# Explainability of Neural Networks (XAI)

CPSC680: Trustworthy Deep Learning

Rex Ying

### Readings

- Readings are updated on the website (syllabus page)
- Lecture 5 readings:
  - **LIME** (local interpretation)
  - **SHAP** (attribution)

#### Content

Methods using Surrogate Models

Explainability via Attention

Counterfactual Explanations

#### Content

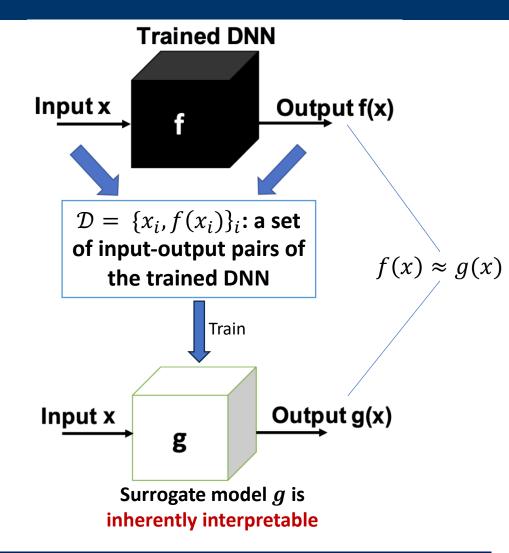
Methods using Surrogate Models

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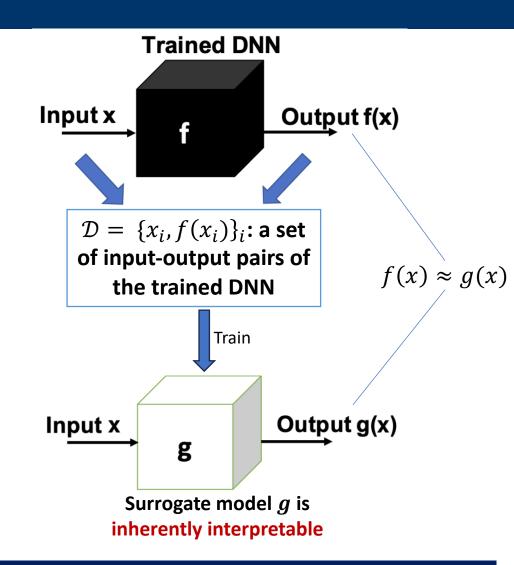
### Local Explanations with Surrogate Models

- Explanation with Surrogate Model
  - Post-hoc, model-agnostic explanation
  - Learn an inherently interpretable model (e.g. decision trees, linear models) that (locally) approximates the behaviors of the original model.
  - We can analyze the **local** behaviors of f around  $x_0$  using g.



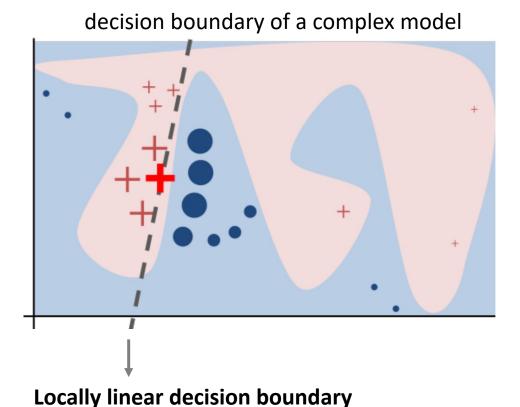
### Local Explanations with Surrogate Models

- Explanation with Surrogate Model
- Given input instance  $x_0$  and model f.
- Steps:
  - 1. Sample points around  $x_0$
  - 2. Use model to predict labels for each example  $(x_i, f(x_i))$
  - 3. Weight examples according to the distance to the input instance  $x_0$
  - 4. Learn a linear model on weighted samples
  - 5. Use simple linear model to explain



#### Intuition of LIME

Local Interpretable Model-Agnostic Explanations (LIME)



learned by LIME

- the pink and blue background: complex decision function f of the black-box model
- + : instance to be explained
- lacktriangle +: instances with different predicted labels by f
- Size of +: the proximity to the instance to be explained

(larger size ⇔ closer to the explained instance)

