Yale

Machine Unlearning

CPSC 471/571: Trustworthy Deep Learning

Rex Ying

Content

- Machine Unlearning
 - Introduction and Motivation
 - Unlearning Definition
 - Model-agnostic Approach
 - Boundary Unlearning
 - Model-intrinsic Approach
 - Projective Residual Update for Linear Models
 - Forget-Me-Not for Attention Model
 - SalUn for Diffusion Model
 - Data-driven Approach
 - SISA Training

Content

- Machine Unlearning
 - Introduction and Motivation
 - Unlearning Definition
 - Model-agnostic Approach
 - Boundary Unlearning
 - Model-intrinsic Approach
 - Projective Residual Update for Linear Models
 - Forget-Me-Not for Attention Model
 - SalUn for Diffusion Model
 - Data-driven Approach
 - SISA Training

Real-world Use Cases

• There is a need for **information removal** from ML systems e.g., user's request, inappropriate information, sensitive data, outdated or inaccurate information.



Privacy Protection



Healthcare Data Sensitivity



Personal Identity Unlearning

Machine Unlearning Motivation

- Motivation: enable the ML system to delete and unlearn certain information to address the privacy concerns that arise from the data storage.
- Naïve Solution: Remove data point and retrain the model from scratch (exact unlearning of the data)
- However, the cost of retraining is increasingly expensive as ML models are trained on large datasets.

Focus of this lecture: how to efficiently and effectively unlearn certain information?

Machine unlearning | European Data Protection Supervisor

<u>Machine Unlearning – A Potential Option for Remedy?</u>

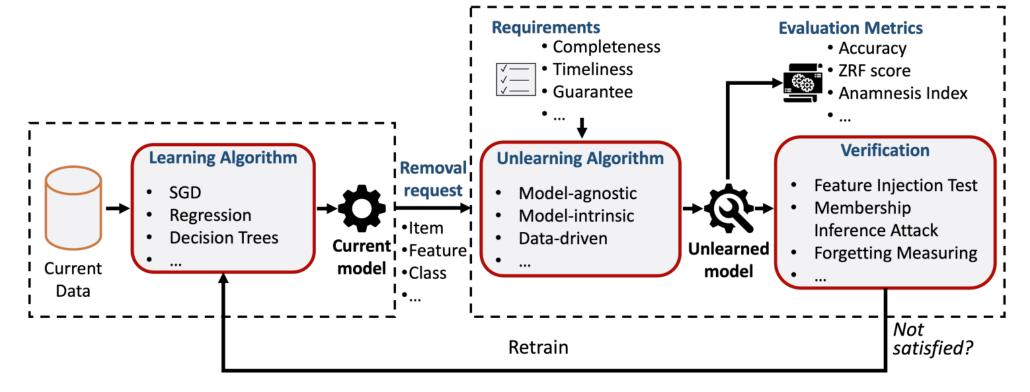
Leveraging Per-Example Privacy for Machine Unlearning

<u>Deep Forgetting & Unlearning for Safely-Scoped LLMs —</u>

AI Alignment Forum

Machine Unlearning Setting

Goal of Machine Unlearning: To design efficient (low retraining cost)
unlearning protocols that satisfy guarantees of data removal and model
performance



Types of Unlearning Requests

Item / data removal

• Requests to remove certain items/data points from the training set

Feature removal

- Malicious or sensitive features that are present in a set of data
- Requests to remove certain features in a set of training data

Class/label removal

Examples?

- The samples to be forgotten belong to a single class
- Requests to remove the entire class and the samples belonging to it.

Concept removal

Requests to remove specific knowledge or patterns learned by a model

Design Requirements

- Completeness (Consistency): the unlearned model and the re-trained model should make the same predictions about training samples.
 - Usually formulated as an optimization objective in an unlearning algorithm
- Timeliness and light-weight: the unlearned model should be more efficient than retraining and light-weight
- Model-agnostic: an ideal unlearning algorithm should be generic for different machine learning models.
- Provable guarantees: the unlearning algorithm should be able to provide provable guarantees of unlearning

Machine Unlearning Approaches

Model-agnostic Approaches

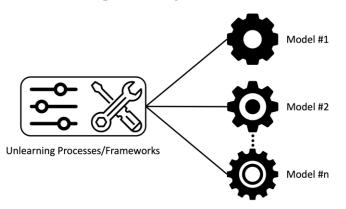
• Machine unlearning processes or frameworks that are applicable for different models, such as linear models, deep neural networks, etc.

Model-intrinsic Approaches

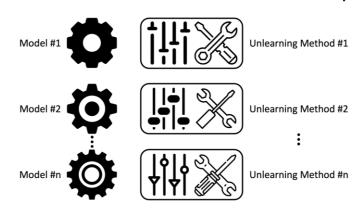
Machine unlearning methods designed for a specific type of models.

Data-driven Approaches

• Using data partition, data augmentation and data influence to speed up the retraining process.

