Linear Regression

```
import pandas as pd
import sklearn as sk
from sklearn import model_selection
from matplotlib import pyplot as plt
import numpy as np
from sklearn.metrics import r2 score
```

```
In [2]:
```

data = pd.read_csv("F:/assignments/Sem 6 Assignments/ML Assignment 1/Q2/abalone.data")

Raw Data

```
In [3]:
data
```

Out[3]:

	Sex	Length	Diameter	Height	Whole Weight	Shucked weight	Viscera weight	Shell weight	Rings
0	М	0.455	0.365	0.095	0.5140	0.2245	0.1010	0.1500	15
1	М	0.350	0.265	0.090	0.2255	0.0995	0.0485	0.0700	7
2	F	0.530	0.420	0.135	0.6770	0.2565	0.1415	0.2100	9
3	М	0.440	0.365	0.125	0.5160	0.2155	0.1140	0.1550	10
4	ı	0.330	0.255	0.080	0.2050	0.0895	0.0395	0.0550	7
4172	F	0.565	0.450	0.165	0.8870	0.3700	0.2390	0.2490	11
4173	М	0.590	0.440	0.135	0.9660	0.4390	0.2145	0.2605	10
4174	М	0.600	0.475	0.205	1.1760	0.5255	0.2875	0.3080	9
4175	F	0.625	0.485	0.150	1.0945	0.5310	0.2610	0.2960	10
4176	М	0.710	0.555	0.195	1.9485	0.9455	0.3765	0.4950	12

4177 rows × 9 columns

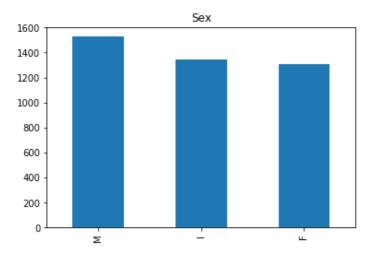
Visualization of dataset

```
In [4]:
```

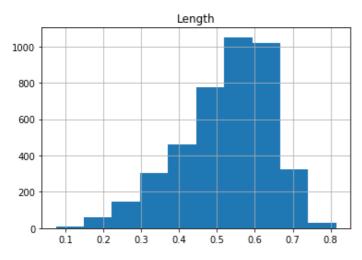
```
data['Sex'].value_counts().plot(kind='bar')
plt.title('Sex')
plt.figure()
data.hist(column='Length')
plt.figure()
data.hist(column='Diameter')
plt.figure()
data.hist(column='Height')
plt.figure()
data.hist(column='Whole Weight')
```

```
plt.figure()
data.hist(column='Shucked weight')
plt.figure()
data.hist(column='Viscera weight')
plt.figure()
data.hist(column='Shell weight')
```

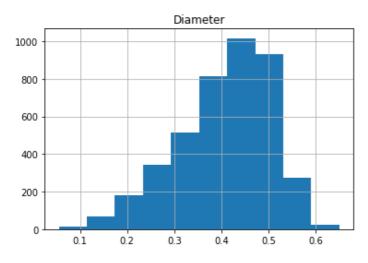
Out[4]:



<Figure size 432x288 with 0 Axes>

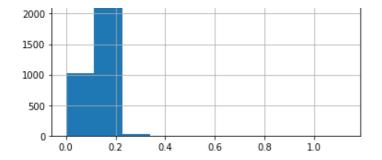


<Figure size 432x288 with 0 Axes>

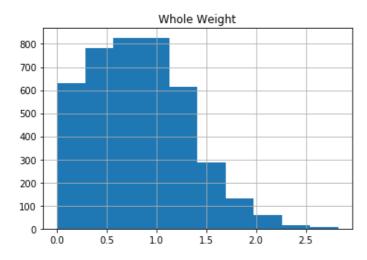


<Figure size 432x288 with 0 Axes>

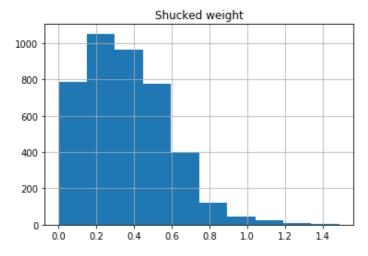
	Height								
3000 -									
3000									
2500 -									
2500									