LIME samples instances around the given instance +, and weighs them by the **proximity** to the instance +. **Goal of LIME:** learn a local surrogate model around the given instance +

#### LIME for Tabular Data

#### LIME

- Given input instance  $x_0$  and model f.
- Steps:
- $\longrightarrow$  1. Sample points around  $x_0$ 
  - 2. Use model to predict labels for each example  $(x_i, f(x_i))$
  - 3. Weight examples according to the distance to the input instance  $x_0$
  - Learn a linear model on weighted samples
  - 5. Use simple linear model to explain

#### **Sampling Mechanism**

- For continuous features: Adding a Gaussian noise  $x_i \sim \mathcal{N}(x_0, \sigma I)$
- For categorical features: perturb by sampling according to the training distribution

#### LIME for Tabular Data

#### LIME

- Given input instance  $x_0$  and model f.
- Steps:
  - 1. Sample points around  $x_0$
  - 2. Use model to predict labels for each example  $(x_i, f(x_i))$
- $\longrightarrow$  3. Weight examples according to the distance to the input instance  $x_0$ 
  - 4. Learn a linear model on weighted samples
  - 5. Use simple linear model to explain

#### **Weighting Function**

 $\pi_{x_0}(z)$ : similarity kernel for the recovered representation z around the original input  $x_0$ 

$$\pi_{x_0}(x_i) = e^{-\frac{\mathbf{D}(x_0, x_i)^2}{\sigma^2}}$$

- **D** is the distance function (e.g.,  $L_2$  distance)
- $\sigma$  is a hyper-parameter for the kernel

LIME targets at **local approximation**  $\Rightarrow$  samples z with relatively larger  $\pi_{x_0}(z)$  (i.e., smaller distance  $D(x_0, x_i)$ ) should have larger weights during the training of the surrogate model

#### LIME for Tabular Data

#### LIME

- Given input instance  $x_0$  and model f.
- Steps:
  - 1. Sample points around  $x_0$
  - 2. Use model to predict labels for each example  $(x_i, f(x_i))$
  - 3. Weight examples according to the distance to the input instance  $x_0$
- 4. Learn a linear model g on weighted samples
  - 5. Use simple linear model to explain

#### **Training Objective**

The training objective of LIME to search a surrogate model around input x:

$$g^* = \operatorname*{argmin}_{g \in \mathcal{G}} \mathcal{L}\left(f, g, \pi_{x_0}\right) + \Omega(g)$$

- $\mathcal{G}$  is the class of interpretable models (linear model or decision tree)
- $\mathcal{L}(f, g, \pi_{x_0})$  is the loss function penalizes the differences between f and g
- $\Omega(g)$  controls the complexity of the model g

### LIME for Tabular Data: Objective and Loss

**Training objective** of LIME to search a surrogate model around input  $x_0$ :

$$g^* = \underset{g}{\operatorname{argmin}} \, \mathcal{L}\left(f, g, \pi_{\chi_0}\right) + \underbrace{\Omega(g)} \longrightarrow \underset{\text{the interpretable model}}{\operatorname{Control complexity of}}$$

where

$$\mathcal{L}(f,g,\pi_{x_0}) = \sum_{\substack{x_i \in \mathcal{D} \\ \pi_{x_0}(x_i) = e^{\frac{D(x_0,x_i)^2}{\sigma^2}}}} \pi_{x_0}(x_i) \left(f(x_i) - g(x_i)\right)^2$$
 optimize  $g$  to locally approximate the behavior of  $f$ 

- $\Omega(g)$ : a measure of **complexity** of the surrogate mode g
  - $\Omega(g)$ : the depth of tree for a decision tree; the number of weights for a linear model
  - A simple local surrogate is prefered! (Occam'z Razor)
  - Lasso is a possible choice

### LIME for Images: Data Representation (1)

- Given an original input  $x \in \mathbb{R}^d$ , let  $x' \in \{0, 1\}^M$  denote a binary vector as its interpretable representation
  - *M* is the number of features in the interpretable representation
  - For images, x' can be a binary vector indicating the "presence" or "absence" of a patch of similar pixels
  - For text, x' can be a binary vector indicating the "presence" or "absence" of a word
  - Example:



1 denotes "presence" of the pixel 0 denotes "absence" of the pixel

0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0
0	0	0	1	1	1	0	0	0
0	0	1	1	1	1	0	0	0
0	0	1	1	1	1	0	0	0
0	0	1	1	1	1	0	0	0
0	0	1	1	1	0	0	0	0
0	0	0	0	0	0	0	0	0

x: Original image

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x': Interpretable representation

### Choice of Interpretable Representation

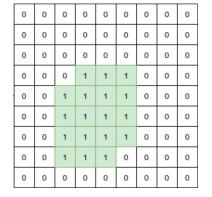
- Given an original input  $x \in \mathbb{R}^d$ , let  $x' \in \{0, 1\}^M$  denote a binary vector as its interpretable representation
  - In the context of images, a segmentation method can be used to decompose the image into interpretable components (see skimage.segmentation)



Original Image



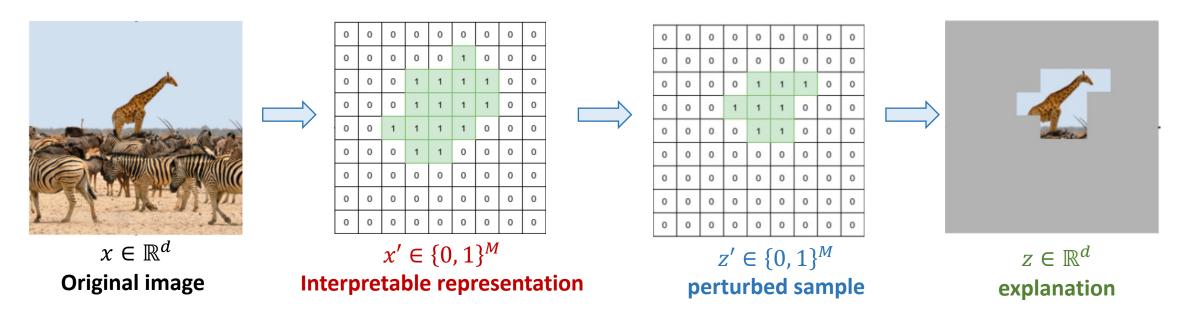
Interpretable Components



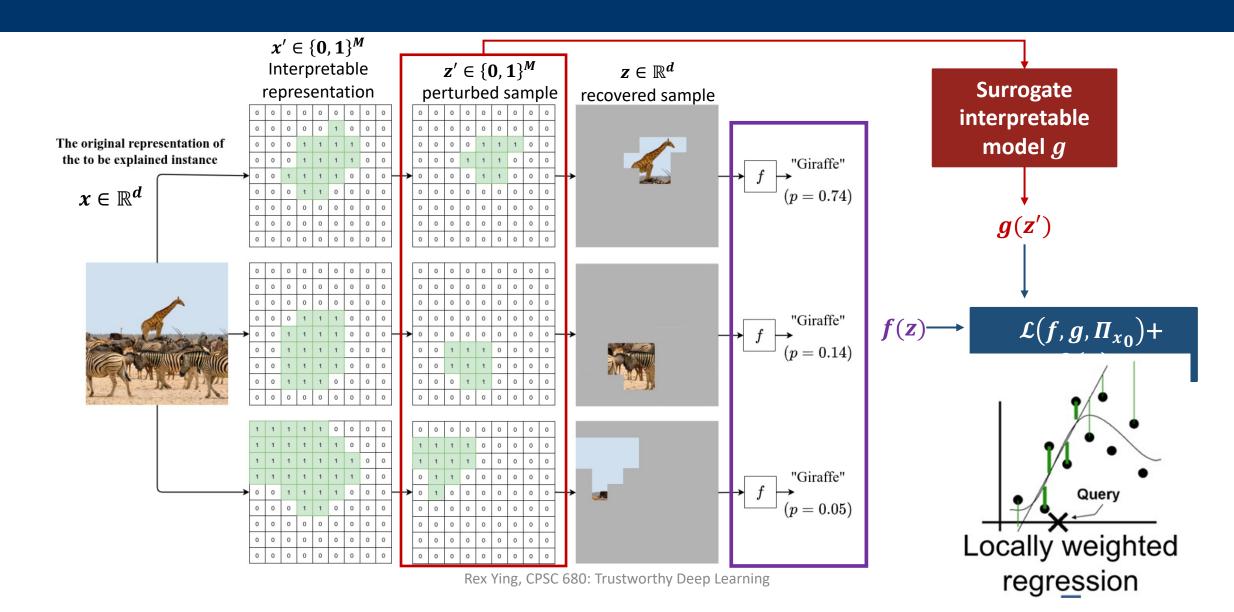
Mask corresponding to a super-pixel (segment)

