# Explainability Evaluation and Global Explainability

**CPSC680: Trustworthy Deep Learning** 

Rex Ying

# Readings

- Readings are updated on the website (syllabus page)
- Lecture 6 readings:
  - 1710.10547.pdf (arxiv.org) Explanations can also be vulnerable to adversarial attacks
  - 2005.00631.pdf (arxiv.org) Evaluating Explanations

#### Content

- Evaluating Explainability Methods
- Model-level Explainability
- Intrinsic Explainability / Interpretability

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- Evaluating Explainability Methods
- Model-level Explainability
- Intrinsic Explainability / Interpretability

# Criteria of Good Explanation

Fidelity

The explanation maximally supports model's prediction

Sensitivity

The explanation is stable for similar model input and output

Conciseness

The explanation cannot be too large (Occam's razor)

Interpretability

ēnecessitas quare ocheat poni thus of scretum mensuras motum angeli. naz "pluarity is not to be

non est ponenda sine necessitate 7 non

The explanation can be easily understood by human

"pluarity is not to be posited without necessity"

# Explanation Goal

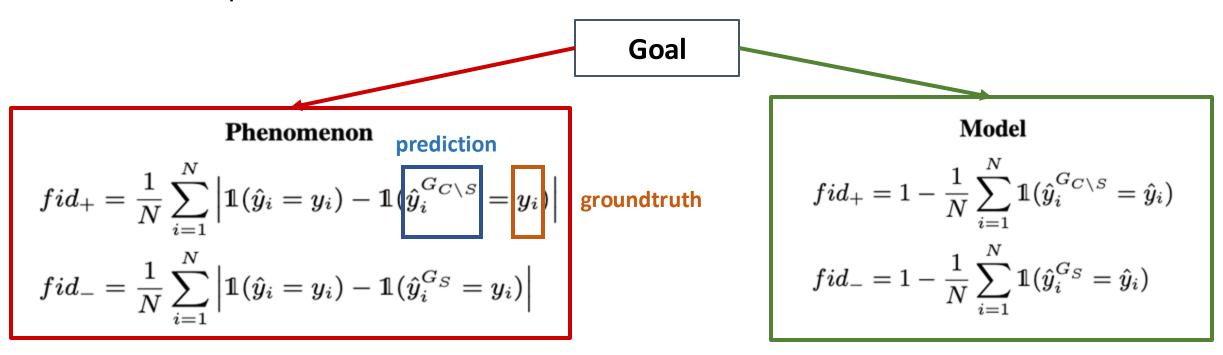
- Phenomenon Explanation
  - Explain the underlying reasons for the ground truth phenomenon

- Model Explanation
  - Explain why model makes a particular prediction

We will explain the fidelity metric in both cases:

# Explanation Goal: Fidelity Metric

- Define 2 fidelity metrics:  $fid_+$  and  $fid_-$  to capture different aspects of **explanation quality**
- The formula of fidelity depends on the goal:
  - Goal 1: explain phenomenon of the data
  - Goal 2: explain what has the model learned



### Fidelity Metric Details

- Characteristics of a good explanation
- $fid_+$ : removal important features will result in large decrease of the model confidence
- $fid_-$ : Using only the important features will result in similar confidence

#### **Phenomenon**

$$fid_+ = rac{1}{N} \sum_{i=1}^N \left| \mathbb{1}(\hat{y}_i = y_i) - \mathbb{1}(\hat{y}_i^{G_C \setminus S} = y_i) \right| ext{Removal of important features}$$
  $fid_- = rac{1}{N} \sum_{i=1}^N \left| \mathbb{1}(\hat{y}_i = y_i) - \mathbb{1}(\hat{y}_i^{G_S} = y_i) \right| ext{Keeping only the important features}$ 

Original prediction probability / confidence

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## Explanation Evaluation Criteria

- Notably, the explanation evaluation criteria are multi-dimensional
- Explanation quality
  - High fidelity / characterization scores
  - Sufficiency and necessity aspects (see the previous slide)

- Explanation stability
  - Explanations are consistent across random optimization seeds (measure variance)

- Explanation complexity
  - The explanation should be concise and easy to understand by human (measure size)

# Types of Explanations

#### Sufficiency

• An explanation is sufficient if it leads by its own to the initial prediction of the model explanation.  $(fid_- \rightarrow 0)$ 

#### Necessity

- An explanation is necessary if the model prediction changes when removing it from the initial graph.  $(fid_+ \rightarrow 1)$
- Use the Characterization score to summarize the explanation quality

$$charact = \frac{w_{+} + w_{-}}{\frac{w_{+}}{fid_{+}} + \frac{w_{-}}{1 - fid_{-}}} = \frac{(w_{+} + w_{-}) \times fid_{+} \times (1 - fid_{-})}{w_{+} \cdot (1 - fid_{-}) + w_{-} \cdot fid_{+}}$$

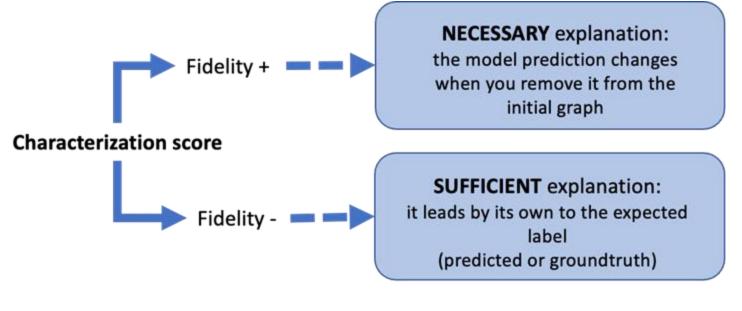
Where  $w_+$  and  $w_-$  are the weights of both fidelity metrics (commonly set  $w_+ = w_- = 1$ )