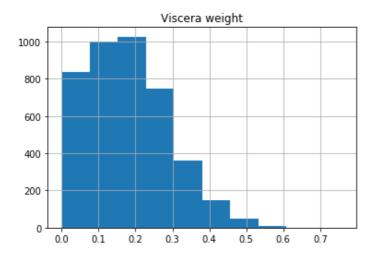
<Figure size 432x288 with 0 Axes>



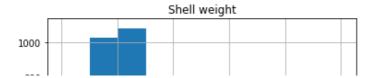
<Figure size 432x288 with 0 Axes>

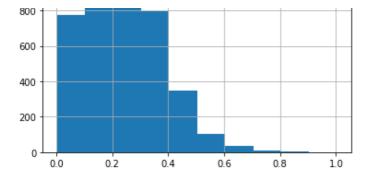


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<Figure size 432x288 with 0 Axes>





In [5]:

```
#one hot encoding for Sex
one_hot = pd.get_dummies(data['Sex'])
data = data.drop('Sex',axis = 1)
data = data.join(one_hot)
```

Data after One Hot Encoding for Discrete Values (Sex)

In [6]:

data

Out[6]:

	Length	Diameter	Height	Whole Weight	Shucked weight	Viscera weight	Shell weight	Rings	F	ı	M
0	0.455	0.365	0.095	0.5140	0.2245	0.1010	0.1500	15	0	0	1
1	0.350	0.265	0.090	0.2255	0.0995	0.0485	0.0700	7	0	0	1
2	0.530	0.420	0.135	0.6770	0.2565	0.1415	0.2100	9	1	0	0
3	0.440	0.365	0.125	0.5160	0.2155	0.1140	0.1550	10	0	0	1
4	0.330	0.255	0.080	0.2050	0.0895	0.0395	0.0550	7	0	1	0
4172	0.565	0.450	0.165	0.8870	0.3700	0.2390	0.2490	11	1	0	0
4173	0.590	0.440	0.135	0.9660	0.4390	0.2145	0.2605	10	0	0	1
4174	0.600	0.475	0.205	1.1760	0.5255	0.2875	0.3080	9	0	0	1
4175	0.625	0.485	0.150	1.0945	0.5310	0.2610	0.2960	10	1	0	0
4176	0.710	0.555	0.195	1.9485	0.9455	0.3765	0.4950	12	0	0	1

4177 rows × 11 columns

Min-Max Scaling

```
In [7]:
```

```
#min max normalization
for column in data.columns:
    data[column] = (data[column] - data[column] .min()) / (data[column] .max() - data[column] .min())
```

Splitting Dataset into 90% train 10% test

```
In [8]:
```

```
train_,test=model_selection.train_test_split(data, test_size=0.1, train_size=0.9)
```

Note: Training is done using the 5-fold validation. RMSE is

reported on the validation set. Best Model from the 5 folds is determined using the RMSE value. Lower the RMSE, better is the model

Linear Regression w/o Regularization LR=0.00001

```
In [9]:
```

```
def linear(w,x train,y train,x test,y test):
   lr=0.00001
   x train=np.array(x train)
   y train=np.array(y train)
   x test=np.array(x test)
   y test=np.array(y test)
    for i in range(x train.shape[0]): #3007
        for j in range(x train.shape[1]): #10
            grad=grad+(np.dot(x_train[i],w)-y_train[i])*x_train[i][j]
            w[j]=w[j]-lr*grad
    #validation
   y pred=np.dot(x test,w)
   mse=np.sqrt(np.sum(np.square(y_pred-y_test)))/x_test.shape[0]
   return(w, mse)
```

In [10]:

```
best rmse=10000
kf=model selection.KFold(n splits=5)
# train=kf.get n splits(train )
# print(train .shape)
# print(y.shape)
y = train_['Rings']
new_train = train_.drop(['Rings'], axis=1)
# print(train .shape)
# print(y.shape)
for train_index, test_index in kf.split(train):
     print("TRAIN:", train index, "TEST:", test index)
    x train, x test = new_train.iloc[train_index], new_train.iloc[test_index]
   w=np.zeros((x train.shape[1],1))
    print(X_train.shape)
print(X_test.shape)
    y_train, y_test = y.iloc[train_index], y.iloc[test index]
     print(y test.shape)
    for i in range (50):
        w,mse=linear(w,x train,y train,x test,y test)
        rmse.append (mse)
    plt.plot(rmse)
    if(sum(rmse) < best rmse):</pre>
        w best=w
        best rmse=sum(rmse)
plt.figure()
```

