

CS 381 Homework 3 – Syntax

Submit a pdf for problems 1 – 4 and a Haskell *.hs file for problem 5.

1. Using the grammar below, show a parse tree and a leftmost derivation for the sentence

$A = B * (C + A)$

.
 $\langle \text{assign} \rangle \rightarrow \langle \text{id} \rangle = \langle \text{expr} \rangle$
 $\langle \text{expr} \rangle \rightarrow \langle \text{expr} \rangle * \langle \text{term} \rangle$
 $| \langle \text{term} \rangle$
 $\langle \text{term} \rangle \rightarrow \langle \text{factor} \rangle + \langle \text{term} \rangle \mid \langle \text{factor} \rangle - \langle \text{term} \rangle$
 $| \langle \text{factor} \rangle$
 $\langle \text{factor} \rangle \rightarrow (\langle \text{expr} \rangle)$
 $| \langle \text{id} \rangle$
 $\langle \text{id} \rangle \rightarrow A \mid B \mid C$

2. Rewrite the following BNF to add the prefix ++ and -- unary operators of Java.

.
 $\langle \text{assign} \rangle \rightarrow \langle \text{id} \rangle = \langle \text{expr} \rangle$
 $\langle \text{expr} \rangle \rightarrow \langle \text{expr} \rangle * \langle \text{term} \rangle$
 $| \langle \text{term} \rangle$
 $\langle \text{term} \rangle \rightarrow \langle \text{factor} \rangle + \langle \text{term} \rangle \mid \langle \text{factor} \rangle - \langle \text{term} \rangle$
 $| \langle \text{factor} \rangle$
 $\langle \text{factor} \rangle \rightarrow (\langle \text{expr} \rangle)$
 $| \langle \text{id} \rangle$
 $\langle \text{id} \rangle \rightarrow A \mid B \mid C$

3. Show that the following grammar is ambiguous

.
 $\langle \text{compare} \rangle \rightarrow \langle \text{boolexpr} \rangle == \langle \text{boolexpr} \rangle$
 $\langle \text{boolexpr} \rangle \rightarrow \langle \text{boolexpr} \rangle \text{ AND } \langle \text{boolexpr} \rangle$
 $| \langle \text{boolexpr} \rangle \text{ OR } \langle \text{boolexpr} \rangle$
 $| \langle \text{bool} \rangle$
 $| \text{NOT } \langle \text{bool} \rangle$
 $\langle \text{bool} \rangle \rightarrow \langle \text{boolvalue} \rangle \mid \langle \text{boolvar} \rangle$
 $\langle \text{boolvalue} \rangle \rightarrow \text{True} \mid \text{False} \mid 0 \mid 1$
 $\langle \text{boolvar} \rangle \rightarrow \mathbf{u} \mid \mathbf{v} \mid \mathbf{w}$

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4. Write a grammar G for the language L consisting of strings of 0's and 1's that are the binary representation of odd integers greater than 4. For example $11 \notin L$, $101 \in L$, $110 \notin L$. Draw parse trees for the strings 1011 and 1101

5. Below is the EBNF grammar for the animal sentence language

```
<sentence> -> <noun> <verb> [<noun>]
           | <sentence> `and` <sentence>

<noun>     -> <adj> <noun> | <noun> `and` <noun>
           | `cats` | `dogs` | `ducks` | `bunnies`

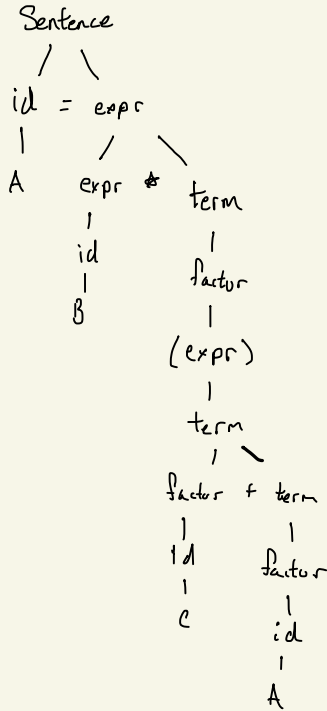
<verb>     -> `chase` | `cuddle` | `hug` | `scare`
<adj>      -> `silly` | `small` | `old` | `happy`
```

Note: the nonterminals are in $\langle \rangle$ and the terminals are in ``.

