

Physics 225

Section 2,
Fall 2018

Clicker question #1

Question 3.4a Firing Balls I

A small cart is rolling at **constant** velocity on a flat track. It fires a ball straight up into the air as it moves. After it is fired, what happens to the ball?

A

it depends on how fast the cart is moving

B

it falls behind the cart

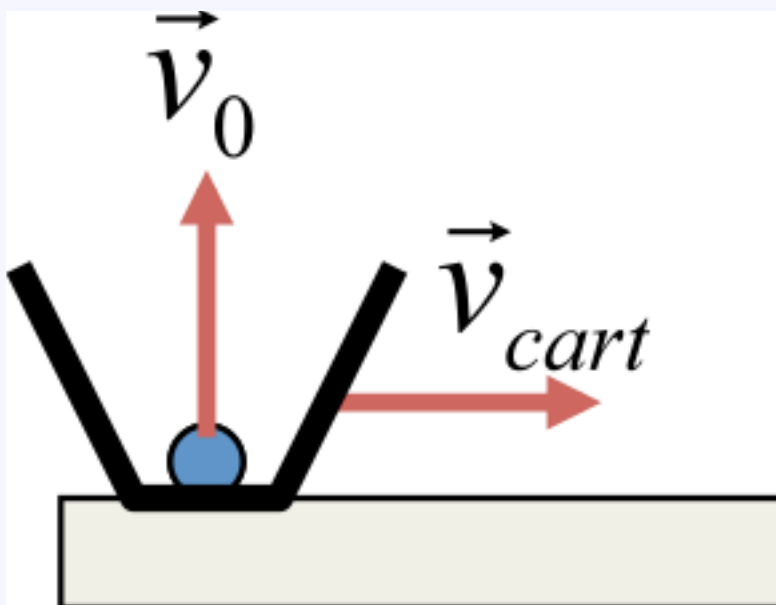
C

it falls in front of the cart

D

it falls right back into the cart

it remains at rest





Clicker question #2

Which is the initial *velocity*?

A



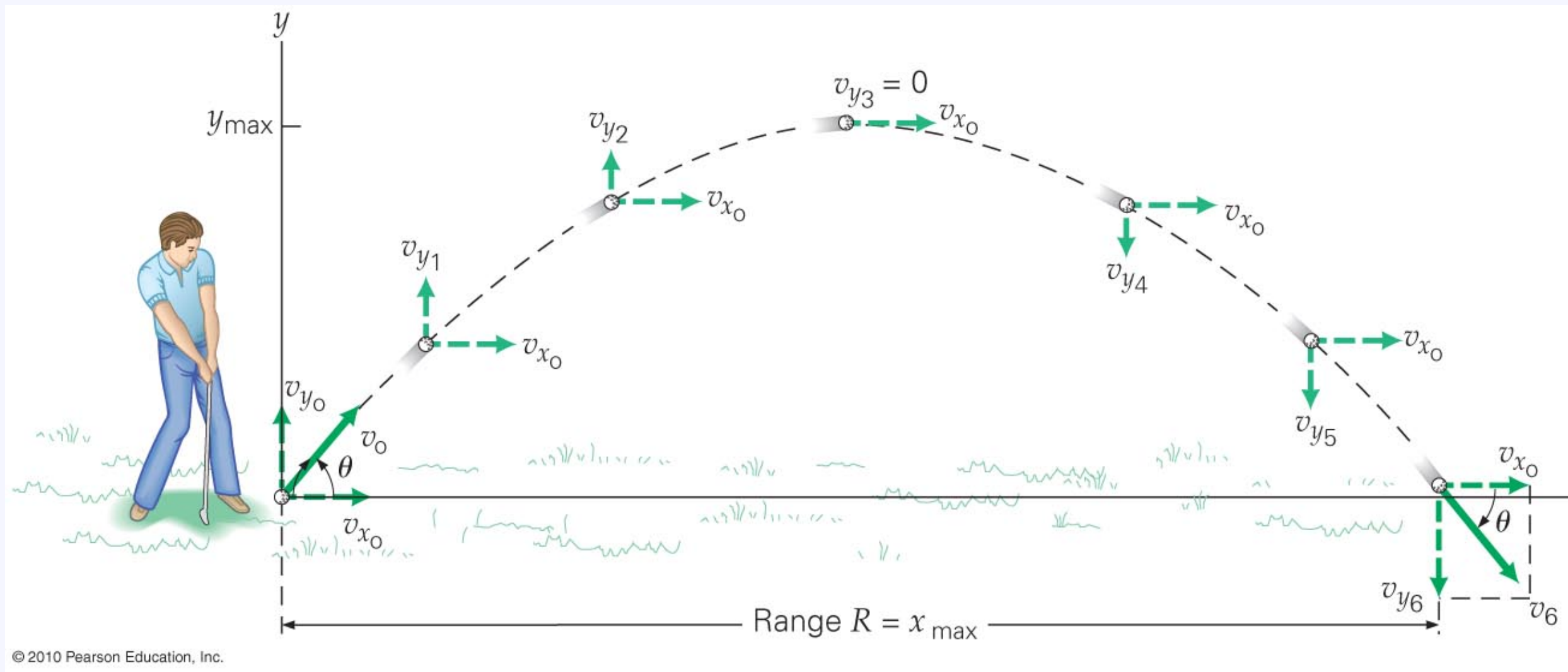
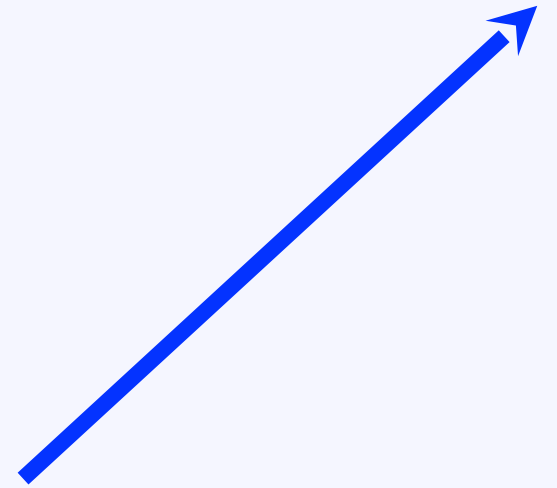
B



C



D



Clicker question #2a

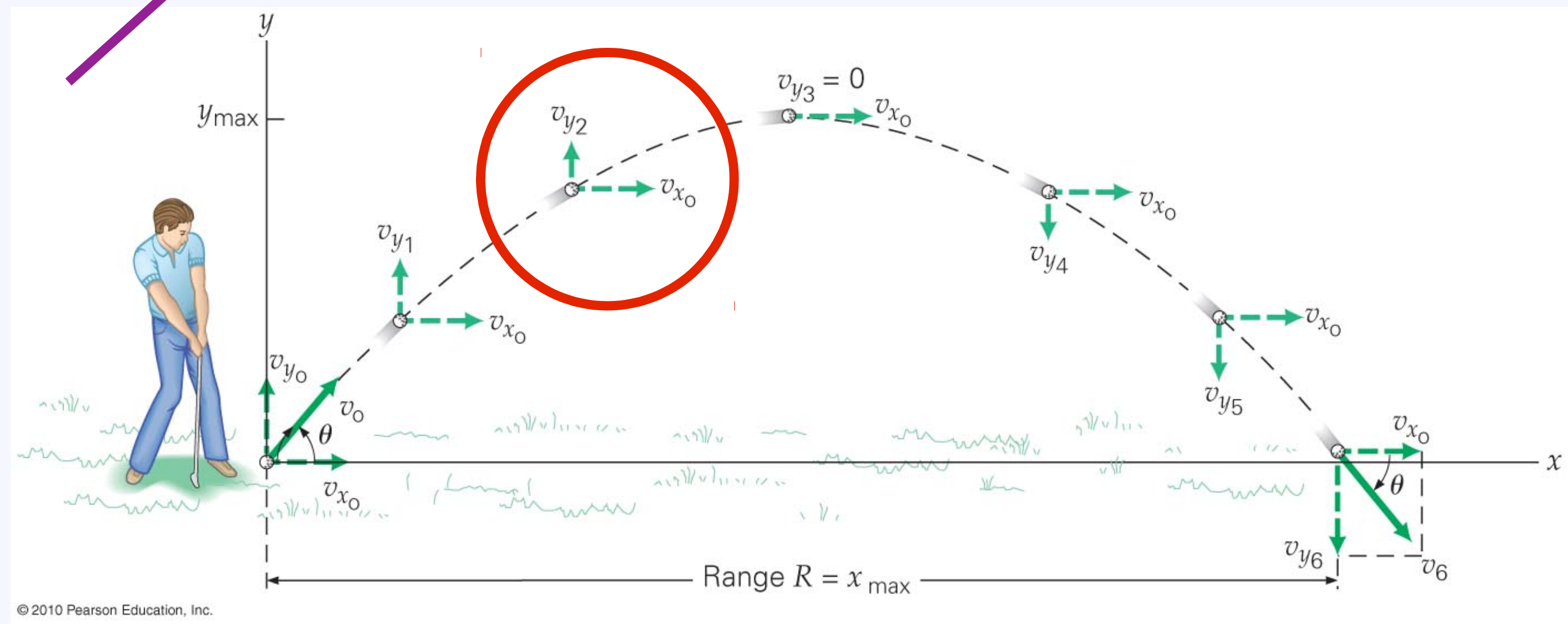
Which is the *position* at the **circled** time?

A

B

C

D



Clicker question #2b

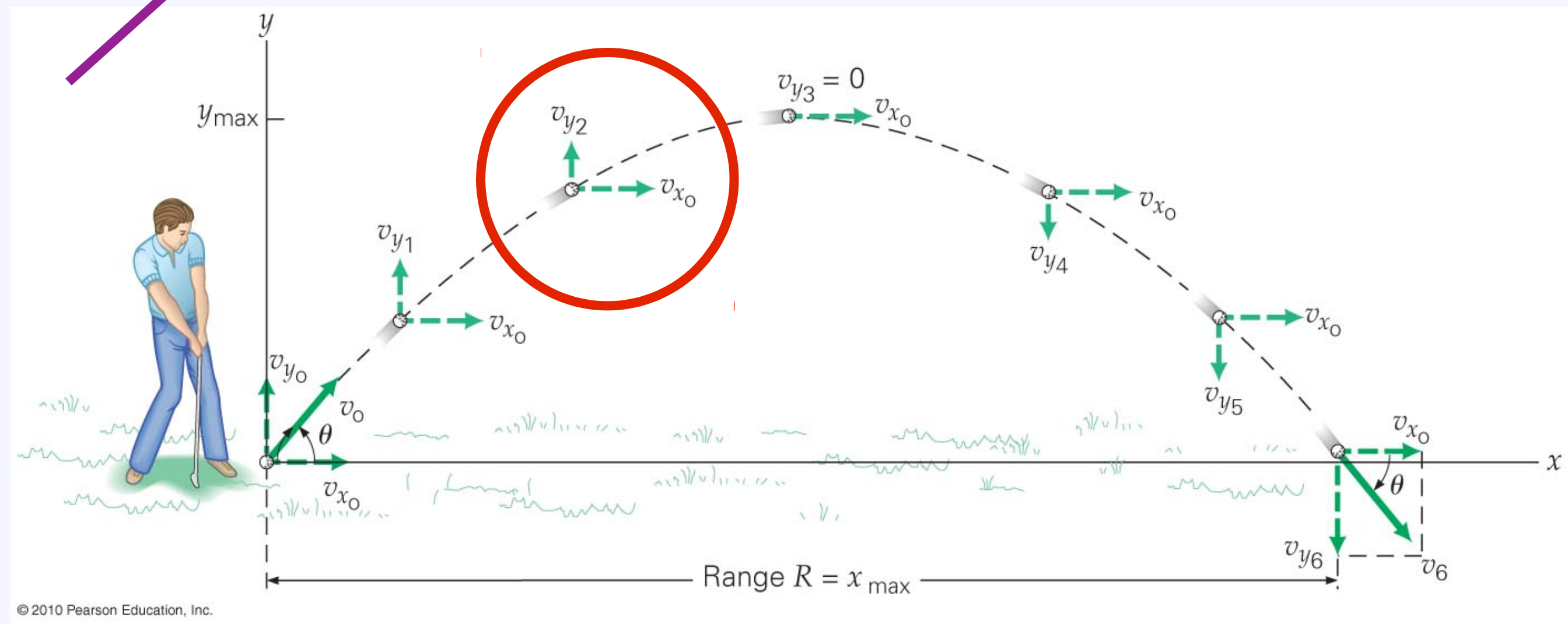
Which is the *acceleration* at the **circled** time?