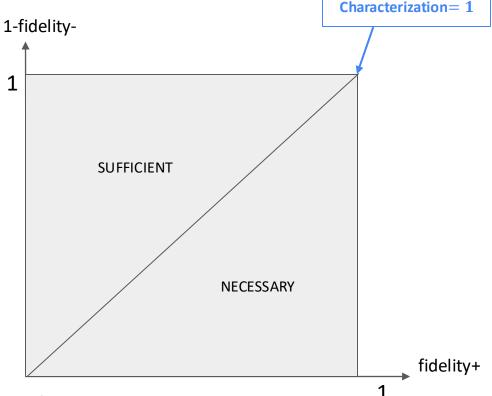
#### Characterization Score

Characterization score to summarize the explanation quality

$$charact = \frac{w_{+} + w_{-}}{\frac{w_{+}}{fid_{+}} + \frac{w_{-}}{1 - fid_{-}}} = \frac{(w_{+} + w_{-}) \times fid_{+} \times (1 - fid_{-})}{w_{+} \cdot (1 - fid_{-}) + w_{-} \cdot fid_{+}}$$

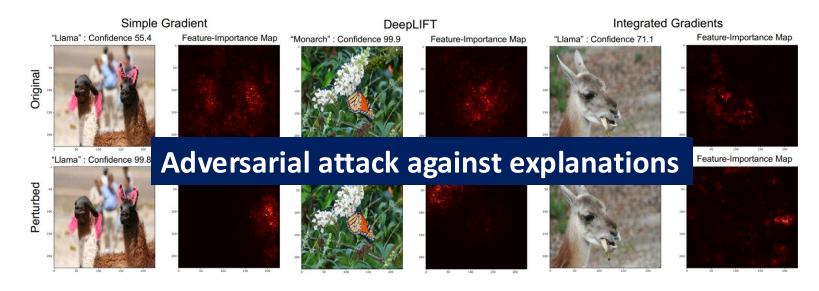
Necessary AND sufficient





### Sensitivity Desiderata

- Similar input & output → explanations should be similar
- Also called "stability"
- Local smoothness is not usually true for deep neural networks, but is a very common assumption in human cognition



### Sensitivity Definition

• Define the neighborhood of a point of interest x

$$N_r = \{ z \in D_x | \rho(x, z) \le r, f(x) = f(z) \}$$

- The local region around prediction of x that's stable
- Max Sensitivity  $\mu_M$

$$\mu_M(f,g,r;x) = \max_{z \in N_r} D(g(f,x),g(f,z))$$

Average Sensitivity

$$\mu_A(f,g,r;x) = \int_{z \in N_r} D(g(f,x),g(f,z)) dz$$

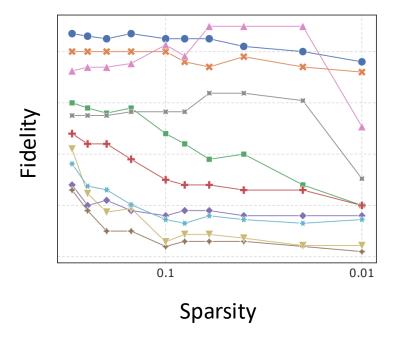
 $\rho$ : distances between input features

*D*: distance metric between explanation results

g: explanation method

# Conciseness – Low Complexity

- Sparsity is important to ensure that the model explanation highlights the most relevant part of the input
- Sparsity can be measured by the size of the explanation
  - Often controlled in the experiments
- Sparsity can also be measured by entropy
  - For explanations with importance scores
  - Attribution methods, Mask-based methods etc.



Allows us to investigate the tradeoff

## Global Explainability Evaluation

Relative performance loss

$$RPF = \frac{(\log \mathcal{L}(M_{-F}) - \log \mathcal{L}(M))}{\log \mathcal{L}(M)}$$

- $\log \mathcal{L}(M)$ : loss function value on all test data
- $\mathcal{L}(M_{-F})$ : loss function value after feature pruning (on all test data)
- Analogous to instance-level fidelity

#### Human Evaluation



(a) Raw input image. Note that this is not a part of the tasks (b) and (c)

#### What do you see?



Your options:

- Horse
- Person

(b) AMT interface for evaluating the classdiscriminative property

#### **Both robots predicted: Person**

Robot A based it's decision on Robot B based it's decision on





Which robot is more reasonable?

- Robot A seems clearly more reasonable than robot B
- O Robot A seems slightly more reasonable than robot B
- O Both robots seem equally reasonable
- O Robot B seems slightly more reasonable than robot A
- O Robot B seems clearly more reasonable than robot A

(c) AMT interface for evaluating if our visualizations instill trust in an end user

**Utilizes human evaluation platform such as Amazon Mechanical Turk (AMT)** 

#### Content

- Evaluating Explainability Methods
- Global-level Explainability
- Intrinsic Explainability / Interpretability

# Model-level Explanation

- Model-level explanations aim to shed light on a model's overall decision-making process on *a set of inputs*, instead of a specific instance.
- provides a bird-eye-view of the model behavior, analyzing potential bias affecting a group/subgroup of instances.
- Examples:
  - Concept-based explanations: provide importance measurement for high-level concepts, instead of individual features or pixels.
  - Influence functions: measure the impact of each data point in the training set on the model's predictions

## Global Explanation via Model Distillation

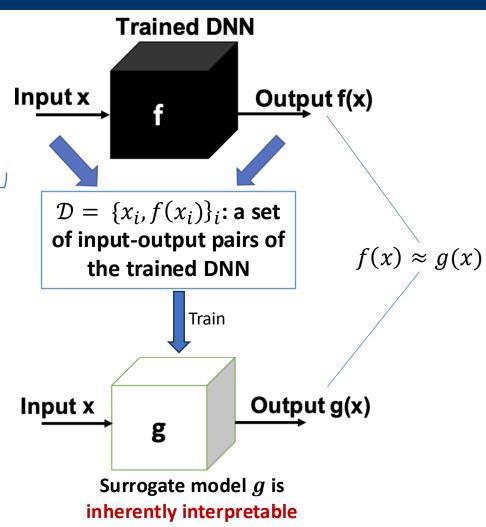
#### Generalized Additive Model (GAM)

$$g(x) = h_0 + \sum_{i} h_i(x_i) + \sum_{i \neq j} h_{ij}(x_i, x_j) + \sum_{i \neq j} \sum_{i \neq k} h_{ijk}(x_i, x_j, x_k) + \dots$$

Functions of individual features

Higher-order feature interaction terms

What are the potential issues?



