## THEORY

- Day 2: Independent events happen same time, not affecting one another  $(P(A \cap B) = P(A)P(B))$ . Disjoint is the opposite  $(P(A \cap B) = 0)$ . Probability Mass Function (PMF) is a dictionary mapping of events to positive probabilities. Over an infinite amount of iterations, RVs converge to a number.
- Day 3: Law of Large Numbers: more times means more precise result.
- Day 4: Parameter: any numerical quantity that characterizes a given population. Population proportion: a percentage value associated with a population. Sample proportion: the proportion of individuals in a sample sharing a certain trait  $(\hat{p})$ . Sample  $\overline{\text{Mean}(\bar{X})}$ . Sampling distribution: probability distribution of statistic obtained through a large number of samples drawn (sample must be know).
- Day 5: We want low bias and high variability. Bias bad. Variability  $\downarrow$  as the sample size  $\uparrow$ . 'X' denotes the number of successes and 'n' is the number of elements in your sample.  $\hat{P}$  does **NOT** have a binomial distribution.
- Day 6: Interacting variables: one variable can affect the another variable (non-independent). Confounding variables a factor that influences the results of an experiment. Block design: split sample initially based on traits (possibly confounding) then randomly assign in those groups. Matched Pairs Design: blocks sizes of two (only looking with two levels). Repeated Measures Design two similar subjects have the same tests and those results are compared. Hawthorne Effect: individuals know they are being experimented on.
- Day 7: Sensitivity: proportion of actual positive. Specificity: proportion of actual negative. Predictive Value: proportion of positive tests that were actually positive. Negative Predictive Value: same as above but for negative. Prevalence: base rate. In the tree diagram, sensitivity goes on top and the specificity goes on the bottom.
- Day 8: Null Hypothesis: nothing unexpected (original hypothesis, H<sub>0</sub>). Alternate Hypothesis: "something is happening and we should change our minds" (H<sub>a</sub>). Critical region: range of values that corresponds to the rejection of H<sub>0</sub> at some chosen probability level. Type I Error: occurs when a significance test results in the rejection of a true null hypothesis. Type II Error: the data do not provide strong evidence that the null hypothesis is false.  $\alpha < \beta$  and if not, switch hypothesis.  $\beta \ge 0.8$ . Compute CR: need  $\alpha$ ,  $H_0$  (value of P under  $H_0$ ) and sampling distribution of test statistic under  $H_0$ . Compute Power: need CR,  $H_1$  (value of P under H<sub>1</sub>) and sampling distribution of test statistic under H<sub>1</sub>.
- Day 9: We want low  $\alpha$  and high power. Power analysis steps: define p (proportion in sample), let X be the number of successes, identify  $H_0$  and  $H_1$ .
- Day 10: One-tailed testing: The critical area of a distribution is either < or > a certain value but not both. Two-tailed the sample is greater than or less than a certain range of values. P-Value: a measure of "strength" of evidence against H<sub>0</sub> (always calculated after observation).
- Day 11: Approximate the sampling distribution one of two ways: 1) Under  $H_0$ ,  $\chi^2$  has approximately a  $\chi^2$  distribution with (number of categories 1)  $\leftarrow$  degrees of freedom | 2) Simulate a lot of times assuming  $H_0$  is true and compute their respective  $\chi^2$ . When we expected  $\leq 5$  in each category in our sample, both approaches give similar results. Else, we use method 2. Find case(county), variable(leading digit in diabetes prevalence). You **need** prevalence to calculate the PPV and NPV.
- Day 12: Examples will need us to find the probability within a sample population, then use that prevalence to make a more generalized claim for the larger population. P-Value is always above or equal to degrees of freedom.

No context information: A case is an entity of interest. Population is  $(\forall)$  and sample is  $(\subset)$ . Distribution of a variable is the relative number of each possible outcome will occur in 'N' trials. Explanatory variable  $\rightarrow$  independent and variable  $\rightarrow$  dependent. Levels of factor

## **FORMULAS**

- Mean of Probability Dist. :  $\mu_x = \Sigma x \times p(x)$
- Variance:  $\sigma^2_{\mathbf{x}} = \Sigma[x^2 \times P(x)] \mu^2_{\mathbf{x}}$
- Standard Deviation :  $\sigma_x = \sqrt{\sigma_x}$  and  $\sigma_{x+y} = \sqrt{\sigma_x + \sigma_y}$
- Number successes :  $X \sim B(n, p)$
- Mean of binomial RV: nP
- Variance of Bernoulli RV: P(1-P)
- Variance of binomial RV: nP(1-P)
- Standard deviation of binomial RV:  $\sqrt{nP(1-P)}$
- Bayes' Rule:  $\frac{P(B|A)P(A)}{P(B)}$
- $P(B|A) = \frac{number\ of\ outcomes\ in\ A\cap B}{number\ of\ outcomes\ in\ A} = \frac{P(A\cap B)}{P(A)} > 0$  Independent events:  $P(A\cap B) = P(A) \times P(B)$
- Conditional probability:  $P(A \cap B) = P(A) \times P(B|A)$  [Tree Mapping]

- Population proportion:  $\hat{P} = \frac{X}{n}$
- Variance( $\hat{P}$ ) =  $\frac{P(1-P)}{P}$
- Standard Deviation( $\hat{P}$ ) =  $\sqrt{\frac{P(1-P)}{P(1-P)}}$
- Sensitivity:  $\frac{TP}{TP+FN}$
- Specificity:  $\frac{TN}{TN+FP}$
- PPV:  $\frac{TP}{TP+FP}$
- NPV:  $\frac{TN}{TN+FN}$
- Prevalence: Actual Positive + Actual Negative
  P(1) P(2) P(3) P(4) P(4)
- $\alpha = P(1) P(\text{Concluded } \mathbf{H_a} \mid \mathbf{H_0} \text{ is true})$
- Baseline  $\alpha = 0.05$
- $\beta = P(2) P(Concluded H_0 \mid H_a)$
- Power:  $1 \beta$ Residual:  $\frac{O E}{\sqrt{E}}$  (O: Observed, E: Expected)
- $\chi^2 = \Sigma \ residual^2 = \frac{(O-E)^2}{E}$ Degrees of freedom = (r-1)(c-1). r = rows, c = columns.

## TESTING FRAMEWORKS

Null Hypothesis Significance Testing: an experimental factor is tested against a hypothesis of no effect or no relationship based on a given observation. We start off assuming H<sub>0</sub> is true. Evidence is then collected and analyzed. An assessment is made upon those findings. If our significance level is breached, then we can reject H<sub>0</sub>. Neyman-Pearson: will allow us to make preemptive decisions based on conditions presented before the study is conducted. These are the theoretical outcomes WITHOUT taking any sample data. Fisher Significance Hypothesis Testing: More concerned with model design rather than actual data collection/analysis. Interested in when/why the test failed to make a more efficient model. Goodness of Fit: how well did the data fit with the observations. Binomial Probability Distribution Conditions: Binary outcome (TF), Independent (previous outcomes do not affect next.), Number of outcomes, Success is equally likely. Test of Homogeneity: Is the variable's distribution the same in all populations (we initially assume it is and we consider the population to be the explanatory variable). Test of Independence: used to determine if there is a significant association between two variables.