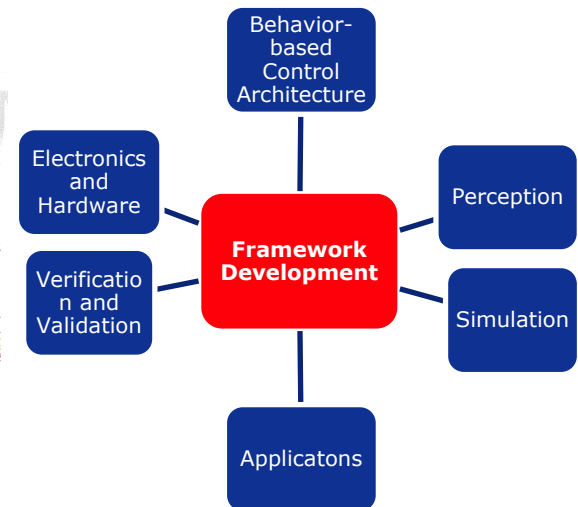
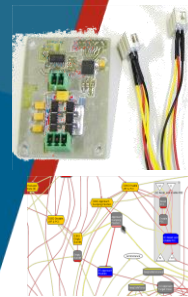


# Foundations of Robotics – Subsystems and Components



**Prof. Dr. Karsten Berns**

Robotics Research Lab (RRLab)  
Department of Computer Science  
TU Kaiserslautern, Germany

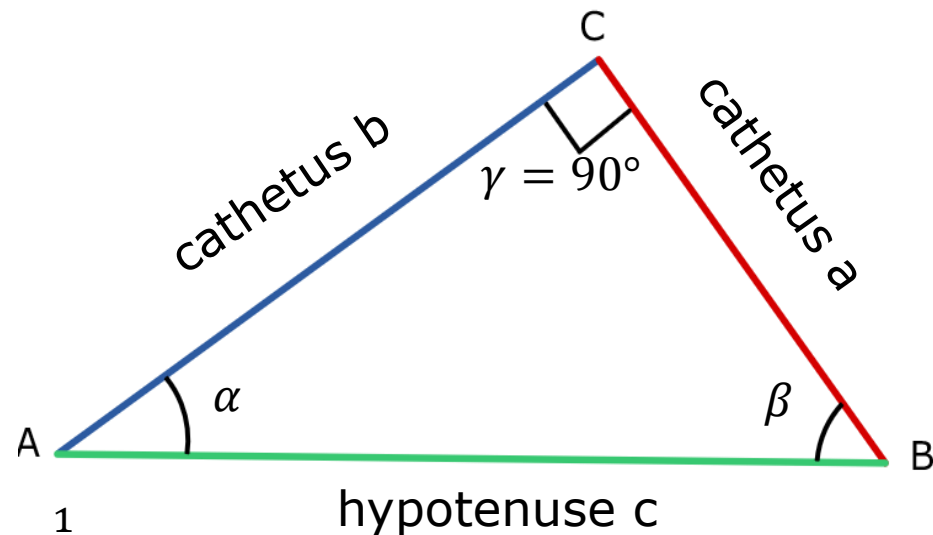
# Content

- Mechanical components
  - Workspace
  - Joints
  - Basic configuration for a robot
  - Robotic Wrists
  - Actuators
- Open and closed loop control
- Sensors
- Hardware Architecture
- Simulation

## Reminder: Trigonometric Functions

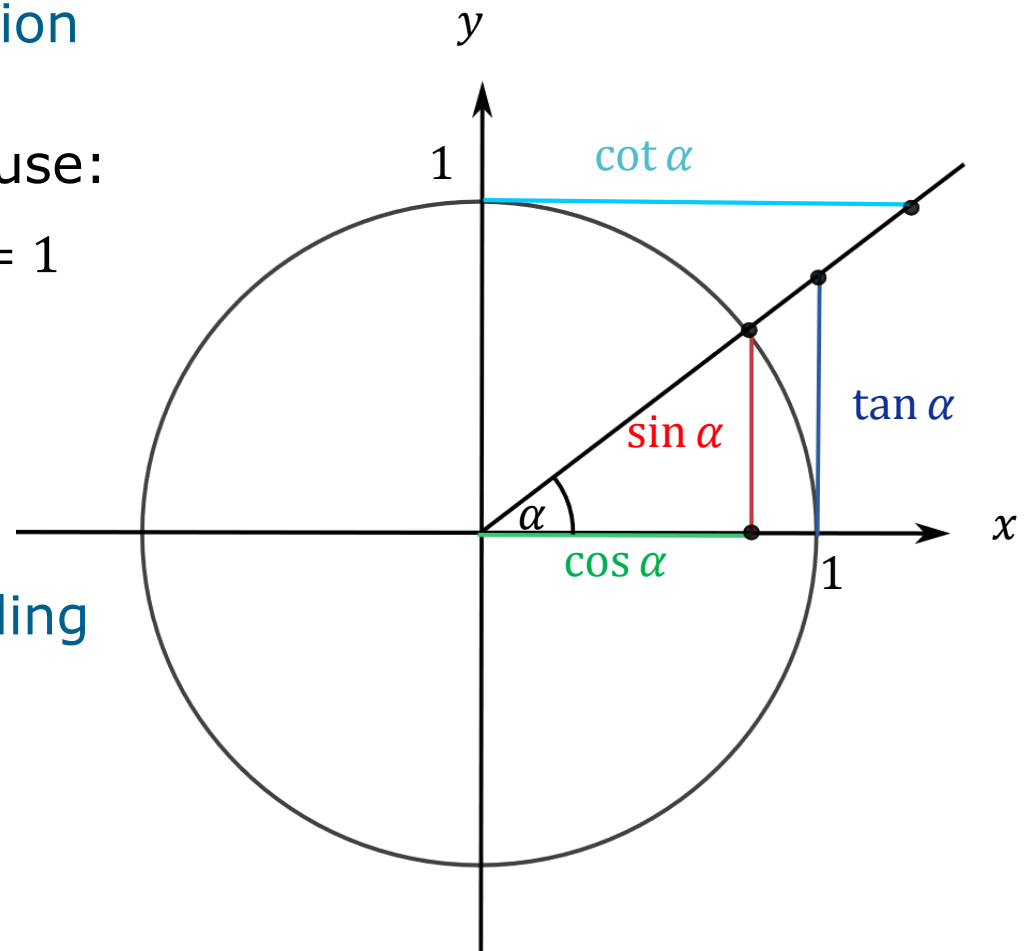
The trigonometric functions  $\sin$ ,  $\cos$ ,  $\tan$ ,  $\cot$  are defined as the ratios of corresponding sides in a right triangle (between  $0^\circ$  and  $90^\circ$ ).

- $\cos \alpha = \frac{\text{adjacent}}{\text{hypotenuse}} = \frac{b}{c}$
- $\sin \alpha = \frac{\text{opposite}}{\text{hypotenuse}} = \frac{a}{c}$
- $\tan \alpha = \frac{\text{opposite}}{\text{adjacent}} = \frac{a}{b} = \frac{a/c}{b/c} = \frac{\sin \alpha}{\cos \alpha}$
- $\cot \alpha = \frac{\text{adjacent}}{\text{opposite}} = \frac{b}{a} = \frac{b/c}{a/c} = \frac{\cos \alpha}{\sin \alpha} = \frac{1}{\tan \alpha}$



## Reminder: Trigonometric Functions

- Unit circle for the definition of  $\sin$ ,  $\cos$ ,  $\tan$ ,  $\cot$ 
  - Length of the hypotenuse:  
 $\sqrt{x^2 + y^2} = 1$ , or  $x^2 + y^2 = 1$ 
    - $\sin \alpha = y$
    - $\cos \alpha = x$
- Radian of an angle  $\alpha$ :  
 Length of the arc of the unit circle corresponding to angle  $\alpha$