A

B

C

D



Clicker question #2c

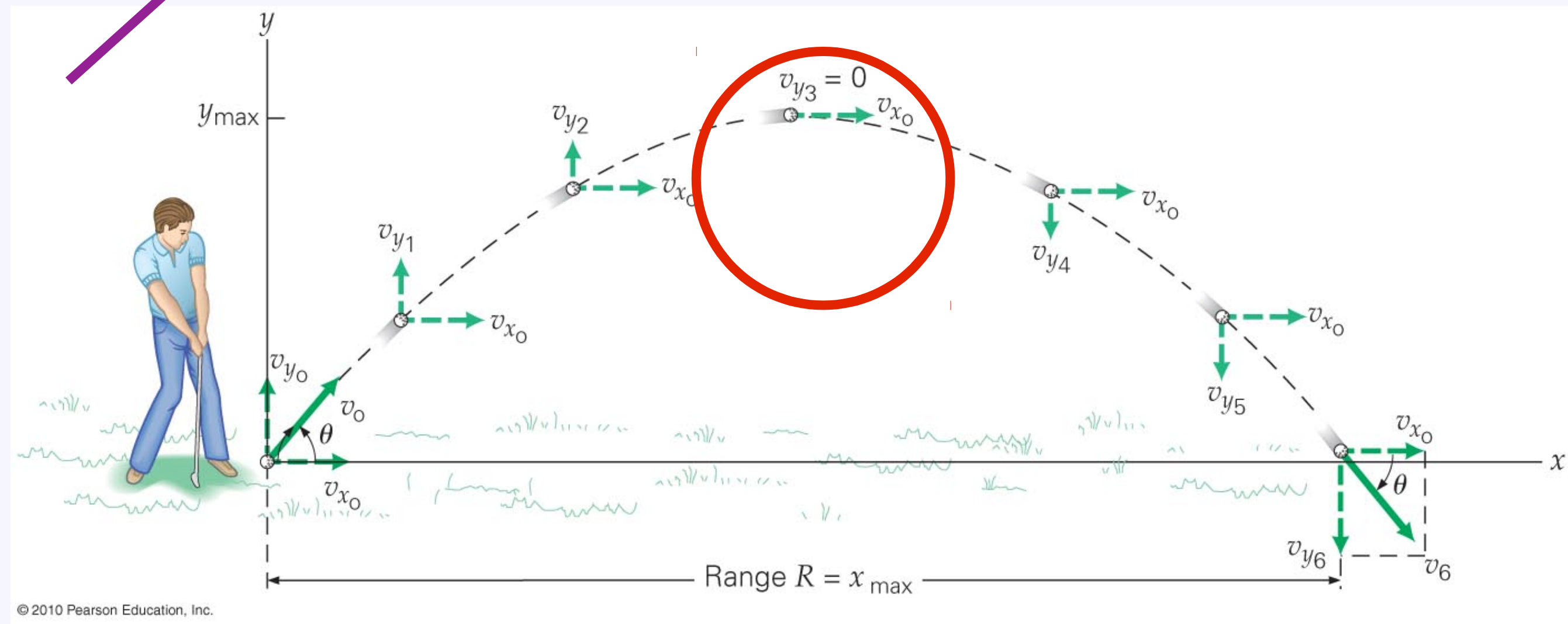
Which is the *acceleration* at the **circled** time?

A

B

C

D



Clicker question #2d

What is the x component of the velocity at the **circled** time?

A



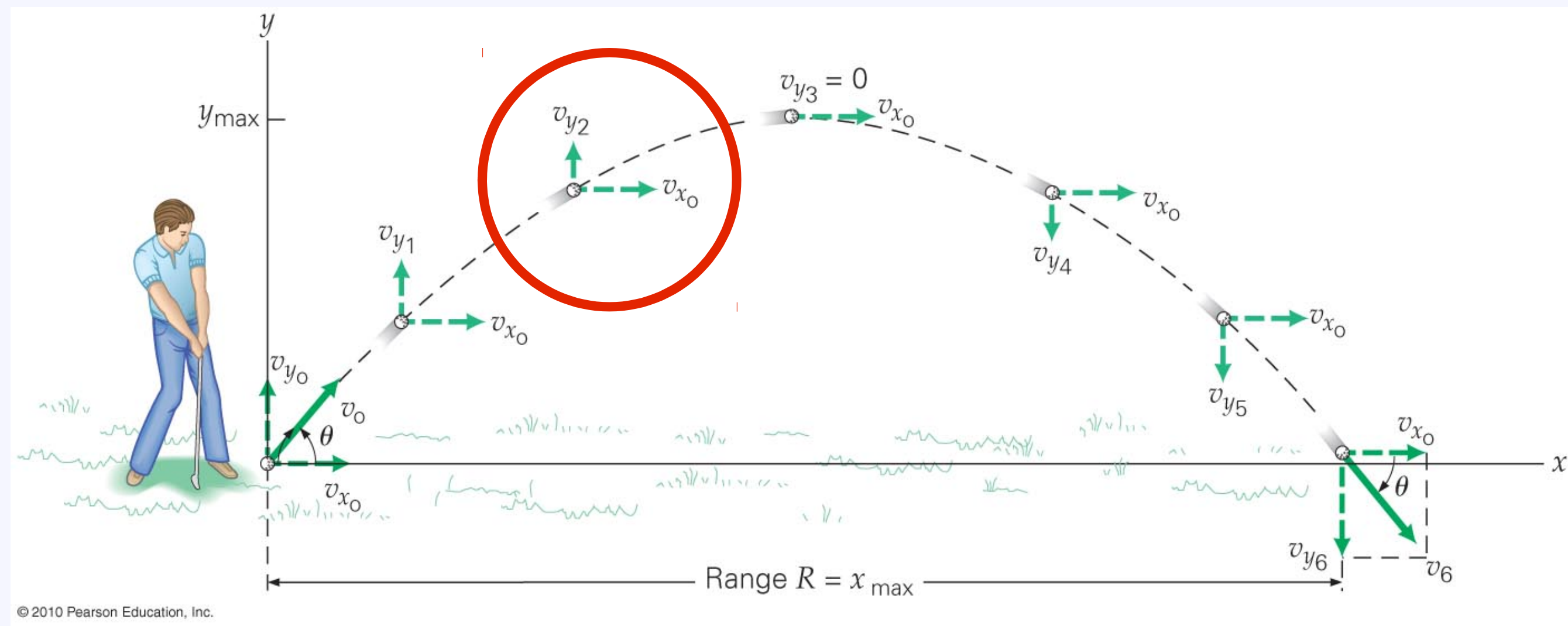
B



C



D



Clicker question #2e

What is the *y* component of the velocity at the **circled** time?

A



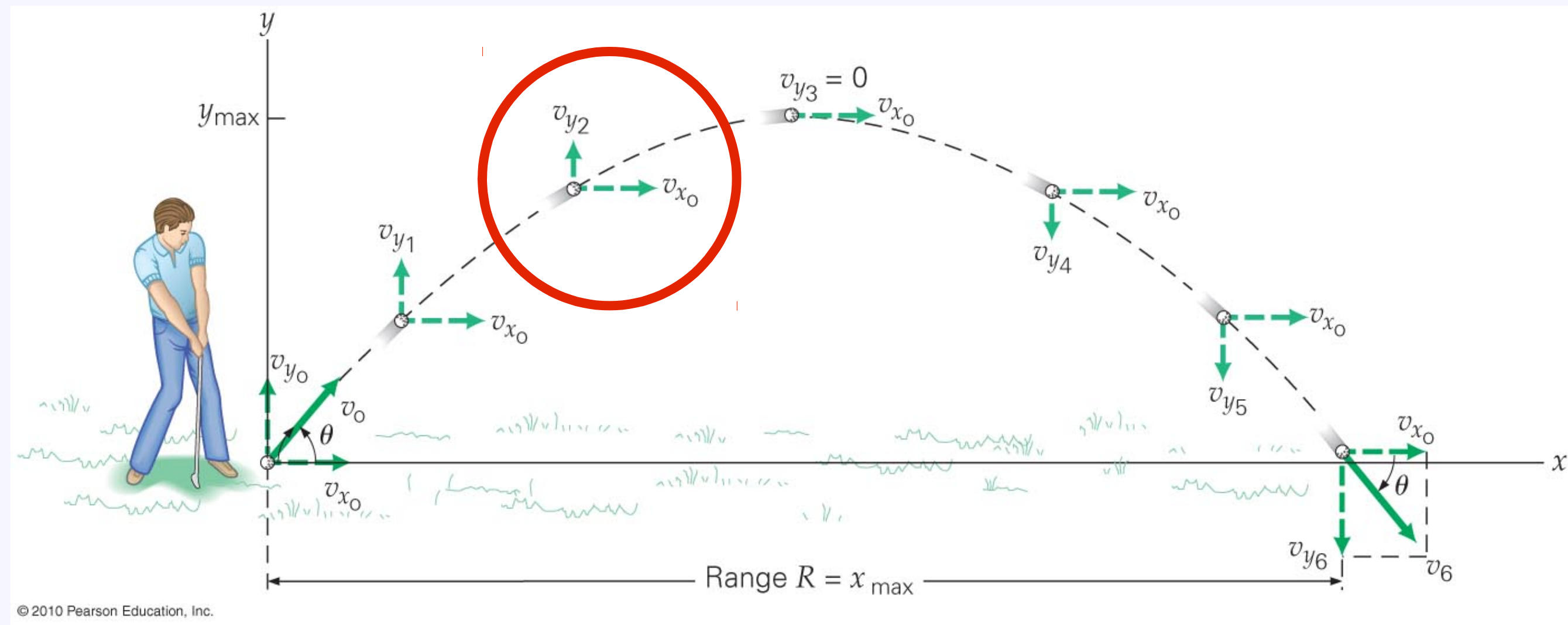
B



C



D



Clicker question #2f

What is the x component of the velocity at the **circled** time?

