heart Disease	
Yes	No
24	29

$$Gini_{CP} = 0.3$$

Good Blood Circulation

37/127

100/33

Blocked Arteries

Heart Disease	
Yes	No
24	25

Heart Disease	
Yes	No
13	102

$$Gini_{BA} = 0.290$$



Chest Pain

Heart Disease	
Yes	No
17	3

Heart Disease	
Yes	No
7	22

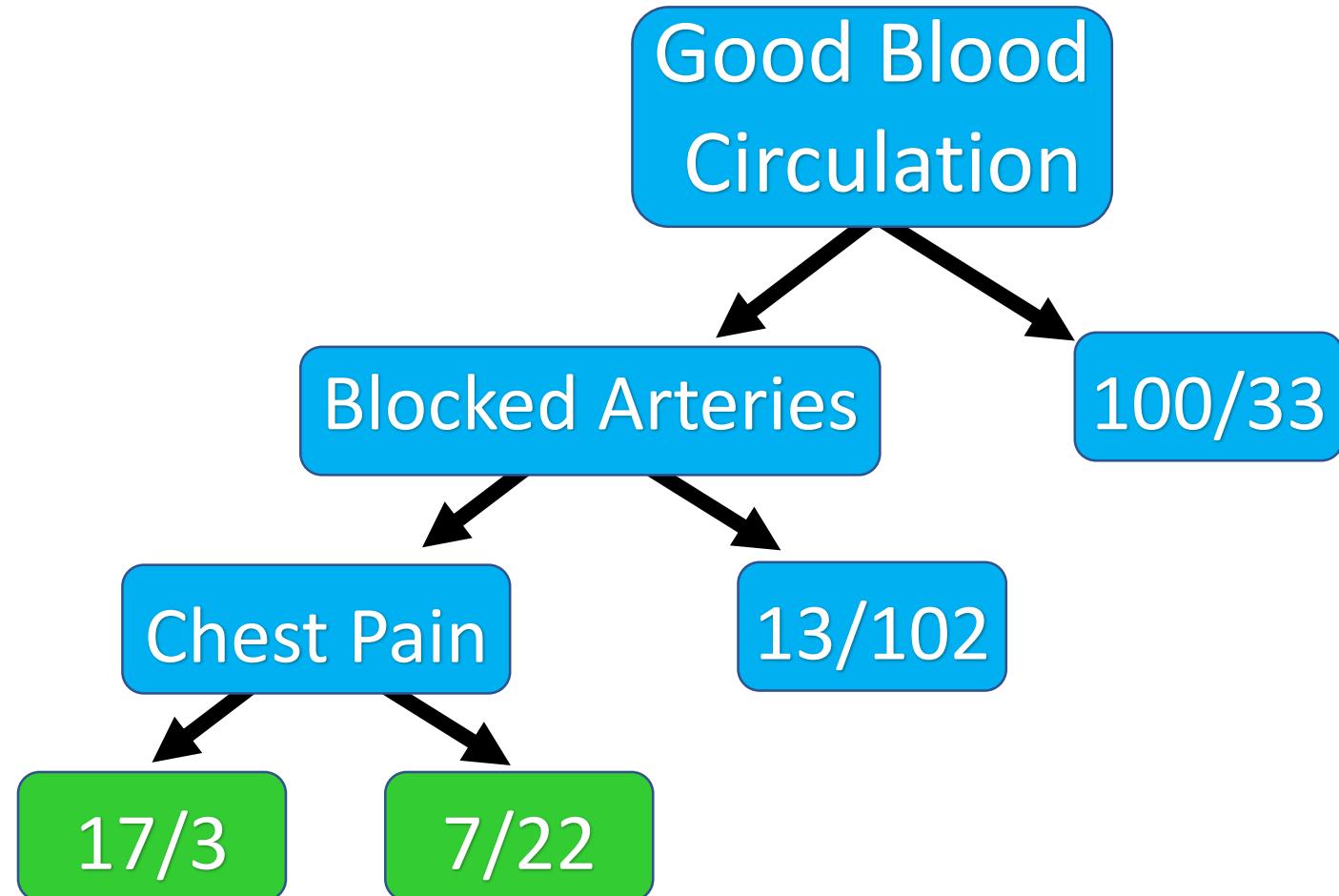
Good Blood Circulation

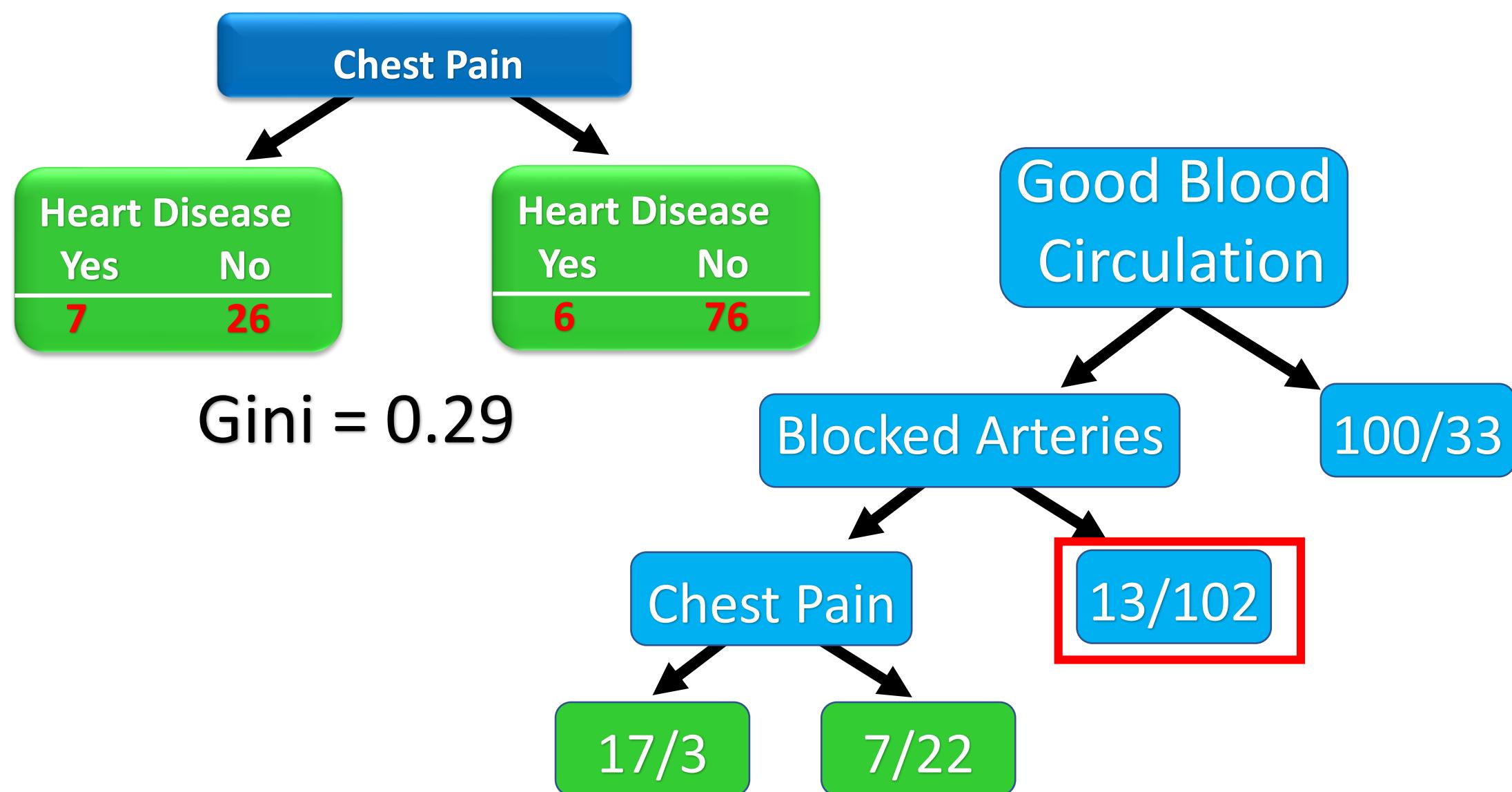