## Reminder: Properties of Sine and Cosine

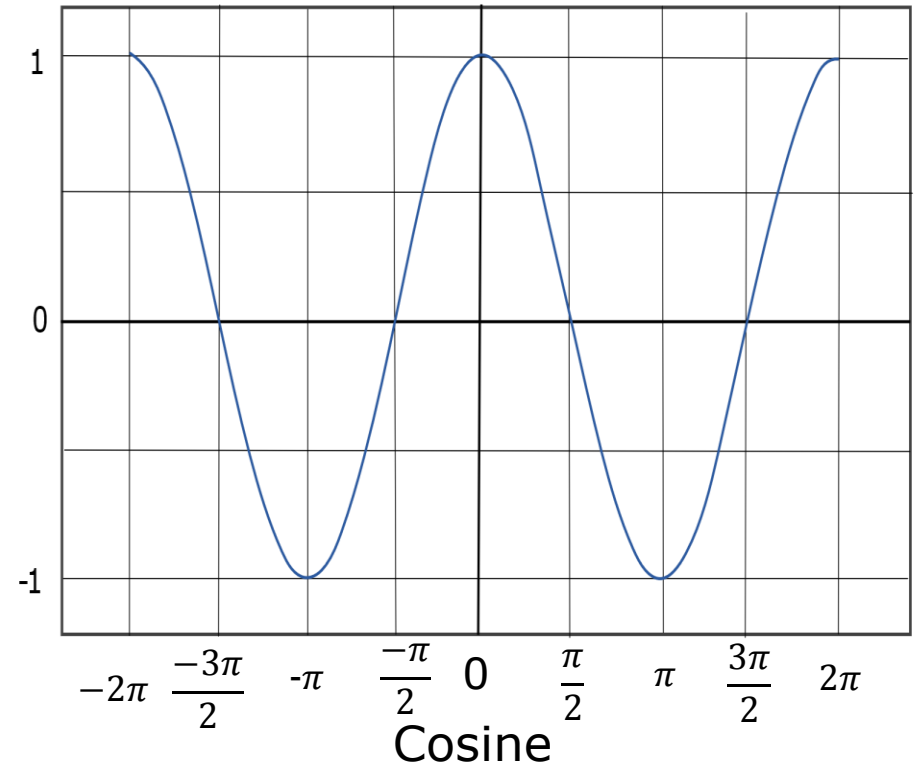
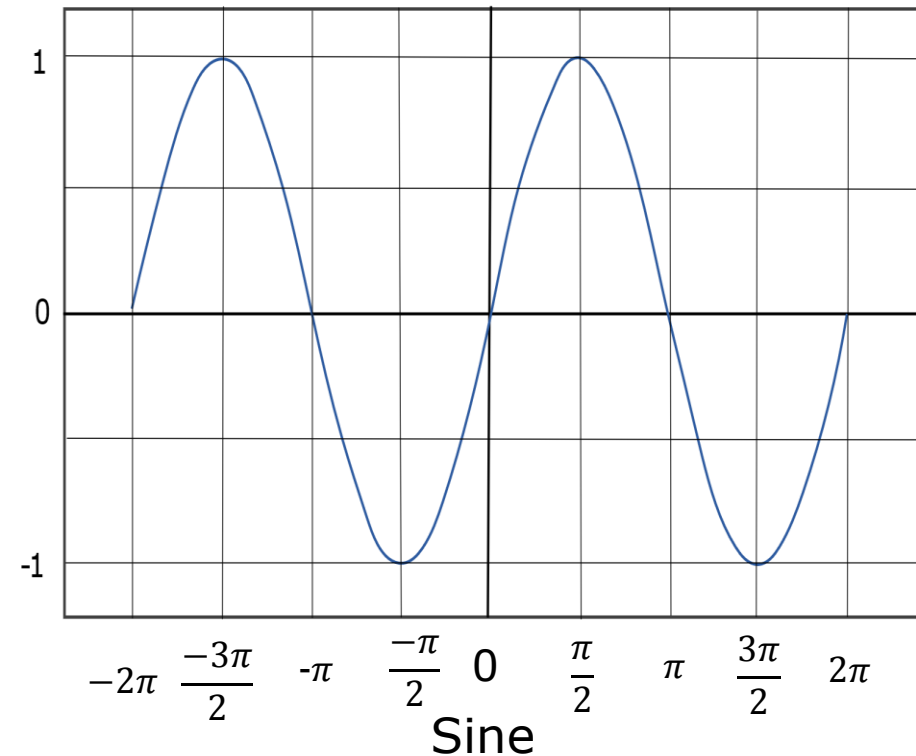
	$\sin x$	$\cos x$
Domain	$-\infty < x < \infty$	
Codomain	$-1 \leq \sin x \leq 1$	$-1 \leq \cos x \leq 1$
Period	$2\pi$	
Symmetry	Odd	Even
Roots	$x_k = k \cdot \pi$	$x_k = \frac{\pi}{2} + k \cdot \pi$
Maxima	$x_k = \frac{\pi}{2} + k \cdot 2\pi$	$x_k = k \cdot 2\pi$
Minima	$x_k = \frac{3\pi}{2} + k \cdot 2\pi$	$x_k = \pi + k \cdot 2\pi$
Transformations	$\sin(90^\circ - \alpha) = \cos \alpha$	$\cos(90^\circ - \alpha) = \sin \alpha$

## Reminder: Table of Values

	Sine	Cosine
0°	$\frac{1}{2}\sqrt{0} = 0$	$\frac{1}{2}\sqrt{4} = 1$
30°	$\frac{1}{2}\sqrt{1} = \frac{1}{2}$	$\frac{1}{2}\sqrt{3}$
45°	$\frac{1}{2}\sqrt{2} = \frac{1}{\sqrt{2}}$	
60°	$\frac{1}{2}\sqrt{3}$	$\frac{1}{2}\sqrt{1} = \frac{1}{2}$
90°	$\frac{1}{2}\sqrt{4} = 1$	$\frac{1}{2}\sqrt{0} = 0$

## Reminder: Additional Theorem and Graphs

- $\sin(x_1 \pm x_2) = \sin x_1 \cdot \cos x_2 \pm \cos x_1 \cdot \sin x_2$
- $\cos(x_1 \pm x_2) = \cos x_1 \cdot \cos x_2 \mp \sin x_1 \cdot \sin x_2$
- $\tan(x_1 \pm x_2) = \frac{\tan x_1 \pm \tan x_2}{1 \mp \tan x_1 \cdot \tan x_2}$



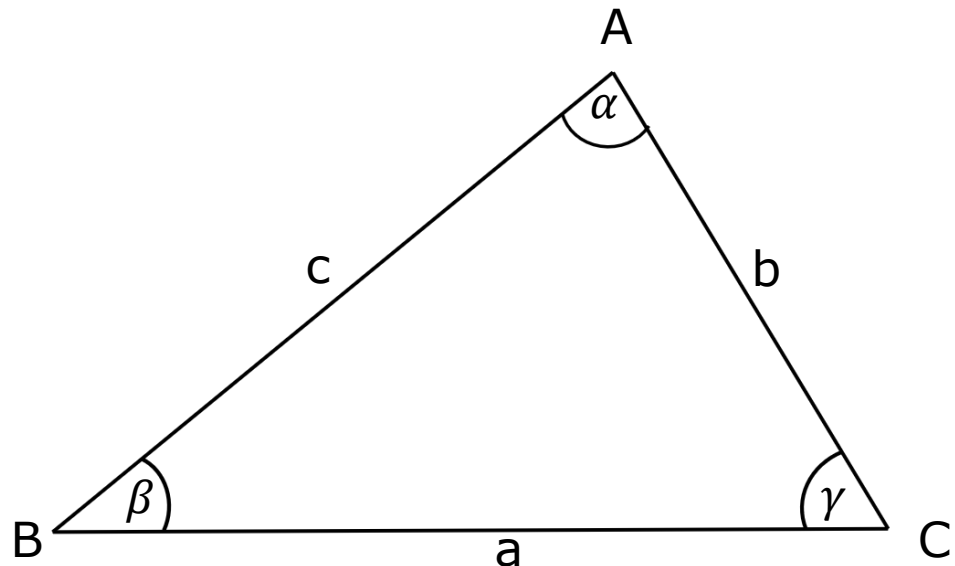
# Cosine/Sine Rule

- Cosine Rule:

- $a^2 = b^2 + c^2 - 2bc \cos(\alpha)$
- $b^2 = a^2 + c^2 - 2ac \cos(\beta)$
- $c^2 = a^2 + b^2 - 2ab \cos(\gamma)$

- Sine Rule:  $\beta$

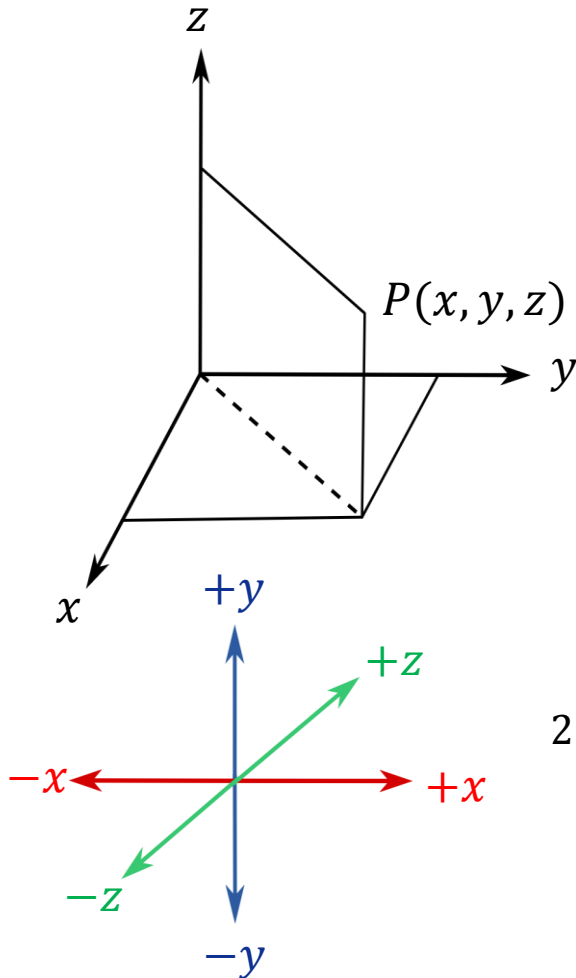
- $$\frac{\sin \alpha}{a} = \frac{\sin(\beta)}{b} = \frac{\sin(\gamma)}{c}$$