Out[10]:

```
<Figure size 432x288 with 0 Axes>
```

```
0.28
0.26
0.24
0.22
```

<Figure size 432x288 with 0 Axes>

RMSE for model without penalty on test set

```
In [11]:
```

```
y=test['Rings']
new test=test.drop(['Rings'],axis=1)
new test=np.array(new test)
y pred=np.dot(new test,w)
y=np.array(y)
# np.sqrt(np.sum(np.square((y-y pred))))/y.size
# r2 score(y, y pred)
np.sqrt(np.sum(np.square(y pred-y)))/len(y)
Out[11]:
```

0.14695609463470916

L2 Regularization LR:0.00001 lambda=0.01

Notice the loss function here. The square of the norm of the weights of the model are added to the loss function.

```
In [12]:
```

```
def 12(w,x_train,y_train,x_test,y_test):
    lr=0.00001
   x train=np.array(x train)
   y train=np.array(y train)
   x test=np.array(x test)
    y test=np.array(y test)
    lamb=0.0001
    for i in range(x train.shape[0]): #3007
        grad=0
        for j in range(x train.shape[1]): #10
            grad=grad+(np.dot(x_train[i],w)-y_train[i])*x_train[i][j] + lamb*w[j]
            w[j]=w[j]-lr*grad
    #validation
    y pred=np.dot(x test,w)
   mse=(np.sqrt(np.sum(np.square(y_pred-y_test))) + lamb*np.square(np.linalg.norm(w)))
/x test.shape[0] #notice the change in loss function
   return(w, mse)
```

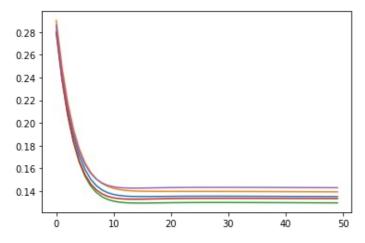
In [13]:

```
best_rmse=10000
kf=model selection.KFold(n splits=5)
# train=kf.get n splits(train )
# print(train .shape)
# print(y.shape)
y = train ['Rings']
new train = train .drop(['Rings'], axis=1)
# print(train .shape)
# print(y.shape)
```

```
for train_index, test_index in kf.split(train_):
    rmse=[]
     print("TRAIN:", train_index, "TEST:", test_index)
    x train, x test = new train.iloc[train index], new train.iloc[test index]
    w12=np.zeros((x train.shape[1],1))
     print(X train.shape)
     print(X test.shape)
    y train, y test = y.iloc[train index], y.iloc[test index]
     print(y test.shape)
    for i in range (50):
        wl2,mse=l2(wl2,x train,y train,x test,y test)
        rmse.append (mse)
    plt.plot(rmse)
    if(sum(rmse) < best rmse):</pre>
        w best 12=w12
        best rmse=sum(rmse)
plt.figure()
```

Out[13]:

<Figure size 432x288 with 0 Axes>



<Figure size 432x288 with 0 Axes>

RMSE for L2 on test set

```
In [14]:
```

```
y=test['Rings']
new_test=test.drop(['Rings'],axis=1)
new_test=np.array(new_test)
y_pred=np.dot(new_test,w_best_12)
y=np.array(y)
# np.sqrt(np.sum(np.square((y-y_pred))))/y.size
# r2_score(y,y_pred)
np.sqrt(np.sum(np.square(y_pred-y)))/len(y)
```

Out[14]:

0.14705283270813393

L1 Regularization LR:0.00001, lambda=0.001

Notice the loss function here. The absolute value of the weights of the model are added to the loss function

```
In [15]:
```

```
def l1(w,x_train,y_train,x_test,y_test):
    lr=0.00001
```

```
x_train=np.array(x_train)
y_train=np.array(y_train)
x_test=np.array(x_test)
y_test=np.array(y_test)
constant=0.5
lamb=0.001

for i in range(x_train.shape[0]): #3007
    grad=0
    for j in range(x_train.shape[1]): #10
        grad=grad+(np.dot(x_train[i],w)-y_train[i])*x_train[i][j] + lamb*constant
        w[j]=w[j]-lr*grad

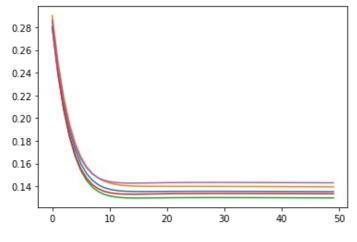
#validation
y_pred=np.dot(x_test,w)
mse=(np.sqrt(np.sum(np.square(y_pred-y_test))) + lamb*np.sum(np.abs(w)))/x_test.shap
e[0]#notice the change in loss function here
return(w,mse)
```