### Details of LIME: Data Representation (2)

- Based on an interpretable representation  $x' \in \{0, 1\}^M$ , a perturbed sample  $z' \in \{0, 1\}^M$  contains a fraction of the nonzero elements of x'
- $z \in \mathbb{R}^d$ : recovered explanation in the original domain
- Example:

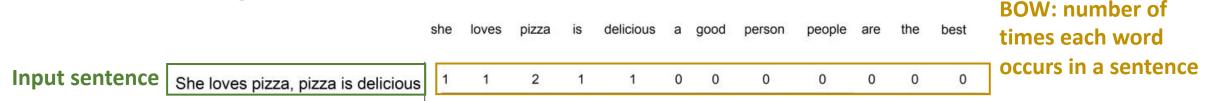


### LIME for Images - Architecture



### Evaluation: important feature selection (1)

- Dataset: sentiment analysis datasets (BOOKs and DVDs)[1]
- Features: bag of words (BOW)

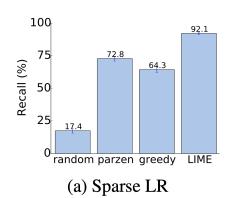


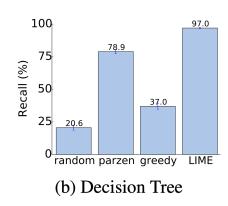
- Measure faithfulness of explanations for classifiers that are intrinsically interpretable
  - Train a sparse logistic regression or decision tree to select 10 most important features as the ground truth
- Generate explanations for each prediction in the test set and compute the fraction of truly important features recovered by the explanations

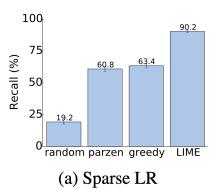
# Evaluation: important feature selection (2)

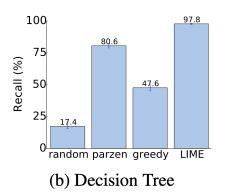
#### • Baselines:

- Random: randomly pick 10 features
- Parzen: pick 10 features with the highest absolute gradients
- **Greedy:** greedily remove 10 features that contribute the most to the predicted class and take these 10 features as an explanation
- Recall:  $\frac{TP}{TP+FN}$  (true positive rate; TP: True Positive, FN: False Negative)









LIME provides faithful explanations with > 90% recall for both logistic regression and decision trees!

**BOOKs dataset** 

**DVDs** dataset

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# Shapley Additive Explanation

- SHAP: a local additive feature attribution methods based on Shapley values for each input feature
- Given a black-box model f and an input  $x \in \mathbb{R}^d$  to be explained
  - $z \in \{0,1\}^M$ : interpretable representation of x

recall the representation used in LIME

- $h_{\chi}$ :  $\{0,1\}^M \to \mathbb{R}^d$  recovering function that maps to original domain  $\mathbb{R}^d$
- Surrogate model:

null output

Shapley value of the *i*-th feature

$$g(z) = \phi_0 + \sum_{i=1}^{M} \phi_i z_i$$

- $z_i \in \{0,1\}$ : the *i*-th element of  $z_i$ , indicating the presence/absence of the *i*-th feature
- g(z) locally approximates f(x) when  $x = h_x(z)$

map to the original domain

- The concept of Shapley values is originally from cooperative game theory
- Cooperative games model scenarios where agents can benefit by cooperating together and a binding agreement.
  - Probably not the part of game theory you've heard of

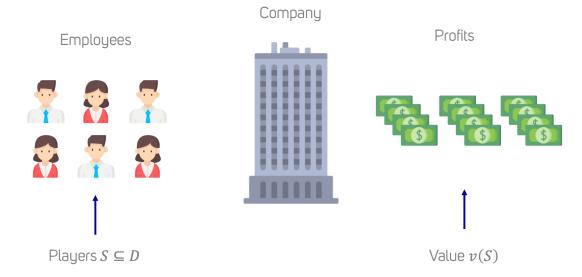
#### **Cooperative game**

- Players can benefit by cooperating
- Binding agreements are possible
- Answer the question: How to divide the surplus when joining the grand coalition?