## Concept Definition

- Concept: high-level units that are more understandable to human than individual features, pixels, etc.
- For example, **the wheel** and the **police logo** are important concepts for police vans.



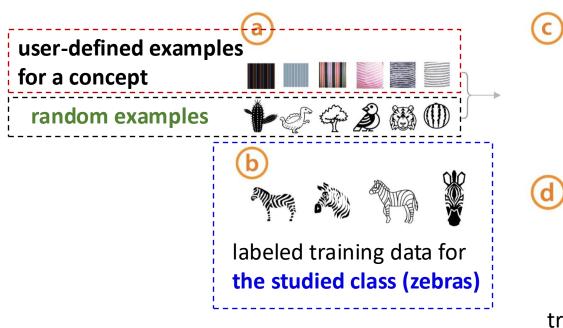
concept 1: wheel



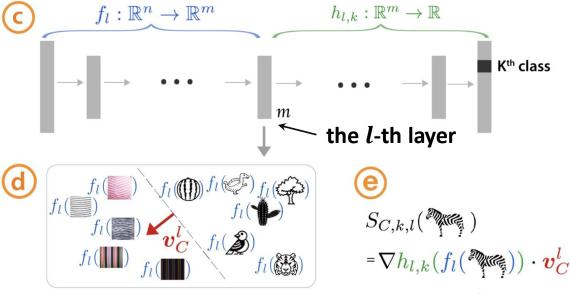
concept 2: police logo

## TCAV Pipeline

Testing with Concept Activation Vectors (CAV) [paper]



#### A network trained on **b**



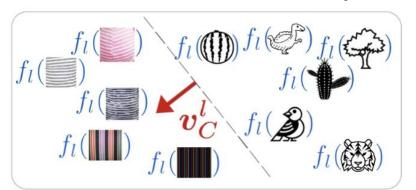
train a linear classifier in the activation space of the *l*-th layer

Conceptual Sensitivity to "striped" for the class of "zebras"

#### CAV Definition

- ${f \cdot}$  For a user-defined concept, we seek a **vector in the embedding space** of the l-th layer that represents this concept
- Concept Activation Vector (CAV): a unit vector orthogonal to the classification boundary
   Activation produced by

random examples



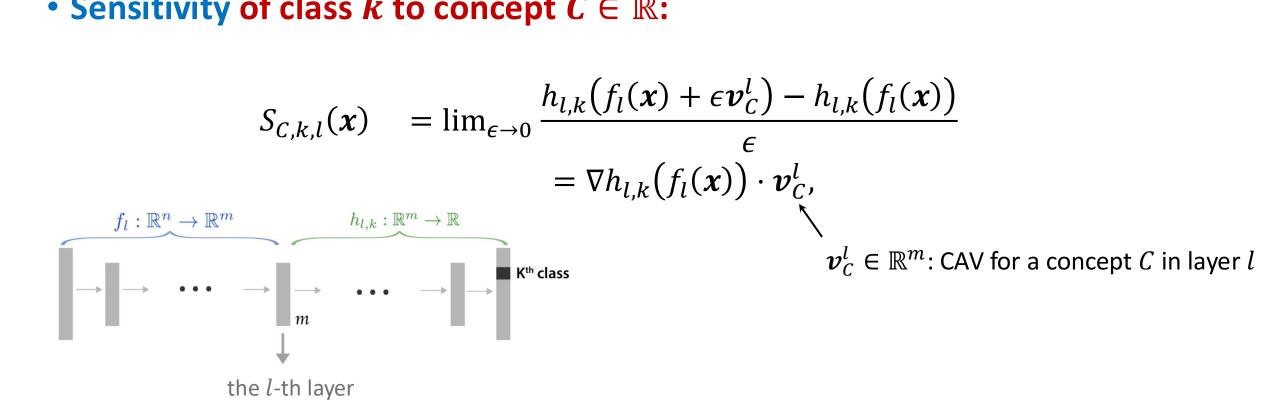
 $v_C^l$ : CAV for a concept C in layer l

Activation produced by inputs with the studied concept

Train a linear classifier to separate examples without a concept and examples with a concept

## Conceptual Sensitivity

- $f_l(x)$ : the activations for input x at layer l;  $h_{l,k}(f_l(x))$ : the logit for class k
- Sensitivity of class k to concept  $C \in \mathbb{R}$ :



# Testing with CAVs

TCAV score is defined as:

$$TCAVQ_{C,k,l} = \frac{\left|\left\{x \in X_k : S_{C,k,l}(x) > 0\right\}\right|}{|X_k|} \in [0,1]$$

- $X_k$ : all inputs with the class k
- TCAV measures the fraction of inputs with the class k whose l-th layer activation vector was **positively sensitive** to concept C (i.e.,  $S_{C,k,l}(x) > 0$ )
- Note: TCAV only depends on the sign of  $S_{C,k,l}$  (sensitivity)
  - could be further improved to consider the magnitude

# Example: Sorting Images with CAVs

- CAV essentially encodes the direction of a concept.
- The **cosine similarity** between the picture of interest to the CAV reflects the relation between the picture and the concept.
  - First learn a CAV from CEO / Model Women class (collected from ImageNet)
  - Sort similar/dissimilar images with respect to the learned CAVs