A



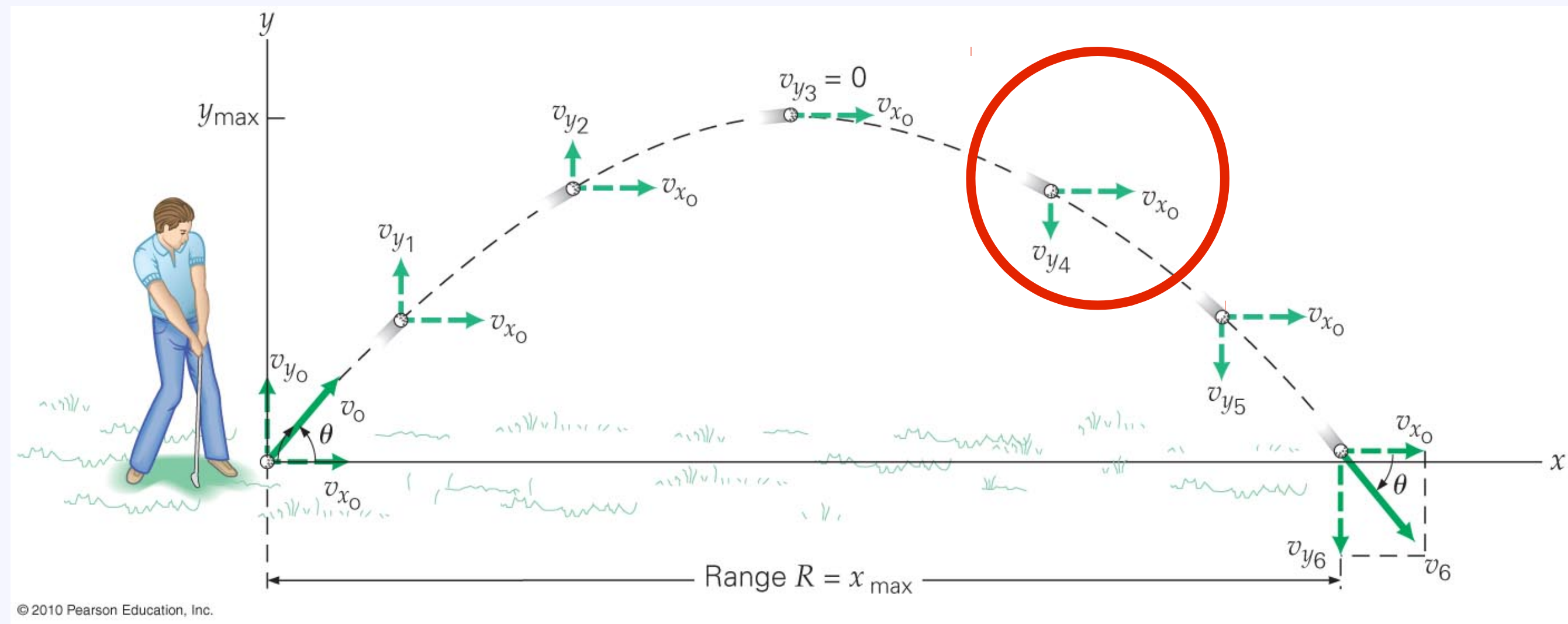
B



C



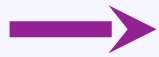
D



Clicker question #2g

What is the *y* component of the velocity at the **circled** time?

A



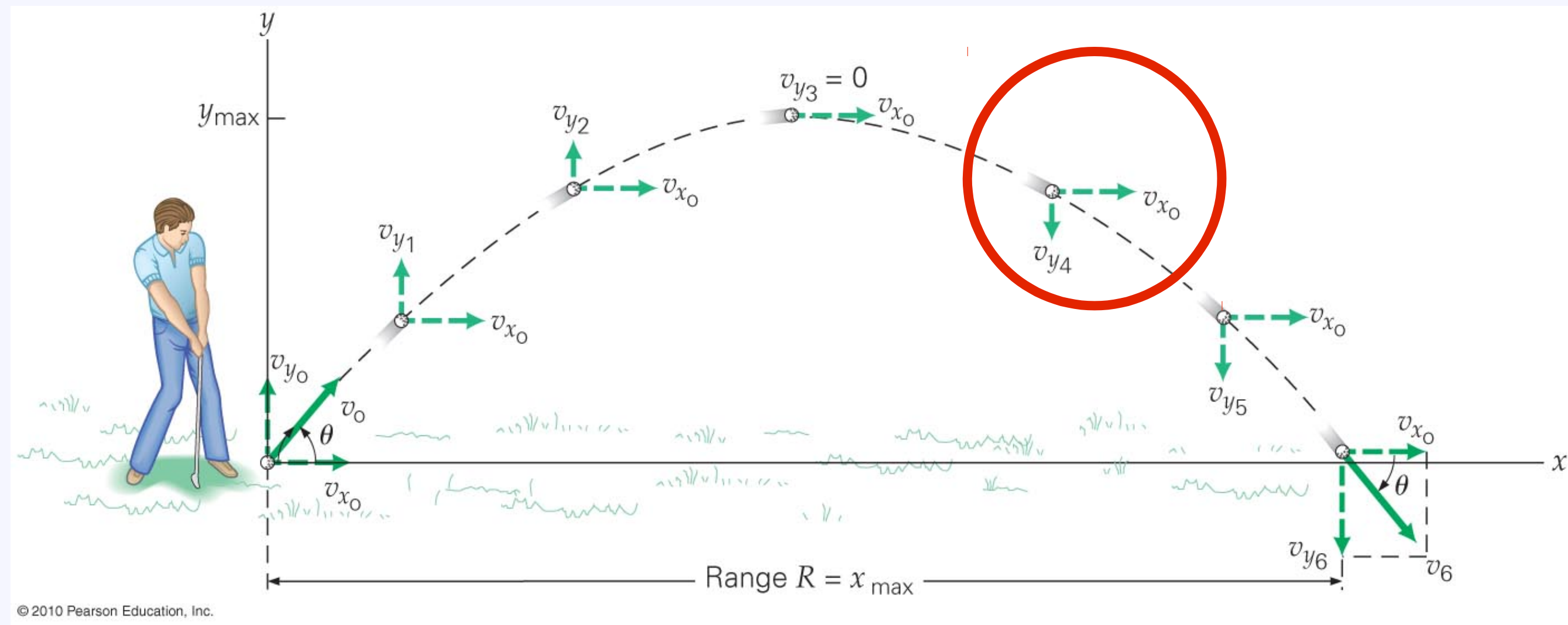
B



C



D



Clicker question #2h

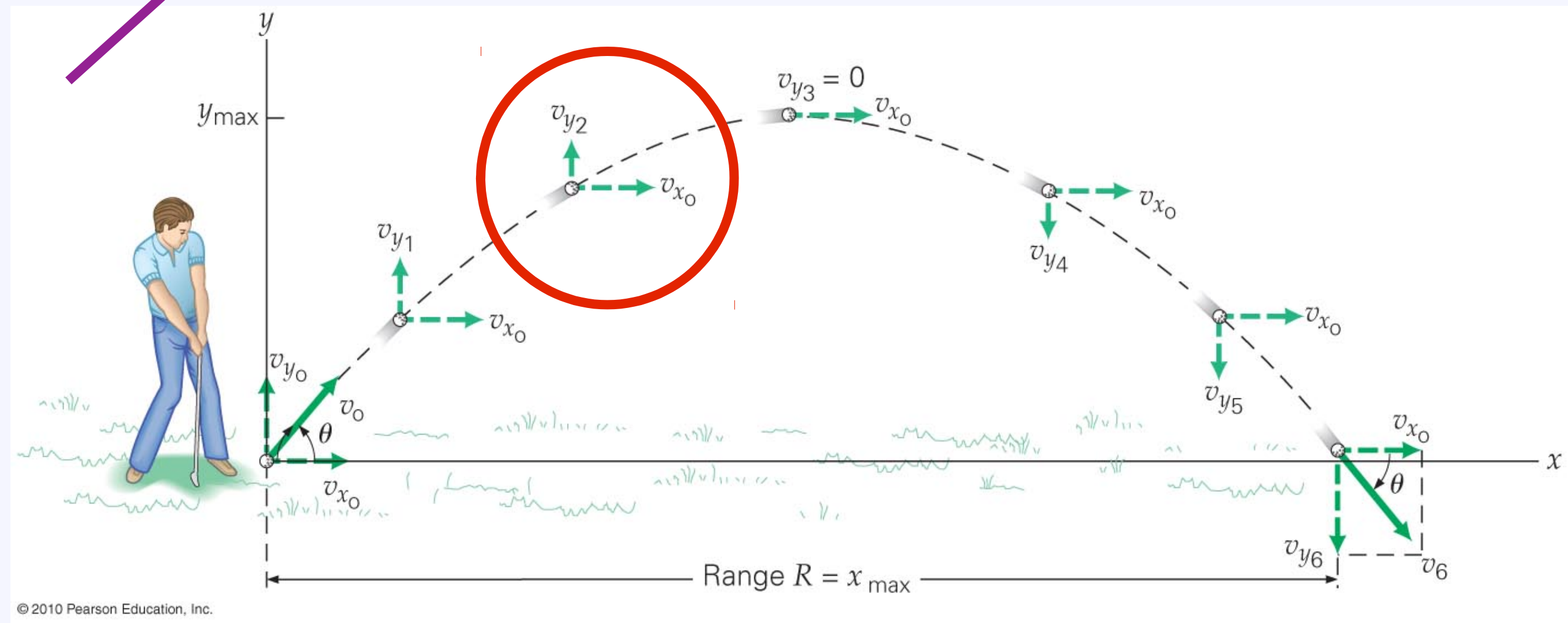
Which is the *velocity* at the **circled** time?