Blocked Arteries

100/33

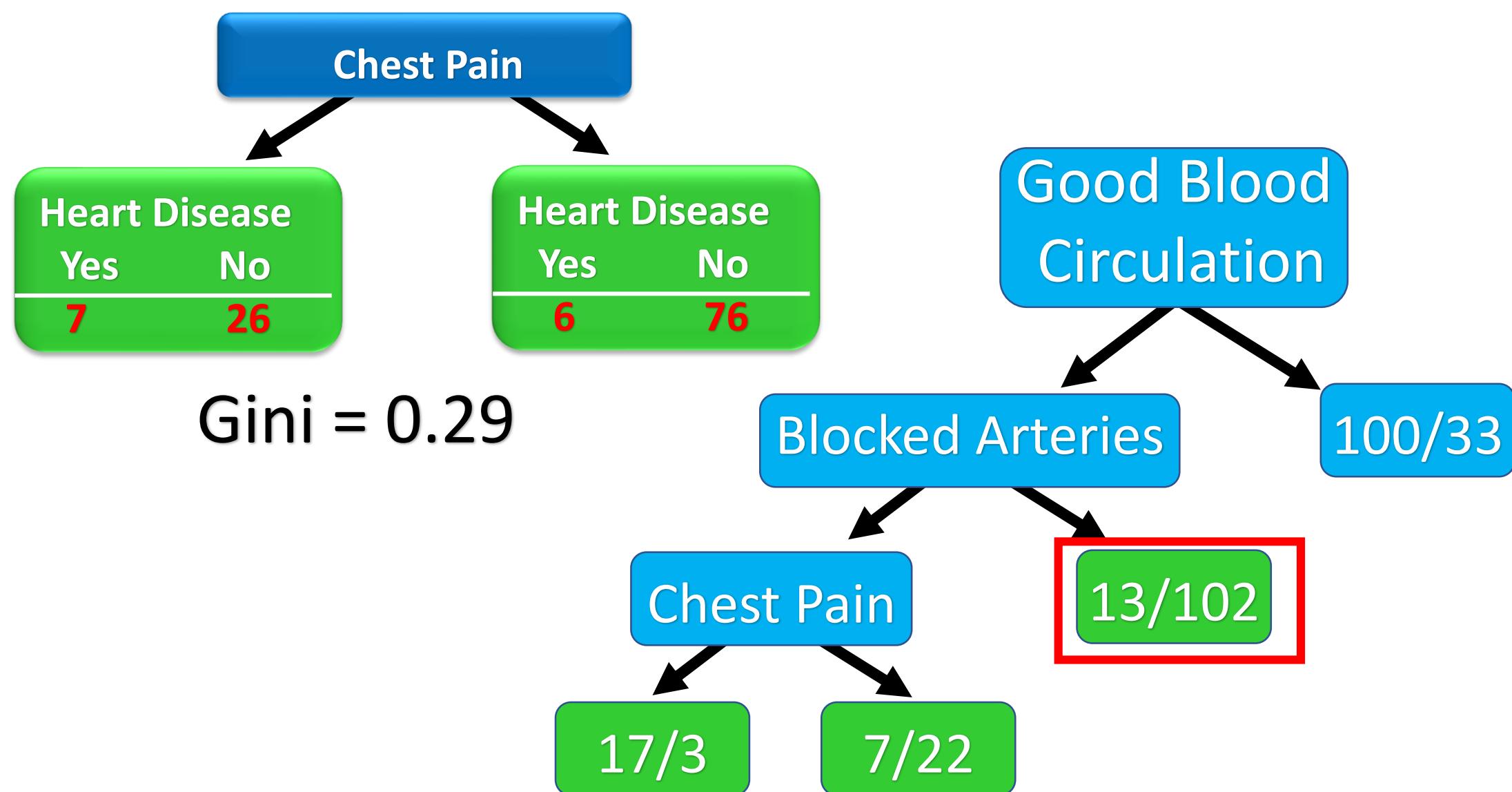
24/25

13/102

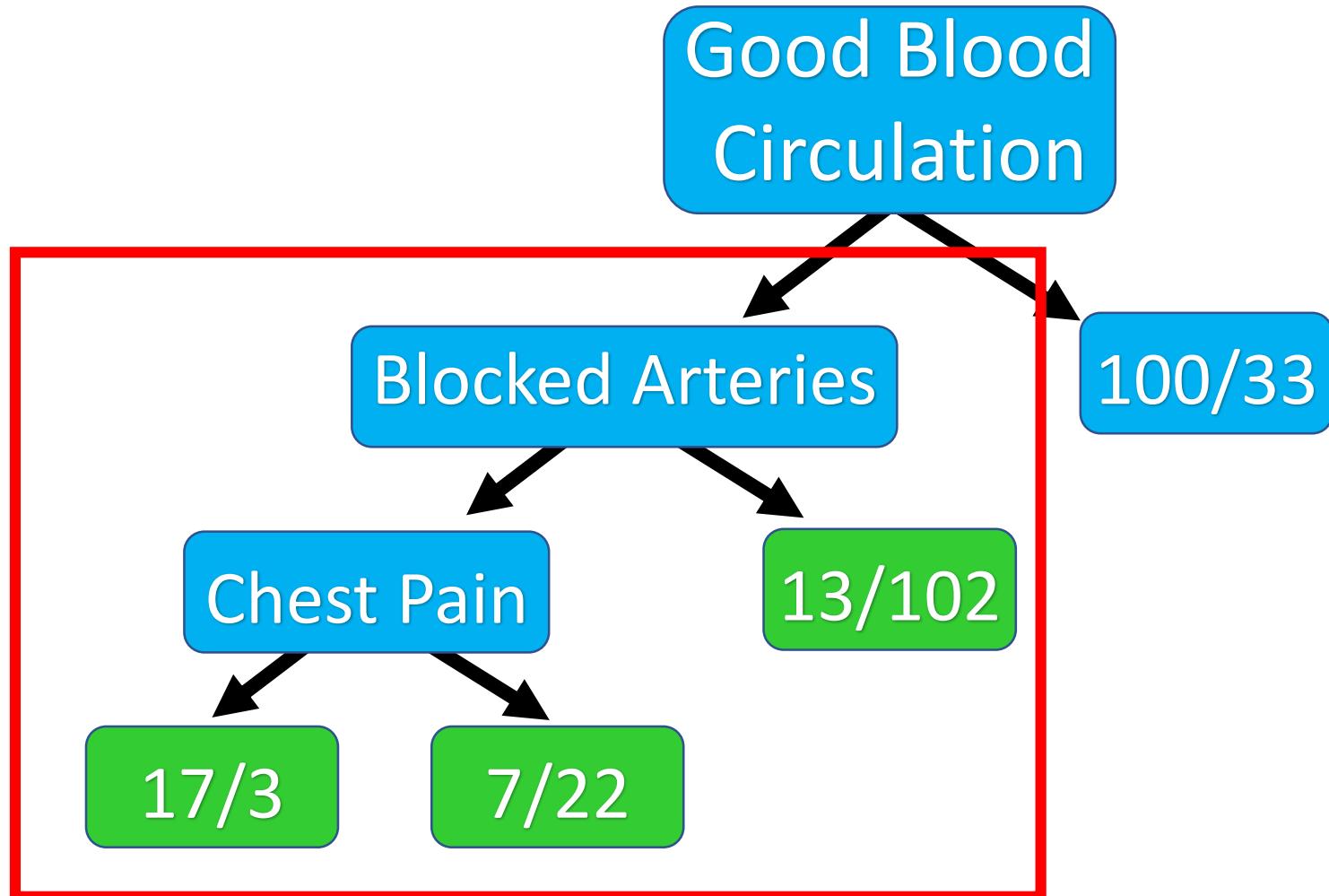




$$\text{Gini}_0 = 1 - \left(\frac{13}{13 + 102}\right)^2 - \left(\frac{102}{13 + 102}\right)^2 = 0.2$$



$$\text{Gini}_0 = 1 - \left(\frac{13}{13+102}\right)^2 - \left(\frac{102}{13+102}\right)^2 = 0.2$$