In [16]:

```
best rmse=10000
kf=model selection.KFold(n_splits=5)
# train=kf.get n splits(train )
# print(train .shape)
# print(y.shape)
y = train ['Rings']
new_train = train_.drop(['Rings'], axis=1)
# print(train_.shape)
# print(y.shape)
for train_index, test_index in kf.split(train ):
    rmse=[]
     print("TRAIN:", train index, "TEST:", test index)
    x train, x test = new train.iloc[train index], new train.iloc[test index]
    wll=np.zeros((x train.shape[1],1))
      print(X train.shape)
     print(X test.shape)
    y train, y test = y.iloc[train index], y.iloc[test index]
      print(y_test.shape)
    for i in range (50):
        wl1, mse=l1(wl1, x train, y train, x test, y test)
        rmse.append (mse)
    plt.plot(rmse)
    if(sum(rmse) < best rmse):</pre>
        w best l1=wl1
        best rmse=sum(rmse)
plt.figure()
```

Out[16]:

<Figure size 432x288 with 0 Axes>



<Figure size 432x288 with 0 Axes>

RMSE for L1 on test set

```
In [17]:

y=test['Rings']
new_test=test.drop(['Rings'],axis=1)
new_test=np.array(new_test)
y_pred=np.dot(new_test,w_best_11)
y=np.array(y)
# np.sqrt(np.sum(np.square((y-y_pred))))/y.size
np.sqrt(np.sum(np.square(y_pred-y)))/len(y)

Out[17]:
0.1471399932030919
```

SkLearn implementation of Linear Regression no Penalty

```
In [18]:
```

```
from sklearn.linear model import LinearRegression
reg=LinearRegression()
kf=model selection.KFold(n splits=5)
# train=kf.get n splits(train )
# print(train .shape)
# print(y.shape)
y = train ['Rings']
new train = train .drop(['Rings'], axis=1)
# y1=test['Rings']
# new test=test.drop(['Rings'],axis=1)
# new test=np.array(new test)
best rmse=10000
# print(train .shape)
# print(y.shape)
for train index, test index in kf.split(train ):
     print("TRAIN:", train index, "TEST:", test index)
   x train, x test = new train.iloc[train_index], new_train.iloc[test_index]
     wl1=np.zeros((x train.shape[1],1))
     print(X train.shape)
     print(X test.shape)
   y train, y test = y.iloc[train index], y.iloc[test index]
    print(y test.shape)
   reg.fit(x train,y_train)
   y_pred=reg.predict(x test)
   rmse=np.sqrt(np.sum(np.square(y pred-y test)))/len(y pred)
    print(rmse)
   if(rmse<best rmse):</pre>
       best rmse=rmse
       best model=reg
     print(reg.score(new test,y1))
y=test['Rings']
new test=test.drop(['Rings'],axis=1)
```

RMSE for inbuilt Linear Regression on test set

```
In [19]:
```

```
from sklearn.metrics import mean_squared_error

y=test['Rings']
new_test=test.drop(['Rings'],axis=1)
```

```
y_pred=best_model.predict(new_test)
rms = mean_squared_error(y, y_pred, squared=False)
rms
Out[19]:
```