#### Non-cooperative game

- Players are independent
- No cooperation, focus on individual actions
- Answer the question: What is the "good" strategy for each player to maximize their individual return?

• Example of a cooperative game:



- Question: How to measure each player's contribution? How to divide a surplus (profit) to shareholders so that everyone is satisfied?
- Lloyd Shapley's idea: members should receive payments proportional to their average marginal contributions ⇒ Shapley Values

- Consider the following example where there are three players and got 19\$
- The marginal contribution of player A

• to coalition 
$$S = \emptyset$$
 is  $7 - 0 = 7$ \$

• to coalition 
$$S = \{B\}$$
 is  $7 - 4 = 3$ \$

• to coalition 
$$S = \{C\}$$
 is  $15 - 6 = 9$ \$

• to coalition 
$$S = \{B, C\}$$
 is  $19 - 9 = 10$ \$

The player A should get

$$\frac{1}{3} \left( \frac{1}{\binom{2}{0}} \right)^{7} + \frac{1}{\binom{2}{1}} 3 + \frac{1}{\binom{2}{1}} 9 + \frac{1}{\binom{2}{2}} 10 \right) = 7.667$$

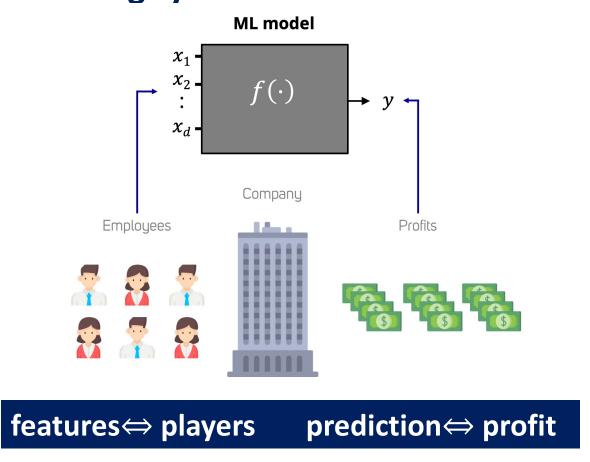
Marginal contribution



Every coalition with the same size is equally likely to appear

All sizes are equally likely to appear.

In context of a deep learning system:



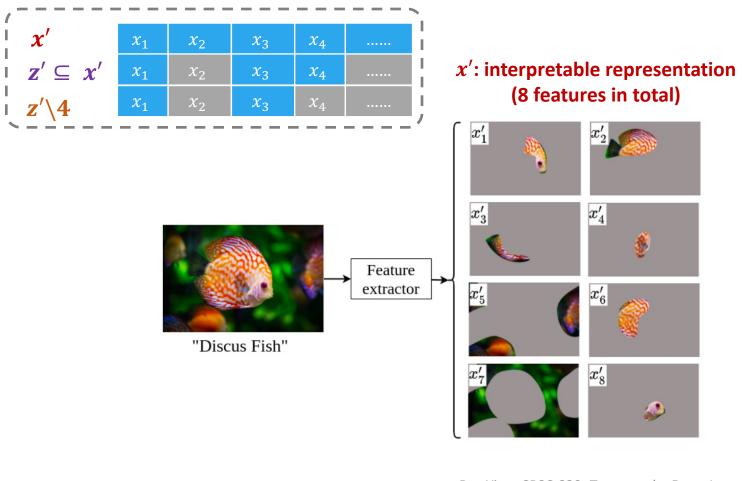
### Calculating Shapley Values

- f: black-box model;  $x \in \mathbb{R}^d$ : input to be explained;  $h_x$ : recovering map to  $\mathbb{R}^d$
- Shapley value for the *i*-th input feature:

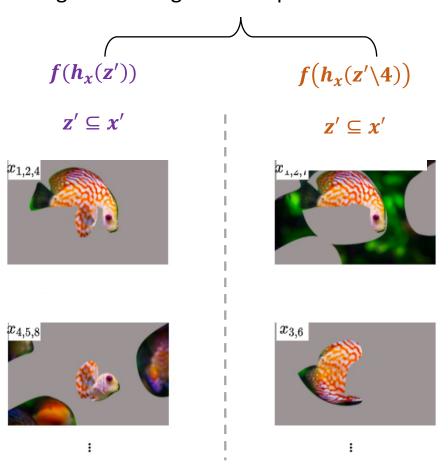
- $z' \subseteq x'$  represents all z' vectors where the non-zero entries are a **subset** of the non-zero entries in x'
- |z'|: the number of none-zero entries in z'
- *M*: number of features in the **interpretable representation**

### Example of SHAP

#### Example: calculating the **Shapley value of feature 4**:



Compute  $f(h_x(z')) - f(h_x(z' \setminus 4))$ , and weighted average over all possible subset z'



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# Properties of SHAP (1)

• Linearity: The importance score of a linear combination of two models is a linear combination of the importance score

$$\phi_i(f_1 + \alpha f_2) = \phi_i(f_1) + \alpha \phi_i(f_2)$$

• **Dummy:** If the model is not sensitive to a feature, its importance score should be zero

$$\forall z \ \delta_i(z) = f(h_x(z)|z_i = 1) - f(h_x(z)|z_i = 0) \Rightarrow \phi_i = 0$$

• Symmetry: Symmetric features get similar importance scores

$$\forall z \ \delta_i(z) = \delta_j(z) \Rightarrow \phi_i = \phi_j$$

• **Efficiency**: The sum of importance scores of all features recovers the prediction

$$f(x) = g(z) = \phi_0 + \sum_{i=1}^{M} \phi_i z_i$$

The model output is fully distributed to all input features.

# Properties of SHAP (2)

• **Theorem:** Shapley value is a *unique* solution concept that satisfies four axioms: *linearity, dummy, symmetry,* and *efficiency*.

- **Pros: This uniqueness** implies that the Shapley values is the "best" (only one) method to allocate importance scores to input features if we accept four properties (axioms)
- Cons: Computationally expensive.
  - E.g., to compute exactly the Shapley value with 50 features, we need to compute the summation over  $2^{50} > 10^{15}$  perturbation  $z' \in Z$ .
  - We need to do Monte-Carlo sampling to approximate the Shapley values.
     In practice, 1000 10000 perturbations are sufficient.

### The equivalence between LIME and SHAP

• Theorem: The Shapley values is a special case of the LIME framework

#### LIME

LIME solves the following optimization problem

$$w^* = \underset{w}{\operatorname{argmin}} \sum_{x \in \mathfrak{D}} \pi_x(z) [f(x) - (w^{\mathsf{T}}x + b)]^2 + \Omega(w)$$

where  $\mathcal{D}$  is the set of perturbations around  $x_0$ 

#### **SHAP**

Importance score using Shapley value

$$\phi_i = \sum_{z' \subseteq x'} \frac{|z'|! (M - |z'| - 1)!}{M!} [f(\mathbf{h}_x(z')) - f(\mathbf{h}_x(z' \setminus i))]$$

x' is the interpretable representation of x

$$\mathbf{f} = \mathbf{\Omega}(w) = 0$$

$$\mathbf{f} = \mathbf{\Omega}(w) = \frac{M-1}{M}$$

$$\binom{|z|}{|z|} |Z|(M-|z|)$$

Then  $w^* = \phi_i$ 

See proof in the original paper

#### Content

Methods using Surrogate Models

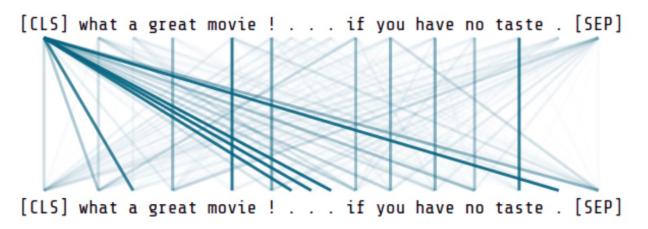
Explainability via Attention

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### Explainability via Attention