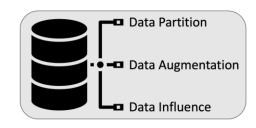


Model-agnostic Approaches



Model-intrinsic Approaches

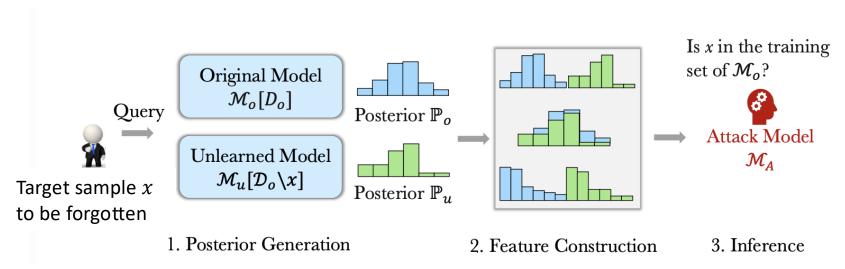
<u>Figure source</u>



Data-driven Approaches

Unlearning Verification

- Goal: verify the effectiveness of the machine unlearning by detecting information leaks
- Methods: membership inference, feature injection test, backdoor attacks, etc.
- Recall the threats to information exposure:
 - e.g., membership inference attack is trained to predict whether a data item belongs to the training set. Hence, it can be used in unlearning verification



Chen, Min, et al. "When machine unlearning jeopardizes privacy."

Rex Ying, CPSC 471/571: Trustworthy Deep Learning

Content

- Machine Unlearning
 - Introduction and Motivation
 - Unlearning Definition
 - Model-agnostic Approach
 - Boundary Unlearning
 - Model-intrinsic Approach
 - Projective Residual Update for Linear Models
 - Forget-Me-Not for Attention Model
 - SalUn for Diffusion Model
 - Data-driven Approach
 - SISA Training

Definition of Unlearning (1)

- Train a model $A: \mathcal{Z}^* \to \mathcal{H}$, where \mathcal{Z}^* : all possible training datasets; \mathcal{H} : a hypothesis space of all possible machine learning models
- $D_f \subset D$ denotes the forgetting dataset, D is the original dataset
- $U(D, D_f, A(D))$: the unlearned model;
- $A(D \setminus D_f)$: the retrained model from scratch.
- Exact Unlearning: the distributions of $U(D,D_f,A(D))$ and $A(D\backslash D_f)$ are exactly the same.

 distribution of the parameters / outputs
- Approximate Unlearning: the distance between distributions of $U(D, D_f, A(D))$ and $A(D \setminus D_f)$ is bounded.

Definition of Unlearning (2)

• **Definition [Exact Unlearning]** Given a learning algorithm $A(\cdot)$, the unlearning algorithm $U(\cdot)$ is an exact unlearning process iff $\forall \mathcal{T} \subseteq \mathcal{H}, D \in \mathcal{Z}^*, D_f \subset D$:

$$\Pr(A(D \setminus D_f) \in \mathcal{T}) = \Pr(U(D, D_f, A(D)) \in \mathcal{T})$$

where $Pr(\cdot)$ is the distribution of the parameters / outputs of the model over a function space \mathcal{T} .

• **Definition** [ε -Approximate Unlearning] Given a learning algorithm $A(\cdot)$, the unlearning algorithm $U(\cdot)$ is an ε -approximate unlearning process iff $\forall \mathcal{T} \subseteq \mathcal{H}, D \in \mathcal{Z}^*, z \in D$:

$$e^{-\varepsilon} \le \frac{\Pr(U(D, z, A(D)) \in \mathcal{T})}{\Pr(A(D \setminus z) \in \mathcal{T})} \le e^{\varepsilon}$$

where z is the single removed sample

Relationship to DP

Recall differential privacy:

$$\forall \mathcal{T} \subseteq \mathcal{H}, D \text{ and } z \in D, e^{-\varepsilon} \leq \frac{\Pr(A(D) \in \mathcal{T})}{\Pr(A(D \setminus z) \in \mathcal{T})} \leq e^{\varepsilon}$$

where z is the single removed sample.

• ε -Differential Privacy implies ε -approximate unlearning.

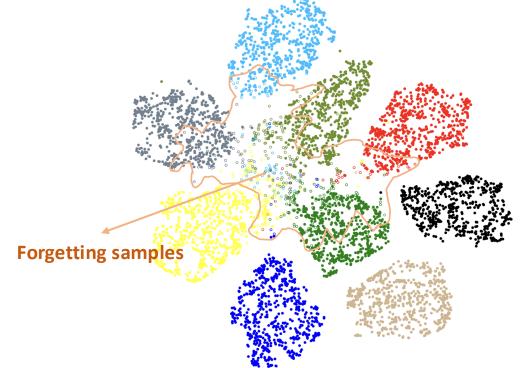
Note: ε -differential privacy is a very strong condition. If $A(\cdot)$ is differentially private for any data, then it will **suffer significant accuracy loss**!

Content

- Machine Unlearning
 - Introduction and Motivation
 - Unlearning Definition
 - Model-agnostic Approach
 - Boundary Unlearning
 - Model-intrinsic Approach
 - Projective Residual Update for Linear Models
 - Forget-Me-Not for Attention Model
 - SalUn for Diffusion Model
 - Data-driven Approach
 - SISA Training

Decision Space of an Unlearned Model

Colors represent Classes (Figure source)



The decision space of the model retrained on the remaining dataset from scratch

- The solid dots are remaining samples.
- The hollow circles are the forgotten samples

Observation:

- the forgetting samples spread around the decision space of the retrained model
 - => the decision boundary of the forgetting samples has been broken after unlearning
- most of the forgetting samples move to the borders of other clusters
 - => samples at the cluster borders in the decision space will be predicted with large uncertainty.