A

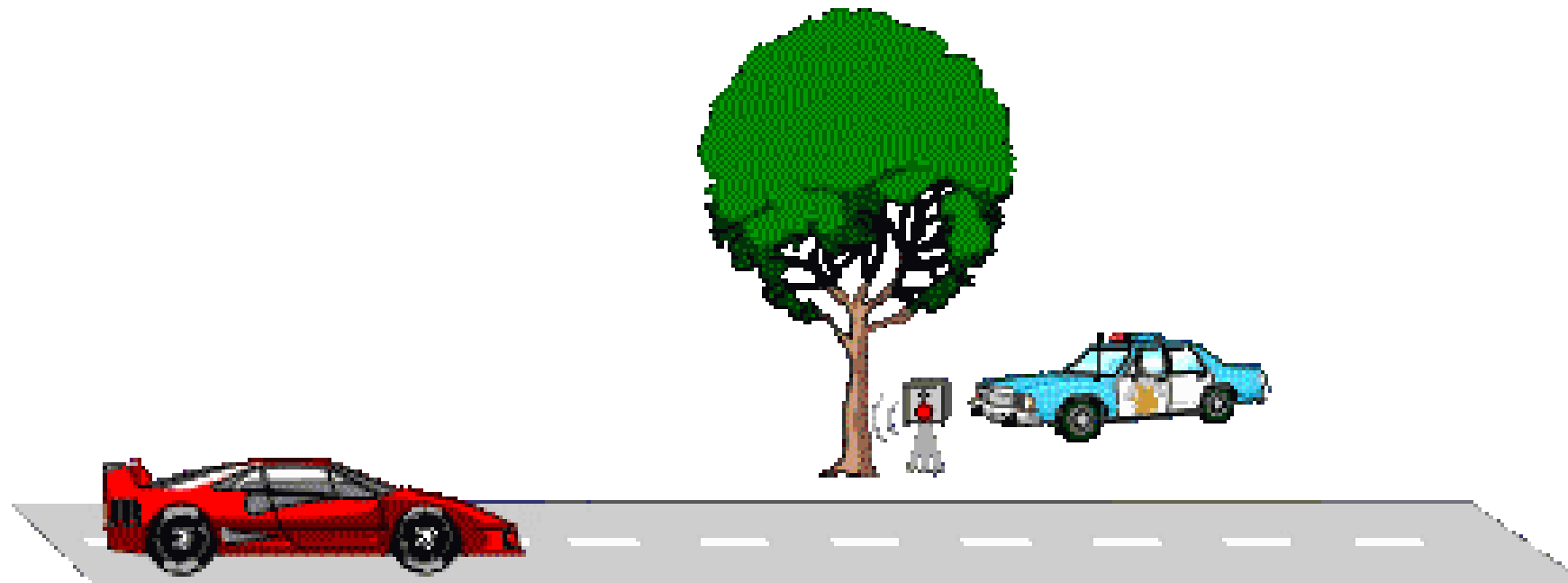
B

C

D

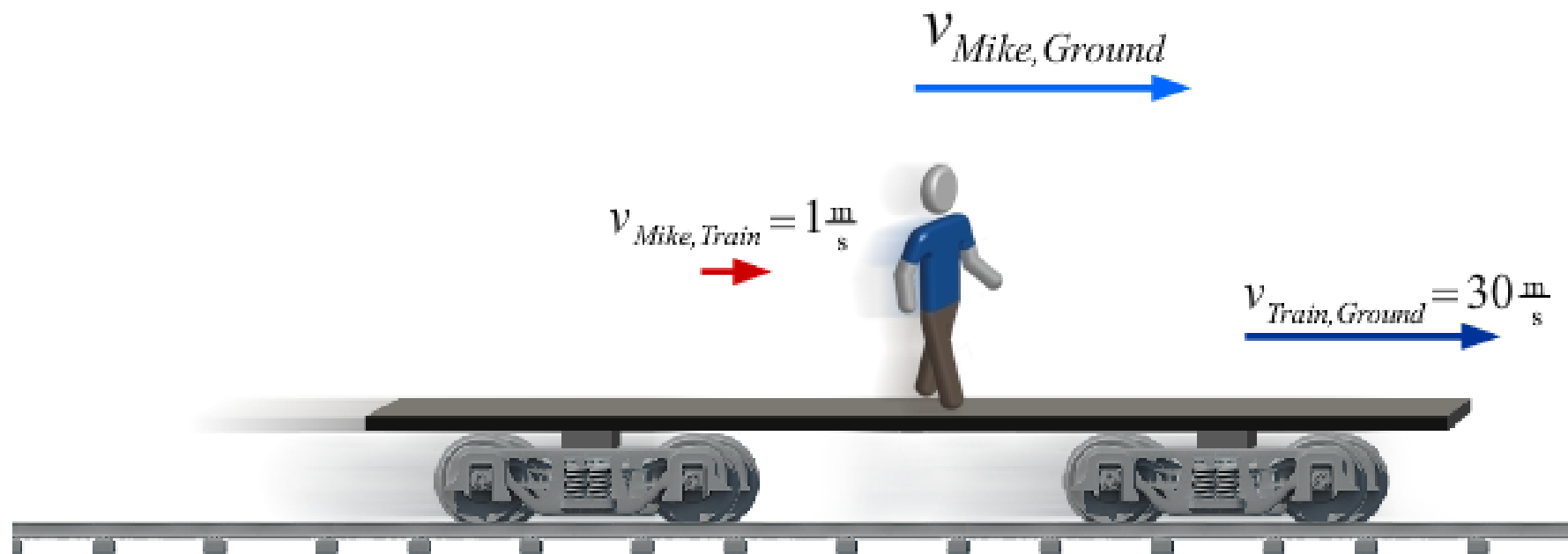


Relative Motion



- Relative motion means the velocity of a particle depends on the **reference frame** of the **observer**
- Reference frame is the physical object to which we attach our **coordinate system**
- **e.g.** seeing a plane fly by vs. being on the plane

Relative Motion



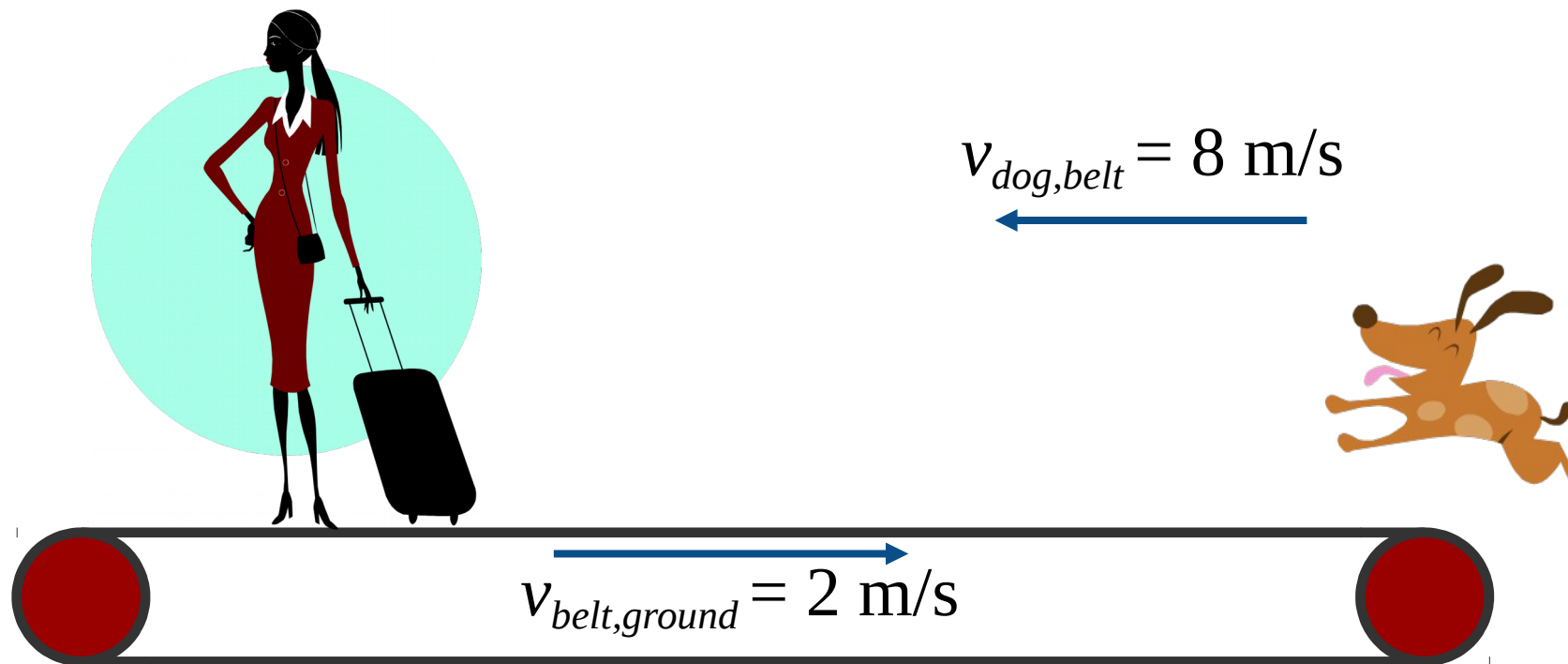
$$v_{Mike, Ground} = v_{Mike, Train} + v_{Train, Ground}$$

$$\vec{v}_{ac} = \vec{v}_{ab} + \vec{v}_{bc}$$

Clicker Question #2

A woman stands on a moving sidewalk that moves to the right at 2 m/s relative to the ground. A dog runs toward the girl in the opposite direction along the sidewalk at a speed of 8 m/s relative to the sidewalk.

What is the speed of the dog relative to the ground?



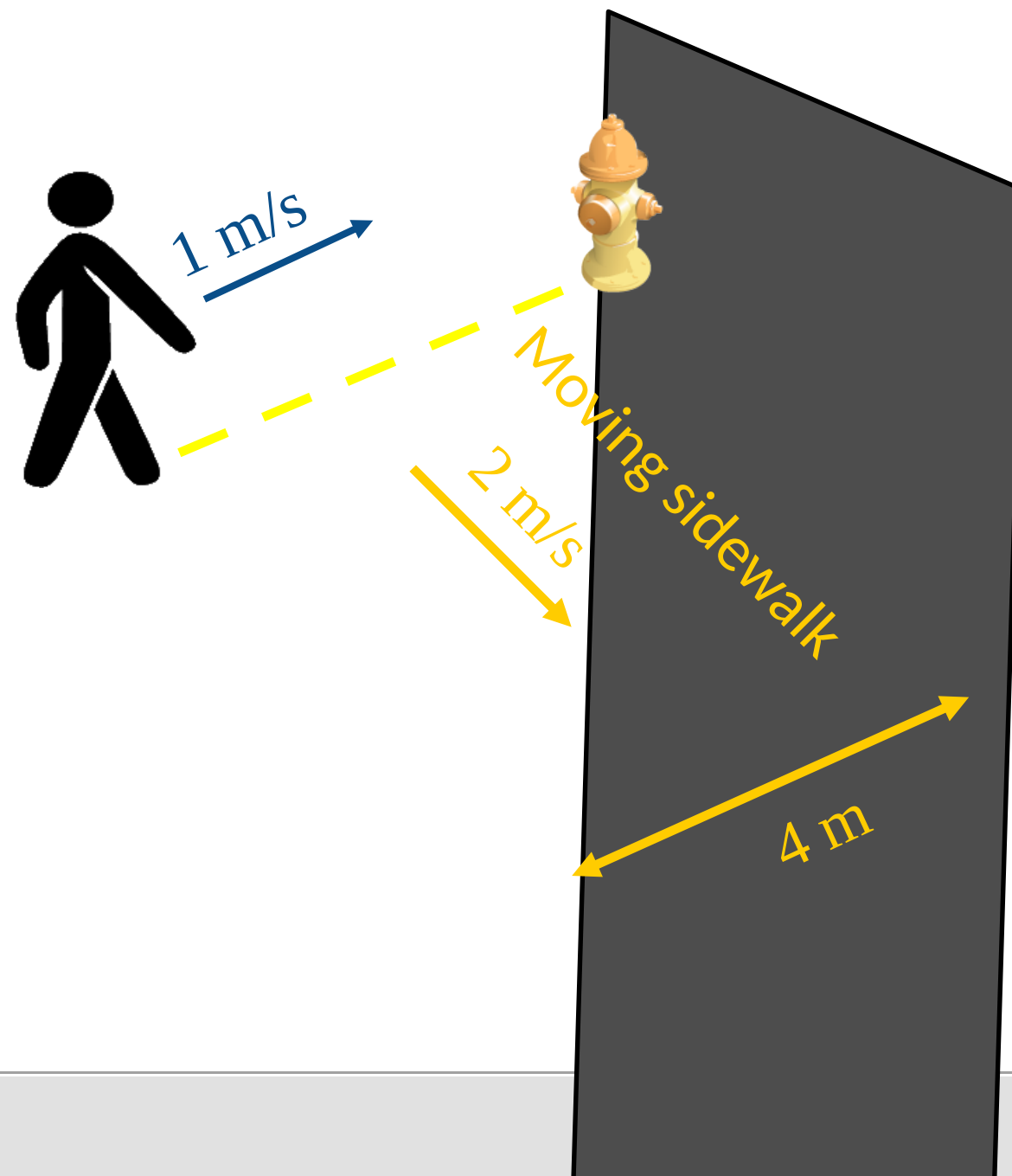
- A) 6 m/s B) 8 m/s C) 10 m/s

Clicker Question #3

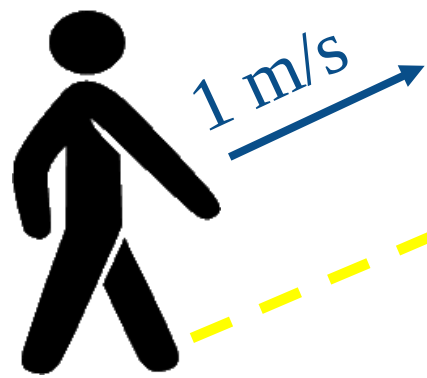


A man starts to walk along the dotted line painted on a moving sidewalk toward a fire hydrant that is directly across from him. The width of the walkway is 4 m , and it is moving at 2 m/s relative to the fire-hydrant. If his walking speed is 1 m/s , how far away will he be from the hydrant when he reaches the other side?