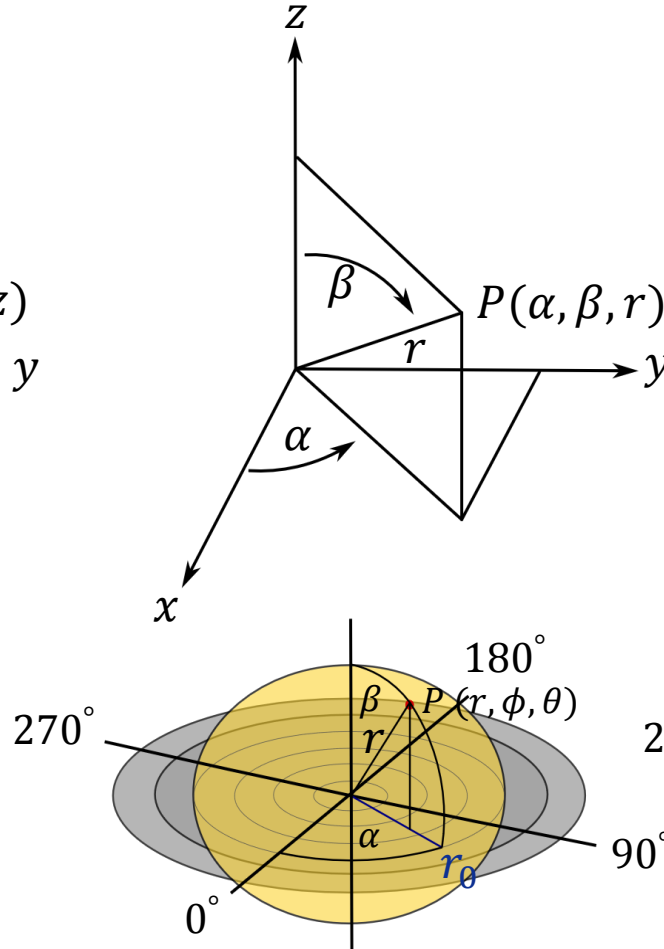


# Reminder: 3D Coordinate Systems

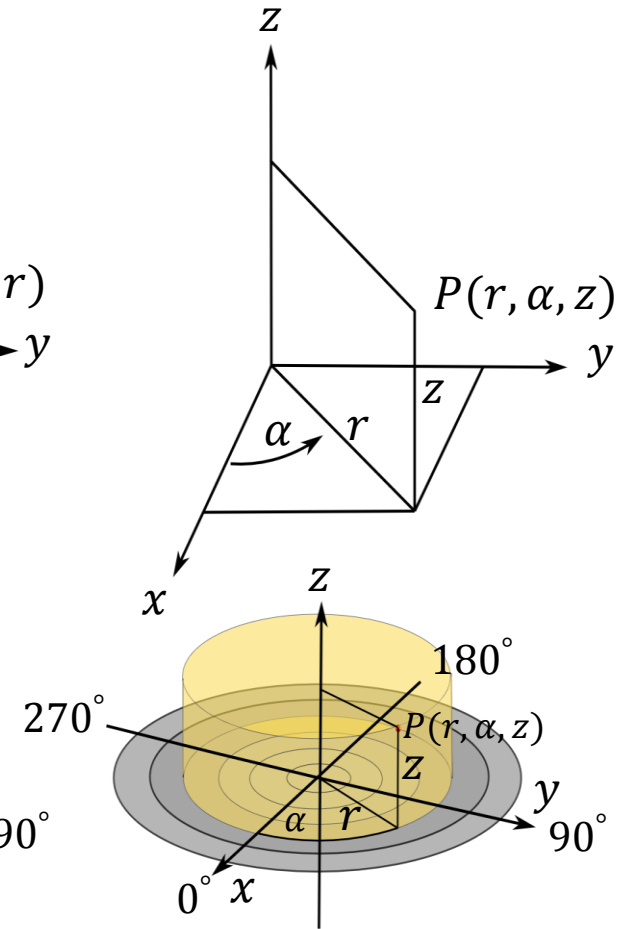
Cartesian coordinates



Spherical coordinates



Cylindrical coordinates



# Transformation of Coordinate Systems

- Cartesian coordinates  $\rightarrow$  Cylindrical coordinates

- $(x, y, z) \rightarrow (r, \alpha, z)$

- $r = \sqrt{x^2 + y^2}$

- $\tan \alpha = \frac{y}{x}$

- $z = z$

- Cylindrical coordinates

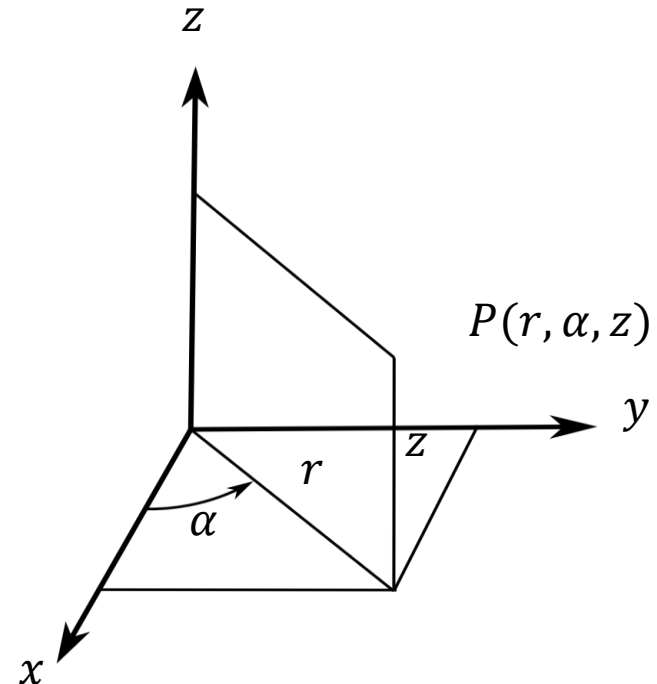
$\rightarrow$  Cartesian coordinates

- $(r, \alpha, z) \rightarrow (x, y, z)$

- $x = r \cdot \cos \alpha$

- $y = r \cdot \sin \alpha$

- $z = z$



# Transformation of Coordinate Systems

- Cartesian coordinates  $\rightarrow$  Spherical coordinates

- $(x, y, z) \rightarrow (r, \alpha, \beta)$

- $r = \sqrt{x^2 + y^2 + z^2}$

- $\cos \beta = \frac{z}{r}$

- $\tan \alpha = \frac{y}{x}$

- Spherical coordinates

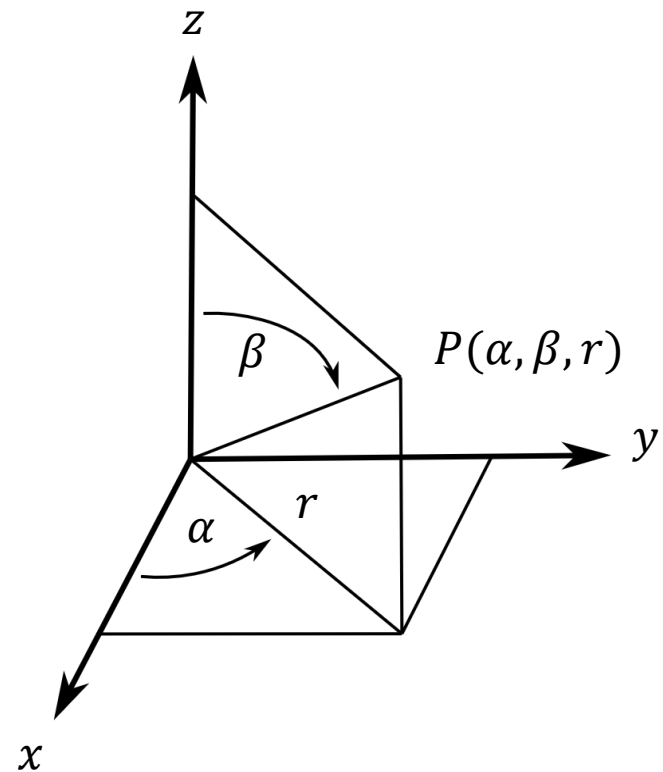
$\rightarrow$  Cartesian coordinates

- $(r, \alpha, \beta) \rightarrow (x, y, z)$

- $x = r \cdot \sin \beta \cdot \cos \alpha$

- $y = r \cdot \sin \beta \cdot \sin \alpha$

- $z = r \cdot \cos \beta$



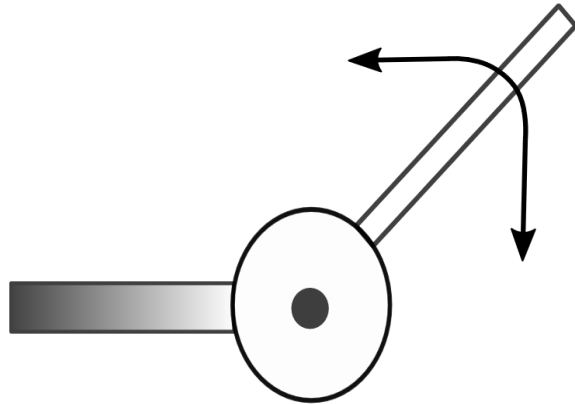
## Definition: Workspace

- Workspace consists of all points, which are reachable by the robot hand
  - At least 3 DOF (degree of freedom) necessary for a 3-D space
  - At least 3 basic joints necessary for a 3-D space
- Basic shape of workspace consists of all points, which are reachable by the robot hand without considering any restrictions by the joints or obstacles

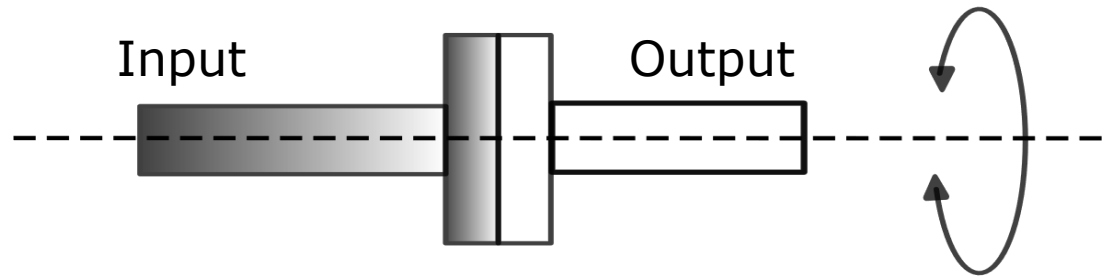
# Relation between Degrees of Freedom and Joints

