Math 125 Exam #4 - Fall 2017

Version G

Chapter	10,	Sections	1,2
Chapter	11,	Sections	1-5

Name: _____ Date: ____

Instructions: You must solve each question completely, explaining your reasoning. Partial credit will be awarded for answers that are incorrect, but show progress towards a correct solution. You will not receive credit if you do not clearly show how you are obtaining your answers. Grading will be based on the solution and your write-up. Do all the work on the exam.

- 1. (12 Points) The profit earned by a producer to manufacture and sell n units of a good is given by P(n) = 14n 3038. The average profit for n units is given by $A(n) = \frac{P(n)}{n}$.
 - A) Compute A(1), A(217), A(284).
 - B) Interpret the economic significance of each the values in part (A).

- C) What trend do you notice in the values of A(n) as n gets large? Explain this trend in economic terms.
- 2. (10 points) Let $P = 30 \ln(t)$ give the annual profit of a company (in thousands of dollars) t years after its formation.

What is $P^{-1}(80)$? Round to the nearest whole number and include units. Explain what this expression means in the context of this problem.

3. (10 points) List a set functions (g(x), h(x), p(x)) that is a decomposition of $f(x) = \cos^6(\ln x)$ in the form of g(h(p(x))).

4. (10 points) Write a possible formula for a rational function, f(x), with zeros at x = -5, x = 2, vertical asymptotes at x = 11, x = -13, and a horizontal asymptote at y = 2.

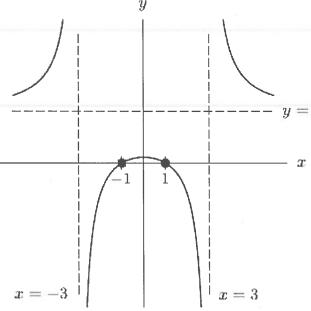
- 5. (20 points) Given the function $f(x) = \frac{1}{x+6} \frac{x}{x-3}$.
 - A) Rewrite the function $f(x) = \frac{p(x)}{q(x)}$, a ratio of polynomials (Get a common denominator and subtract).

B) Find any vertical asymptotes

C) Find any horizontal asymptotes.

D) Describe the long term behavior of the graph.

6. (12 points) The graph of $f(x) = \frac{16}{x^2 - 9} + 2$ is shown below.

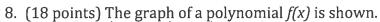


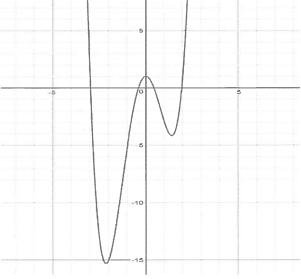
A) State the domain of f(x). What are the vertical asymptotes?

B) Does f(x) have an inverse over the domain you stated in part A? Explain your reasoning.

C) Define (Restrict) a new domain and find the inverse of $f(x) = \frac{16}{x^2 - 9} + 2$.

7. (8 points) Suppose f and g are invertible functions such that f(-12) = -9, f(-13) = -4, f(-14) = -7, g(-2) = -12, g(-7) = -4, and g(-4) = -9. Find $f^{-1}(g(f(-13)))$.





- A) What is the y-intercept of f(x)?
- B) What are the zeros of f(x)? State which of these are multiple zeros and whether their multiplicities are even or odd. Give reasons for your conclusions.

- C) What is the long run behavior of f(x)?
- D) Find a possible formula for f(x). Do not multiply the factors.

Bonus If $\frac{3\pi}{2} < \theta < 2\pi$ and $\sin(\theta) = \frac{-4}{7}$, find $\sin(2\theta)$, $\cos(2\theta)$, and $\tan(2\theta)$ exactly.

Double Angle Formulas

$$\sin 2\theta = 2\sin \theta \cos \theta$$

$$\cos 2\theta = \cos^2 \theta - \sin^2 \theta$$

$$=2\cos^2\theta-1$$

$$=1-2\sin^2\theta$$

$$\tan 2\theta = \frac{2\tan \theta}{1 - \tan^2 \theta}$$