MATH-338 Midterm 1 Study Guide

THEORY

Day 2: Independent events happen same time, not affecting one another $(P(A \cap B) = P(A)P(B))$. Disjoint is the opposite $(P(A \cap B) = 0)$. Probability Mass Function (PMF) is a dictionary mapping of events to positive probabilities. Over an infinite amount of iterations, RVs converge to a number.

Day 3: Law of Large Numbers: more times means more precise result.

Day 4: Parameter: any numerical quantity that characterizes a given population. Population proportion: a percentage value associated with a population. Sample proportion: the proportion of individuals in a sample sharing a certain trait (\hat{p}) . Sample Mean (\bar{X}) . Sampling distribution: probability distribution of statistic obtained through a large number of samples drawn (sample must be know).

Day 5: We want low bias and high variability. Bias bad. Variability ↓ as the sample size ↑. Binomial Probability Distribution Conditions: Binary outcome (TF), Independent (previous outcomes do not affect next.), Number of outcomes, Success is equally likely. 'X' denotes the number of successes and 'n' is the number of elements in your sample. \hat{P} does **NOT** have a binomial distribution.

Day 6: Interacting variables: one variable can affect the another variable (non-independent). Confounding variables a factor that influences the results of an experiment. Block design: split sample initially based on traits (possibly confounding) then randomly assign in those groups. Matched Pairs Design: blocks sizes of two (only looking with two levels). Repeated Measures Design two similar subjects have the same tests and those results are compared. Hawthorne Effect: individuals know they are being experimented on.

Day 7: Sensitivity: proportion of actual positive. Specificity: proportion of actual negative. Predictive Value: proportion of positive tests that were actually positive. Negative Predictive Value: same as above but for negative. Prevalence: base rate.

Day 8: Neyman-Pearson Testing: This test will allow us to make preemptive decisions based on conditions presented before the study is conducted. These are the theoretical outcomes WITHOUT taking any sample data. Null Hypothesis: nothing unexpected (original hypothesis, H₀). Alternate Hypothesis: "something is happening and we should change our minds" (Ha). Critical region: range of values that corresponds to the rejection of Ho at some chosen probability level. Type I Error: occurs when a significance test results in the rejection of a true null hypothesis. Type II Error: the data do not provide strong evidence that the null hypothesis is false.

FORMULAS

• Mean of Probability Dist. : $\mu_{\rm x} = \Sigma x \times p(x)$ • Variance : $\sigma^2_{\ {\rm x}} = \Sigma [x^2 \times P(x)] - \mu^2_{\ {\rm x}}$

• Standard Deviation : $\sigma_x = \sqrt{\sigma_x}$ and $\sigma_{x+y} = \sqrt{\sigma_x + \sigma_y}$

• Number successes : $X \sim B(n, p)$

Mean of binomial RV: nP

• Variance of Bernoulli RV: P(1-P)

• Variance of binomial RV: $n\hat{P}(1-\hat{P})$

• Standard deviation of binomial RV: $\sqrt{nP(1-P)}$

• Bayes' Rule: $\frac{P(B|A)P(A)}{P(B)}$

• $P(B|A) = \frac{number of outcomes in A \cap B}{number of outcomes in A} = \frac{P(A \cap B)}{P(A)} > 0$

• Population proportion: $\hat{P} = \frac{X}{n}$

 $Variance(\hat{P}) = \frac{P(1-P)}{P(1-P)}$

• Standard Deviation(\hat{P}) = $\sqrt{\frac{P(1-P)}{n}}$

• Sensitivity: $\frac{TP}{TP+FN}$

• Specificity: $\frac{TN}{TN+FP}$

• PPV: $\frac{TP}{TP+FP}$

• NPV: $\frac{TN}{TN+FN}$

 $\alpha = P(1) - P(\text{Concluded H}_{a} \mid \text{H}_{0} \text{ is true})$

Baseline $\alpha = 0.05$

 $\beta = P(2) - P(Concluded H_0 \mid H_a)$

Power: $1 - \beta$

ABBREVIATIONS AND MISC

· TP: True Positive

• TN: True Negative

• FP: False Positive • FN: False Negative Independent events: $P(A \cap B) = P(A) \times P(B)$

Conditional probability: $P(A \cap B) = P(A) \times P(B|A)$ [Tree Mapping]