- Number of possible independent movements of an object in relation to a fixed coordinate system
- Pose of an object that can move freely in space is defined by
  - Position (3 values)
  - Orientation (3 values)
- Joints necessary to achieve the degree of freedom (DOF)
- Rotary joints are required for orientation, as linear joints would not change the orientation of the wrist
- Active (actuated) and passive DOF

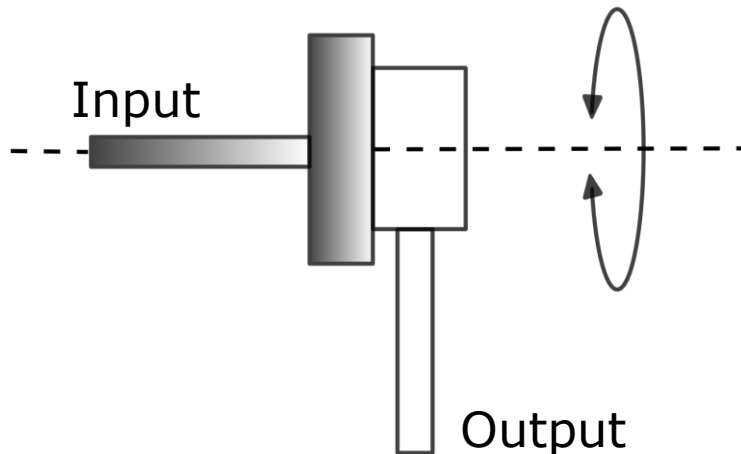
# The 4 Basic Joint Types of Robotic Systems



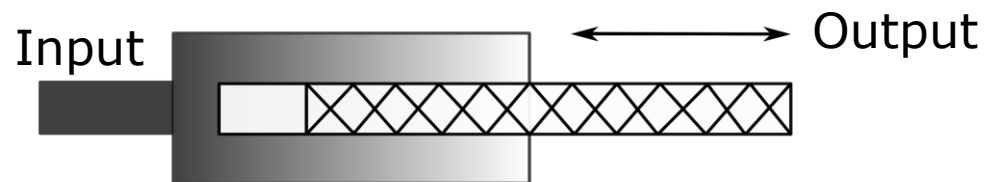
**Rotational Joint (R)**



**Torsion Joint (T)**



**Revolute Joint (V)**



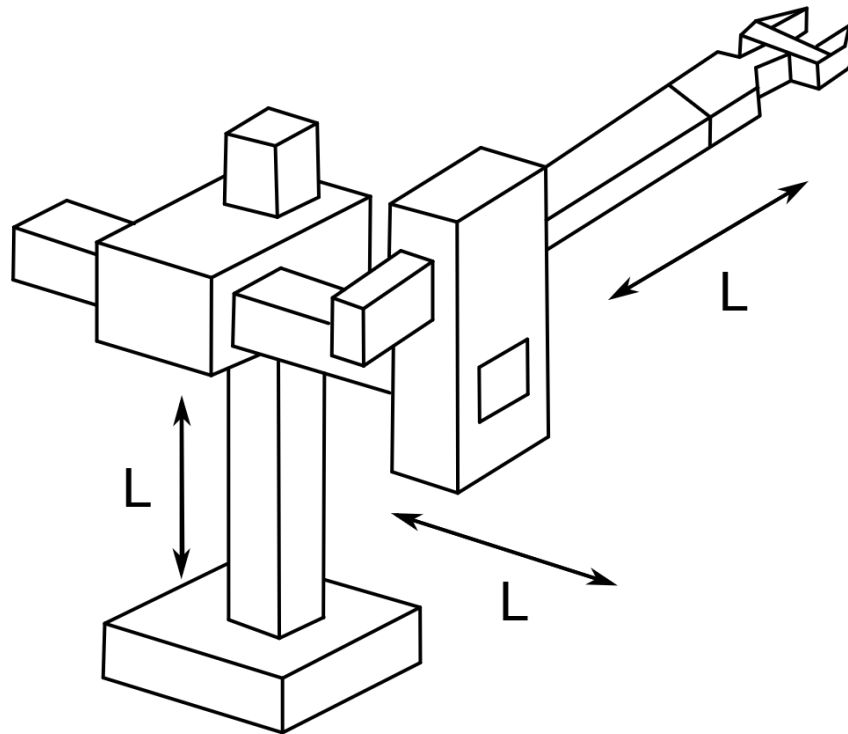
**Linear Joint (L)**

see also [Siegert, Bocionek 96]

# Basic Robot Types

- Cartesian Robot (LLL)

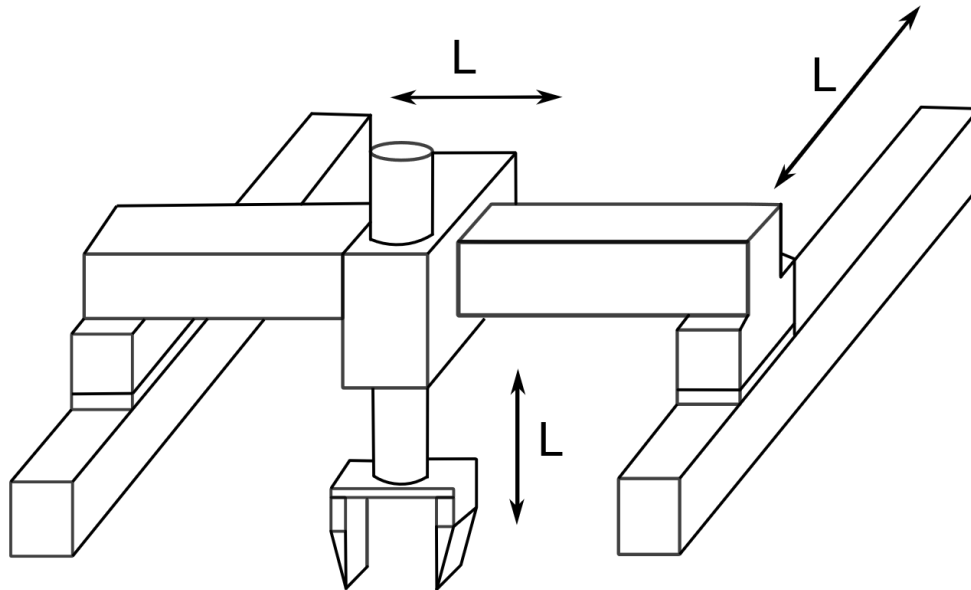
Basic shape of operational space: Cuboid



[Siegert, Bocionek96]

# Basic Robot Types

- Cartesian Robot (LLL)  
Basic shape of operational space: Cuboid

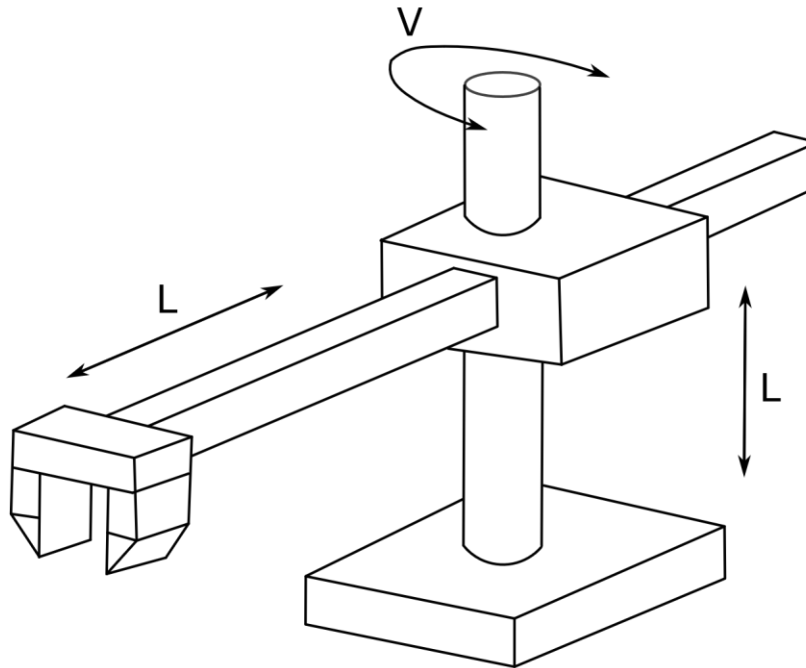


[Siegert, Bocionek96]



# Basic Robot Types

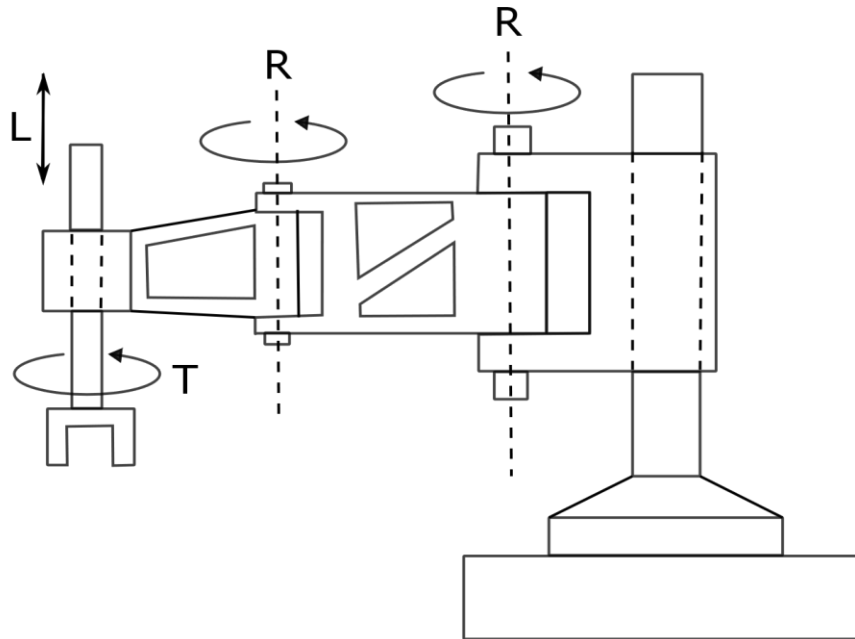
- Robot Arm (LVL)
  - Basic shape of operational space: Cylinder
  - Other possibilities: TLL, LTL