A dataset of Strip Images



CEO concept: most similar striped images









the CAVs correctly reflect the concept of interest

A dataset of

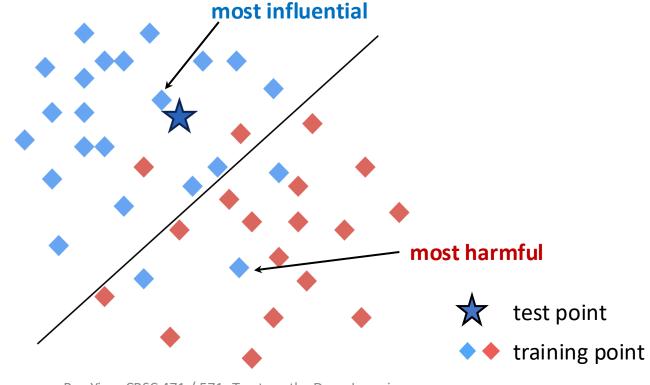
#### TCAV Results



#### Influence Functions: Motivation

Given a well-trained deep learning model, we are interested in

- Which training points were most influential for this prediction?
- Which training points were most harmful for the prediction?



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# Influence Functions: Setting (1)

- Question: How to measure the impact of a training point on a prediction?
- We are given training points  $z_1, \dots, z_n$ . How to measure the impact of a training point  $z_{train}$  on the prediction of  $z_{test}$
- Instead of retraining the model on  $\hat{Z} = \{z_i\}_{i=1}^n \cup z_{train}$ , we use <u>influence</u> <u>functions</u> to measure the model changes as we upweight  $z_{train}$  by an infinitesimal amount

# Influence Functions: Setting (2)

- Let  $L(z_i, \theta)$  be the loss, where  $\theta \in \Theta$  represents model parameters.
- $\hat{\theta} \coloneqq argmin_{\theta \in \Theta} \frac{1}{n} \sum_{i=1}^{n} L(z_i, \theta)$  is the original optimal parameters
- Given  $\hat{Z} = \{z_i\}_{i=1}^n \cup z_{train}$ , the optimal parameters become:

$$\hat{\theta}_{\varepsilon, \mathbf{z}_{train}} \coloneqq argmin_{\theta \in \Theta} \left[ \frac{1}{n} \sum_{i=1}^{n} L(z_i, \theta) \right] + \varepsilon L(\mathbf{z}_{train}, \theta)$$

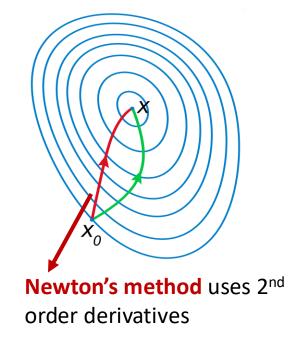
**Assumption**: the empirical risk is twice-differentiable and strictly convex in  $\theta$ .

• Goal: approximate the change in  $L(z_{test}, \hat{\theta}_{\varepsilon, z_{train}})$  as we increase  $\varepsilon$  In order to measure the influence of the example  $z_{train}$  Rex Ying, CPSC 471/571: Trustworthy Deep Learning

#### Influence Functions: Definition

Under smoothness assumptions:

$$\mathcal{J}_{up,loss}(\mathbf{z}_{train}, \mathbf{z}_{test}) \stackrel{\text{def}}{=} \frac{dL(\mathbf{z}_{test}, \hat{\theta}_{\varepsilon, \mathbf{z}_{train}})}{d\epsilon} \Big|_{\epsilon=0} \\
= \nabla_{\theta} L(\mathbf{z}_{test}, \hat{\theta})^{\mathsf{T}} \frac{d\hat{\theta}_{\varepsilon, \mathbf{z}_{train}}}{d\epsilon} \Big|_{\epsilon=0} \\
= -\nabla_{\theta} L(\mathbf{z}_{test}, \hat{\theta})^{\mathsf{T}} H_{\hat{\theta}}^{-1} \nabla_{\theta} L(\mathbf{z}_{train}, \hat{\theta})$$



- where  $H_{\widehat{\theta}} = \frac{1}{n} \sum_{i=1}^{n} \nabla_{\theta}^{2} L(z_{i}, \widehat{\theta})$
- In essence, influence functions form a quadratic approximation (via Hessian) to the empirical risk around  $\hat{\theta}$  and take a single Newton step.

### Use case: Understand Model Behavior (1)

Influence functions reveal insights about how models rely on and extrapolate from the training data.

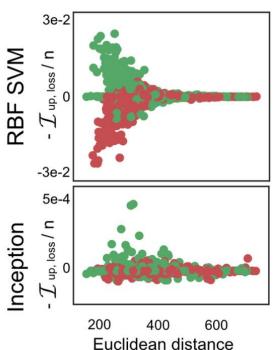
- Dataset: Dog & Fish image classification from ImageNet dataset
- Two well trained models: (1) <u>Inception v3 network</u> and (2) an SVM with an RBF kernel
- Investigate the impact of training points on a test image (fish) that both models got correct prediction

Test image



# Use case: Understand Model Behavior (2)

 $\mathcal{I}_{up,loss}(\mathbf{z}_{train}, \mathbf{z}_{test})$  V.S. Euclidean distance  $\|\mathbf{z}_{train} - \mathbf{z}_{test}\|$ 



In RBF-SVM: training images far from the test image in pixel space having almost no influence; (emphasizing nearby samples)
Fish images are mostly helpful, while dog images are mostly harmful

In Inception network, fish and dogs both could be helpful or harmful for correctly classifying the test image. The influence is not related to the distance. Most helpful training images for RBF-SVM



Most helpful training images for **Inception** 





the 5th most helpful training image for **Inception** is a dog image

**Green dot: fish** 

Red dot: dog

Note: the test image is a **fish** image

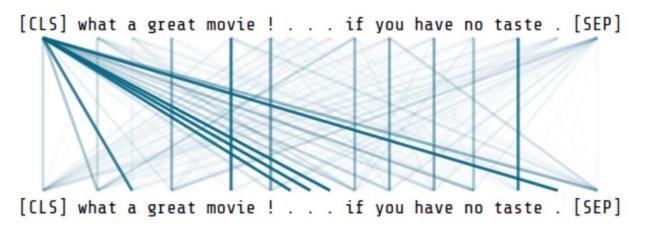
#### Content

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### Explainability via Attention

