

STATISTICS
Greeshma Gudhimalla
05/05/2023

Research question: Is there a significant difference between the reflex times of people over the age of 40 vs people under the age of 40?

Claim: People under the age of 40 have a shorter reflex time than people over the age of 40.

Experimental methods:

We surveyed 12 people each - 6 under the age of 40 and 6 over the age of 40. We each made a list of 16 people (8 of each age group) and used a random number simulator to pick the subjects being surveyed. After doing so, we collected our data by measuring the reflexes through the reflex test on humanbenchmark.com. We performed three trials for each subject and the average reflex time was recorded as the data value for that subject.

- This is a Left-tailed test.
- Our samples are independent.

Null hypothesis – The mean reflex times for the people who are below 40 would be the same as the mean reflex time for people who are above 40.

Alternative Hypothesis - The mean reflex times for the people who are below 40 would be less than the mean reflex time for the people who are above 40.

RAW data:

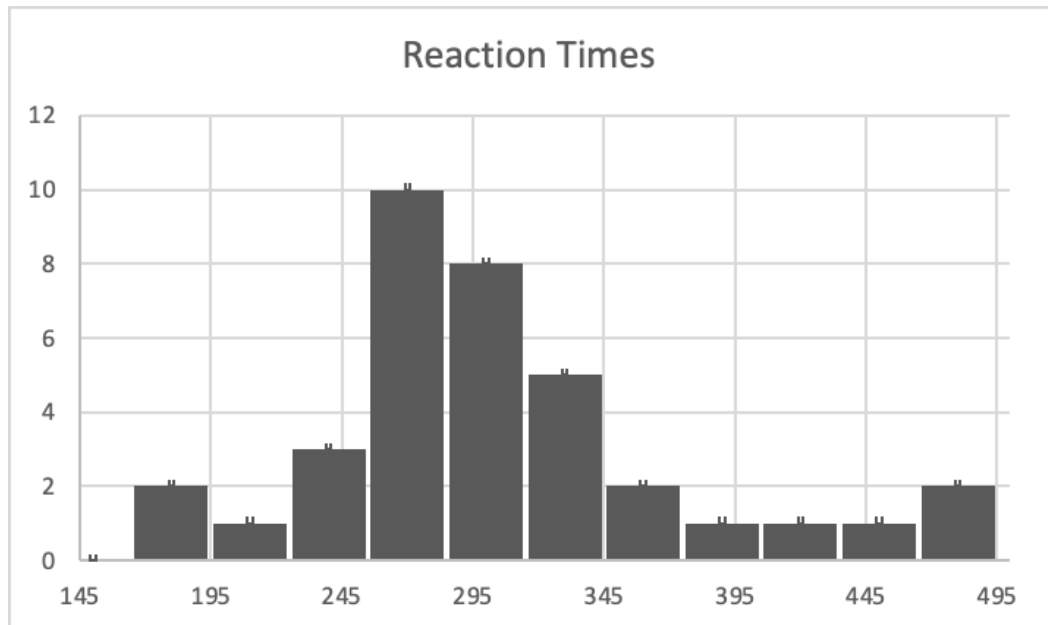
Subject Number	Subject Age	Subject Gender	Reaction Time (ms)
1	24	Female	177 ms
2	19	Female	285 ms
3	21	Male	235 ms
4	22	Female	247 ms
5	21	Male	278 ms
6	20	Female	244 ms

7	55	Female	329 ms
8	60	Female	327 ms
9	69	Male	450 ms
10	45	Male	282 ms
11	56	Female	290 ms
12	63	Female	274 ms
13	20	Female	350 ms
14	16	Male	264 ms
15	9	Female	212 ms
16	15	Male	189 ms
17	26	Female	329 ms
18	12	Female	159 ms
19	32	Female	274 ms

20	41	Female	464ms
21	55	Male	458 ms
22	68	Male	403 ms
23	49	Male	309 ms
24	52	Female	249 ms
25	47	Male	350ms
26	45	Female	372ms
27	12	Male	289ms
28	20	Female	329ms