[Siegert, Bocione96]

# Basic Robot Types

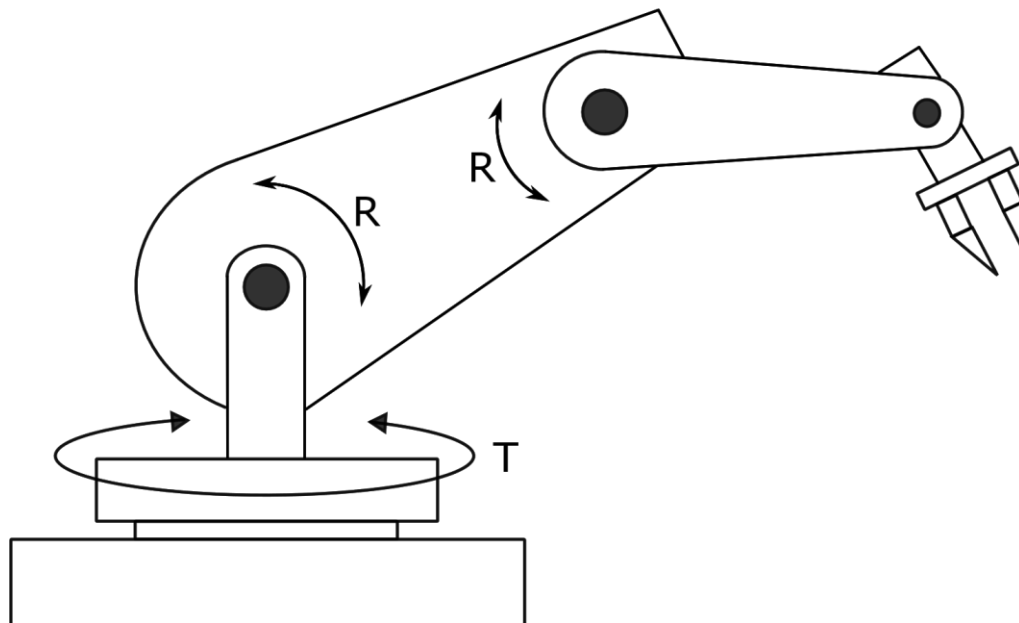
- SCARA-Robot (RRLT)
  - **S**elective **c**ompliance **a**ssembly **r**obot **a**rm
  - Basic shape of operational space: Cylinder



[Siegert, Bocionek96]

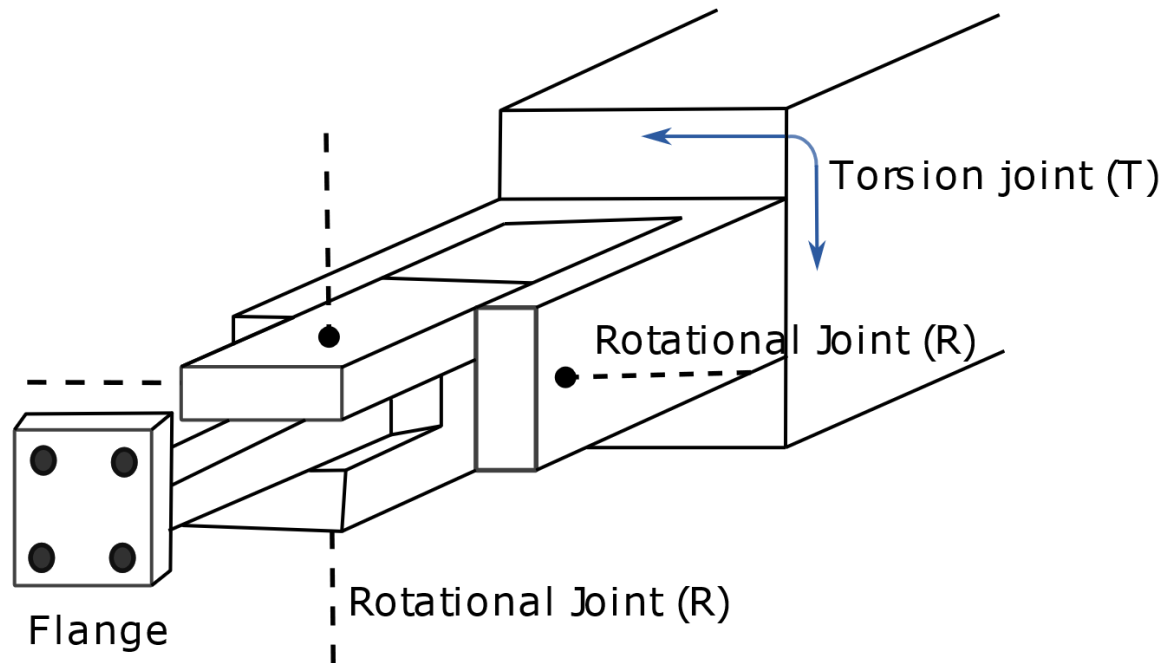
# Basic Robot Types

- Universal Robot Arm (TRR)
  - Basic shape of operational space: Sphere
  - Other possibilities: VVR



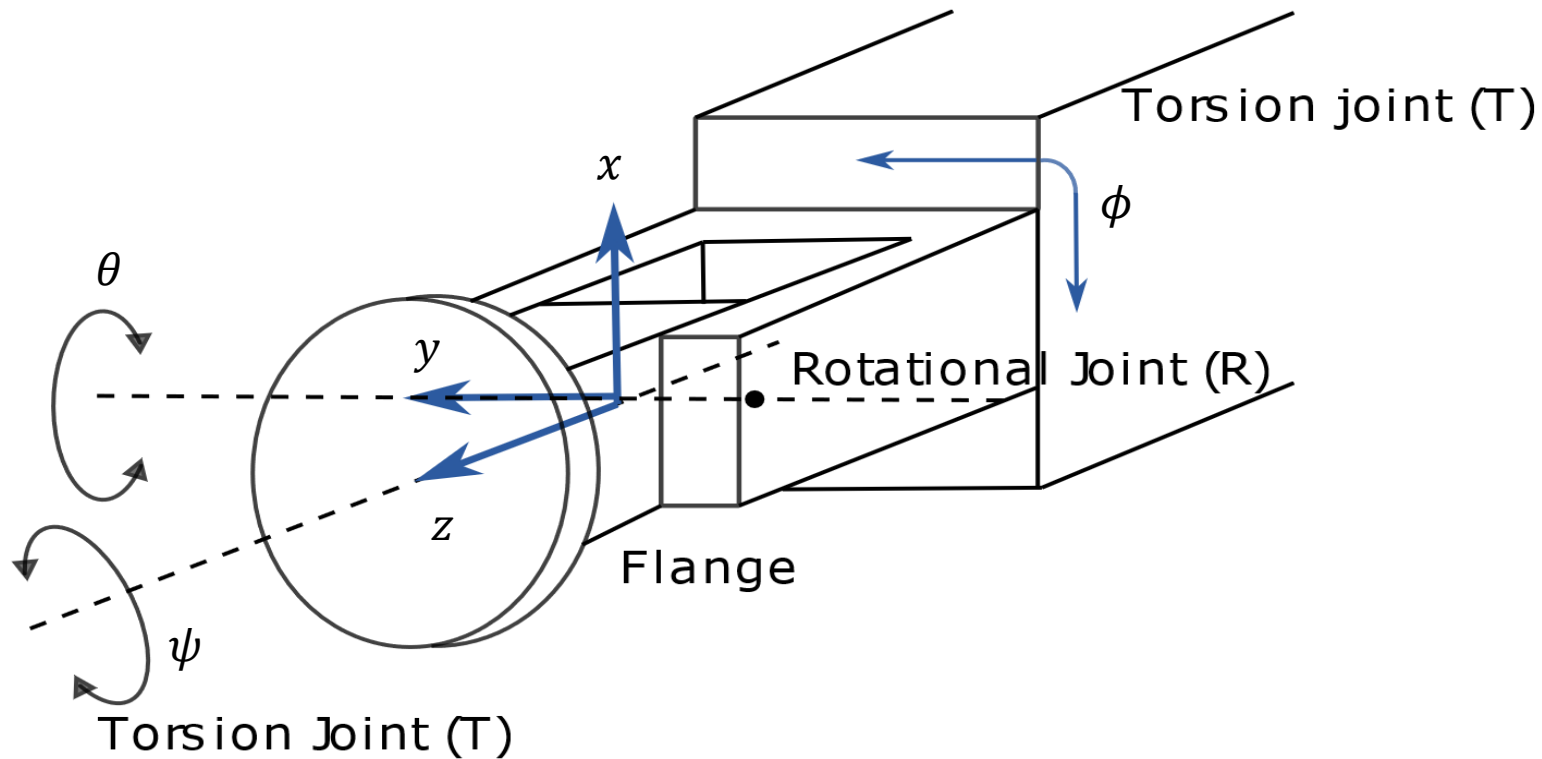
# Robotic Wrists:

- Basic Shape of Wrist (TRR)