Good Blood Circulation

Prawda

Fałsz

Blocked Arteries

Prawda

Fałsz

Chest Pain

13/102

Prawda

Fałsz

17/3

7/22

Blocked Arteries

Prawda

Fałsz

Blocked Arteries

Prawda

Fałsz

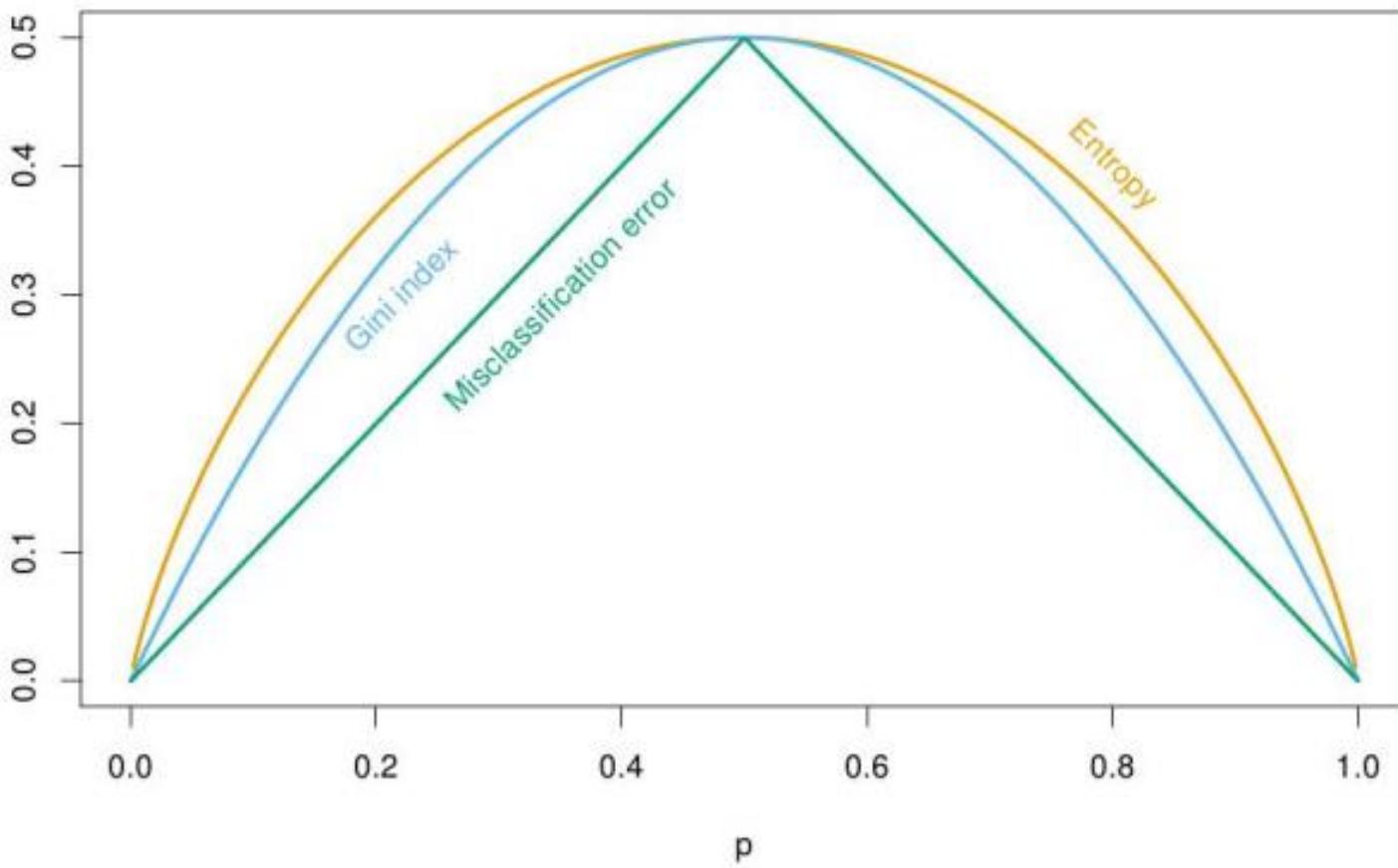
8/0

0/30

1, Classification error:  $1 - \max_k p_k$

2, Gini Index:  $1 - \sum_k p_k^2$

3, Entropy:  $-\sum_k p_k \ln p_k$



# Pytania rekrutacyjne





# Algorytmy i struktury danych

## Uczenie nadzorowane vs nienadzorowane

## Zadania z prawdopodobieństwa

## Metody numeryczne



# Task 1

For a Poisson random variables X and Z, the probability mass function was given by:

$$P(X = x_i; \lambda_i, z_i) = \frac{\lambda_i^{x_i} e^{-\lambda_i}}{x_i!} = \frac{(\theta_0 + \theta_1 z_i)^{x_i} e^{-(\theta_0 + \theta_1 z_i)}}{x_i!}, x_i \in \{0, 1, \dots, \infty\}, 0 < \lambda_i = (\theta_0 + \theta_1 z_i), z_i \in \{0, 1\}$$

