# 1 Kinematics

### 1.1 Scalar Product

$$\vec{A} \cdot \vec{B} = AB \cos \theta$$
$$\vec{A} \cdot \vec{B} = A_x B_x + A_y B_y + A_z B_z$$

## 1.2 Cross Product

$$\vec{A} \times \vec{B} = -\vec{B} \times \vec{A} = AB \sin \theta$$
  
$$\vec{A} \times \vec{B} = (A_y B_z - A_z B_y) \hat{i} + (A_z B_x - A_x B_z) \hat{j} + (A_x B_y - A_y B_x) \hat{k}$$

Use right hand rule (point fingers along the first vector, curl hand in towards next vector).

### 2 Newton's Laws of Motion

$$\vec{F} = m\vec{a}$$

$$F_g = mg = weight$$

$$F_g = \frac{GMm}{r^2}$$

$$g = \frac{GM}{r^2} = \frac{F_g}{m}$$

$$F_N = mg \quad \text{(horizontal surface)}$$

$$F_N = mg \cos\theta \quad \text{(angled surface)}$$

$$F_{f_s} = \mu_s F_N$$

$$F_{f_k} = \mu_k F_N$$

$$\mu_k < \mu_s \quad \text{(always)}$$

$$F_c = ma_c = \frac{mv^2}{r} = mr\omega^2$$

$$F_{drag} = \frac{1}{2}C\rho Av^2$$

$$\tan\theta = \frac{v^2}{rg} \quad \text{(banked curve)}$$

$$F_c = mg \tan\theta = F_{Nx} \quad \text{(banked curve)}$$

# 1.3 1D/2D Kinematics

$$v_i = v_o + at$$

$$\Delta x = v_o t + \frac{1}{2}at^2$$

$$v_f^2 = v_o^2 + 2a\Delta x$$

$$\Delta x = \frac{1}{2}t(v_o + v_i)$$

#### 1.3.1 Projectile Motion

$$\begin{split} t &= \frac{2v_o \sin \theta}{-g} \\ \Delta x &= \frac{v_o^2 \sin \left( 2\theta \right)}{-g} = \frac{2v_o^2 \sin \theta \cos \theta}{-g} \end{split}$$

# FREE-BODY DIAGRAMS ONLY INCLUDE EXTERNAL FORCES

# 3 Work Power Energy

# 3.1 Energy

$$E_k = \frac{1}{2}mv^2 = \frac{p^2}{2m}$$

$$E_{pg} = mgh = \frac{-GMm}{r}$$

$$E_{ps} = \frac{1}{2}k \left(\Delta x\right)^2$$

### 3.2 Work

$$\Delta \sum E = \Delta E_k + \Delta E_p = W$$

$$= Fd \cos \theta \quad \text{(Force parallel to direction of motion)}$$

### 3.3 Power

$$P = \frac{W}{t} = Fv$$
 
$$h_{min} = \frac{5r}{2} \quad \text{(rollercoaster loop)}$$

# 1.4 Relative Motion

$$v_{pw} = v_{pg} + v_{gw}$$

- 4 Linear Momentum/Collisions
- 4.1 Momentum
- 4.2 Impulse
- 4.3 Centre of Mass
- 5 Rotational Motion
- 5.1 Rotational Kinematics
- 5.2 Rotational Work Power Energy
- 5.3 Inertia
- 6 Angular Momentum
- 6.1 Centre of Mass
- A Terms/Definitions
- **B** Constants
- C Conversions
- D Orders of Magnitude
- E Trigonometry
- F Calculus

3