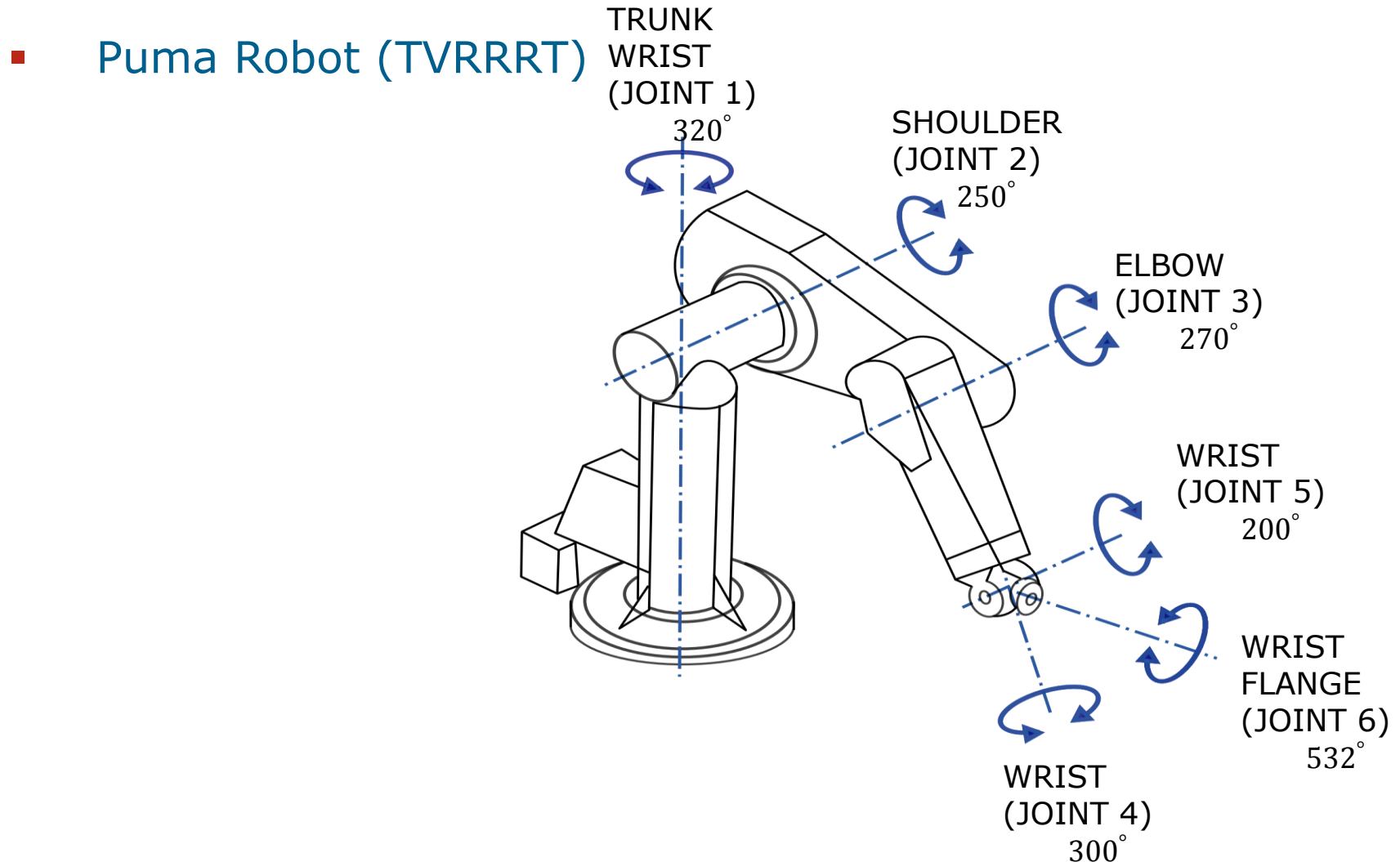


# Robotic Wrists


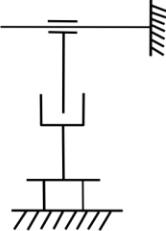
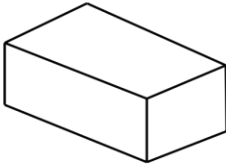

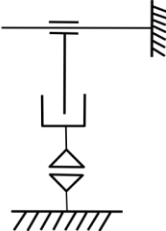
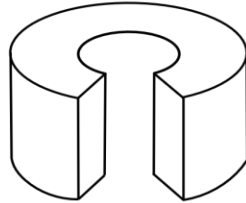
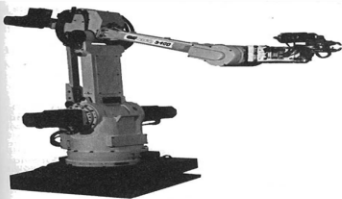
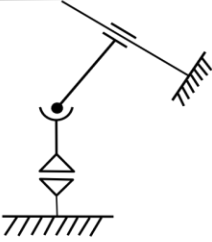

- Basic Shape of Wrist (TRT)



# Degrees of Freedom and Joints


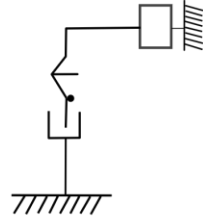
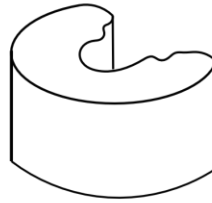

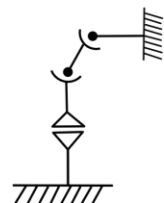
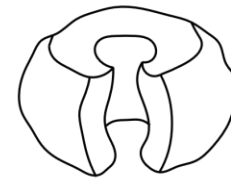

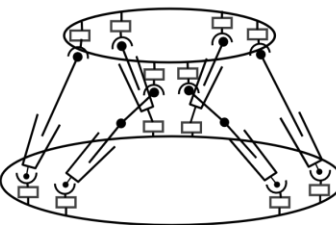



# Robot Kinematics

Robot	Axes	
	Kinematic Structure	Workspace
 Cartesian Robot		
 Cylindrical Robot		
 Spherical Robot		

[World Robotics 2003]

# Robot Kinematics

Robot	Axes	
	Kinematic Structure	Workspace
 Scara Robot		
 Articulated Robot		
 Parallel Robot		

[World Robotics 2003]



# Actuators for the Realization of active Joints

- Fluid actuators (pneumatic/hydraulic)
  - Linear
  - Rotational
  - Muscle principle
- Electric actuators
  - Linear
  - Rotational
  - DC motor (brushless, brushed)
  - AC motor
  - Stepper motors
  - Servo motor

# Pneumatic Actuators

- Used energy and control
  - Compressed air, no gear box
- Pros
  - Cheap, easy setup, fast reaction times
  - Usable in rough environments
- Cons
  - Noisy
  - Difficult control
  - Mostly just point to point
  - Bad accuracy
- Usage
  - Small robots with fast cycles and low force



# Hydraulic Actuators

- Used energy and control
  - Oil pressure, controllable valves
- Pros
  - Very high forces
  - Average speed
- Cons
  - Noise
  - Leakage of oil
  - Additional space for hydraulics are needed
  - Slow and inaccurate due to viscosity of oil
- Usage
  - Big robots



# Electric Actuators

- Used energy and control
  - Electric energy, current (voltage) control
- Pros
  - Small
  - Easy to control
  - High precision
- Cons
  - Small forces
- Usage
  - Small robots for tasks which require high accuracy



# Kinematics Module

Kinematics module (control module) of a robot allows the joints to be positioned.

The basic tasks:

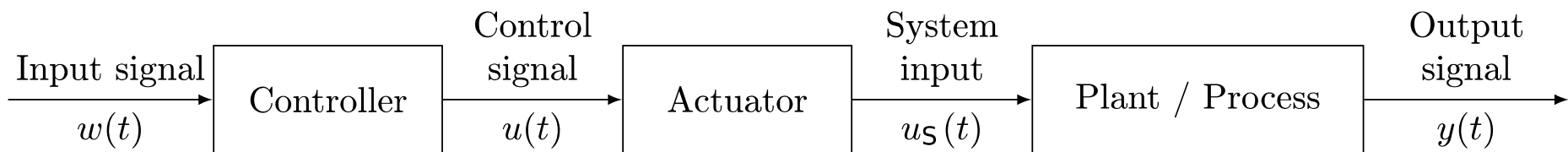
- **Forward calculation:**  
User directly specifies the joint coordinates (joint angle)
- **Backward calculation:**  
User specifies the pose of the effector that the robot should approach or move through with a certain speed and acceleration
- **Teaching path or path points:**  
User manually controls the robot arm in a sequence of target positions.

# Requirements for Joint Control

- The following requirements are often used:
  - Arm movements as fast as possible
  - Movement along the specified path without swinging, in particular no overshooting in tight curves or at the target position
  - Adaptation to loads in hand
  - Holding the arm with the load at the target position (no drifting due to the weight of the load)

# Open Loop Control

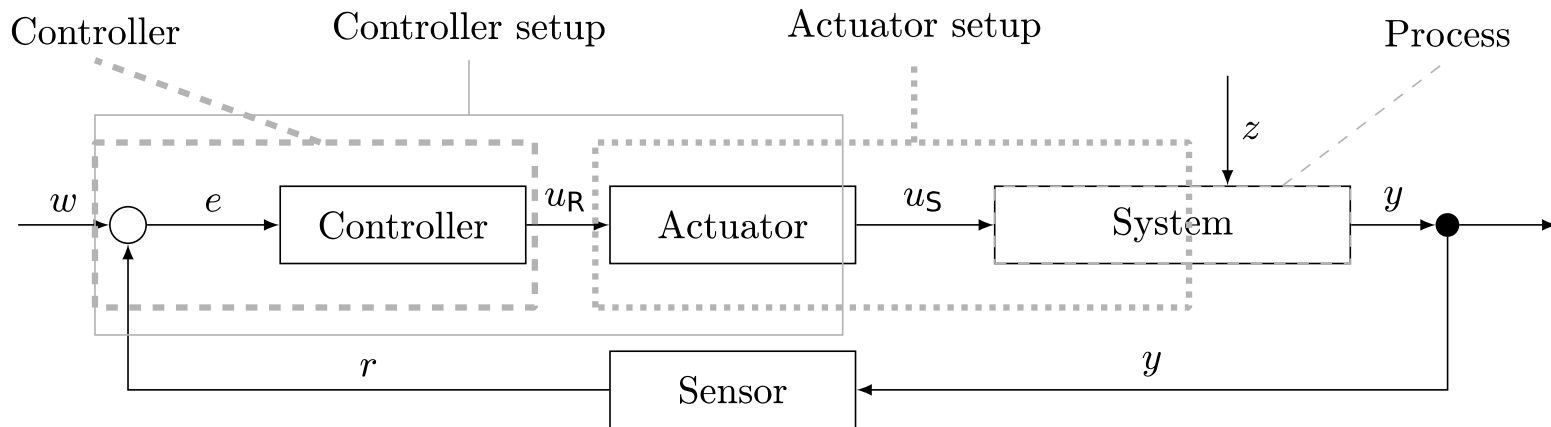
- Control variable are set without any knowledge of the current state
- No Feedback
  - No correction of input variables
  - Noise leads to deviations
  - Needs a exact model of the process
  - Result of the control is unknown



Differences between the goal and the current state can not be detected. Damage to the system is possible.