29	16	Female	242 ms
30	45	Female	270 ms
31	49	Male	263 ms
32	19	Female	250ms
33	57	Female	280ms
34	19	Female	261ms
35	23	Male	251ms
36	58	Male	239ms
Descriptive Stats	Under 40 years old	Mean: 256.05 ms	Stdev: 50.18 ms
Descriptive Stats	Over 40 years old	Mean: 329.94 ms	Stdev: 74.65 ms

The sample is representative of the population of interest because there are greater than 30 people (36 people total) in our sample. It is a simple random sample because our method of choosing the sample was randomly selected from a larger list of individuals. However, our sample may have been less than completely random simply due to our limited ability to sample individuals outside of the circle of people that we know.

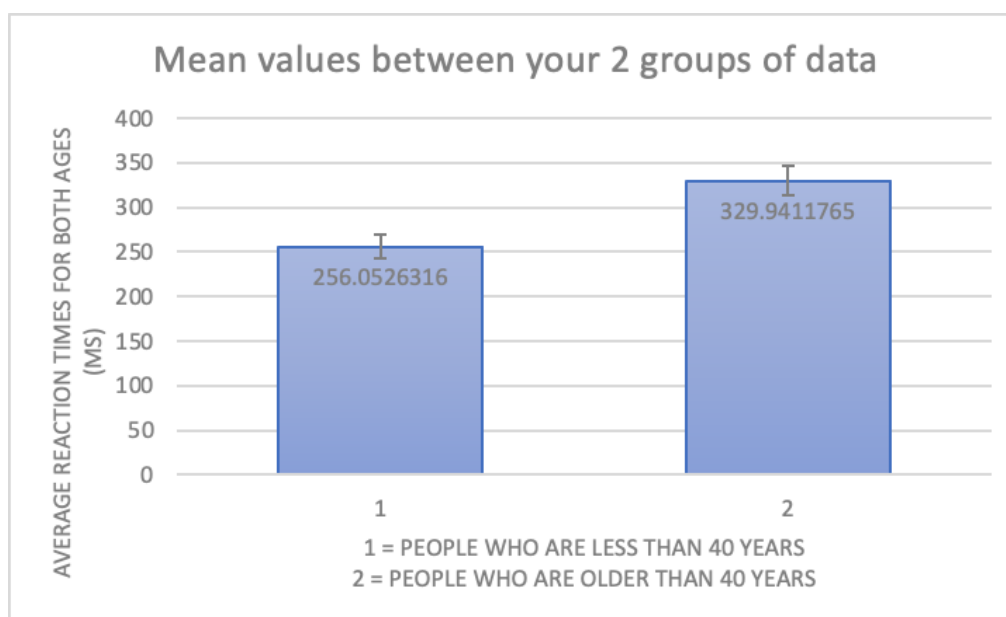


X - axis = The mean values of people who are above and below 40.

Y- axis = Frequency

The data does not fully appear to be normally distributed as the curve on the left tail does not look similar to the right one. The errors may occur because of the limited data set of 36 people. We could have taken the data from 100 people which will give us more diverse values and increase the chance of normality in a curve that would represent the population better.

A graph comparing the mean values between your 2 groups of data:



The confidence interval is 95% and the degrees of freedom for each:

The reaction time of 19 values for ages below 40:

- The mean value = 256.05 ms
- Standard deviation = 50.18 ms
- $CI = \bar{x} + t(\alpha/2) * (S/\sqrt{n}) = 259.7 + (1.7341) * (50.18/\sqrt{19})$
- **Confidence Interval = 239.74 < x < 279.66**

The reaction time of 17 values for ages above 40 :

- The mean value = 329.94 ms
- Standard deviation = 74.64 ms
- $CI = \bar{x} + t(\alpha/2) * (S/\sqrt{n}) = 329.94 + (1.7459) * (74.64/\sqrt{17})$
- **Confidence Interval = 302.65 < x < 357.23**

