1 Kinematics

Scalar Product

$$\vec{A} \cdot \vec{B} = AB\cos\theta$$
$$\vec{A} \cdot \vec{B} = A_x B_x + A_y B_y + A_z B_z$$

Cross Product

$$\vec{A} \times \vec{B} = -\vec{B} \times \vec{A} = AB \sin \theta$$
$$\vec{A} \times \vec{B} = (A_y B_z - A_z B_y) \hat{i} + (A_z B_x - A_x B_z) \hat{j} + (A_x B_y - A_y B_x) \hat{k}$$

Use right hand rule (point fingers along the first vector, curl hand in towards next vector).

1D/2D Kinematics

$$\begin{aligned} v_i &= v_o + at \\ \Delta x &= v_o t + \frac{1}{2} a t^2 \\ v_f^2 &= v_o^2 + 2 a \Delta x \\ \Delta x &= \frac{1}{2} t \left(v_o + v_i \right) \end{aligned}$$

Projectile Motion

$$t = \frac{2v_o \sin \theta}{-g}$$

$$\Delta x = \frac{v_o^2 \sin (2\theta)}{-g} = \frac{2v_o^2 \sin \theta \cos \theta}{-g}$$

Relative Motion

$$v_{pw} = v_{pg} + v_{gw}$$

DRAW VECTOR DIAGRAMS

2 Newton's Laws of Motion

$$\vec{F} = m\vec{a}$$

$$F_g = mg = weight$$

$$F_g = \frac{GMm}{r^2}$$

$$g = \frac{GM}{r^2} = \frac{F_g}{m}$$

$$F_N = mg \quad \text{(horizontal surface)}$$

$$F_N = mg\cos\theta \quad \text{(angled surface)}$$

$$F_{f_s} = \mu_s F_N$$

$$F_{f_k} = \mu_k F_N$$

$$\mu_k < \mu_s \quad \text{(always)}$$

$$F_c = ma_c = \frac{mv^2}{r} = mr\omega^2$$

$$F_{drag} = \frac{1}{2}C\rho Av^2$$

$$\tan\theta = \frac{v^2}{rg} \quad \text{(banked curve)}$$

$$F_c = mg\tan\theta = F_{Nx} \quad \text{(banked curve)}$$

FREE-BODY DIAGRAMS ONLY INCLUDE EXTERNAL FORCES

3 Work Power Energy

Energy

$$E_k = \frac{1}{2}mv^2 = \frac{p^2}{2m}$$

$$E_{pg} = mgh = \frac{-GMm}{r}$$

$$E_{ps} = \frac{1}{2}k \left(\Delta x\right)^2$$

Work

$$\Delta \sum E = \Delta E_k + \Delta E_p = W$$
 = $Fd\cos\theta$ (Force parallel to direction of motion)

Power

$$P = \frac{W}{t} = Fv$$

$$h_{min} = \frac{5r}{2} \quad \text{(rollercoaster loop)}$$

4 Linear Momentum/Collisions

Momentum

Impulse

Centre of Mass

5 Rotational Motion

Rotational Kinematics

Rotational Work Power Energy

Inertia

6 Angular Momentum

Centre of Mass

A Terms/Definitions

B Constants

C Conversions

D Orders of Magnitude

E Trigonometry

F Calculus