# Closed Loop Control

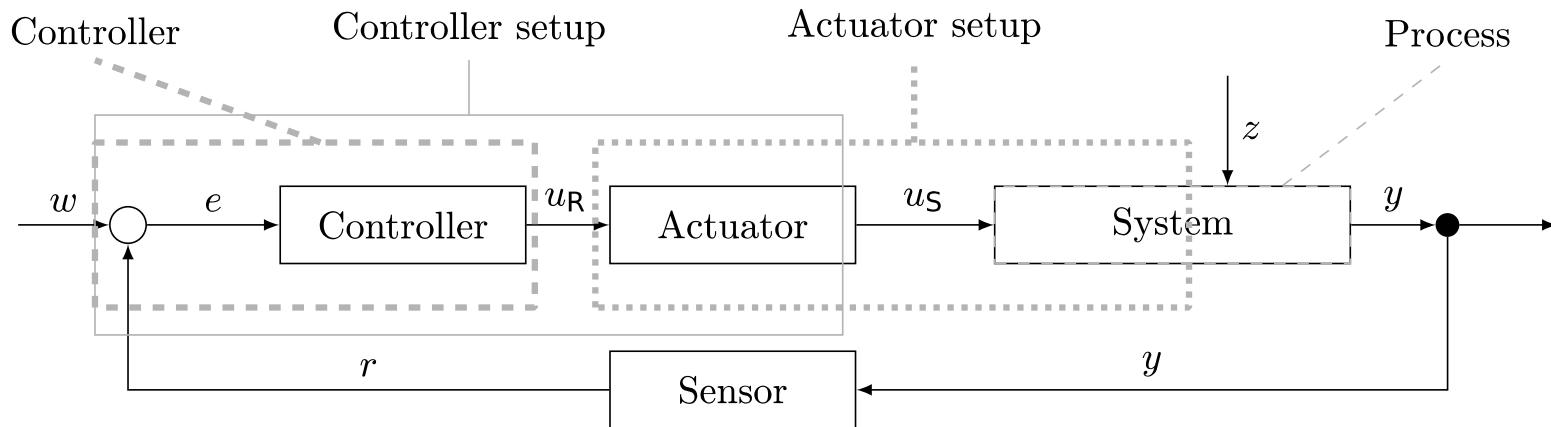
- Observes process via feedback (Closed Loop)
- Can react to Noise
- Process: Part of the system which needs to be controlled
- Reference variable  $w$ : value which the output should trace
- Control difference  $e$ : Difference between  $w$  and process variable  $r$





# Closed Loop Control

- Comparator: Calculates control difference  $e$
- Controller: Calculates from control difference signal  $e$  the output variable, which leads to a possible tracing
- Actuator: Manipulates energy flow or mass flow. Output is the system input  $u_S$ .
- Controller variable/Manipulated variable  $u_R$ : Input to actuator



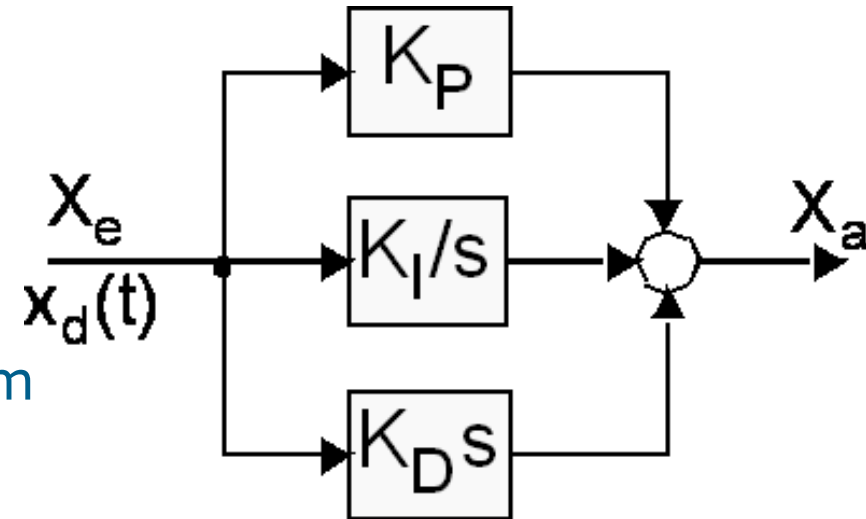
# Requirements of a Closed Loop Control

Selection of controller type and calculation of its parameters for ...

- Steady state accuracy: control difference vanishes for  $t \rightarrow \infty$
- Speed: actual value follows desired value as good/fast as possible
- Stability: no instability of control system due to feedback of system output
- Robustness: small changes of parameters of the control plant do not change the properties of the control system  
→ approximations for calculation of control parameters are feasible

## PID-Controller (often used)

- Stationary accurate
- Fast
- Tends to oscillated when the reference value is reached
- Oscillation is damped by D-term
- Frequency domain



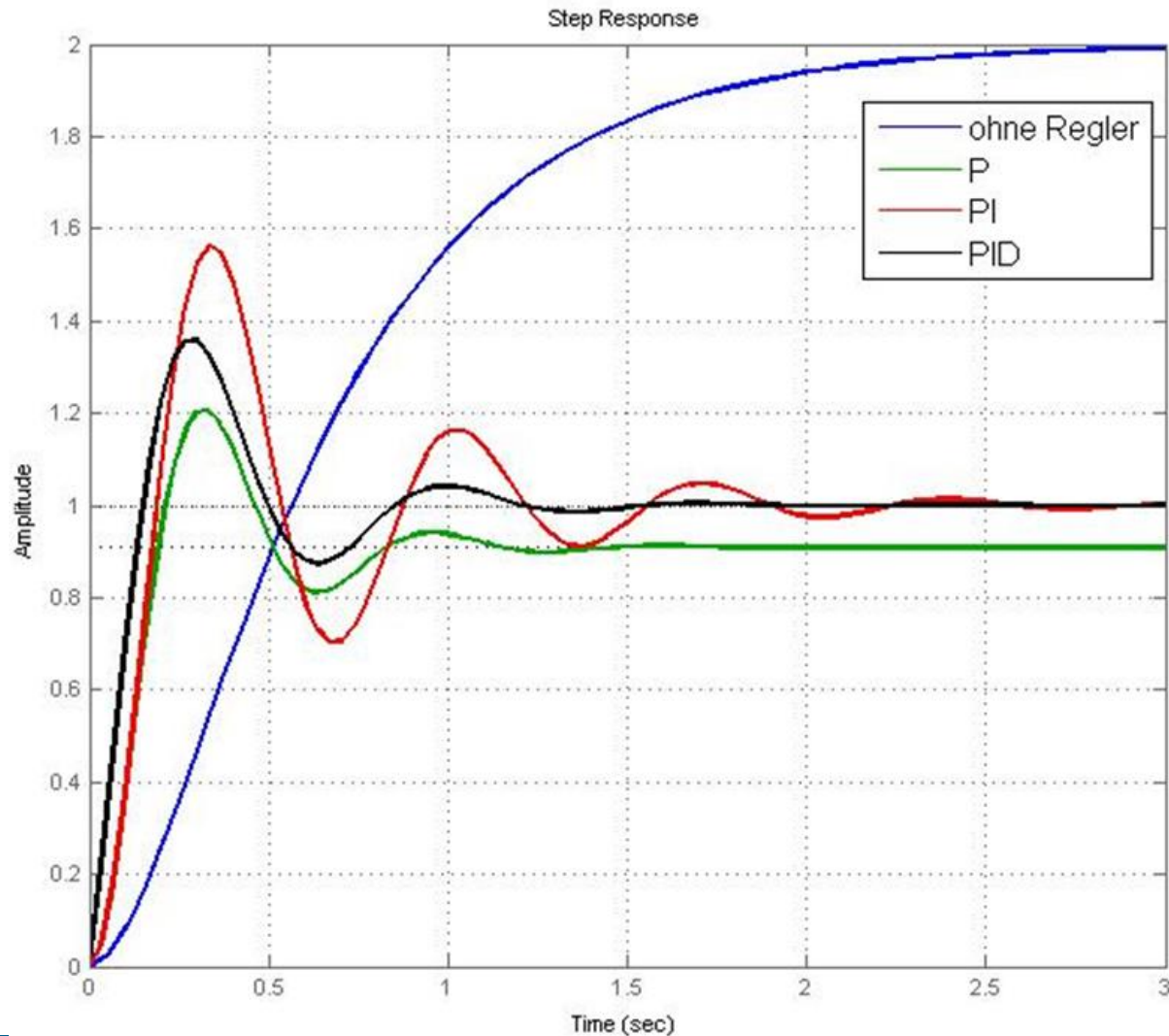
$$G_{PID}(s) = K_P + \frac{K_I}{s} + K_D \cdot s$$

$$\begin{aligned} \Rightarrow X_a(s) &= K_P X_e(s) + \frac{K_I}{s} X_e(s) + K_D \cdot s X_e(s) \\ &= K_P \left( 1 + \frac{1}{T_N s} + T_D s \right) X_e(s) \end{aligned}$$