#### Attention Mechanisms

- DNNs can be endowed with attention mechanisms that simultaneously
  - preserve or even improve their performance
  - obtain **explainable outputs**
- Visualize attention weights in an attention model:



Color represents the value of attention weight darker blue ⇔ larger attention weight

#### Attention in RNN

#### **RNN** model for Natural Language Translation

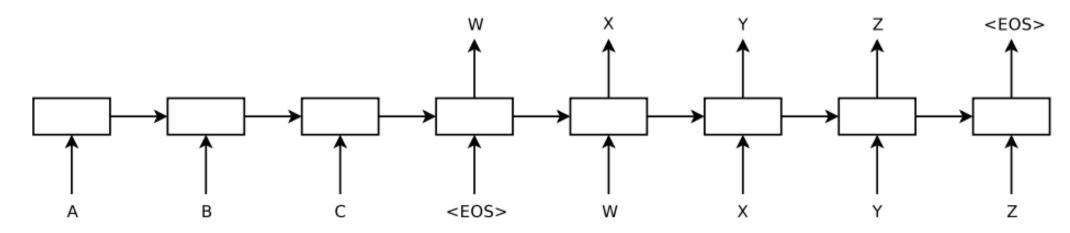


Figure 1: Our model reads an input sentence "ABC" and produces "WXYZ" as the output sentence.

How do we know which word(s) correspond to which word(s)?

#### Attention in RNN

#### Attention-based RNN model for Natural Language Translation

Attention score:  $\alpha_{ij} = \frac{\exp e_{ij}}{\sum_k \exp e_{ik}}$ 

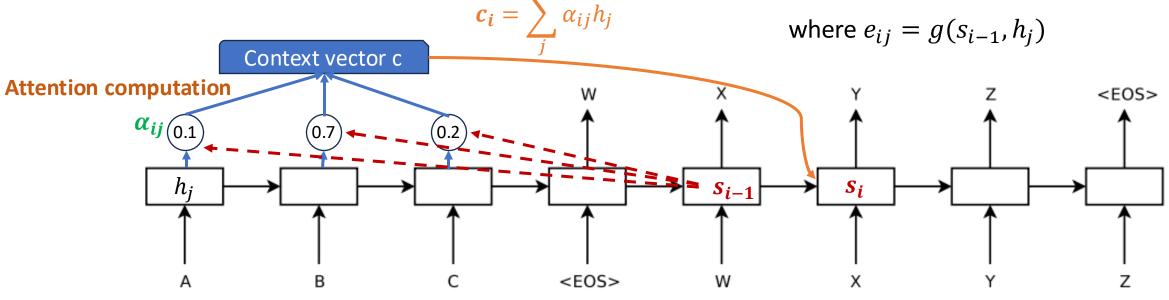


Figure 1: Our model reads an input sentence "ABC" and produces "WXYZ" as the output sentence.

Bahdanau et al. Neural Machine Translation by Jointly Learning to Align and Translate

# Signed Attention (1)

- Attention weight is always positive
- Ideal explanation should discriminate between positive and negative contributions towards a prediction
- Solution: signed attention

$$A_i = -\frac{\partial \mathcal{L}}{\partial \alpha_i} \times \alpha_i$$
 Indicates the positive or negative contribution

• L: loss function

- $\alpha_i$ : original attention weight
- value of  $\alpha_i$  measures the strength of the contribution

Recap: for hidden state  $\mathbf{h_i}$ attention weight:  $\alpha_i = \frac{\exp e_i}{\sum_k \exp e_k} \geq 0$ where  $e_i = \mathbf{v}^{\mathsf{T}} \tanh(W_h \mathbf{h}_i + W_q \mathbf{q})$   $\mathbf{v}, \mathbf{q}, W_h, W_q$ : learnable parameters

# Signed Attention (2)

#### **Explanation for sentiment analysis**

Input: "Though the price may be tooexpensive, I love its surprisingly high quality."

**Output:** y = "Positive"



Though the price may be too expensive, I love its surprisingly high quality.

unimportant

important

# with signed attention

#### signed attention visualization

Though the price may be too expensive, I love its surprisingly high quality.

negative

neutral

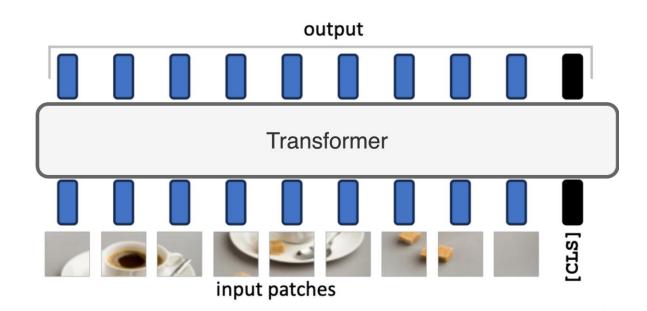
positive

#### Vision Transformer

- Split an input image into MxM patches
- Add a [CLS] token as a global embedding of the input

resize it to (3x3) grid and run interpolation to smoothen the importance score to visualize

Importance score for patches



Architecture

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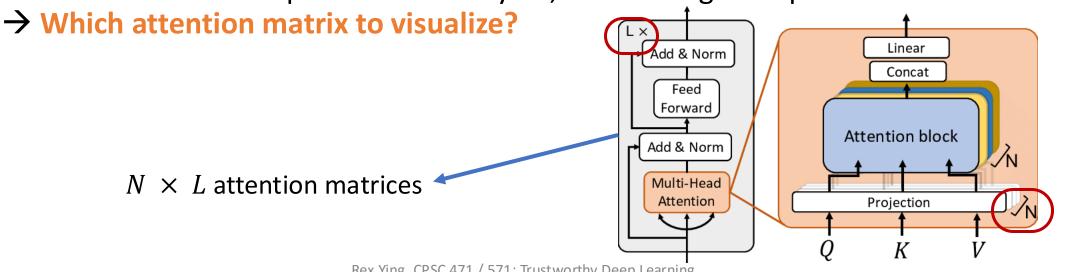
Attention Matrix:  $A = softmax(\frac{Q}{A})$ 

