

## Chapter 6 – Section 6.2 Vertical Stretches and Compressions

## TICKET-IN-THE-DOOR

In order to be prepared for class you must watch the module and complete the following activity. This is due first thing when you get to class.

Given  $y = k f(x)$  describe in words the transformation when  $k$  is a positive constant:

- $y = k f(x)$

- when  $0 < k < 1$

VERTICAL COMPRESSION by factor of  $k$  (WIDE)

- when  $k > 1$

VERTICAL STRETCH by factor of  $k$  (Narrow)

Check your understanding:

1. The domain of  $f(x)$  is  $-6 \leq x \leq 8$  and the range is  $6 \leq y \leq 12$ . If  $g(x) = 3f(x-6)$ , what is the domain and range of  $g(x)$ ?

Domain:  $0 \leq x \leq 14$

Range:  $18 \leq y \leq 36$

2. The US population in millions is  $P(t)$  today and  $t$  is in the years. Write in words the meaning of the following with respect to the context of the problem.

a)  $P(t) - 10$  The U.S. population is 10 million less than today's population @ time  $t$ .

b)  $P(t) + 10$  The U.S. population is 10 million more than today's pop @ time  $t$ .

c)  $P(t+10)$  Today's U.S. population in millions 10 years earlier.

d)  $.10 P(t)$  10 percent of today's U.S. population @ time  $t$  years.

e)  $P(t) + .10$  The U.S. population is 100,000 more than today's pop @ time  $t$ .

3. The graph of  $f(x)$  contains the point  $(3, -2)$ . What corresponding point must be on the graph of  $g(x) = 2f(x-9)$ ?

Sol  $(12, -4)$

4. The graph of  $g(x)$  is the graph of  $f(x)$  after it has been vertically stretched or shrunk. The point  $(3, 6)$  lies on the graph of  $f(x)$ . The corresponding point on the graph of  $g(x)$  is  $(3, 12)$ . What is a possible formula for  $g(x)$  in terms of  $f(x)$ ?

Sol  $g(x) = 2 \cdot f(x)$

# SOLUTIONS

Click Section 6.3 Horizontal Stretches and Combinations

## OPEN THE DOOR

In order to be prepared for class you must watch the module and complete the following activity. This is due first thing when you get to class.

Given  $y = f(kx)$  describe in words the transformation when  $k$  is a positive constant:

- $y = f(kx)$

when  $0 < k < 1$

when  $k > 1$

HORIZONTAL STRETCH by factor of  $\frac{1}{k}$   
HORIZONTAL COMPRESS by factor of  $\frac{1}{k}$

Check your understanding:

- The graph of  $h(x)$  contains the point  $(5, 10)$ . What is the corresponding point on the graph of  $y = h(5x)$ ?

$(-1, 10) \Rightarrow$  HORIZONTAL COMPRESSION by  $\frac{1}{5}$

- The point  $(2, -8)$  lies on the graph of  $f$ . If the graph of  $f$  is compressed vertically by a factor of  $\frac{1}{5}$  and stretched horizontally by a factor of 11, what point must lie on the transformed graph?

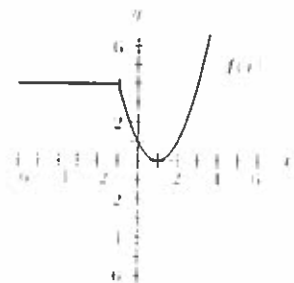
$(22, -\frac{8}{5})$

$\frac{1}{5} f(\frac{1}{11}x)$

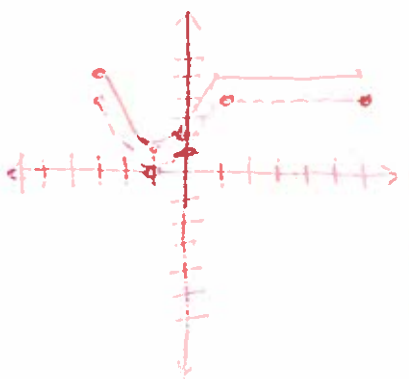
- The graph of a function  $f$  has been stretched vertically by a factor of 8, compressed horizontally by a factor of 6, and then shifted up 2 units and shifted 6 units to the left. The new graph is produced by a function  $g$ . Find a formula for  $g$  in terms of  $f$ .

$$g(x) = 8 \cdot f(6(x+6)) + 2$$

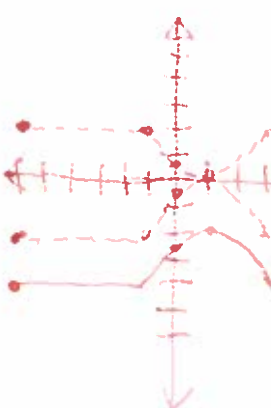
- The graph of the function  $f(x)$  is shown below. Graph the following transformations. Then list in words the transformation used.



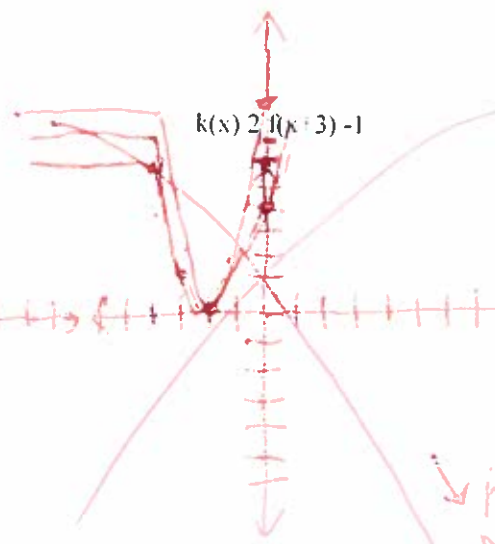
a)  $g(x) = f(-x) + 1$



b)  $h(x) = \frac{1}{2} f(x) - 2$



k(x) = 2 f(x+3) - 1



next page

(c)  $2f(x+3)-1$