Using the animal.hs template provided.

- Define the abstract syntax for the animal language as a Haskell data type.
- Provide “pretty printing” functions for the sentences in the language.
- Provide functions to build a sentence.
- Write a function `isNice` to determine if a sentence only contains the verbs `hug` and `cuddle`.
- Write a function to build a sentence that is a conjunction of other sentences.
- Write a function `wordCount` that computes the number of words in a sentence

1: Parse tree



Leftmost derivation

Program \Rightarrow Sentence

$\Rightarrow id = expr$
 $\Rightarrow A = expr$
 $\Rightarrow A = expr * term$
 $\Rightarrow A = id * term$
 $\Rightarrow A = B * term$
 $\Rightarrow A = B * factor$
 $\Rightarrow A = B * (expr)$
 $\Rightarrow A = B * (term)$
 $\Rightarrow A = B * (factor + term)$
 $\Rightarrow A = B * (id + term)$
 $\Rightarrow A = B * (C + term)$
 $\Rightarrow A = B * (C + factor)$
 $\Rightarrow A = B * (C + id)$
 $\Rightarrow A = B * (C + A)$

2. BNF

assign $\rightarrow id = expr$

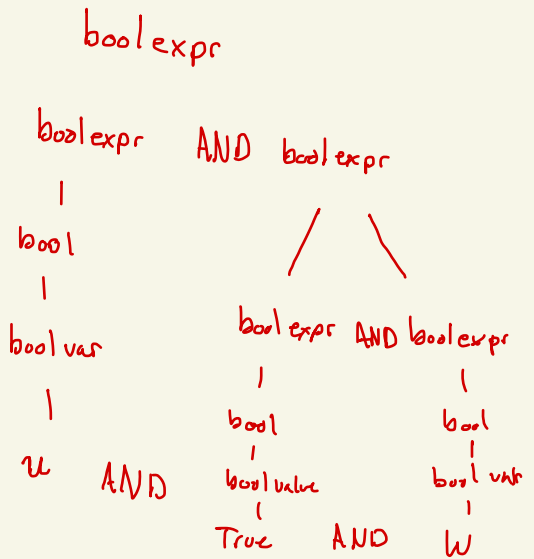
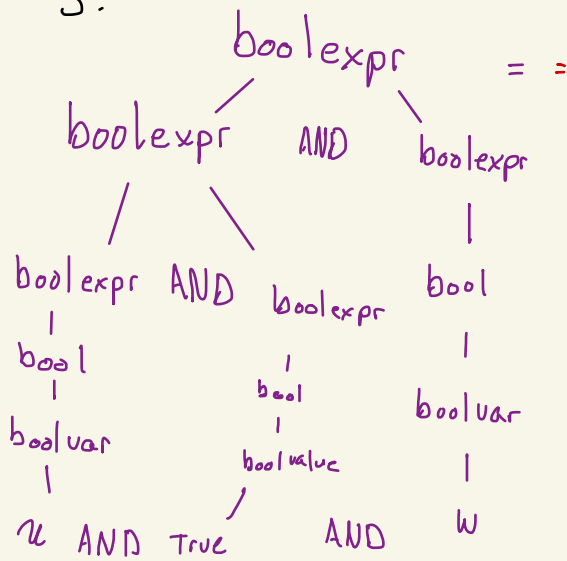
expr $\rightarrow expr * term \mid term$

term $\rightarrow factor + term \mid factor - term \mid factor$

id $\rightarrow A \mid B \mid C$

factors $\rightarrow (expr) \mid id \mid ++id \mid --id$

3:



4.

$$N = \{S, D, V\}$$

$$\Sigma = \{0, 1\}$$

$$P: V \rightarrow DS1$$

$$S \rightarrow SD \mid 01 \mid 0$$

$$D \rightarrow D1 \mid 10 \mid 1$$