- A) 2 m
- B) 4 m
- C) 6 m
- D) 8 m
- E) 0 m



If the sidewalk wasn't moving:



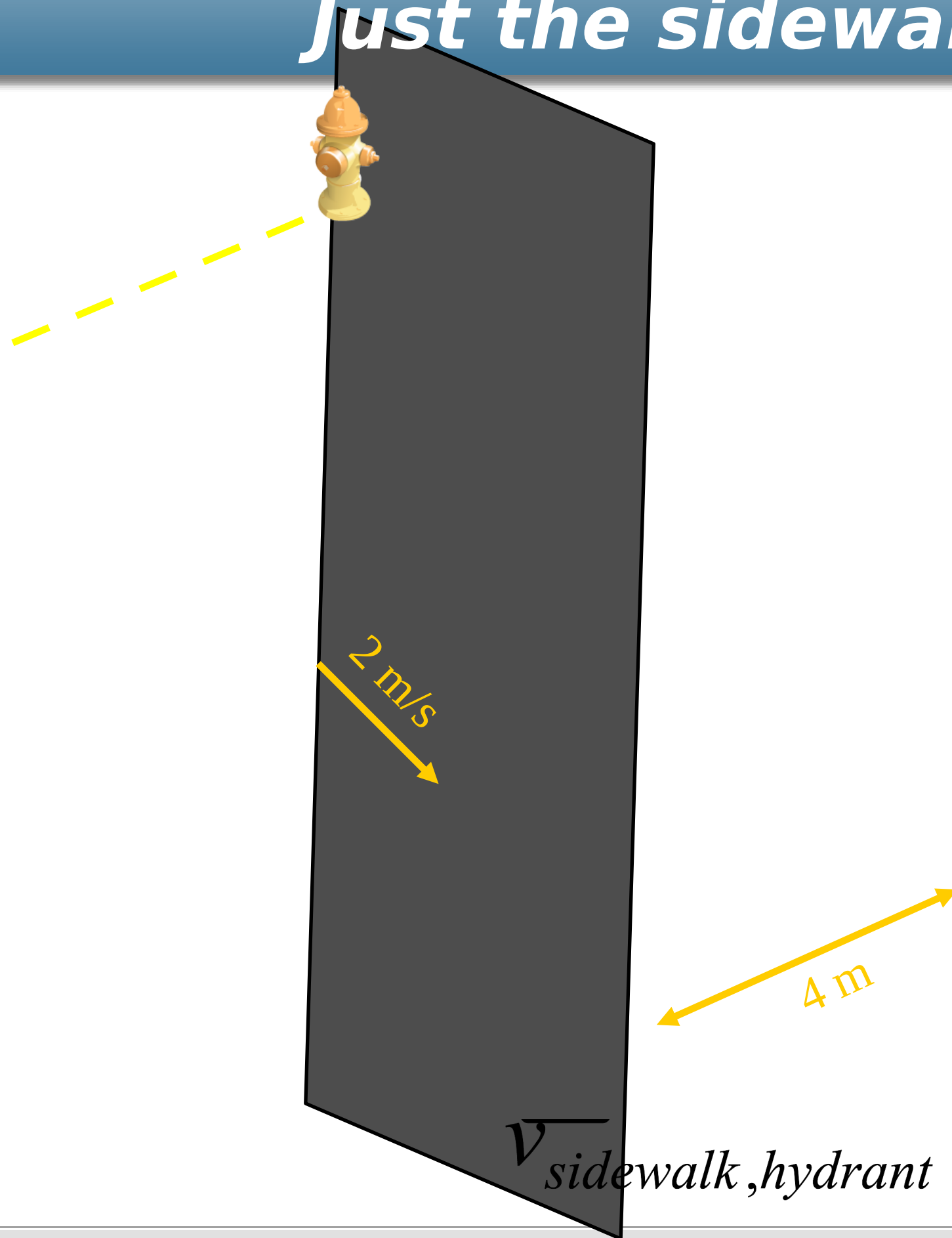
Time to get across:

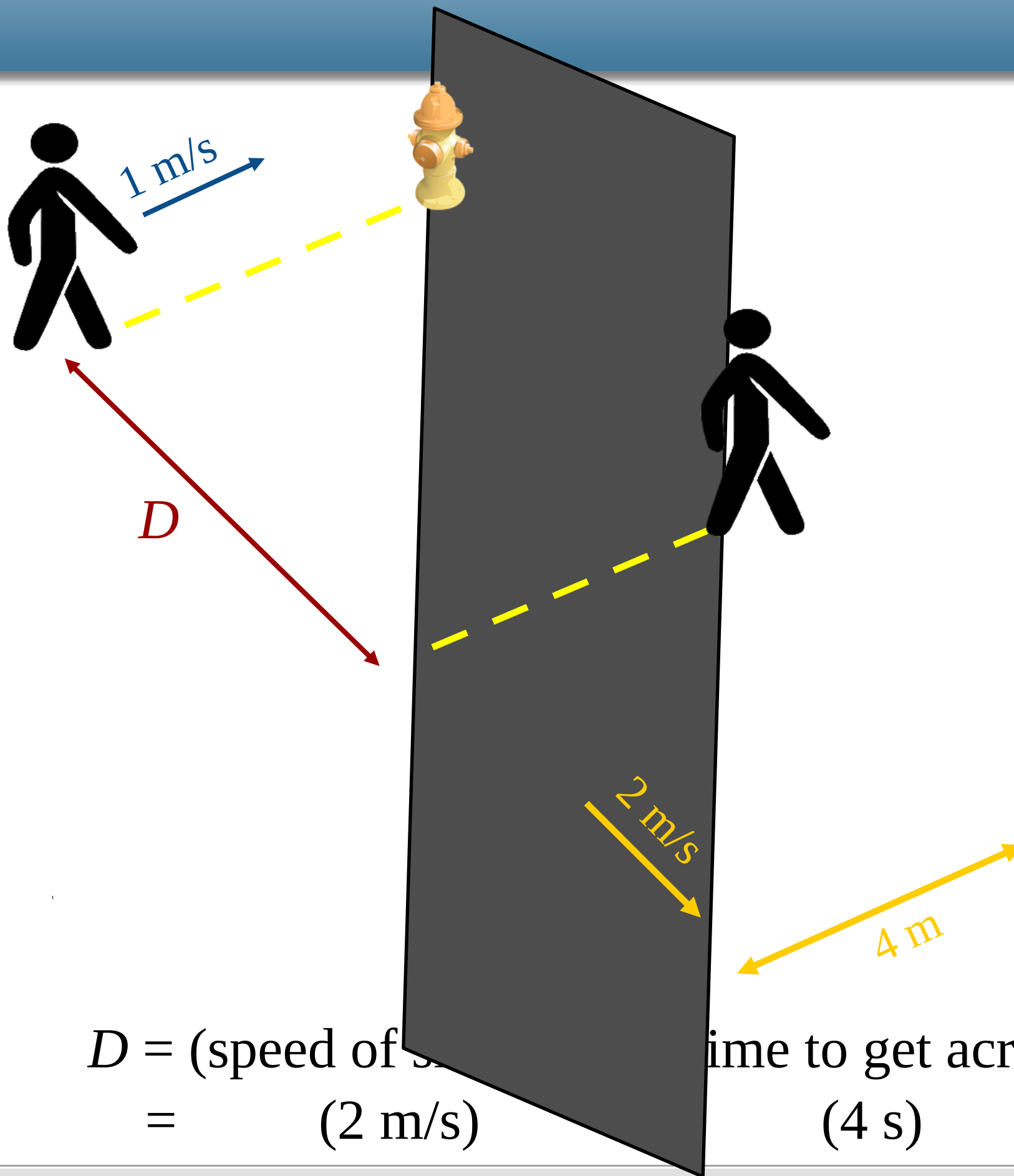
$$\begin{aligned}\Delta t &= \text{distance} / \text{speed} \\ &= 4\text{m} / 1\text{m/s} \\ &= 4 \text{ s}\end{aligned}$$



$v_{\text{man, sidewalk}}$

Just the sidewalk:

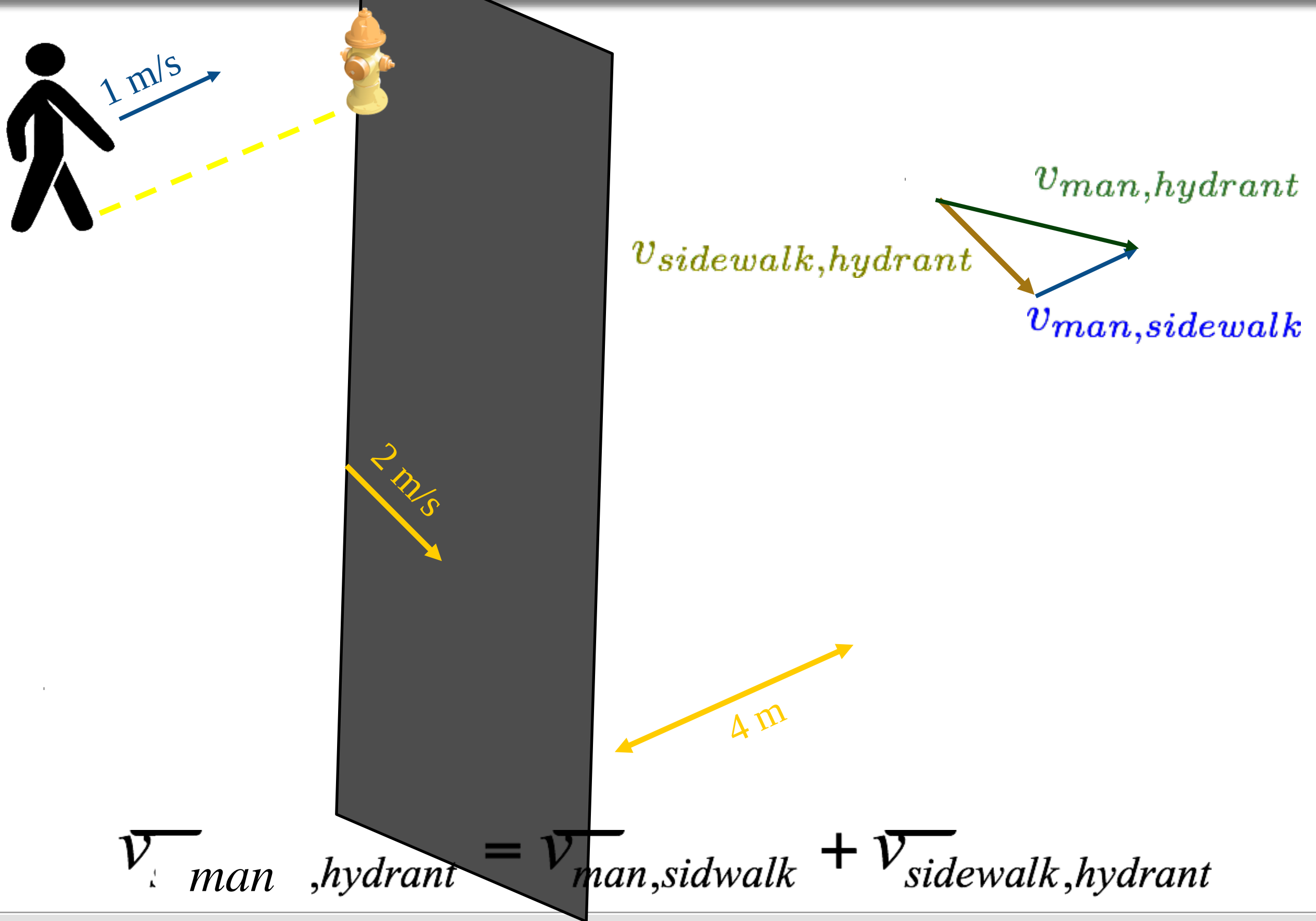




$$D = (\text{speed of barrier}) \times (\text{time to get across})$$

$$= (2 \text{ m/s}) \times (4 \text{ s}) = 8 \text{ m}$$

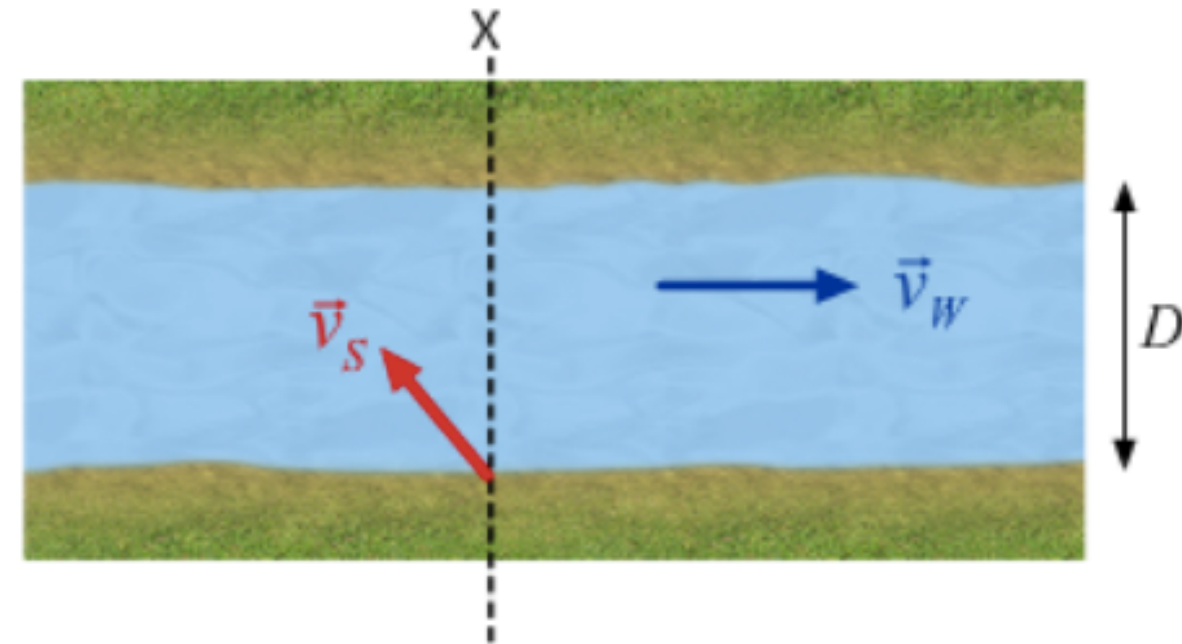
Combination of motions:



Clicker Question #4

A swimmer wishes to swim across the stream as shown. She knows she can maintain a constant speed $v_S = 0.4 \text{ m/s}$ with respect to the water. The water in the stream moves with speed $v_W = 0.5 \text{ m/s}$ as shown.

Which of the following statements is true?



- A** She will not be able to cross the stream since $v_S < v_W$.
- B** She will be able to cross the stream but since $v_S < v_W$, she will never be able to reach any point upstream of X , but will be able to reach point X by choosing an appropriate heading.
- C** She will be able to cross the stream but since $v_S < v_W$, she will never be able to reach point X , no matter what heading she chooses.

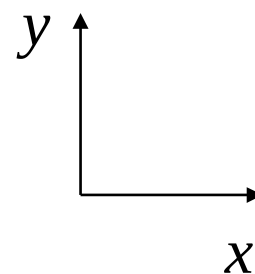
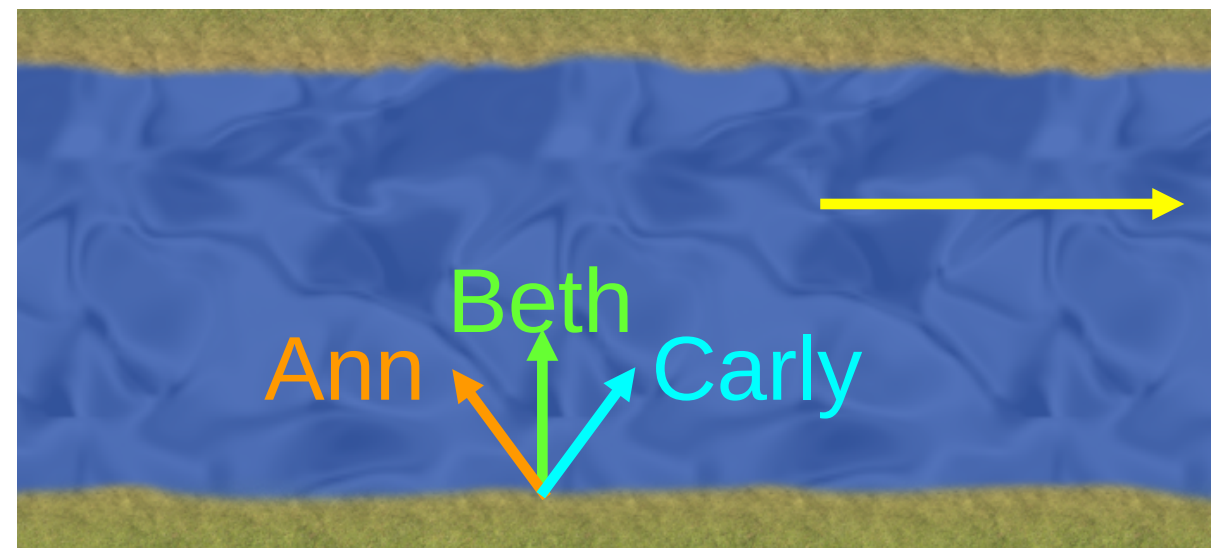
Clicker Question #5a



Three swimmers can swim equally fast relative to the water. They have a race to see who can swim across a river in the least time. Relative to the water, **Beth** swims perpendicular to the flow, **Ann** swims upstream at 30 degrees, and **Carly** swims downstream at 30 degrees.

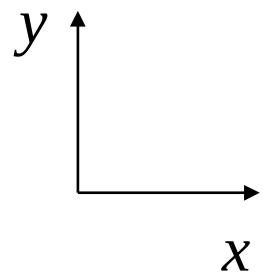
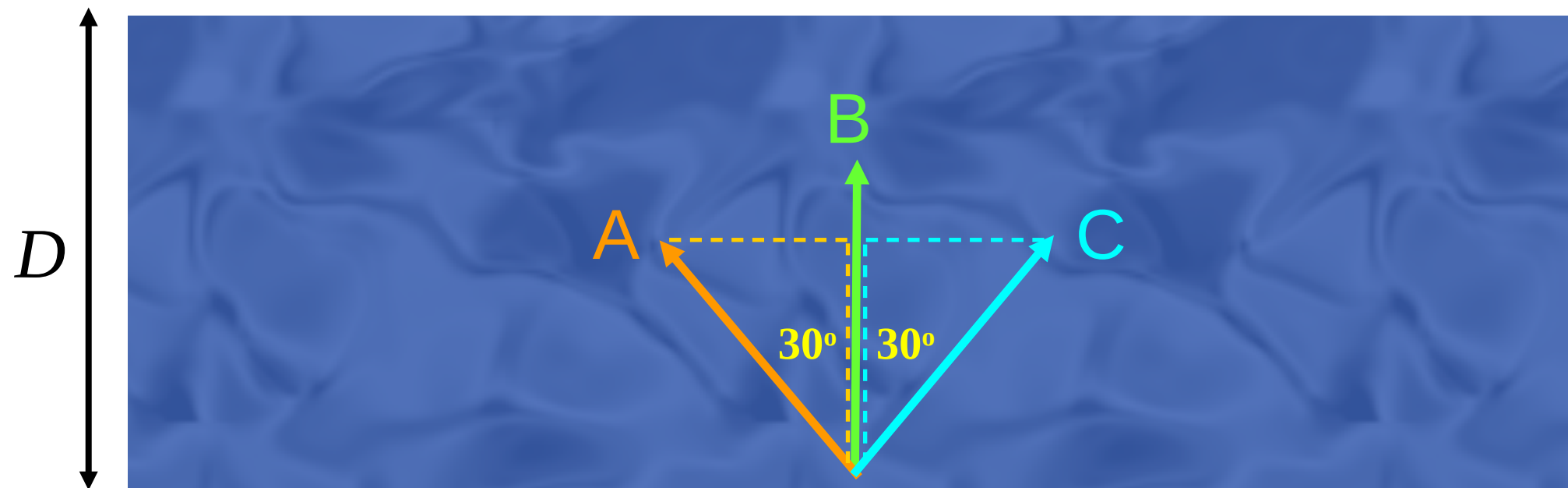
Who gets across the river first?

A) Ann B) Beth C) Carly



Look at just water & swimmers

$$\text{Time to get across} = D / V_y$$



$$V_{y,Beth} = V_o$$

$$V_{y,Ann} = V_o \cos(30^\circ)$$

$$V_{y,Carly} = V_o \cos(30^\circ)$$

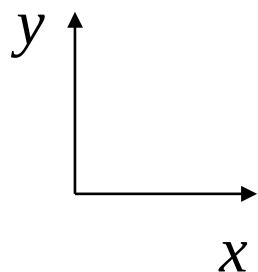
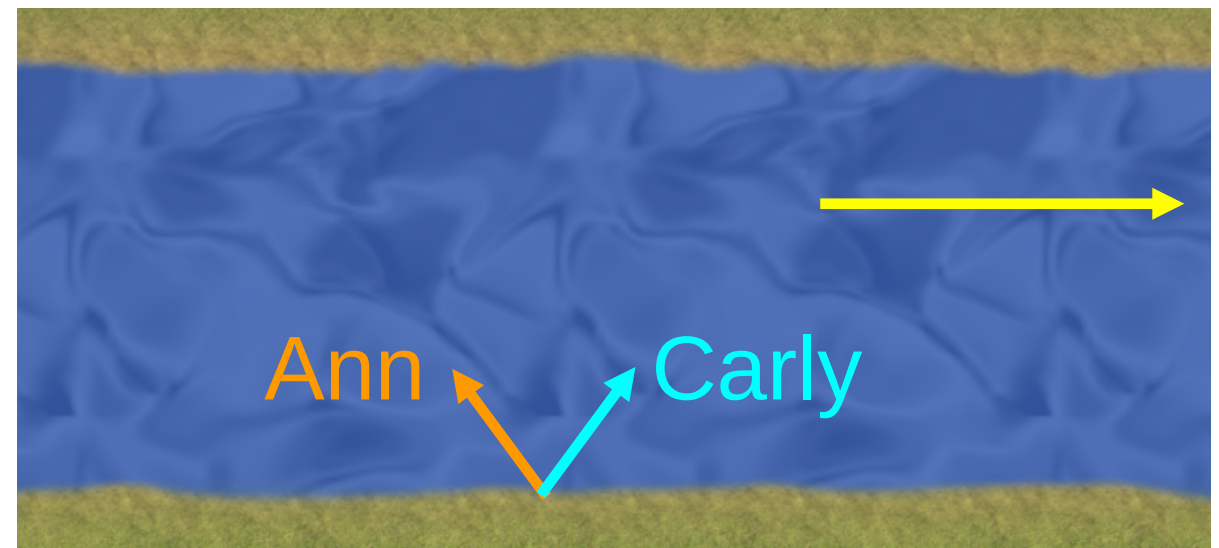
Clicker Question #5b



Three swimmers can swim equally fast relative to the water. They have a race to see who can swim across a river in the least time. Relative to the water, **Beth** swims perpendicular to the flow, **Ann** swims upstream at 30 degrees, and **Carly** swims downstream at 30 degrees.

Who gets across the river second?

A) Ann B) Carly C) Both same



What angle to get straight across river?

Extra slides

Clicker question #5

“Monkey shoot” The monkey starts falling when the gun fires. What angle θ should you aim to hit the monkey?