#### Attention Mechanisms

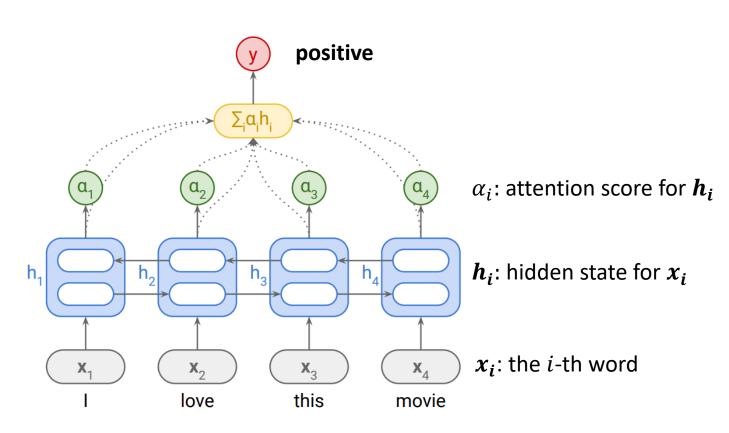
- DNNs can be endowed with attention mechanisms that simultaneously
  - preserve or even improve their performance
  - obtain explainable outputs
- Visualize attention weights in a attention models:



Color represents the value of attention weight darker blue ⇔ larger attention weight

#### Attention in Text Classification

#### **BiLSTM for sentiment analysis (text classification)**



#### **Attention score:**

$$\alpha_i = \frac{\exp e_i}{\sum_k \exp e_k}$$

where  $e_i = \mathbf{v}^{\mathsf{T}} \tanh(W_h \mathbf{h}_i + W_q \mathbf{q})$  and  $\mathbf{v}$ ,  $\mathbf{q}$ ,  $W_h$ ,  $W_q$  are learnable parameters (example of **MLP-based attention**)

 $\alpha_i$  shows the **importance** of the word  $x_i$  to the prediction "y = positive"

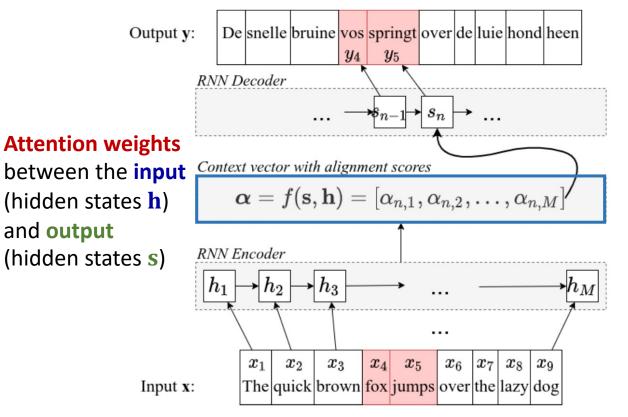


Bastings, Jasmijn, and Katja Filippova. "The elephant in the interpretability room: Why use attention as explanation when we have saliency methods?."

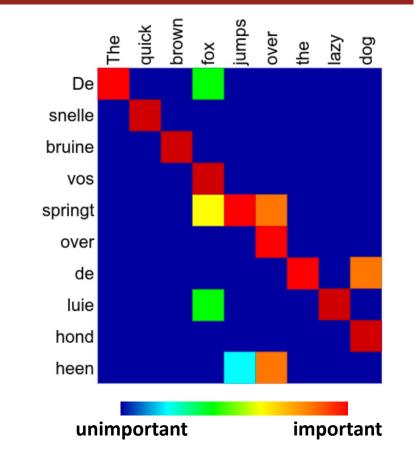
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### Attention in Sequential Generation

#### **RNN** model for Natural Language Translation



Attention weights  $\alpha_{ij}$  shows the importance of input  $x_i$  to the output  $y_i$ 



Ras, Gabrielle, et al. "Explainable deep learning: A field guide for the uninitiated."

