# ECE 549 Computer Vision: Homework 3

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## 1 Single-View Metrology

### 1.1 Vanishing Points and Vanishing Lines

After determining the parallel lines in images, the vanishing points could be obtained by using cross product of two parallel lines. In my implementation, I use the criteria that the best Vanishing Points minimizes the angles between itself and center points of all the lines to choose VP. Detailed implementation is in *getVP.m*. Figure 1, 2 3 show the detected Vanishing points on X, Y, Z directions respectively.

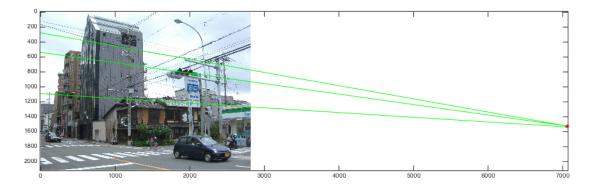


Figure 1: Vanishing Point X:  $10^3 * [7.4953, 1.5383, 0.0010]$ 

Horizon vanishing line could be estimated by taking cross product of VP1 and VP2 (both in horizon directions), which is  $10^3 * [1.1216, -6.4439, 0.0010]$ .

#### 1.2 Focal Length and Optical Center

Given the intrinsic matrix as

$$K = \left(\begin{array}{ccc} f & 0 & u_0 \\ 0 & f & v_0 \\ 0 & 0 & 1 \end{array}\right)$$

and vanishing points  $X_i^T X_j = 0$ ,  $\forall i \neq j$ , we can use the estimated three vanishing points to estimate the intrinsic matrix K, by taking:

$$X_i^T X_j = p_i^T K^{-T} K^{-1} p_j = 0, \forall i \neq j$$



Figure 2: Vanishing Point Y:  $10^3 * [0.0304, 1.5086, 0.0010]$ .

, because the rotation matrix  $R^T R = I$ . Moreover,

$$K^{-T}K^{-1} = \begin{pmatrix} 1/f^2 & 0 & -u_0/f^2 \\ 0 & 1/f^2 & -v_0/f^2 \\ -u_0/f^2 & -v_0/f^2 & \frac{u_0^2 + v_0^2}{f^2} + 1 \end{pmatrix}$$

.

By involving symbol variables in Matlab command *solve*, we can get the solution: f = 2248.48,  $(u_0, v_0) = (803.52, 1247.62)$ .

#### 1.3 Rotation Matrix

Solving the rotation matrix also relies on the detected three vanishing points. Since

$$\omega \left( \begin{array}{c} u \\ v \\ 1 \end{array} \right) = KR \left( \begin{array}{c} X \\ Y \\ Z \end{array} \right)$$

.

we use the correspondences between  $p_1$  and [1,0,0],  $p_2$  and [0,1,0],  $p_3$  and [0,0,1] to solve each column of rotation matrix R, as:

$$\omega_1 * p_1 = KR \begin{pmatrix} 1\\0\\0 \end{pmatrix} = Kr_1$$

$$\omega_2 * p_2 = KR \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix} = Kr_2$$

$$\omega_3 * p_3 = KR \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} = Kr_3$$

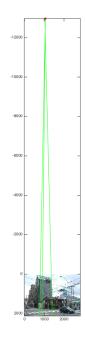


Figure 3: Vanishing Point Z:  $10^3 * [1.1216, -6.4439, 0.0010]$ 

and the constraints that  $R * R^T = I$  to solve rotation matrix R, and got:

$$R = \begin{pmatrix} 0.9499 & -0.3123 & -0.0119 \\ 0.0499 & 0.1140 & 0.9922 \\ 0.3085 & 0.9431 & -0.1238 \end{pmatrix}$$

## 1.4 Height Estimation

First Estimate the horizon line:  $p_1 = 1.0e + 03*[6.3995, 1.3115, 0.0010], p_2 = 1.0e + 03*[-1.4942, 1.2491, 0.0010].$ And horizon line is got by cross product of  $p_1$  and  $p_2$ : [0, -0.0008, 1.000]



Figure 4: Horizontal Vanishing Line, estimated by two VPs, 1.0e + 03 \* [0.0000, -0.0010, 1.5185].