

Q<sub>1</sub> = In a perfectly competitive environment, Marginal Cost is the price.

$$TC = 10 + 3q^2$$

$$MC = \frac{d(TC)}{dq} = 6q = \text{price}$$

0

Q<sub>2</sub> =  $P = 20 - Q$

$$c = 2$$

In perfect competition the Marginal cost is the price

$$P = 2$$

$$Q = 20 - P = 20 - 2 = 18$$

0

Under a cartel the goal is to maximize profit (total).

$$\max_{q_1, q_2} \pi(q_1, q_2) = \left(20 - \sum_{i=1}^2 q_i\right) \sum_{i=1}^2 q_i - TC(q_1 + q_2)$$

$$\frac{d\pi}{dq_1} = 20 - 2(q_1 + q_2) - 2 = 0$$

$$q = q_1 + q_2$$

2

The total output produced will be q

The price will be  $P = 20 - q = 11$

Q3

Under Discriminating monopolist, the avoidance of arbitrage is obtained when

$$p_1 \left( 1 + \frac{1}{\epsilon_1} \right) = p_2 \left( 1 + \frac{1}{\epsilon_2} \right)$$

$$p_1 \left( 1 - \frac{1}{1.7} \right) = p_2 \left( 1 - \frac{1}{3.4} \right)$$

$$\frac{p_1}{p_2} = \frac{2.4}{3.4} \times \frac{1 - \frac{1}{3.4}}{1 - \frac{1}{1.7}}$$

$$\frac{p_1 - p_2}{p_2} = \frac{\frac{1}{1.7} - \frac{1}{3.4}}{1 - \frac{1}{1.7}}$$

$$\frac{p_1 - p_2}{p_2} = \frac{\frac{1}{3.4} - \frac{1}{6.7}}{\frac{0.7}{1.7}} = \frac{0.5}{6.7}$$

$$x = \frac{5}{7} = 71.42\%$$

2

Q4 In renting, the monopolist's goal is to maximize profit

$$TR = (50 - Q)Q$$

$$P = 50 - Q \quad *$$

$$MR = 50 - 2Q$$

$$MC = 5$$

$$q_{max} = TR - TC \text{ max}$$

$$\frac{d\pi}{dQ} = 0 \Rightarrow 50 - 2Q - MC = 0$$

$$= 50 - 2Q - 5 = 0$$

$$\frac{45}{2} = Q$$

$$P = \frac{55}{2}$$

~~Revenue~~ <sup>Profit</sup> in period 1 =  $\frac{55}{2} \times \frac{45}{2} = 618.75$

Total revenue in 2 periods =  $618.75 \times 2$

1237.5

Selling: In the second period the demand will be lowered by exactly the amount sold in the first period (say  $\bar{q}_1$ ).

2<sup>nd</sup> Period :  $q_2 = 50 - p_2 - \bar{q}_1 \quad - (1)$

$$p_2 = 50 - \bar{q}_1 - q_2$$

$$TR = (50 - \bar{q}_1 - q_2)q_2$$

$$MR = 50 - \bar{q}_1 - 2q_2$$

For profit maximization  $MR = MC$

$$\frac{45 - \bar{q}_1}{2} = q_2 \quad - (2)$$

For the marginal buyer in period ①, the utility will be same if he buys in period ① or ②.

