

### Heapsort:

Unsorted List → Heap → Sorted List

```
#define SIZE 10
typedef struct {
    int elem[SIZE];
    int lastNdx;
}HeapList;
```

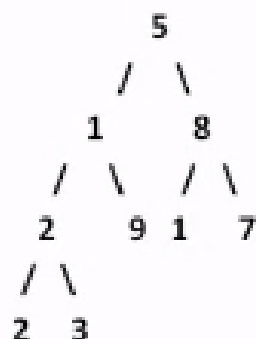
### A) Unsorted List

```
HeapList HL; //Unsorted List
```

elem	5	1	8	2	9	1	7	2	3
	0	1	2	3	4	5	6	7	8

lastNdx

## Binary Tree (not a POT)



## B) Heap [Insert all elements in an initially empty Heap]

HeapList HL; //Unsorted List

elem	5	1	8	2	9	1	7	2	3	
	0	1	2	3	4	5	6	7	8	
lastNdx	8									

## B) Heap [Insert all elements in an initially empty Heap/POT]

HeapList HL; //Unsorted List

elem	5	1	8	2	9	1	7	2	3	
	0	1	2	3	4	5	6	7	8	
lastNdx	-1									
oldLast =	8									

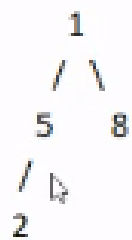
## B) Heap [Insert all elements in an initially empty Heap/POT]

HeapList HL; //Unsorted List

<u>elem</u>	1	5	8	2	9	1	7	2	3	
	0	1	2	3	4	5	6	7	8	
<u>lastNdx</u>	3									

oldLast = 8

POT



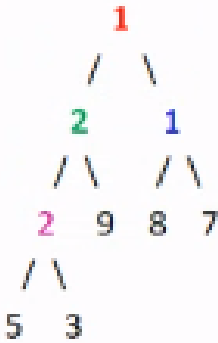
B) Heap [Insert all elements in an initially empty Heap/POT]

HeapList HL; //Unsorted List

<u>elem</u>	1	2	8	5	9	1	7	2	3	
	0	1	2	3	4	5	6	7	8	
<u>lastNdx</u>	<div>8</div>									

oldLast = 8

POT

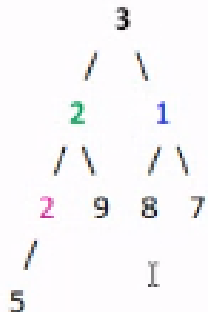


C) Sorted List [Perform deletemin until heap is empty]

HeapList HL; // Sorted List

elem	3	2	1	2	9	8	7	5	3	
	0	1	2	3	4	5	6	7	8	9
lastNdx	7									

oldLast = 8



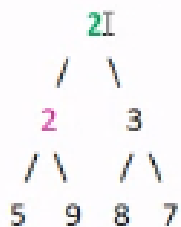
Min = 1

C) Sorted List [Perform deletemin until heap is empty]

HeapList HL; // Sorted List

elem	2	2	3	5	9	8	7	1	1	
	0	1	2	3	4	5	6	7	8	9
lastNdx	6									

oldLast = 8



Min = 1

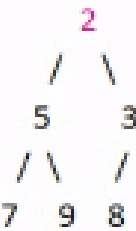
C] Sorted List [Perform deletemin until heap is empty]

HeapList HL; // Sorted List

elem	2	5	3	7	9	8	2	1	1	
	0	1	2	3	4	5	6	7	8	9

lastNdx 5

oldLast = 8



Min = 2

MinHeap	MaxHeap
<pre>graph TD; 3 --&gt; 4; 3 --&gt; 9; 4 --&gt; 6; 4 --&gt; 5; 6 --&gt; 10; 6 --&gt; 18; 5 --&gt; 7; 5 --&gt; 9; 9 --&gt; 10;</pre>	<pre>graph TD; 18 --&gt; 10; 18 --&gt; 9; 10 --&gt; 7; 10 --&gt; 10; 7 --&gt; 5; 7 --&gt; 6; 10 --&gt; 3; 9 --&gt; 9; 9 --&gt; 4;</pre>
POT Property: Priority(Parent) <= Priority(child)	POT Property: Priority(Parent) >= Priority(child)

MinHeap	MaxHeap
<b>POT Property:</b> Priority{Parent} <= Priority(child)	<b>POT Property:</b> Priority{Parent} >= Priority(child)



Type of Heap	POT Property	Root Value			
MinHeap	Priority{Parent} <= Priority(child)	Minimum			
MaxHeap	Priority{Parent} >= Priority(child)	Maximun			

<u>MinHeap</u>	<u>MaxHeap</u>
<pre> graph TD     3 --- 4     3 --- 9     4 --- 6     4 --- 5     9 --- 9     9 --- 10     6 --- 10     6 --- 18     5 --- 7 </pre>	<pre> graph TD     18 --- 10     18 --- 9     10 --- 7     10 --- 10     9 --- 9     9 --- 4     7 --- 5     7 --- 6     10 --- 3 </pre>
<b>POT Property:</b> $\text{Priority}(\text{Parent}) \leq \text{Priority}(\text{child})$	<b>POT Property:</b> $\text{Priority}(\text{Parent}) \geq \text{Priority}(\text{child})$

Type of Heap	POT Property	Root Value	Operations	Heapsort in place
<u>MinHeap</u>	$\text{Priority}(\text{Parent}) \leq \text{Priority}(\text{child})$	Minimum	Insert() and <u>deletemin</u>	Descending order
<u>MaxHeap</u>	$\text{Priority}(\text{Parent}) \geq \text{Priority}(\text{child})$	<u>Maximun</u>	Insert() and <u>deletemax</u>	Ascending order

2 ways in making the unsorted list into a heap

- 1) Insert each element into an initially empty POT (heap)
- 2) Heapify Process

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2 ways in making the unsorted list into a heap

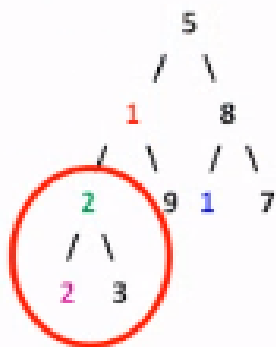
- 1) Insert each element into an initially empty POT (heap)
- 2) Heapify Process

### A) Unsorted List

HeapList HL: //Unsorted List

elem	5	1	8	2	9	1	7	2	3	
	0	1	2	3	4	5	6	7	8	9
lastNdx	8									

Binary Tree (not a POT)



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POT using <u>heapify[]</u> procedure	POT by inserting all elements in an initially empty PO
<pre> graph TD     1[1] --&gt; 1[1]     1 --&gt; 5[5]     1 --&gt; 2[2]     1 --&gt; 9[9]     5 --&gt; 8[8]     5 --&gt; 7[7]     2 --&gt; 2[2]     2 --&gt; 3[3]   </pre>	<pre> graph TD     1[1] --&gt; 2[2]     1 --&gt; 1[1]     2 --&gt; 2[2]     2 --&gt; 9[9]     1 --&gt; 8[8]     1 --&gt; 7[7]     2 --&gt; 5[5]     2 --&gt; 3[3]   </pre> <div> </div>