# Signed Attention (1)

- Attention weight is always positive
- Ideal explanation should discriminate between positive and negative contributions towards a prediction
- Solution: signed attention

$$A_i = -\frac{\partial \mathcal{L}}{\partial \alpha_i} \times \alpha_i$$
 Indicates the positive or negative contribution

• L: loss function

- $\alpha_i$ : original attention weight
- value of  $\alpha_i$  measures the strength of the contribution

Recap: for hidden state  $\mathbf{h_i}$  attention weight:  $\alpha_i = \frac{\exp e_i}{\sum_k \exp e_k} \geq 0$  where  $e_i = \mathbf{v}^{\top} \tanh (W_h \mathbf{h}_i + W_q \mathbf{q})$   $\mathbf{v}, \mathbf{q}, W_h, W_q$ : learnable parameters

# Signed Attention (2)

#### **Explanation for sentiment analysis**

Input: "Though the price may be tooexpensive, I love its surprisingly high quality."

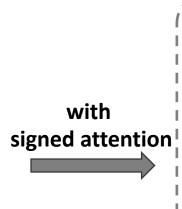
**Output:** y = "Positive"



Though the price may be too expensive, I love its surprisingly high quality.

unimportant

important



#### signed attention visualization

Though the price may be too expensive, I love its surprisingly high quality.

negative

neutral

positive

#### Content

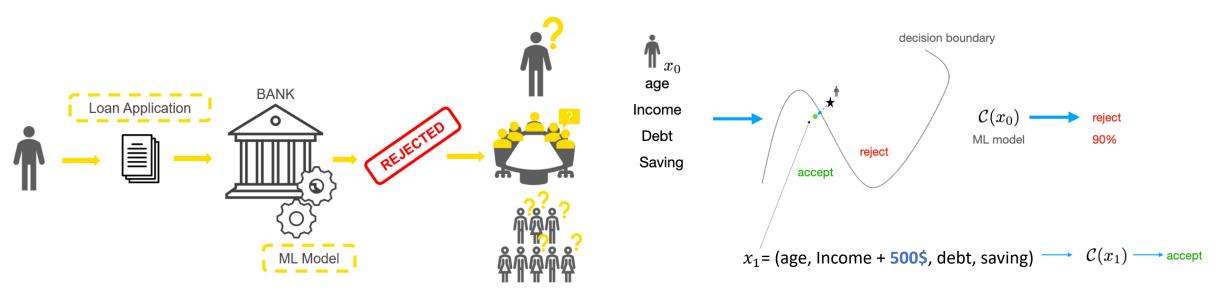
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Counterfactual Explanation

### Counterfactual Explanations

- Counterfactual explanation considers "what-if" scenarios of model predictions, addressing the question of how slight adjustments in the input can lead to different model predictions.
  - useful in consequential applications such as loan approvals, university admission, etc.



You should increase your income by 500\$ in order to be accepted

### Counterfactual Explanations

- Goal: Find a counterfactual example
  - can change the model prediction to a desired outcome
  - a change in the input instance should be minimal in order to reduce the implementation cost for users (loan applicants, students, etc)

• Formulation:  $x_{CF} = \underset{x' \in \mathcal{X}}{\operatorname{argmin}} d(x_0, x')$  Counterfactual Explanation  $s. t. \quad f(x') = y^{\operatorname{target}}$  Constraint to get desired outcome

### Counterfactual Explanations

Formulation:

$$x_{CF} = \underset{x' \in \mathcal{X}}{\operatorname{argmin}} d(x_0, x')$$
  
 $s.t. \quad f(x') = y^{\text{target}}$ 

The above problem has a non-linear constraint, which is difficult to solve

Reformulation: Using Largange multipliers to convert to unconstrained optimization problem:

$$x_{CF} = \underset{x' \in \mathcal{X}}{\operatorname{argmin}} d(x_0, x') + \lambda \mathcal{L}(f(x'), y^{\text{target}})$$
Lagrange multiplier

where

$$\mathcal{L}(f(x'), y^{\text{target}}) = (f(x') - y^{\text{target}})^2$$
 Least Square Error

This problem is differentiable and can be solved by Projected Gradient Descent Algorithm

# Summary

# Q & A