As for the likelihood function, considering an independent sample  $x_1, x_2, \dots, x_n$ , from a Poisson variables

$$L = \prod_{i=1}^N \frac{(\theta_0 + \theta_1 z_i)^{x_i} e^{-(\theta_0 + \theta_1 z_i)}}{x_i!} = \frac{\prod_{i=1}^N (\theta_0 + \theta_1 z_i)^{x_i}}{\prod_{i=1}^N x_i!} e^{-\sum_{i=1}^N (\theta_0 + \theta_1 z_i)} \quad (1)$$

Applying natural logarithm to likelihood function

$$\begin{aligned} \ln L &= \ln \left( \prod_{i=1}^N (\theta_0 + \theta_1 z_i)^{x_i} \right) + \ln \left( e^{-\sum_{i=1}^N (\theta_0 + \theta_1 z_i)} \right) - \ln \left( \prod_{i=1}^N x_i! \right) = \\ &= \sum_{i=1}^N x_i \ln(\theta_0 + \theta_1 z_i) - \sum_{i=1}^N (\theta_0 + \theta_1 z_i) - \sum_{i=1}^N \ln(x_i!) \end{aligned} \quad (2)$$

Calculating gradient

$$\frac{\partial \ln L}{\partial \theta_0} = \sum_{i=1}^N \frac{x_i}{\theta_0 + \theta_1 z_i} - n \quad \frac{\partial \ln L}{\partial \theta_1} = \sum_{i=1}^N \frac{x_i z_i}{\theta_0 + \theta_1 z_i} - \sum_{i=1}^N z_i \quad (3)$$

Calculating Hessian matrix

$$\begin{bmatrix} \frac{\partial^2 \ln L}{\partial \theta_0^2} & \frac{\partial^2 \ln L}{\partial \theta_0 \partial \theta_1} \\ \frac{\partial^2 \ln L}{\partial \theta_1 \partial \theta_0} & \frac{\partial^2 \ln L}{\partial \theta_1^2} \end{bmatrix} = \begin{bmatrix} \sum_{i=1}^N \frac{-x_i}{(\theta_0 + \theta_1 z_i)^2} & \sum_{i=1}^N \frac{-x_i z_i}{(\theta_0 + \theta_1 z_i)^2} \\ \sum_{i=1}^N \frac{-x_i z_i}{(\theta_0 + \theta_1 z_i)^2} & \sum_{i=1}^N \frac{-x_i z_i^2}{(\theta_0 + \theta_1 z_i)^2} \end{bmatrix}$$

The predicted value is positive and its positive

ACTUAL VALUES

		Positive	Negative
PREDICTED VALUES	Positive	TP	FP
	Negative	FN	TN

Type I error :  
The predicted value is positive but it False

Type II error :  
The predicted value is negative but its positive

The predicted value is Negative and its Negative

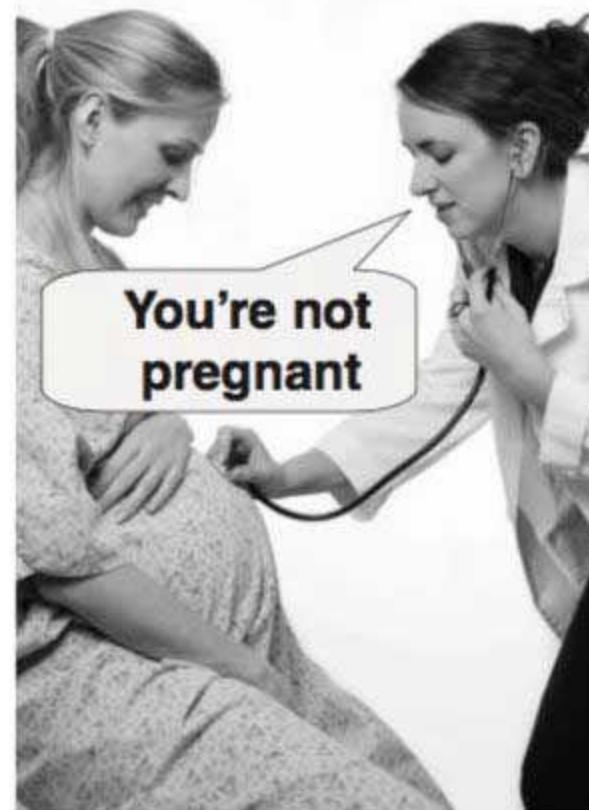
$$P = \frac{T_p}{T_p + F_p}$$

$$R = \frac{T_p}{T_p + F_n}$$

**Type I error**  
(false positive)



**Type II error**  
(false negative)



THANK YOU

