

# Acceleration

Acceleration is the rate of change of velocity.

Either speed and/or direction of motion can change.

For 1D motion:

- object is slowing down
- OR speeding up
- OR changing direction between forward and backward  
OR North to East (2 Dimensions)

$$\vec{a} = \frac{\Delta \vec{v}}{\Delta t} = \frac{\vec{v}_2 - \vec{v}_1}{\Delta t}$$

$$\text{Units: } \frac{m/s}{s} = \frac{m}{s^2}$$

## ACCELERATION PROBLEM:

What is the average acceleration of a train which changes its velocity from 95 km/h north to 22 km/h north in a time of 15 minutes?

Ans:

Let N = +

$V_1 = 95 \text{ km/h [N]}$

$V_2 = 22 \text{ km/h [N]}$

$\Delta t = 15 \text{ min} = 0.25 \text{ h}$

$$a = \frac{(v_2 - v_1)}{\Delta t}$$

$$a = \frac{(22 - 95) \text{ km/h}}{0.25 \text{ h}}$$

$$a = -292 \text{ km/h}^2 \text{ [N]}$$

$$\vec{a} = 2.9 \times 10^2 \text{ km/h}^2 \text{ [S]}$$

## MOTION GRAPH COMPARISON

Imagine a car that is dripping oil at a constant rate moving in three different scenarios:



Constant velocity



Speeding up uniformly

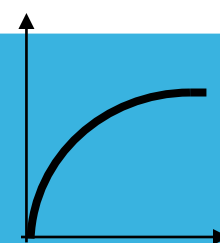
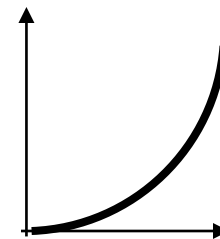
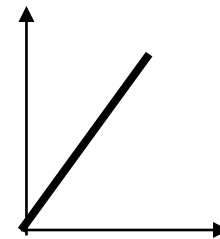


Slowing down uniformly



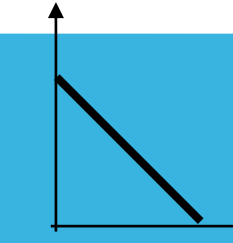
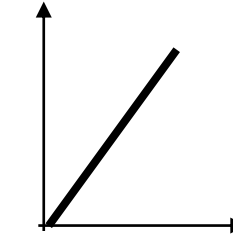
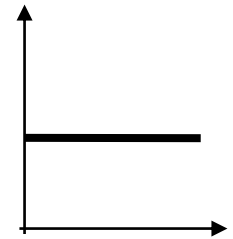
Position-Time

Graph



Velocity-Time

Graph



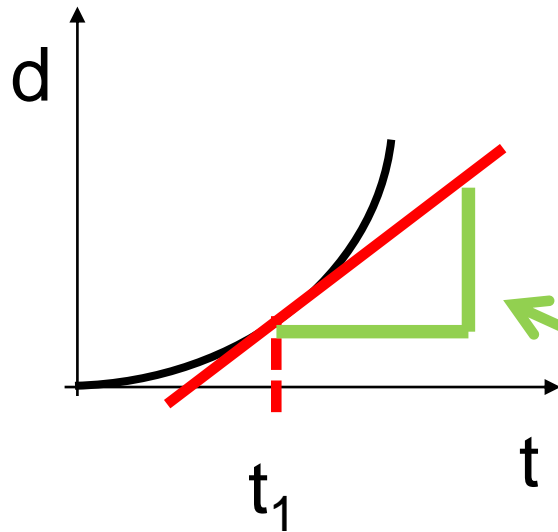
# ACCELERATION IS A VECTOR!

**In 1D, use signs to account for direction.**

Direction of Initial Velocity	Direction of Initial Acceleration	Change in Speed
East (+)	East (+)	+ (Speeds up)
East (+)	West (-)	- (Slows down)
West (-)	East (+)	- (Slows down)
West (-)	West (-)	+ (Speeds up)

**If the acceleration is in the same direction as the initial velocity the object speeds up!!!**

# ANALYZING D-T GRAPHS FOR UNIFORM ACCELERATION



To find velocity from a position-time graph we take the slope.

The slope of this tangent gives us the velocity at time  $t_1$ !

When we have a curved d-t graph the velocity changes!

To find the instantaneous velocity at any moment we draw a tangent to the curve and take the slope of the tangent!