

### Quiz # 3

Please show all of your work for maximum credit. Good luck!!!

1. (4 points) A long distance calling service charges a 10 cent connection charge for each call, 7 cents a minute for the first 10 minutes and 5 cents a minute for each additional minute beyond that. Express the cost  $C$ , in dollars, of a phone call as a piece-wise defined function of the length  $x$  of the call, in minutes.

Sol.  $C(x) = \begin{cases} .10 + 0.07x; & 0 \leq x \leq 10 \\ \underbrace{0.80}_{\downarrow 0.10 + 0.07(10)} + 0.05(x-10); & x > 10 \end{cases}$

2. (3 points) Find the inverse function. Make sure to use the right notation for the inverse function.

$C = g(x) = 600 + 50x$ , where  $C = g(x)$  is the cost of producing  $x$  air-conditioners.

Sol.  $C = 600 + 50x$ ; solve for  $x$

$$\begin{array}{r} C = 600 + 50x \\ -600 \quad -600 \\ \hline C - 600 = 50x \\ \frac{C - 600}{50} = \frac{50x}{50} \end{array}$$

$x = \frac{C - 600}{50}$

$x = g^{-1}(C) = \frac{C - 600}{50}$

3. (3 points) Let  $P = f(t)$  be the population, in millions, of a country at time  $t$  in years and let  $E = g(P)$  be the daily electricity consumption, in megawatts, when the population is  $P$ . Give the meaning and units of the function. Assume both  $f$  and  $g$  are invertible. Interpret the following in terms of the application problem:

(a)  $g(f(t))$ :  $g(f(t))$  represents the daily electricity consumption, in megawatts at time  $t$ , in years.

(b)  $f^{-1}(P) = t$

Sol.  $f^{-1}(P)$  represents the time, in years @ given population, in million of a country.