



Date of examination: 20.09.2022 Session (FN / AN): FN Duration: 2 hours Full marks: 60

Subject No.: AI61005 **Subject:** Artificial Intelligence: Foundations and Applications

Department/Center/School: Centre of Excellence in Artificial Intelligence (CoEAI)

Instructions: Answer all questions. All parts of a question must be answered in the same place.

1. State whether the statements are True or False and justify your answer with a proper proof or a clear counterexample:
 - a) Algorithm A* for a minimization problem with all heuristics 0 and all edge costs positive except one edge which may have negative edge cost may produce a non-optimal solution.
 - b) If the problem is one of minimization, then Algorithms A* and IDA* will always give the same solution cost irrespective of whether the heuristics overestimate or not. Assume positive edge costs and non-negative heuristic estimates.
 - c) In case of a maximization problem with no cycles in the graph, positive edge costs and overestimating heuristics, IDA* may expand more nodes than DFBB considering a total count of nodes expanded including re-expansions.
 - d) There is a two-player game of at least 16 leaf nodes where we may have no pruning if we use alpha-beta pruning using a left to right ordering.
 - e) There is a two-player game of at least 16 leaf nodes where exactly the same set of leaf nodes is pruned by alpha-beta pruning algorithm when we use left to right ordering and when we use right to left ordering.

[(1+2) X 5 = 15 marks]

2. State whether the statements are True or False and justify your answer with a proper proof or a clear counterexample:

- a) A propositional formula of at least four propositional (Boolean) variables which is non-valid can never be satisfiable.
- b) Given a binary predicate $p(x, y)$, is the following first order predicate logic formula valid?

$$\forall_x \exists_y p(x, y) \Rightarrow \exists_x \forall_y p(x, y)$$

- c) Given a binary predicate $p(x, y)$ and the fact that the domain is a finite set of 2 elements only, the predicate logic formula $\exists x \forall y p(x, y)$ be written in using propositional logic constructs only.

- d) Vipin either ate ice-cream or drank hot coffee before going to bed but not both. If he ate ice-cream, he had a sore throat next morning. Vipin did not have a sore throat next morning. Therefore, he drank hot coffee before going to bed. [Use propositional logic based modelling to solve this]

[(1+2) X 3 + (1+5) = 15 marks]

3. Use Resolution Refutation to prove or disprove Goal from Statement 1.

Statement 1: Every student in this class is an atheist or a theist.

Goal: There is a student in this class who is an atheist or a theist.

Does the conclusion of the above reasoning of the goal change when Statement 2 is added in the knowledge base?

Statement 2: There is a student in this class.

Make use of the following steps to answer the question.

- Translate the statements into first order logic using predicates: $\text{studentInClass}(s)$, $\text{atheist}(s)$, $\text{theist}(s)$.
- Convert the translated sentences into Conjunctive Normal Form if required.
- Try to derive the Goal with Statement 1 only and state your conclusion.
- Revise your conclusion (if any) after adding Statement 2 into knowledge base. Show steps of resolution.

[2+2+2+2=8 Marks]

4. Answer the following questions related to the first order logic:

- a) Convert the following first order logic statements into corresponding Conjunctive Normal Forms.

- $\forall x [(\forall y p(y) \Rightarrow r(x, y)) \Rightarrow \exists y r(y, x)]$
- $\neg \exists x \forall y \forall z [(p(y) \Rightarrow q(z)) \Rightarrow (p(x) \Rightarrow q(x))]$
- $\forall x \forall y [p(x, y) \vee r(x, y) \Rightarrow \exists z q(x, y, z)]$

- b) Consider the following first order logic knowledge base

$$\begin{array}{ll} \forall x p(x) \Rightarrow q(x) & \forall x \neg p(x) \Rightarrow r(x) \\ \forall x q(x) \Rightarrow s(x) & \forall x r(x) \Rightarrow s(x) \end{array}$$

Can we use Resolution Rule to infer $s(a)$ from the knowledge base? If so, show inference steps; otherwise explain.

[(3+2+2)+3=10 Marks]

5. Write Prolog program for the following problems:

a) Check whether two sets are equivalent or not:

Implement the Prolog predicate `set_equiv(S1, S2)`, where `S1` and `S2` are two sets represented as Prolog list. For example, `set_equiv([8, 3, 4, 1, 9], [3, 8, 4, 9, 1])` will return true.

b) Implement Prolog predicate `zip_concat(L1, L2, L3)`:

The program takes two lists (`L1` and `L2`) as input and outputs another list `L3`. The list `L3` will place each pair of elements (one from `L1` and other from `L2` in the same index) consecutively. The remaining part of the bigger list will be appended to the final list (`L3`). For example, `zip_concat([3, 4, 7, 1], [9, 6, 10, 2, 5], L3)` will output `L3=[3, 7, 4, 9, 7, 6, 1, 10, 2, 5]`

c) Implement Prolog predicate `split_pivot(P, L, U1, U2)`:

The program splits a list `L` in two lists `U1` and `U2` with respect to a pivot `P` where all the elements in `U1` are less than or equal to `P` and all the elements in `U2` are greater than `P` with original order preserved. For example, `split_pivot(2, [5, 6, 2, 8, 7], U1, U2)` will output `U1=[5, 2]` and `U2=[6, 8, 7]`

[4+4+4=12 Marks]

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