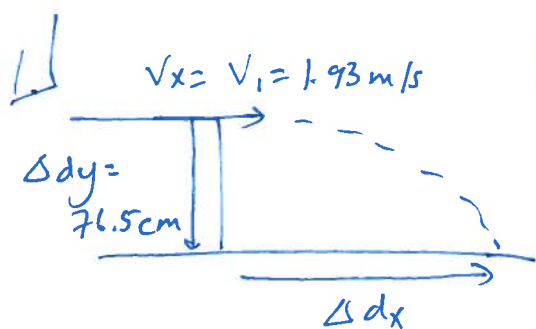


# Projectile Motion Day 9 - P1-4 pg 40 81, 4, 5, 7 pg 43

1/7



$$V_1 = V_x = 1.93 \text{ m/s}$$

$$\Delta dx = ?$$

$$\Delta t = ?$$

$$V_{1y} = 0$$

$$V_{2y} = ?$$

$$a_y = g = 9.80 \text{ m/s}^2 \text{ [down]}$$

$$\Delta dy = 0.765 \text{ m [down]}$$

$$\Delta t = ?$$

a) Solve for time using vertical information

$$\Delta dy = V_{1y} \Delta t + \frac{1}{2} a_y \Delta t^2$$

$$0.765 = 0 + \frac{1}{2} (9.80) \Delta t^2$$

$$0.765 = 4.90 \Delta t^2$$

$$\Delta t = \pm \sqrt{\frac{0.765}{4.90}} = 0.395 \text{ s}$$

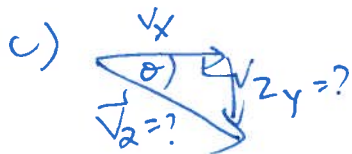
b) Solve for range:

$$\Delta dx = V_x \Delta t$$

$$= (1.93 \text{ m/s}) (0.395 \text{ s})$$

$$= 0.7621 \text{ m}$$

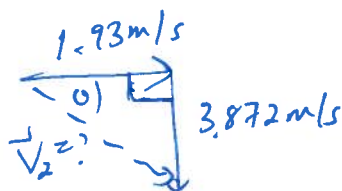
$$= 0.763 \text{ m}$$



$$V_{2y} = V_{1y} + a_y \Delta t$$

$$= 0 + (9.80 \text{ m/s}^2) (0.395 \text{ s})$$

$$= 3.872 \text{ m/s}$$



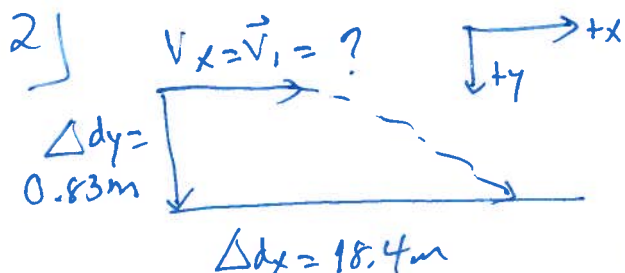
$$V_2 = \sqrt{1.93^2 + 3.872^2} = 4.327 \text{ m/s}$$

$$\theta = \tan^{-1} \left( \frac{3.872}{1.93} \right) = 63.51^\circ$$

$$\therefore \vec{V}_2 =$$

$$4.33 \text{ m/s}$$

[63.5° below the horizontal]



$$V_{1x} = V_1 = ?$$

$$\Delta dx = 18.4 \text{ m}$$

$$\Delta t = ?$$

$$V_{1y} = 0$$

$$\Delta dy = 0.83 \text{ m}$$

$$a_y = g = 9.80 \text{ m/s}^2$$

$$\Delta t = ?$$

Solve for time:

$$\Delta dy = \frac{1}{2} a_y \Delta t^2$$

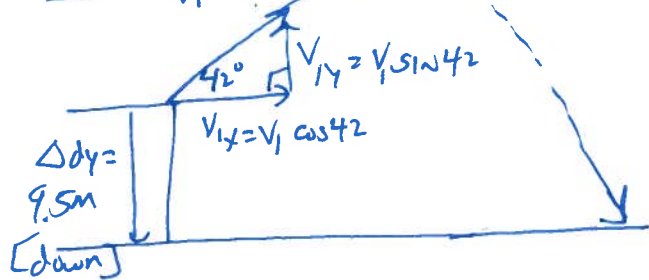
$$\Delta t = \sqrt{\frac{2(\Delta dy)}{a_y}}$$

$$\Delta t = \sqrt{\frac{2(0.83)}{9.80}} = 0.412$$

Solve for Vx:

$$\therefore \Delta dx = 18.4 \text{ m} = \sqrt{447}$$

3]  $\vec{V}_1 = 12 \text{ m/s}$  [42° above horizontal]