#### Vision Transformer

- Split an input image into MxM patches
- Add a [CLS] token as a global embedding of the input

#### Challenge:

• Transformer has multiple heads and layers, thus having multiple attention matrices



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- Naïve approach (Rollout)
  - Aggregate attention matrices across multiple heads: Mean averaging

$$\bar{A}^{(l)} = I + \sum_{i} A^{(l,i)}$$

#### Why do we need to add I?

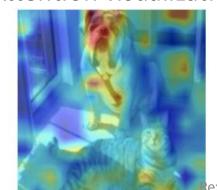
• Aggregate attention matrices across multiple layers: Matrix multiplication

$$C = \bar{A}^1 \bar{A}^2 \dots \bar{A}^L$$

 $Dog \rightarrow$ 



Attention visualization



Why should it be matrix multiplication?

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Importance of patch 3

Attention weights of patch 3 to others

- Naïve approach (Rollout)
  - Aggregate attention matrices across multiple heads: Mean averaging

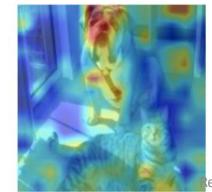
$$\bar{A}^{(l)} = I + \sum_{i} A^{(l,i)}$$

• Aggregate attention matrices across multiple layers: Matrix multiplication  $C = \bar{A}^1 \bar{A}^2 - \bar{A}^L$ 

 $Dog \rightarrow$ 



Attention visualization



However, the explanation for cat prediction is the same as for dog

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 $Cat \rightarrow$ 

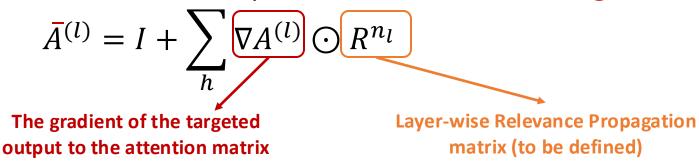


Attention visualization

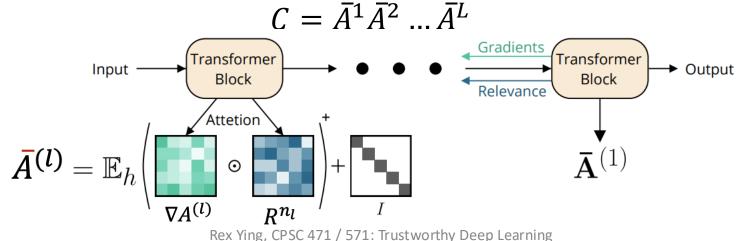


#### Targeted Explanation

Aggregate attention matrices across multiple heads: Relevance and gradient diffusion



• Aggregate attention matrices across multiple layers: Matrix multiplication

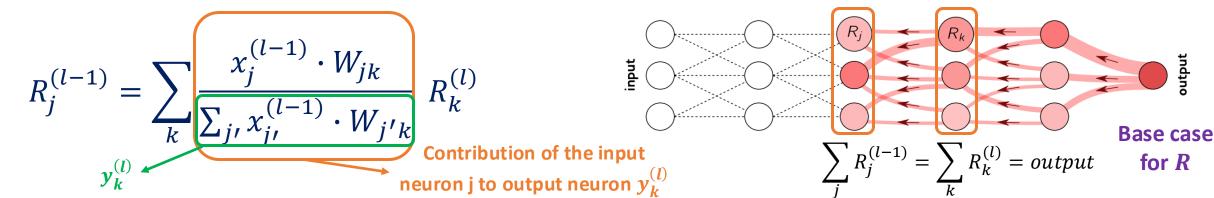


# Layer-wise Relevance Propagation (LRP) (1)

- Layer-wise Relevance Propagation (LRP)
  - LRP is a method to compute the relevance of input to the target output using the
    weights and the neural activations to propagate the output back through the network
    up until the input layer

$$R_j^{(l-1)} = \sum_{k} \frac{Z_{jk}}{\sum_{l} Z_{lk}} R_k^l \qquad \text{A number quantifying the contribution of a neuron } j \text{ at layer } (l-1) \text{ to the relevance score of neuron } k \text{ at layer } (l)$$

E.g., for a linear layer with ReLU activation:  $y^{(l)} = ReLU(W^{T}x^{(l-1)})$ , the relevance propagation can be computed as follows



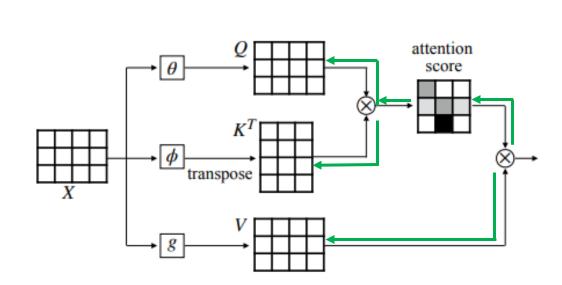
# Layer-wise Relevance Propagation (LRP) (2)