Boundary Unlearning (1)

 Motivation: Boundary unlearning shifts the decision boundary of the original model to imitate the decision behavior of the retrained model

Guideline:

- Destroy the boundary of the forgetting class
- Maintain the boundary of the remain classes
- Push the forgetting data to the border of other clusters
- Boundary Unlearning is a model-agnostic method with two approaches:
 - Boundary Shrink: breaks the decision boundary of the forgetting class
 - Boundary Expanding: disperse the forgetting class

Boundary Unlearning (2)

- $\mathcal{D} = \{x_i, y_i\}_{i=1}^N$ is the training dataset. $\mathcal{Y} = \{1, ..., K\}$ denotes the label space where K is the total number of classes. \mathcal{D}_f is the forgetting dataset.
- ullet Parameters of the original model and the unlearned model are $oldsymbol{ heta}_o$ and $oldsymbol{ heta}_u$
- Boundary unlearning is designed for the case where \mathcal{D}_f consists of the samples of an entire class, e.g., class y (a limitation of the work)
- Unlearning Objective:

The predicted label on the forgetting samples is different from the unlearning label \boldsymbol{y}

$$\underset{k}{\operatorname{argm}} ax f_{\boldsymbol{\theta_u}}^{k}(\boldsymbol{x_f}) \neq y \text{ for } \forall \boldsymbol{x_f} \in \mathcal{D}_f,$$

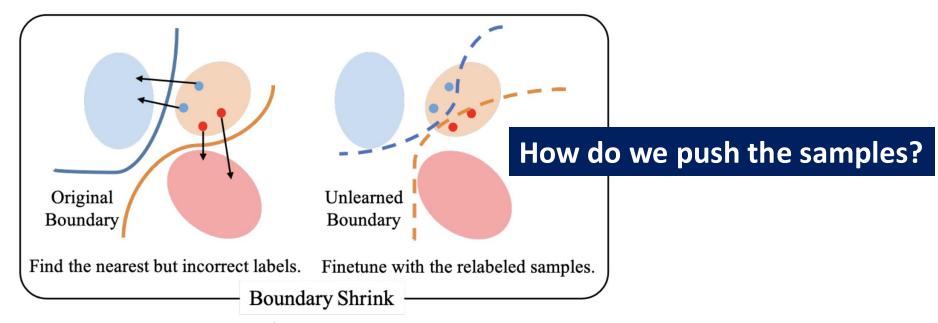
where f^k indicates the logit output on the k-th class

Boundary Shrink (1)

• Finetuning with random labels on forgetting samples will make them too conspicuous, since they are predicted with **excessive uncertainty**.

 Instead, Boundary Shrink pushes the forgetting samples close to the new decision boundary, making the predictions on these forgetting samples with

low certainty.



Boundary Shrink (2)

• (a) Given an initial forgetting sample x_f , update its corrupted example by neighbor searching with a noise bound ϵ :

$$\mathbf{x'}_f = \mathbf{x}_f + \epsilon \cdot \operatorname{sign}\left(\nabla_{\mathbf{x}_f} \mathcal{L}(\mathbf{x}_f, y, \boldsymbol{\theta_o})\right) \begin{vmatrix} \operatorname{sign}(x) := \begin{cases} -1 & \text{if } x < 0, \\ 0 & \text{if } x = 0, \\ 1 & \text{if } x > 0. \end{cases}$$

• (b) Get *nearest but incorrect (nbi)* labels y_{nbi}^f :

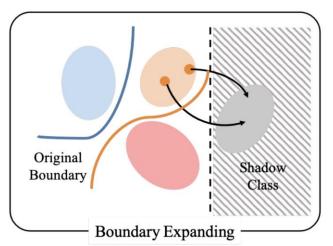
$$y_{nbi}^f \leftarrow \operatorname{softmax}(f_{\theta_o}(x_f'))$$

• (c) Finetune the original model with $oldsymbol{y_{nbi}^f}$ for forgetting samples $oldsymbol{x_f}$:

$$\theta_{u} = \operatorname{argmin}_{\theta}(\sum_{\left(x_{f}, y_{nbi}^{f}\right) \in \mathcal{D}_{f}} \mathcal{L}\left(x_{f}, y_{nbi}^{f}, \theta\right))$$

High-level Intuition of Boundary Expanding

- Recall: in the previous observation, most forgetting samples move to the border of other clusters on the retrained model. Therefore, they are predicted as other classes with low certainty.
- Lower certainty means that the output probabilities (from logits) are more evenly distributed.
- Boundary Expanding assigns all forgetting samples to an extra shadow class of the original model, which will exploit a new area in the decision space.