A

Below
the monkey

B

Straight at
the monkey

C

Above the
monkey

D

It depends on
the dart speed



Monkey shoot



Bonus example

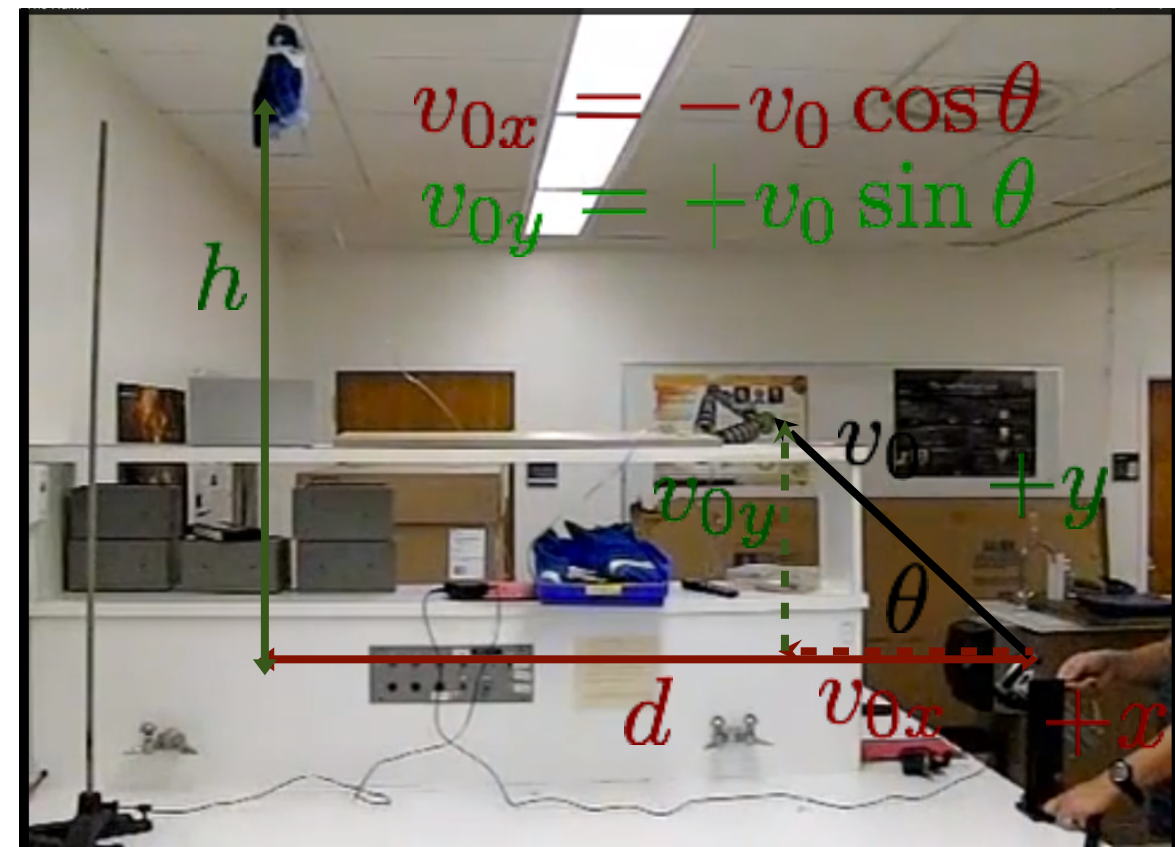
A monkey jumps from a height h out of a tree a horizontal distance d away at the instant a hunter fires a tranquilizer dart from the ground. At what angle should the hunter aim to hit the monkey?

Given: h d

Goal: θ

Principle: projectile

1. Read the problem
2. Draw a sketch
3. Given? Goal?
4. Brainstorm



Monkey shoot

Given: h d

Goal: θ

Projectile

$$x = x_0 + v_{x0}t + \frac{1}{2}a_xt^2 \quad y = y_0 + v_{y0}t - \frac{1}{2}gt^2$$

$$v_x = v_{x0} + a_xt$$

$$v_y = v_{y0} - gt$$

Monkey

$$x_M = x_B$$

$$y_M = y_B$$

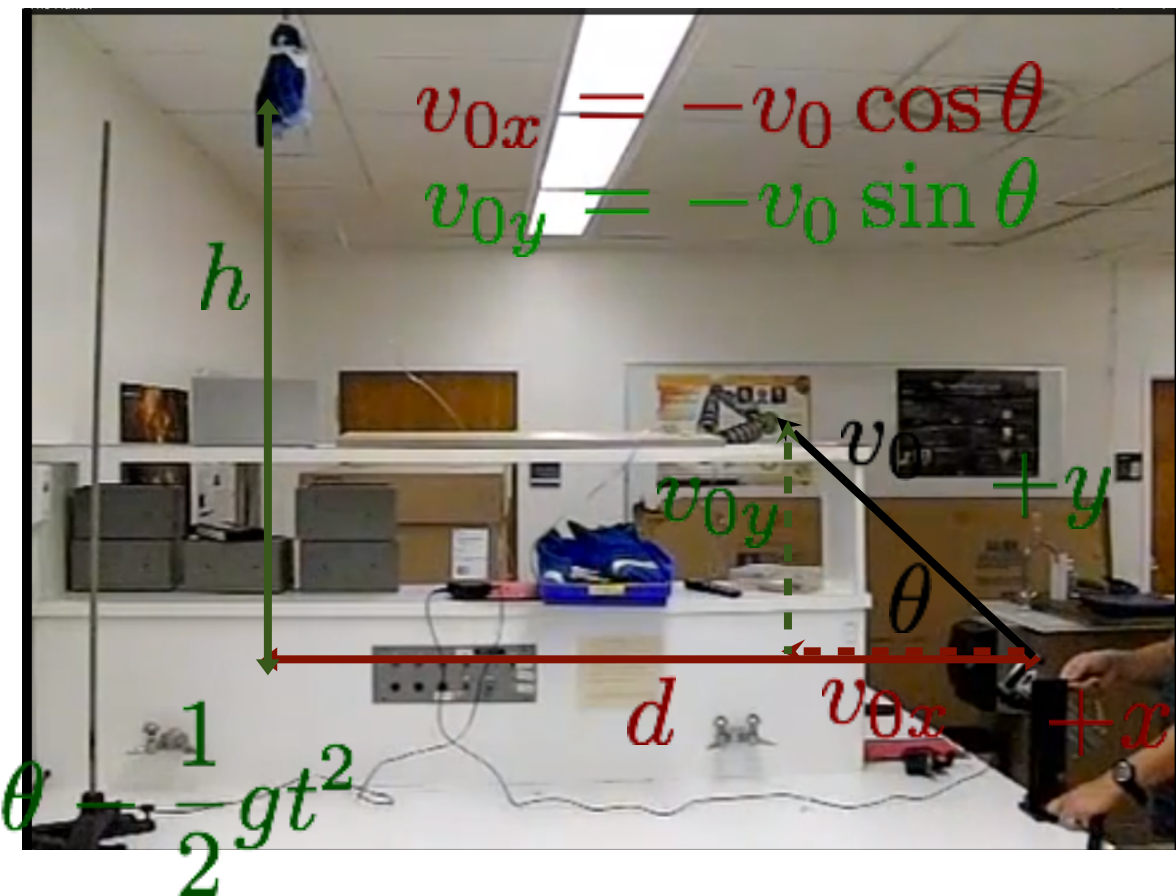
$$x_M = x_{0M} = -d$$

$$y_M = h + \cancel{v_{0yM}}t - \frac{1}{2}gt^2$$

Bullet

$$x_B = \cancel{x_{0B}} - v_{0xB}t = -v_0t \cos \theta$$

$$y_B = \cancel{y_{0B}} + v_{0yB}t - \frac{1}{2}gt^2 = v_0t \sin \theta - \frac{1}{2}gt^2$$



Monkey shoot

Monkey

$$x_M = x_{0M} = -d$$

$$y_M = h + \cancel{v_{0yM}t} - \frac{1}{2}gt^2$$

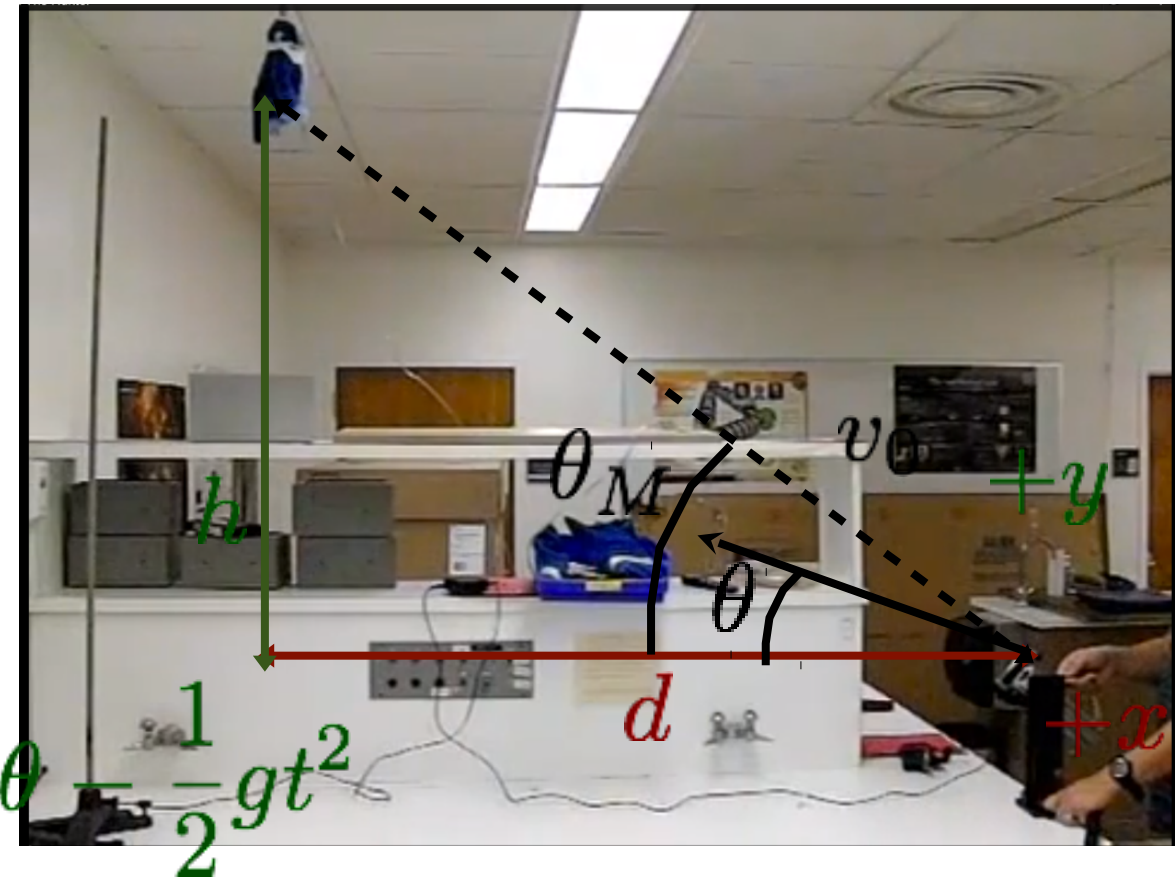
Bullet

$$x_B = \cancel{x_{0B}} - v_{0xB}t = -v_0t \cos \theta$$

$$y_B = \cancel{y_{0B}} + v_{0yB}t - \frac{1}{2}gt^2 = v_0t \sin \theta - \frac{1}{2}gt^2$$

$$\cancel{h} - \frac{1}{2}\cancel{gt^2} = \cancel{v_0t \cos \theta} - \frac{1}{2}\cancel{gt^2}$$

$$\tan \theta = \tan \theta_M = \frac{h}{d} \Rightarrow \theta = \theta_M$$



$$h = v_0t \sin \theta$$

$$d = v_0t \cos \theta$$

$$\frac{h}{d} = \frac{\cancel{v_0t} \sin \theta}{\cancel{v_0t} \cos \theta} = \tan \theta$$