#### Layer-wise Relevance Propagation for Transformer

- In Transformer, for some binary operations (e.g. O = AV, or  $A = softmax(QK^T)$ , or skip connection O = X + Y where Y = f(x)), we need to propagate the relevance score through both input tensors.
- For an operator with two tensors O = f(XY), the relevance score is ensured to be fully distributed to both tensors

$$\sum_{i} R_i^O = \sum_{j} R_j^X + \sum_{k} R_k^Y$$

i, j, k will iterate over all elements in the output matrix O, X, Y



## Layer-wise Relevance Propagation (LRP) (2)

- Layer-wise Relevance Propagation for Transformer
  - E.g., Let us compute LRP for O = AV. Consider an example

$$A=egin{bmatrix} 0.2 & 0.8 \end{bmatrix}, \quad V=egin{bmatrix} 1 \ 3 \end{bmatrix}, \quad O=AV=egin{bmatrix} 2.6 \end{bmatrix}, \quad R^O=egin{bmatrix} 1 \end{bmatrix}$$

• The contribution of each triplet (i, j, k) to the output position (i, k) is

Split the contribution to input components

$$R_{ij}^A = \lambda \sum_k m_{ijk}, \;\; R_{jk}^V = (1-\lambda) \sum_i m_{ijk}$$

Typically, we can choose  $\lambda = \frac{1}{2}$ 

## Layer-wise Relevance Propagation (LRP) (2)

#### Layer-wise Relevance Propagation for Transformer

• E.g., Let us compute LRP for O = AV. Consider an example

$$A=egin{bmatrix} 0.2 & 0.8 \end{bmatrix}, \quad V=egin{bmatrix} 1 \ 3 \end{bmatrix}, \quad O=AV=egin{bmatrix} 2.6 \end{bmatrix}, \quad R^O=egin{bmatrix} 1 \end{bmatrix}$$

• The contribution of each triplet (i, j, k) to the output position (i, k) is (no need  $\varepsilon$ )

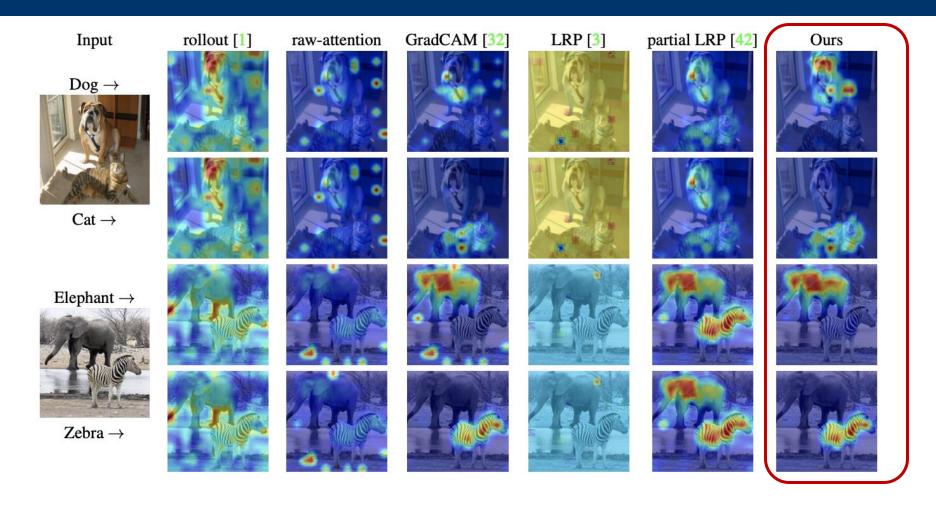
$$m_{111} = rac{A_{11}V_{11}}{O_{11}}R_{11}^O = rac{0.2 \cdot 1}{2.6} \cdot 1 = 0.076923 \qquad m_{121} = rac{A_{12}V_{21}}{O_{11}}R_{11}^O = rac{0.8 \cdot 3}{2.6} \cdot 1 = rac{2.4}{2.6} = 0.923077$$

• Split the contribution to input components (for  $\lambda = 1/2$ )

$$R^A = egin{bmatrix} 0.03846 & 0.46154 \end{bmatrix}, \quad R^V = egin{bmatrix} 0.03846 \ 0.46154 \end{bmatrix}$$

• Check:  $\sum R^A + \sum R^V = 0.5 + 0.5 = 1 = \sum R^O$ 

## Transformer Interpretability



Chefer et al., Transformer Interpretability Beyond Attention Visualization, CVPR2021

#### Attention Artifacts (1)

#### Artifacts in Vision Transformer

 Most of the existing transformer-based models exhibit artifacts on their attention matrix.

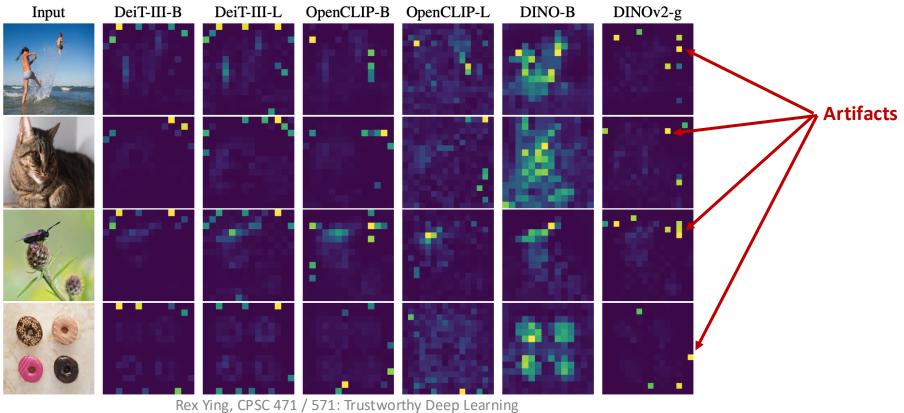
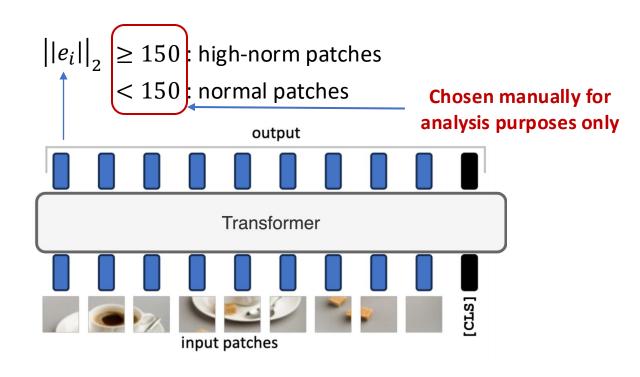
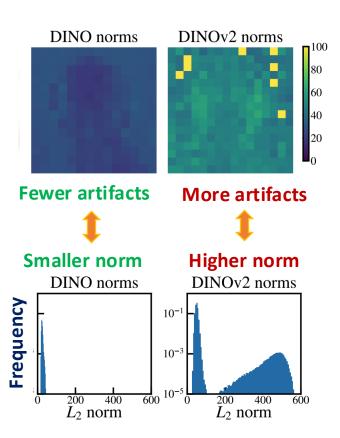