Boundary Expanding

• The model is finetuned with the forgetting samples x_f and the shadow class label y_{shadow} :

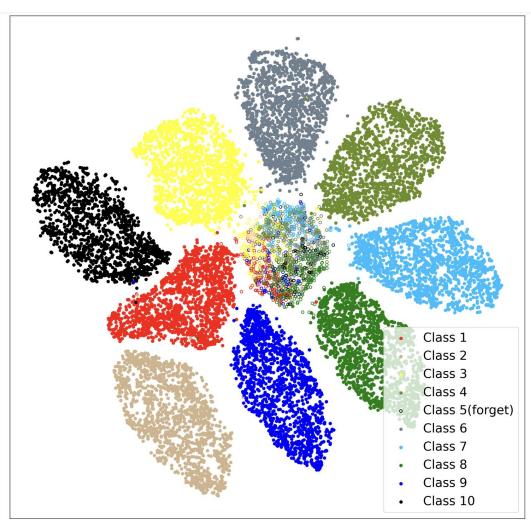
$$\theta_u = \underset{\theta}{\operatorname{argmin}} \sum_{(x_f, y_{shadow}) \in \mathcal{D}_f} \mathcal{L}(x_f, y_{shadow}, \theta)$$

an additional neuron is added at the last layer of the original model for y_{shadow}

• The logit output $f_{\theta_u}(x_f)$ for forgetting sample $x_f \in \mathcal{D}_f$ tends to be **low** and **even** on the original classes => disperse in the decision space of the retrained model.

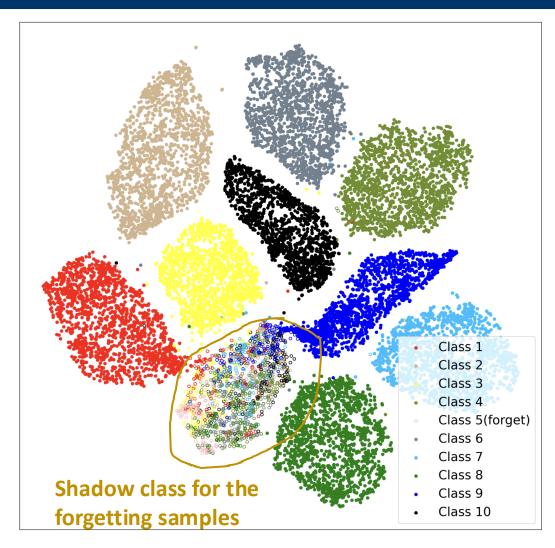
Use the logit output on the original classes during inference stage.

Decision Space (After Boundary Shrink)



- 1. the forgetting data (hollow circles) are predicted **as the nearest classes** after applying Boundary Shrink.
- 2. Some hollow circles move to other clusters, indicating that **the decision space of the forgetting class is split** by its near classes.
- 3. The clusters of remaining classes still keep compact.

Decision Space (After Boundary Expanding)



- 1. The cluster of the forgetting samples is pushed away from the center, creating a shadow class.
- 2. The clusters of remaining classes are maintained.

Content

- Machine Unlearning
 - Introduction and Motivation
 - Unlearning Definition
 - Model-agnostic Approach
 - Boundary Unlearning
 - Model-intrinsic Approach
 - Projective Residual Update for Linear Models
 - Forget-Me-Not for Attention Model
 - SalUn for Diffusion Model
 - Data-driven Approach
 - SISA Training

Forget-Me-Not: Concept Forgetting

 A concept is an abstract term representing an intuited object of thought, which also serves as the foundation for people's perceptions.

• Forget-Me-Not is an efficient, plug-and-play method for concept forgetting

and correction.

Concept Forgetting:

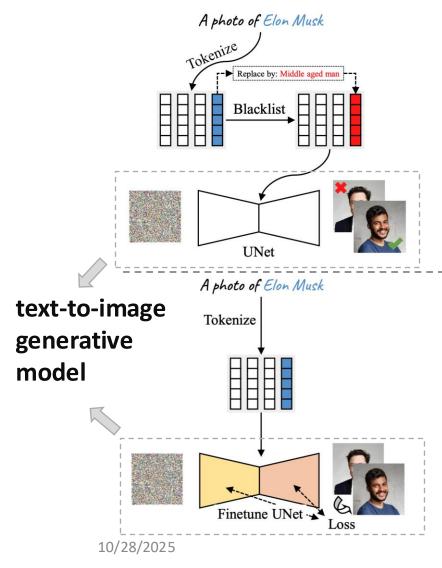
target concepts are removed and forgotten without compromising the output quality (Van Gogh in this case)





Concept Correction & Disentangle: correct a dominant or undesired concept in a prompt

Naïve Forgetting



Target concept to forget: Elon Musk

(a) Token Blacklist: simply replace the target tokens with a different one.

Downsides:

- Does not achieve good forgetting effect.
- May inadvertently affect other concepts that share the same/similar prompt.