Calculating test statistic:

$$S_p = \sqrt{\frac{(s_1^2)(n_1 - 1) + (s_2^2)(n_2 - 1)}{n_1 + n_2 - 2}} = \sqrt{\frac{(50.18^2)(19 - 1) + (74.65^2)(17 - 1)}{19 + 17 - 2}} = 62.89 \text{ ms}$$

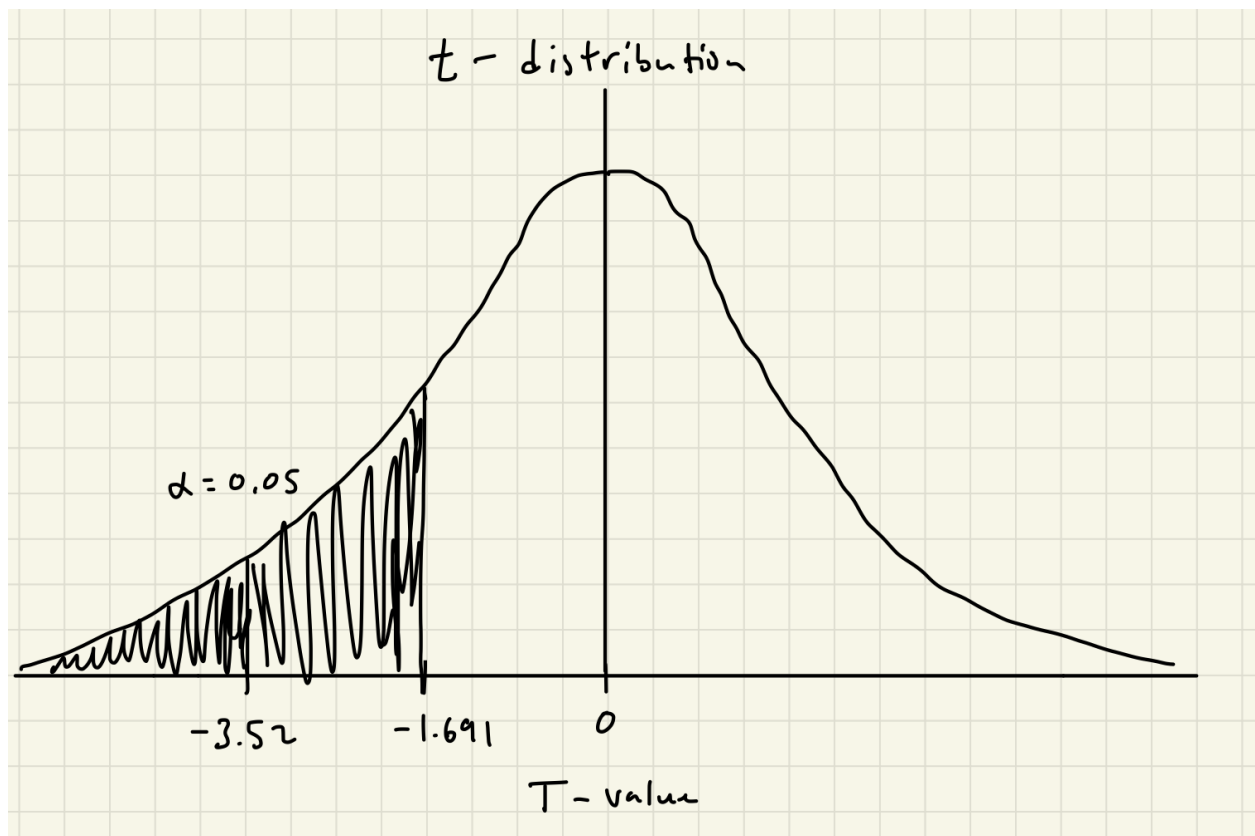
$$t_{\text{stat}} = \frac{(\bar{x}_1 - \bar{x}_2)}{S_p \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}} = -3.52$$

Identifying the critical value(s) :

Degrees of freedom = 34

$$t_{.05} = -1.691$$

A graph of the t-distribution with the critical region(s) shaded:



Do we “reject H_0 ” or “fail to reject H_0 ”?