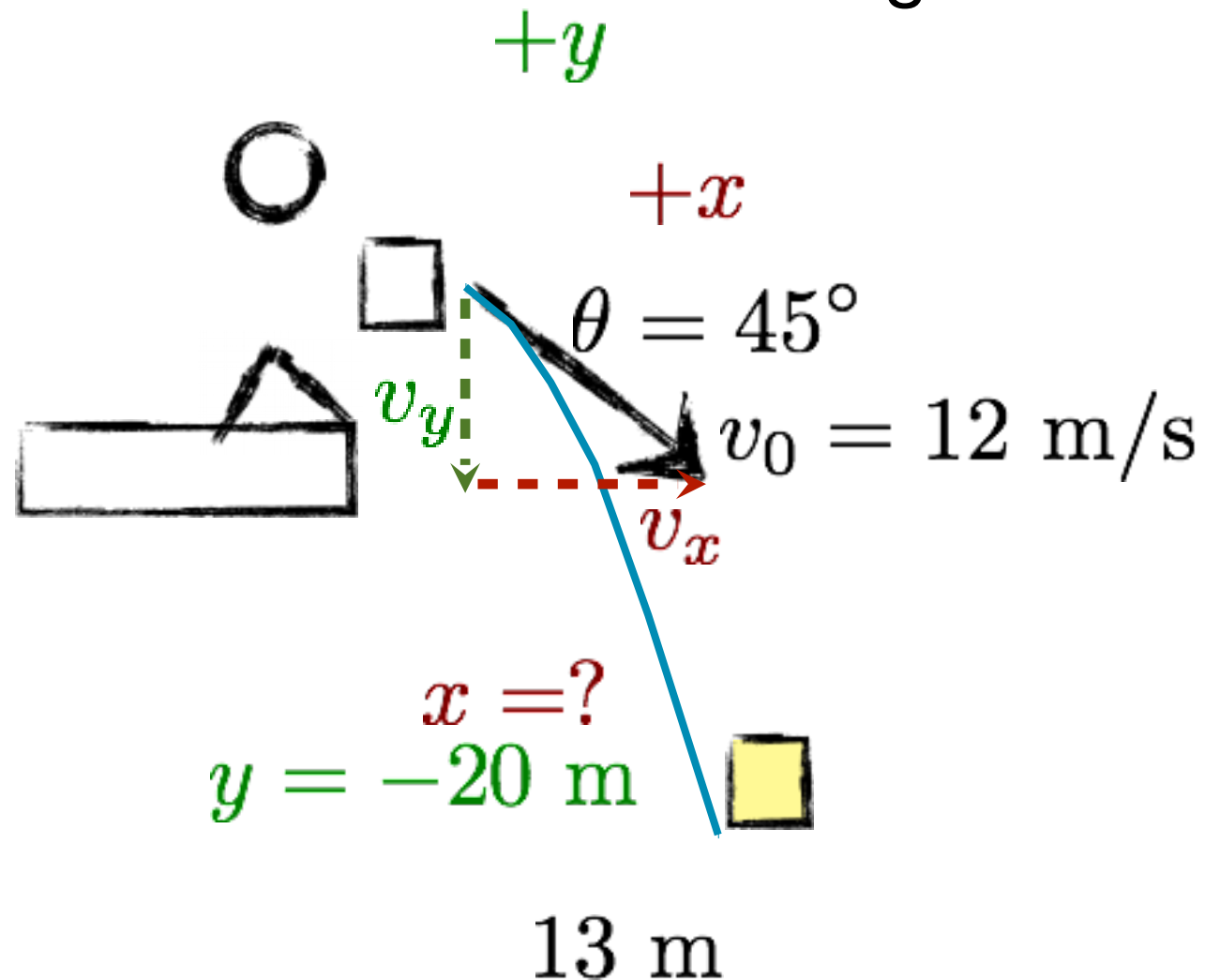
5. Calculate

6. (Plug in numbers)

7. Reasonable?

Ex. 3.7: stone toss

- A girl on a bridge (height 20 m) throws a stone at 12 m/s, 45° below horizontal. Does the block hit a target on the water that is 13 m from where it goes under the bridge?



Given: $x_0 = y_0 = 0$ $y = -20 \text{ m}$
 $v_0 = 12 \text{ m/s}$ $\theta = 45^\circ$

Goal: $x = ?$

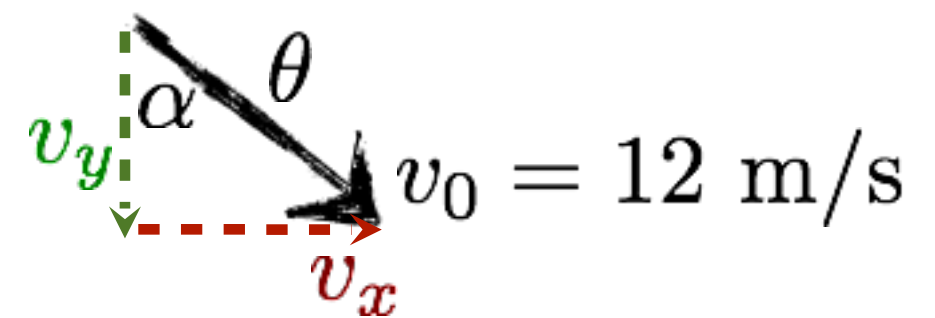
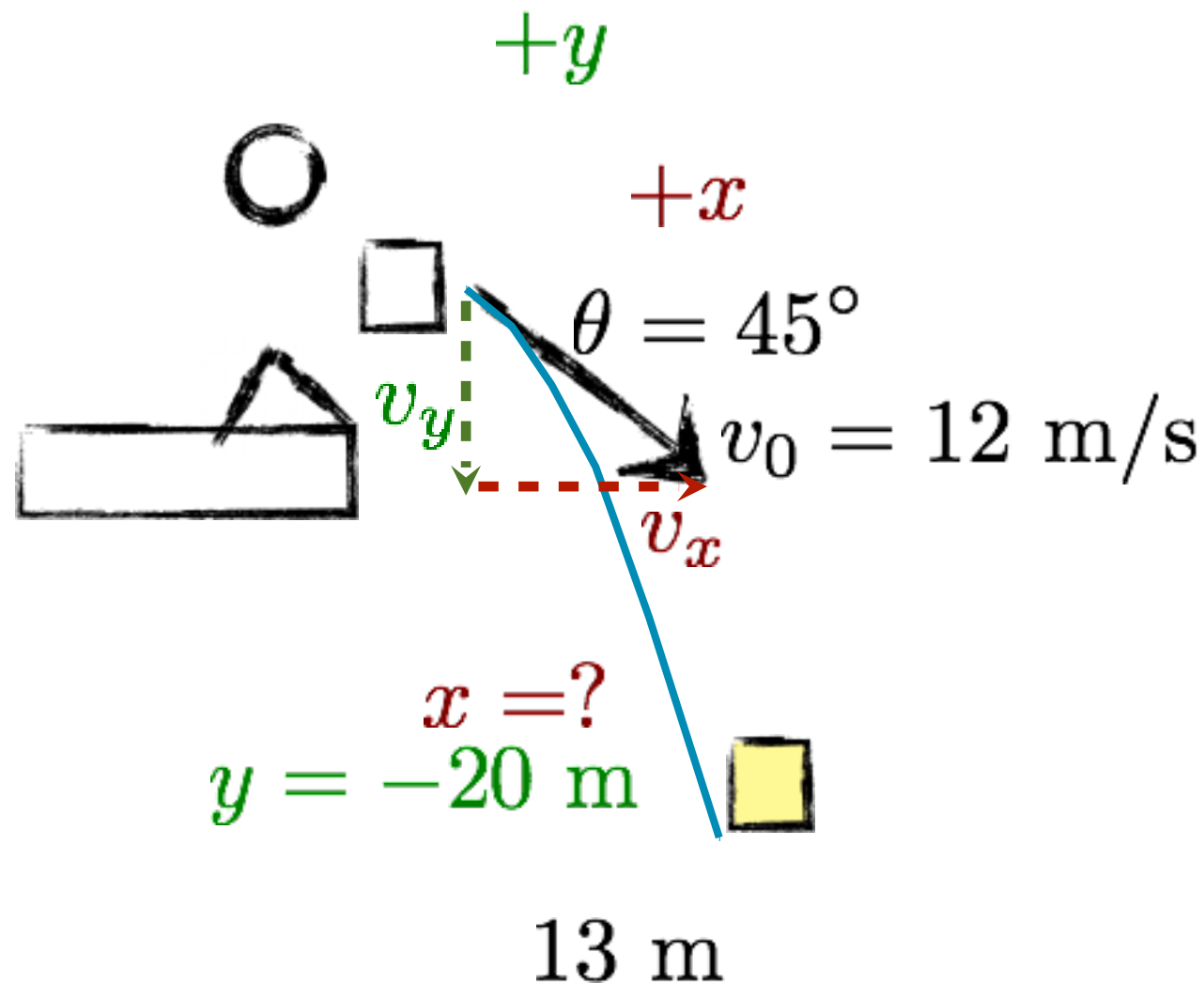
Concept: Projectile

1. Read carefully
2. Draw a sketch
3. Given? Goal?
4. Brainstorm

Ex. 3.7

Given: $x_0 = y_0 = 0$ $y = -20$ m
 $v_0 = 12$ m/s $\theta = 45^\circ$

Goal: $x = ?$ **Concept:** Projectile



$$|v_{0x}| / |v_0| = \sin \alpha$$

$$|v_{0x}| = |v_0| \sin \alpha$$

$$v_{0x} = +v_0 \sin \alpha$$

$$|v_{0y}| / |v_0| = \cos \alpha$$

$$|v_{0y}| = |v_0| \cos \alpha$$

$$v_{0y} = -v_0 \cos \alpha$$

1. Read carefully
2. Draw a sketch
3. Given? Goal?
4. Brainstorm
5. Calculate

Ex. 3.7

Given: $x_0 = y_0 = 0$ $y = -20 \text{ m}$ $v_{0x} = +v_0 \sin \alpha$
 $v_0 = 12 \text{ m/s}$ $\theta = 45^\circ$ $v_{0y} = -v_0 \cos \alpha$

Goal: $x = ?$ **Concept:** Projectile

$$x = \cancel{x_0} + v_{0x}t \quad t = \frac{x}{v_{0x}} \quad t = \frac{x}{v_0 \sin \alpha}$$

$$\sin^2 45^\circ = \cos^2 45^\circ = \frac{1}{2}$$

$$\sin^2 \alpha = \cos^2 \alpha = \frac{1}{2}$$

$$y = y_0 + v_{0y}t - \frac{1}{2}gt^2$$

$$y = \cancel{y_0} - (\cancel{v_0} \cos \alpha) \left(\frac{x}{\cancel{v_0} \sin \alpha} \right) - \frac{1}{2}g \left(\frac{x}{v_0 \sin \alpha} \right)^2$$

$$0 = \left(\frac{g}{v_0^2} \right) x^2 + x + y$$

1. Read carefully
2. Draw a sketch
3. Given? Goal?
4. Brainstorm
5. Calculate

Ex. 3.7

Given: $x_0 = y_0 = 0$ $y = -20$ m
 $v_0 = 12$ m/s $\theta = 45^\circ$

Goal: $x = ?$ **Concept:** Projectile

$$0 = \left(\frac{g}{v_0^2} \right) x^2 + x + y$$

$$x = \frac{-1 + \sqrt{1 - 4 \frac{gy}{v_0^2}}}{2 \left(\frac{g}{v_0^2} \right)}$$

$$x = \frac{-1 + \sqrt{1 - 4 \left[9.8 \cancel{\text{m/s}^2} \right] \left[-20 \cancel{\text{m}} \right] / \left[12 \cancel{\text{m/s}} \right]^2}}{2 \left(\left[9.8 \cancel{\text{m/s}^2} \right] / \left[12 \cancel{\text{m/s}} \right]^2 \right)} = 11 \text{ m}$$

Target at $x = 13$ m. Stone does not hit target.

Note: book uses different method, rounds differently, gets 12 m (though I get 11 m)

1. Read carefully
2. Draw a sketch
3. Given? Goal?
4. Brainstorm
5. Calculate
6. Plug in numbers
7. Reasonable?

In-class activity - Uniform Circular Motion

A particle undergoes uniform circular motion on a horizontal ***xy*** plane. At time ***t=0 s***, it moves through coordinates ***(3.0 m, 0)*** with velocity ***$\mathbf{v} = (6 \text{ m/s})\mathbf{j}$*** . At ***t=5 s***, it moves through ***(11.0 m, 0)*** with velocity ***$\mathbf{v} = (-6 \text{ m/s})\mathbf{j}$*** . In unit vector notation, what is its acceleration at ***t = 2.5 s***?