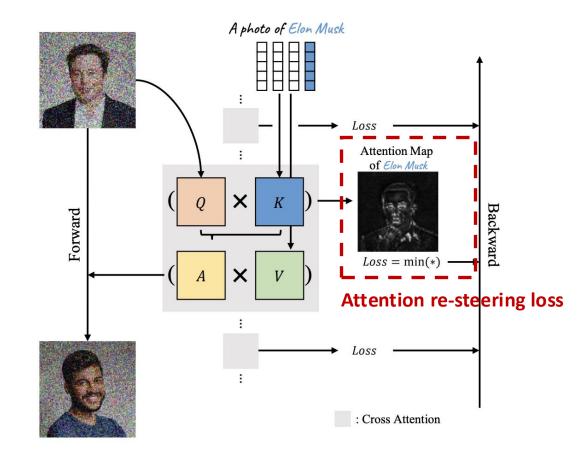
(b) Naïve Finetuning: finetune model weights such that the new weights generate outputs with unrelated concepts

Downside:

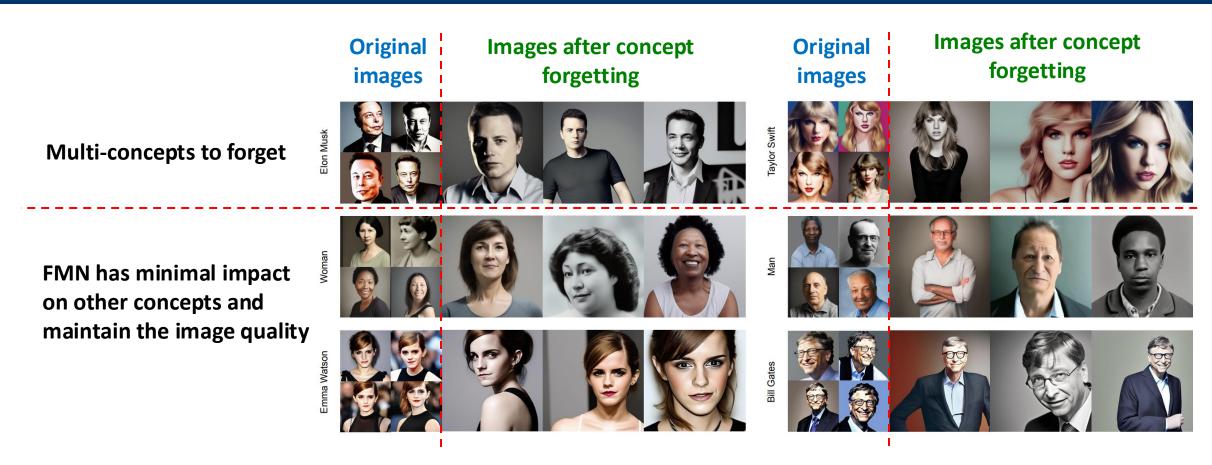
- It breaks model integrity by simultaneously corrupting other unrelated concepts during its finetuning process.

FMN: Attention Re-steering

- Forget-Me-Not (FMN) is a modelintrinsic approach for all attention-based text-to-image generative models.
- Attention Resteering:
 - Locate the part of text embeddings associated with the forgetting concepts.
 - Compute the attention maps between input features and these embeddings
 - Minimize the attention maps and backpropagate the network



Results on Multi-Concept Model



FMN (1) successfully removes the concepts of Elon Musk and Taylor Swift, (2) while maintaining the image quality with unrelated concepts.

Content

- Machine Unlearning
 - Introduction and Motivation
 - Unlearning Definition
 - Model-agnostic Approach
 - Boundary Unlearning
 - Model-intrinsic Approach
 - Projective Residual Update for Linear Models
 - Forget-Me-Not for Attention Model
 - SalUn for Diffusion Model
 - Data-driven Approach
 - SISA Training

SalUn: Saliency-based Unlearning

- Motivation of SalUn: utilize weight saliency to identify model weights that are sensitive to the forgetting data/class/concept.
- SalUn is a model-intrinsic approach for diffusion-based models on image tasks (e.g., image classification and image generation).

• recall the notations:

 $\mathcal{D} = \{ \mathbf{z}_i = (\mathbf{x}_i, \mathbf{y}_i) \}_{i=1}^N$ is the original N data points with data feature \mathbf{x}_i and label \mathbf{y}_i . $\mathcal{D}_f \subseteq \mathcal{D}$ denotes the forgetting dataset and $\mathcal{D}_r = \mathcal{D} \setminus \mathcal{D}_f$ is the remaining dataset. Original model trained on \mathcal{D} is parameterized as $\boldsymbol{\theta}_o$ Unlearned model from $\boldsymbol{\theta}_o$ on \mathcal{D}_f or \mathcal{D}_r is parameterized as $\boldsymbol{\theta}_u$

Diffusion Process

- SalUn is specifically designed for diffusion-based model
 - Let θ denote the parameters of the diffusion generator, conditioned on the text prompt/concept c. \mathbf{x}_t is the latent feature at the diffusion step t.
 - A diffusion model (DM) training uses MSE loss: $\star_{\theta} : \text{Diffusion generator parameterized by } \theta$

$$\ell_{\text{MSE}}(\boldsymbol{\theta}; \mathcal{D}) = \mathbb{E}_{\mathcal{D}} \mathbb{E}_{t, \epsilon \sim \mathcal{N}(0, 1)} \left[\| \epsilon - \left[\epsilon_{\boldsymbol{\theta}}(\mathbf{x}_t \mid c) \right] \|_2^2 \right]$$

- Main idea: Decompose the original model weights $oldsymbol{ heta}_o$ into two distinct components:
 - The salient model weights to be updated during machine unlearning process
 - The intact model weights that remain unchanged

Question: how to detect the salient model weights?