Reject H_0 .

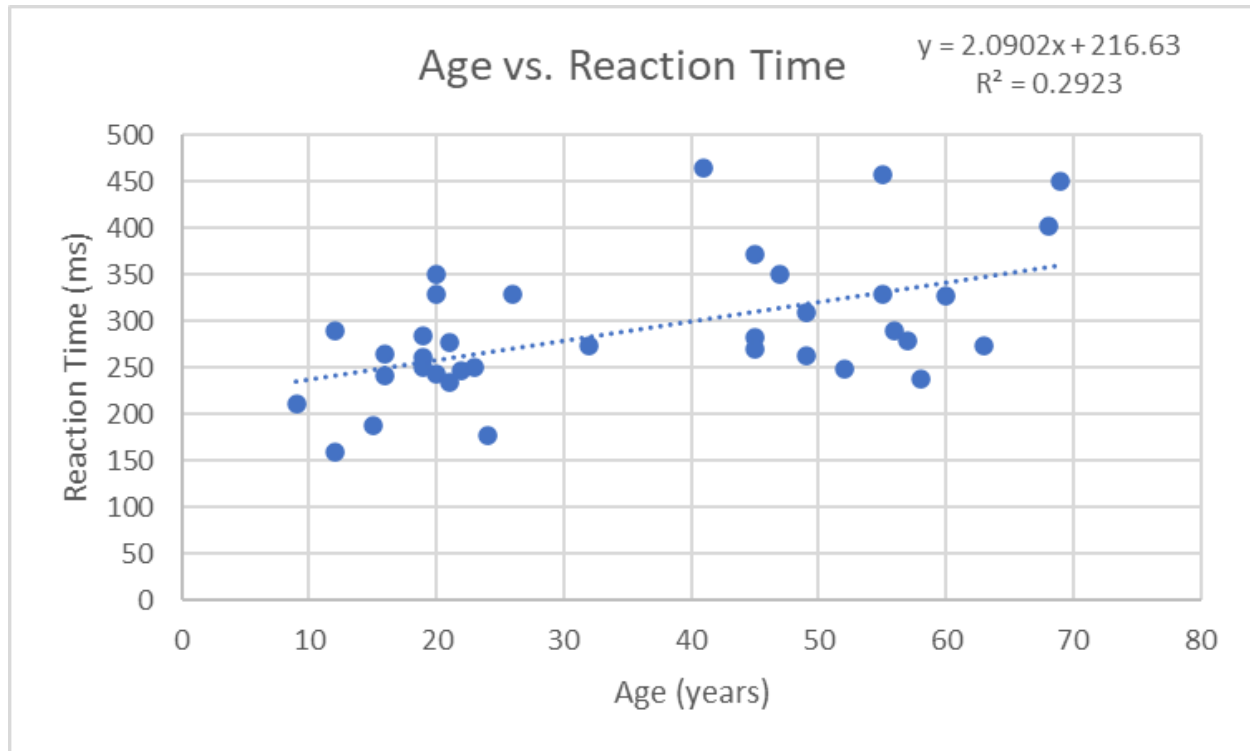
Conclusion: There is sufficient evidence to warrant the claim that people under the age of 40 have a shorter reflex time than people over the age of 40.

Linear regression equation:

$$y = 2.0902x + 216.63$$

$$r^2 = 0.2923$$

A plot of the linear regression:



There is not sufficient evidence to support the claim that a linear correlation exists between age and reflex time because the r^2 value is 0.2923, which is low, and thus does not suggest a strong linear correlation.

Example: The value of your dependent variable collected from somebody who is 45 years old:

Linear regression equation:

$$y = 2.0902x + 216.63$$

For someone who is 45 years old, the linear regression model predicts that the reaction time is $2.0902(45) + 216.63 = 310.69$ ms.