$$2(50 - \bar{q}_1) - p_1 = (50 - q_2) - p_2$$

$$100 - 2\bar{q}_1 - p_1 = \bar{q}_1 \quad \text{--- from ①}$$

$$\frac{100 - p_1}{3} = \bar{q}_1$$

$$\frac{100 - p_1}{3} = 50 - p_1$$

$$100 - p_1 = 150 - 3p_1$$

$$2p_1 = 50$$

$$p_1 = 25$$

$$q_1 = 75$$

$$q_2 = \frac{45 - \bar{q}_1}{2} = 10$$

$$p_2 =$$

$$\bar{q}_1 = 25 \quad \text{from ①}$$

$$q_2 = \frac{45 - \bar{q}_1}{2} = 10 \quad \text{--- from ②}$$

$$q_2 = 10 \quad \text{--- from ①}$$

$$p_2 = 15$$

$$\text{Total Revenue} = p_1 q_1 + p_2 q_2$$

$$= 625 + 150$$

$$= 775$$

Total Revenue  
of seller

0

Q5  $MC_{OPEC} = 5$

$MC_{NOPEC} = 10$

Let OPEC produce  $q_1$

if Non OPEC "  $q_2$

$$\pi_{OPEC} = \left( 65 - \frac{q_1 + q_2}{3} \right) q_1 - TC_{OPEC}$$

$$\frac{d\pi}{dq_1} = 0 \Rightarrow 65 - \frac{(2q_1 + q_2)}{3} - 5 = 0$$

do

$$60 = \frac{2q_1 + q_2}{3}$$

$$180 = 2q_1 + q_2$$

$$\pi_{Non OPEC} = \left( 65 - \frac{q_1 + q_2}{3} \right) q_2 - TC_{NOPEC}$$

$$\frac{d\pi}{dq_2} = 0 \quad 65 - \frac{(q_1 + 2q_2)}{3} - 10 = 0$$

$$55 \times 3 = q_1 + 2q_2$$

$$165 = q_1 + 2q_2$$

$$180 \times 2 - 165 = 3q_1$$

$$\boxed{\begin{matrix} q_1 = 120 \\ q_2 = 50 \end{matrix}}$$

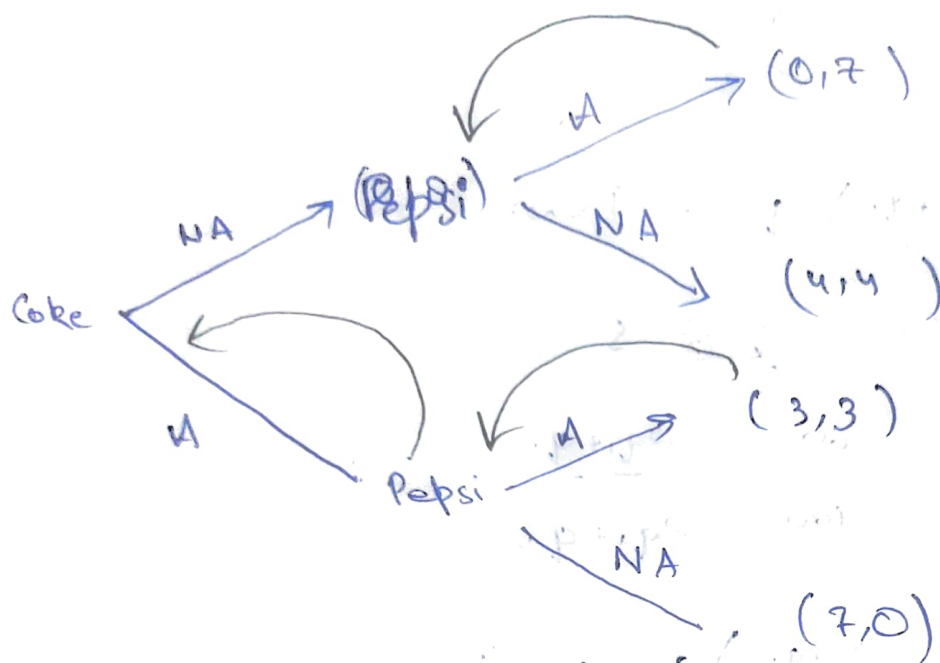
$$\text{Price} = \left( 65 - \frac{q_1 + q_2}{3} \right)$$

$$= \left( 65 - \frac{115}{3} \right) \Rightarrow \boxed{P = 26.667}$$

Q46

Advertising = -1

Net size = 0



Coke \ Pepsi		
	A	NA
A	(3, 3)	(7, 0)
NA	(0, 7)	(4, 4)

~~whether coke chooses to advertise or not, Pepsi will choose to advertise~~

If coke chooses to advertise, Pepsi will also choose to advertise, as it is better off. Same and vice versa

If coke decides to not advertise, pepsi will still choose to advertise, as it'll be better off. & vice versa

Hence the outcome will be where both choose to advertise & gain 3 billion each.

(B)