SkLearn Implementation of Ridge (L2)

```
In [20]:
```

0.08471284911075605

```
from sklearn.linear model import Ridge
reg=Ridge(alpha=0.000001)
kf=model selection.KFold(n splits=5)
# train=kf.get n splits(train )
# print(train .shape)
# print(y.shape)
y = train_['Rings']
new train = train .drop(['Rings'], axis=1)
# y1=test['Rings']
# new test=test.drop(['Rings'],axis=1)
# new test=np.array(new test)
best_rmse=10000
# print(train .shape)
# print(y.shape)
for train index, test index in kf.split(train ):
     print("TRAIN:", train index, "TEST:", test index)
   x train, x test = new train.iloc[train index], new train.iloc[test index]
     wl1=np.zeros((x train.shape[1],1))
     print(X train.shape)
     print(X test.shape)
   y train, y test = y.iloc[train index], y.iloc[test index]
    print(y test.shape)
    reg.fit(x train, y train)
   y pred=reg.predict(x test)
   rmse=np.sqrt(np.sum(np.square(y pred-y test)))/len(y pred)
    print(rmse)
    if(rmse<best rmse):</pre>
       best_rmse=rmse
       best model=reg
     print(reg.score(new test,y1))
y=test['Rings']
new test=test.drop(['Rings'],axis=1)
```

RMSE for Ridge on test set

```
In [21]:

from sklearn.metrics import mean_squared_error

y=test['Rings']
new_test=test.drop(['Rings'],axis=1)
y_pred=best_model.predict(new_test)
rms = mean_squared_error(y, y_pred,squared=False)
rms

Out[21]:
```

0.08471285141421189

SkLearn Implementation of Lasso (L1)

In [22]:

```
from sklearn.linear model import Lasso
reg=Lasso(alpha=0.00001)
kf=model selection.KFold(n splits=5)
# train=kf.get_n_splits(train_)
# print(train .shape)
# print(y.shape)
y = train ['Rings']
new train = train .drop(['Rings'], axis=1)
# y1=test['Rings']
# new test=test.drop(['Rings'],axis=1)
# new test=np.array(new test)
best rmse=10000
# print(train .shape)
# print(y.shape)
for train index, test index in kf.split(train ):
     print("TRAIN:", train index, "TEST:", test index)
   x train, x test = new train.iloc[train index], new train.iloc[test index]
     wl1=np.zeros((x train.shape[1],1))
    print(X train.shape)
     print(X test.shape)
   y train, y test = y.iloc[train index], y.iloc[test index]
    print(y test.shape)
   reg.fit(x train, y train)
   y pred=reg.predict(x test)
   rmse=np.sqrt(np.sum(np.square(y pred-y test)))/len(y pred)
    print(rmse)
   if(rmse<best rmse):</pre>
       best rmse=rmse
       best model=reg
     print(reg.score(new test,y1))
y=test['Rings']
new test=test.drop(['Rings'],axis=1)
```

RMSE for Lasso on test set

```
In [23]:
```

0.08480590164862717

```
from sklearn.metrics import mean_squared_error

y=test['Rings']
new_test=test.drop(['Rings'],axis=1)
y_pred=best_model.predict(new_test)
rms = mean_squared_error(y, y_pred,squared=False)
rms
Out[23]:
```

The introduction of penalty (L1 and L2) does not seem to have much effect on the RMSE value. After running multiple runs of this code, no conclusive best model can be found. Sometimes L1 performs the best, sometimes L2 and sometimes no penalty is the best model. The RMSE values are very close to each other.

The inbuilt regression models give slightly lower RMSE (about 0.06)

Closed Form RMSE on validation set

In [24]:

```
kf=model selection.KFold(n splits=5)
y = train ['Rings']
new_train = train_.drop(['Rings'], axis=1)
# y1=test['Rings']
# new test=test.drop(['Rings'],axis=1)
# new test=np.array(new test)
idx=1
for train_index, test_index in kf.split(train_):
    x train, x test = new train.iloc[train index], new train.iloc[test index]
    y train, y test = y.iloc[train index], y.iloc[test index]
    w=np.dot(np.linalg.inv(np.dot(np.transpose(x train),x train)),np.dot(np.transpose(x
train),y train))
    y_pred=np.dot(x test,w)
    y_test=np.array(y_test)
   print("RMSE of fold "+str(idx)+":", np.sqrt(np.sum(np.square(y_pred-y_test)))/len(y_t
est))
    idx+=1
RMSE of fold 1: 0.0027954060476873955
RMSE of fold 2: 0.003147262374071904
```

```
RMSE of fold 1: 0.0027954060476873955

RMSE of fold 2: 0.003147262374071904

RMSE of fold 3: 0.002681020281461619

RMSE of fold 4: 0.0026932049414070255

RMSE of fold 5: 0.0029880871585471888
```