Forgetting Loss

- SalUn uses the gradient of a forgetting loss as the weight saliency map
- Forgetting loss usually follows the training loss on the forgetting dataset \mathcal{D}_f , denoted as $\ell_{\mathrm{f}}(m{ heta};\mathcal{D}_f)$
 - For classification: $\ell_f(\boldsymbol{\theta}; \mathcal{D}_f) = \mathbb{E}_{(\mathbf{x}, y) \sim \mathcal{D}_f}[\ell_{CE}(\boldsymbol{\theta}; \mathbf{x}, y)]$; (CE: cross-entropy)
 - For generation: $\ell_f(\boldsymbol{\theta}; \mathcal{D}_f) = \ell_{MSE}(\boldsymbol{\theta}; \mathcal{D}_f)$

Weight Saliency Map

Weight Saliency Map Calculation:

Reflects the weight sensitivity to the forgetting instance in \mathcal{D}_f

$$\mathbf{m}_{\mathrm{s}} = \mathbf{1} \big(| \nabla_{\boldsymbol{\theta}} \ell_{\mathrm{f}}(\boldsymbol{\theta}; \mathcal{D}_{\mathrm{f}}) |_{\boldsymbol{\theta} = \boldsymbol{\theta}_{0}} | \geqslant \gamma \big)$$

• $\mathbf{1}(g \ge \gamma)$ an element-wise indicator function that yields binary outputs. $\gamma > 0$ is a hard threshold.

The **unlearning model** θ_u is then updated as:

Tunable in the unlearning process $\theta_u = \mathbf{m}_s \odot \boldsymbol{\theta} + (\mathbf{1} - \mathbf{m}_s) \odot \boldsymbol{\theta}_o$ Salient weights

Pre-trained, fixed in the unlearning process $\theta_u = \mathbf{m}_s \odot \boldsymbol{\theta} + (\mathbf{1} - \mathbf{m}_s) \odot \boldsymbol{\theta}_o$

SalUn Training: classification

 Assign Random image label to a forgetting data point and fine-tune the salient weights:

$$\min_{\boldsymbol{\theta}} L_{\text{SalUn}}^{(1)}(\boldsymbol{\theta}_{\boldsymbol{u}}) := \mathbb{E}_{(\mathbf{x}, \mathbf{y}) \sim \mathcal{D}_f, \, \mathbf{y'} \neq \mathbf{y}} [\ell_{\text{CE}}(\boldsymbol{\theta}_{\boldsymbol{u}}; \mathbf{x}, \mathbf{y'})]$$

- Tune $m{ heta}$ to update $m{ heta}_u$ by $m{ heta}_u = \mathbf{m}_{\scriptscriptstyle \mathrm{S}} \odot m{ heta} + (\mathbf{1} \mathbf{m}_{\scriptscriptstyle \mathrm{S}}) \odot m{ heta}_o$
- y' is the random label of the image $x \in \mathcal{D}_f$, which is different from the original one
- Random Label Assignment removes the knowledge from \mathcal{D}_f and maintain the model's performance on unrelated samples.

SalUn Training: generation

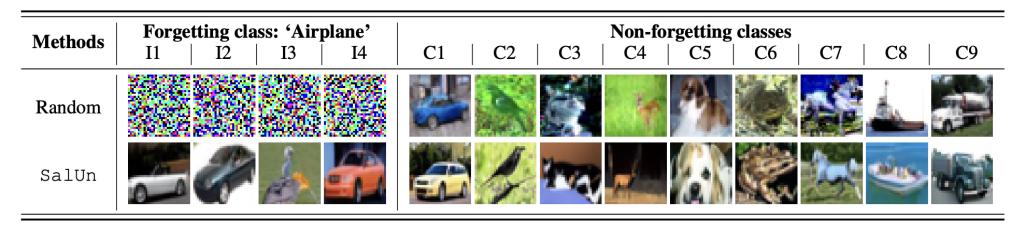
• In diffusion-based generation task, SalUn associates the forgetting concept c with a misaligned image x' that does not belong to the concept c.

$$\begin{aligned} & \underset{\boldsymbol{\theta}}{\text{minimize}} L_{\text{SalUn}}^{(2)}(\boldsymbol{\theta_u}) \colon & \text{Remove the concept knowledge from } \boldsymbol{\mathcal{D}_f} \\ &= \mathbb{E}_{(\boldsymbol{x}, \boldsymbol{c}) \sim \mathcal{D}_f, t, \epsilon \sim \mathcal{N}(0, 1), c' \neq c} \begin{bmatrix} \parallel \boldsymbol{\epsilon_{\theta_u}}(\boldsymbol{x}_t \mid c') - \boldsymbol{\epsilon_{\theta_u}}(\boldsymbol{x}_t \mid c) \parallel_2^2 \end{bmatrix} + \alpha \ell_{\text{MSE}}(\boldsymbol{\theta_u}; \mathcal{D}_r) \end{aligned}$$

- $c' \neq c$ indicates that c' is different from c.
- α is a regularization parameter that balances unlearning quality and image generation quality (preserved by $\ell_{\text{MSE}}(\boldsymbol{\theta_u}; \mathcal{D}_{\text{r}})$).