- Time domain

$$y(t) = K_P x_d(t) + K_I \int_0^t x_d(t) dt + K_D \cdot \dot{x}_d(t)$$

# PID-Controller (Example)



# Sensor Classification: Proprioceptive

Acquisition of internal states of a robot/machine e. g.: Joint position, joint velocity, joint acceleration, orientation

- Position

- Potentiometer
- Optical encoder
- Differential transformer transducer
- Magnetic-inductive encoder

- Velocity

- Speed generator
- Optical encoder

- Acceleration

- Si-sensor
- Piezo-electric sensor

- Orientation

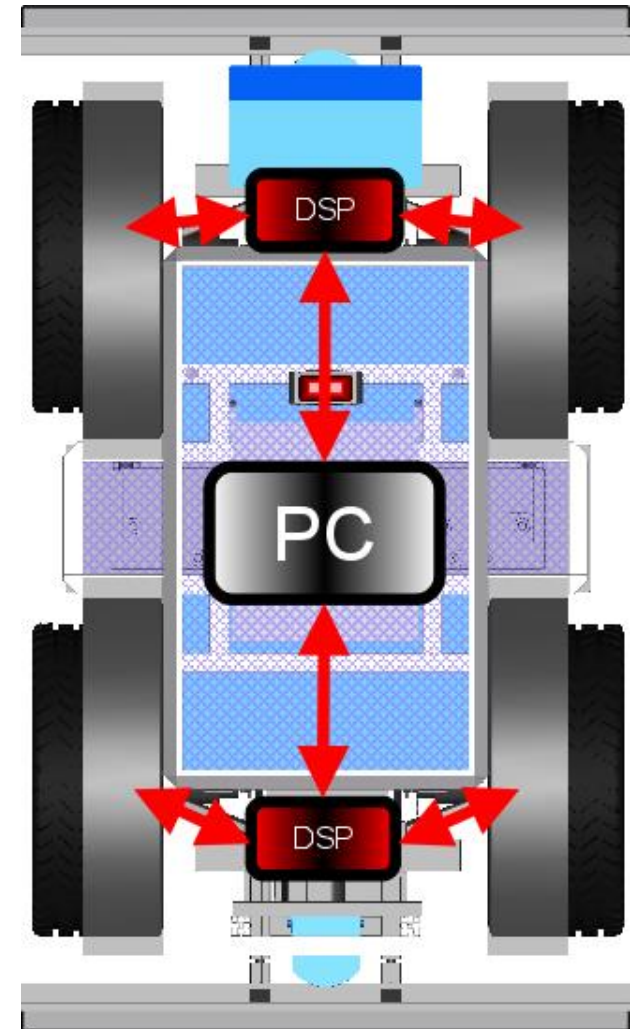
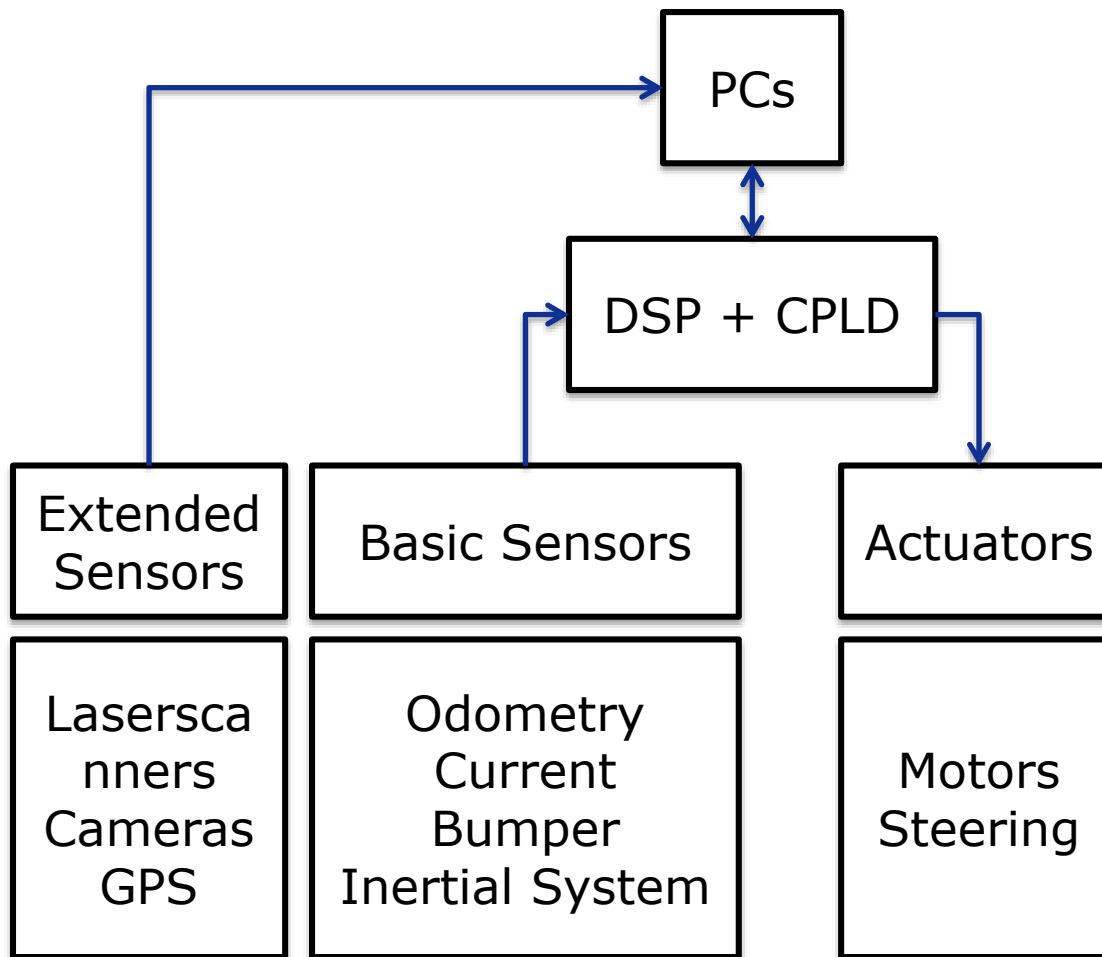
- Gyroscope
- Geomagnetic sensor

# Sensor Classification: Exteroceptive

Acquisition of external states ( $\Rightarrow$  environment) e. g.:  
obstacle distance, object identification, object position

- “Feel”
  - Artificial skin
  - Sliding sensors
  - Force-torque-sensors
- Approach
  - Inductive, capacitive sensors
  - Optical sensors
  - Acoustic sensors

# Electronics and Computing Architecture



# Simulation

## Why simulation?

- Control and perception algorithms can be developed before the robot exists
- Safe testing of algorithms
- Tests in simulation are faster (several tests in parallel on a computer cluster)
- Test can be repeated under absolutely the same conditions
- Test environments can be exchanged
- Different light and weather conditions can be generated

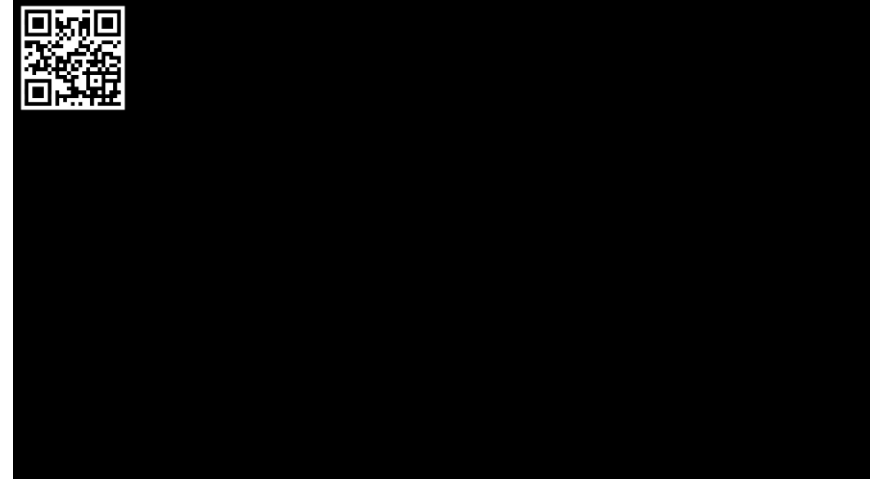


# Simulation

## Problems with simulation?

- High effort for a realistic simulation of sensor systems (real-time requirements often not fulfilled)
- Physical Engine are weak in the modelling of dynamics
- High effort for the development of simulators
- Adequate interfaces to the control system must be implemented
- Still differences between simulation and real robots in its operational environment

# Simulations using Unreal Engine



# Literature

- [Siegert, Bocionek 96] Siegert, H.-J. and Bocionek, S. (1996) Robotik: Programmierung intelligenter Roboter. Springer Verlag
- [World Robotics 2003] International Federation of Robotics, United Nation, New York and Geneva, 2003

**Coming up next ...**

# *Spatial Kinematics*

—

## *Foundations I*