Figure 2: Illustration of artifacts observed in the attention maps of modern vision transformers.

## Attention Artifacts (2)

- Why does it happen?
  - The artifacts have a connection to the norm of token embedding.
  - → Let's analyze tokens with high-norm





#### Role of High-norm Patches

#### Settings

- For each patch/token embedding, add simple linear layers to
  - Predict the position of the patch
  - Reconstruct pixel values on the patch
  - Predict image class from the patch embedding

#### Observation

- Position prediction & reconstruction: normal patches give better results.
  - normal patches can maintain local information about patches
- Image class classification:
   high-norm patches perform better
  - → high-norm patches discard local information, having more global information (image class)

	positio	reconstruction	
	top-1 acc	avg. distance↓	L2 error ↓
normal	41.7	0.79	18.38
outlier	22.8	5.09	25.23

(b) Linear probing for local information.

	IN1k	P205	Airc.	CF10	CF100	CUB
[CLS]	86.0	66.4	87.3	99.4	94.5	91.3
normal	65.8	53.1	17.1	97.1	81.3	18.6
outlier	<u>69.0</u>	<u>55.1</u>	<u>79.1</u>	<u>99.3</u>	<u>93.7</u>	<u>84.9</u>

Image classification

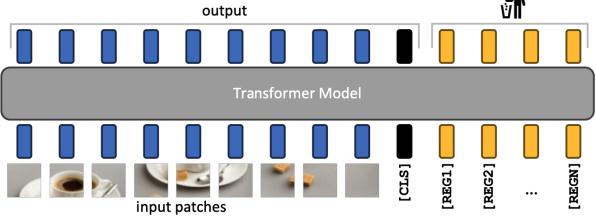
#### Register Tokens

#### Hypothesis

- Large Transformer models can recognize redundant patches (do not have much information) and leverage them to store, process, and retrieve global information.
- It may be undesirable as it may discard information from some patches.

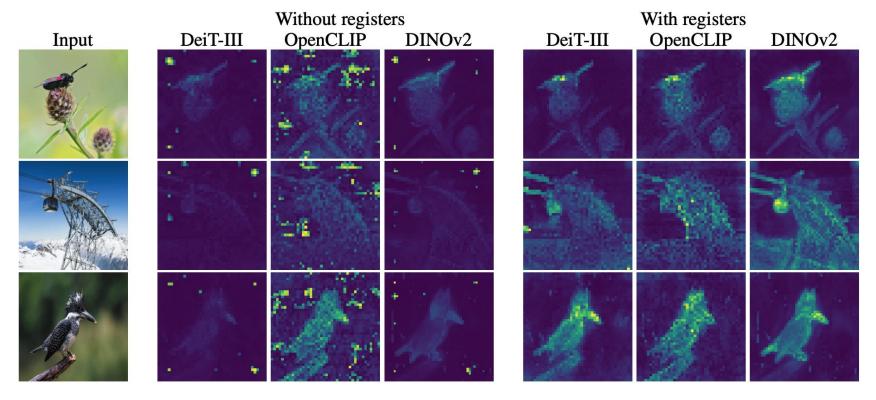
#### Solution

 Use some additional tokens as registers (along with [CLS]) for saving global information purposes



## Register Improves Interpretability

 Adding registers provides much better interpretability and reduces artifacts for the attention matrix.



Rex Ying, CPSC 471 / 571: Trustworthy Deep Learning

## Register Improves Performance

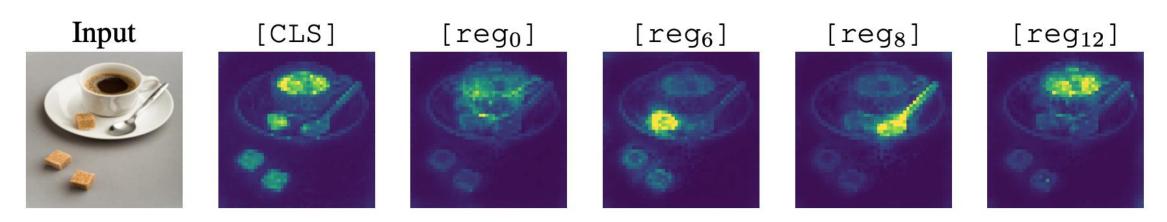
- Adding registers provides much better interpretability and reduces artifacts for the attention matrix.
- Performance slightly improved

	ImageNet	ADE20k	NYUd
	Top-1	mIoU	rmse ↓
DeiT-III	84.7	38.9	0.511
DeiT-III+reg	84.7	39.1	0.512
OpenCLIP	78.2	26.6	0.702
OpenCLIP+reg	78.1	26.7	0.661
DINOv2	84.3	46.6	0.378
DINOv2+reg	84.8	47.9	0.366

(a) Linear evaluation with frozen features.

## Vision Transformers Need Registers

- Adding registers provides much better interpretability and reduces artifacts for the attention matrix.
- Performance slightly improved.
- Each register pays attention to different regions (naturally emerged from training).



Oral ICLR24 -> A simple idea but good analyses/observations would also be appreciated