Experiments: Image Generation

Generated Images under I_i : forgotten class (airplane) or C_i : non-forgetting class



- Random: apply random weight saliency mask in SalUn
- For the given forgetting class, using random weight saliency mask in SalUn generates noisy and unrecognizable images
- For the non-forgetting classes, random weight saliency mask degrades the generation quality
- SalUn leverages a proper weight saliency map, leading to better forgetting performance

Content

- Machine Unlearning
 - Introduction and Motivation
 - Unlearning Definition
 - Model-agnostic Approach
 - Boundary Unlearning
 - Model-intrinsic Approach
 - Projective Residual Update for Linear Models
 - Forget-Me-Not for Attention Model
 - SalUn for Diffusion Model
 - Data-driven Approach
 - SISA Training

SISA Training

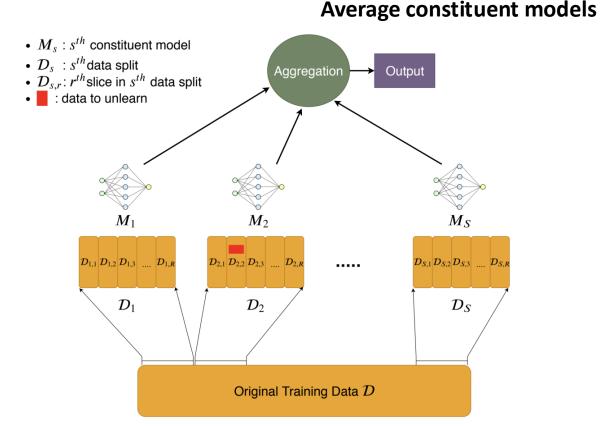
SISA: Sharded, Isolated, Sliced, and Aggregated Training

At Training phase:

- Data is divided into shards D_s
- Each shard is further split into slices $D_{s,r}$
- Incrementally train the constituent model M_s by saving the parameters of M_s before training it with a new slice.

At Inference phase:

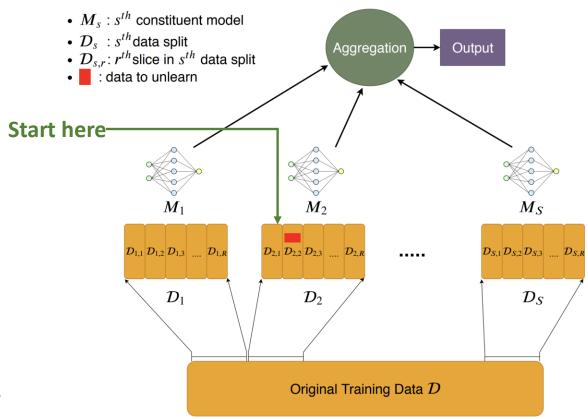
aggregate the responses of constituent models



SISA: Unlearning Guarantee

Limited Retraining Cost due to the incremental training process:

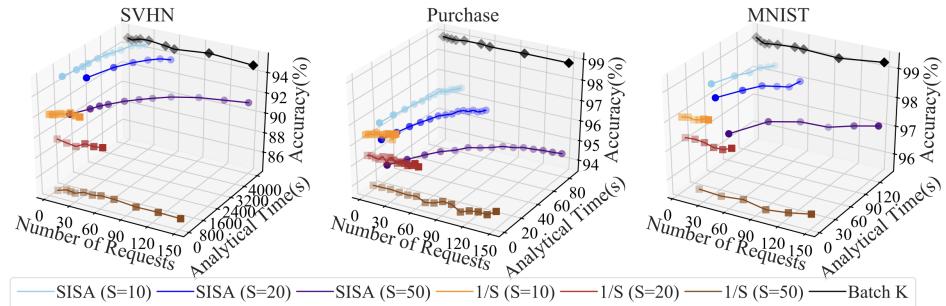
- only the constituent model whose shard contains the point to be unlearned is affected.
- retraining starts from the last parameter state saved prior to the slice containing this point,.
- e.g., $D_{2,2}$ is to be unlearned, only retrain M_2 from the state saved after $D_{2,1}$



Evaluation: Accuracy & Retraining Time (1)

Baselines:

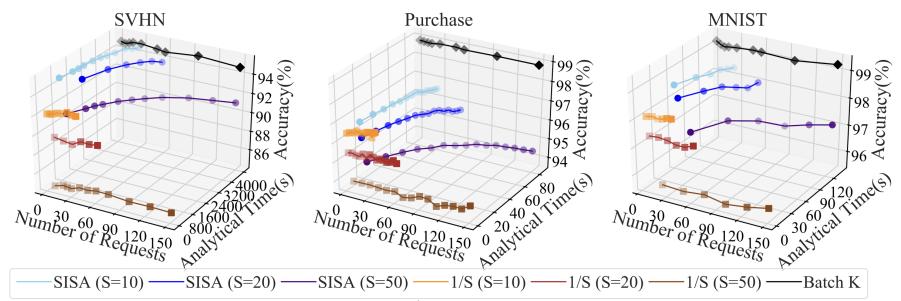
- Batch K: retrain the entire model after every K unlearning requests
- $\frac{1}{S}$: split the data into S shards and only retrain the one that contains the point to be unlearned
- Dataset: SVHN, Purchase, MNIST
- S: number of shards



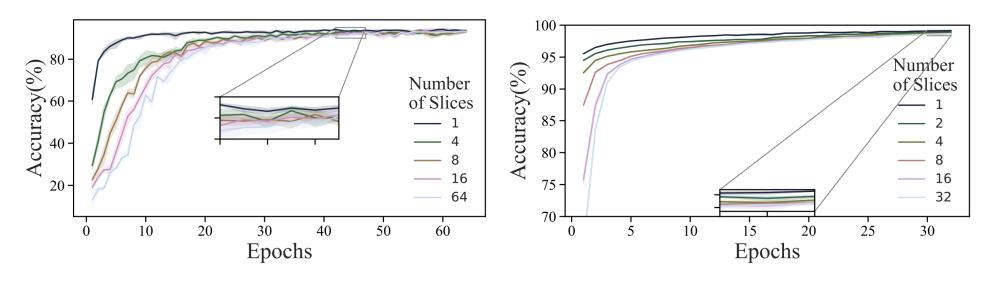
Evaluation: Accuracy & Retraining Time (2)

- Batch K achieves high accuracy, but needs a longer retraining time
- $\frac{1}{S}$ achieves low accuracy, and needs a shorter retraining time
- SISA achieves the best trade-off between accuracy and retraining time
- Increasing S will degrade the accuracy

Ensure each shard has sufficiently many data points to ensure high accuracy for each constituent model!



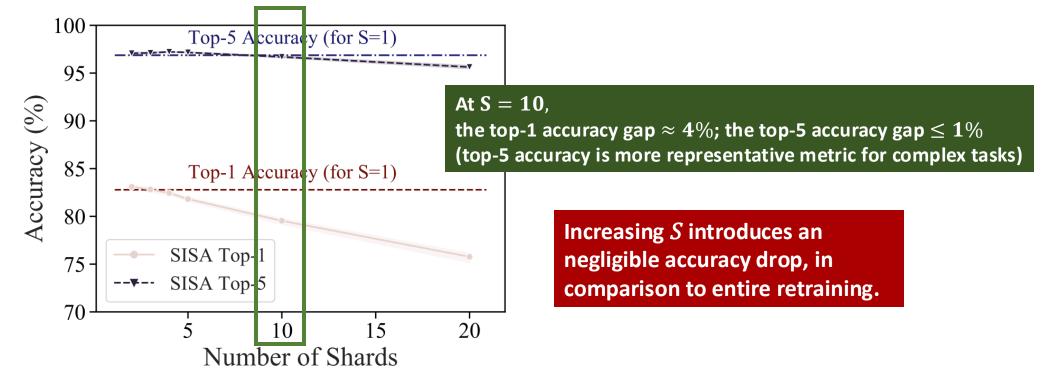
Evaluation: Impact of Slicing



- (a) Accuracy vs. Number of epochs for SVHN dataset. (b) Accuracy vs. Number of epochs for Purchase dataset.
- 1. Slicing the shard takes more epochs to achieve high accuracies
- 2. For a small number of epochs, models with more slicing have lower accuracy, due to the fact that they have significantly less amount of data at the beginning.

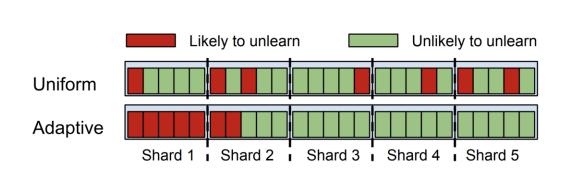
Evaluation: Transfer Learning / Pretraining

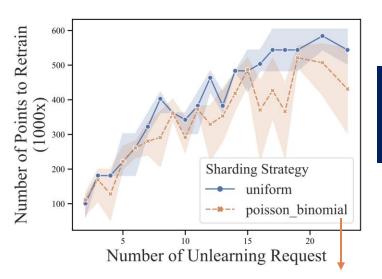
- Train a base ResNet-50 on Imagenet (relatively complex dataset) and transfer it to CIFAR-100 dataset (simpler dataset)
- Baseline: S = 1 (retrain over the entire dataset)



Adaptive Unlearning

- A priori knowledge of users' probability for requesting unlearning can improve SISA unlearning
- **Distribution-aware sharding:** maximize shard size; minimize the chance that a shard has at least one unlearning request





The adaptive sharding can reduce analytical retraining time!

Assume each request is an independent Bernoulli trial, then group of requests follows a Poisson Binomial distribution

Summary of the Lecture

- Machine Unlearning Motivation: the data/user have the "right to be forgotten"
- Goal of Machine unlearning: to design efficient unlearning algorithms that forget certain data, class, feature, concept, etc.
- Machine unlearning algorithms should maintain performance on the unchanged data
- Machine unlearning methods include model-agnostic approaches, model-intrinsic approaches and data-driven approaches.