		2/7
X	Y	
$\Delta dx = ?$	$V_{1y} = 12 \sin 42 \text{ m/s}$	
$\Delta t = ?$	$a_y = g = -9.80 \text{ m/s}^2$	
$V_{1x} = 12 \cos 42 \text{ m/s}$	$\Delta dy = -9.5 \text{ m}$	
	$\Delta t = ?$	

a) Solve for time using y component:

$$\Delta dy = V_{1y} \Delta t + \frac{1}{2} a_y \Delta t^2$$

$$-9.5 = 12 \sin 42 \Delta t - 4.90 \Delta t^2$$

$$4.90 \Delta t^2 - 12 \sin 42 \Delta t - 9.5 = 0$$

Solve for  $\Delta t$  using quadratic formula:

$$\Delta t = \frac{12 \sin 42 \pm \sqrt{(12 \sin 42)^2 - 4(4.90)(-9.5)}}{2(4.90)}$$

$$\Delta t = \frac{8.03 \pm 15.83}{9.80} = 2.43 \text{ s or } -0.7$$

$\therefore$  the time of flight is 2.43 s.

b)  $\Delta dx = ?$   $\Delta dx = V_{1x} \Delta t$

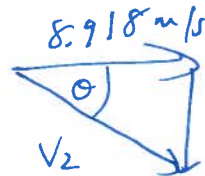
$$= (12 \cos 42)(2.43) = 21.7 \text{ m} \approx 22 \text{ m}$$

$\therefore$  The width of the moat is 22 m.

c)  $V_{2y} = ?$   $V_{2y} = V_{1y} + a_y \Delta t$

$$= 12 \sin 42 - 9.80(2.43)$$

$$= -15.8 \text{ m/s}$$

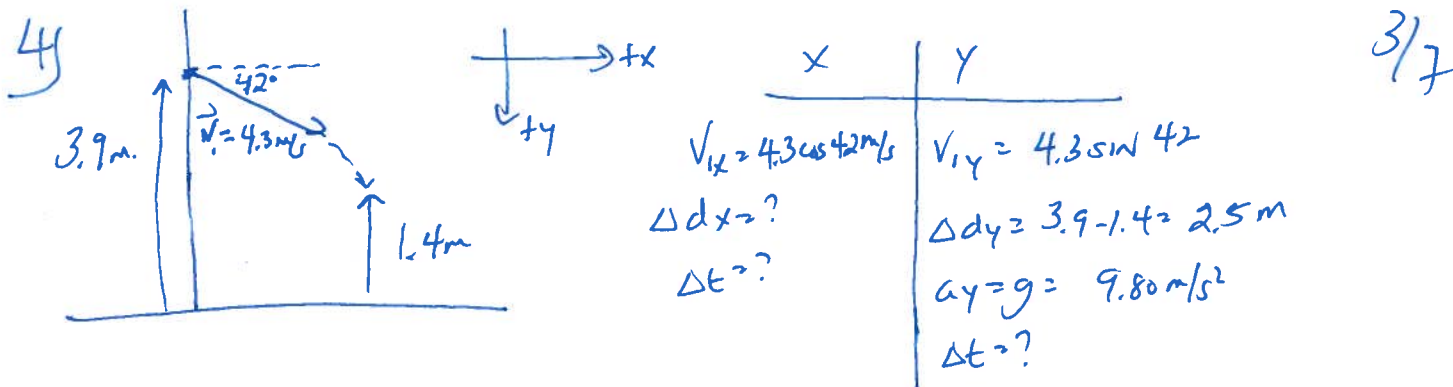


$$V_2 = \sqrt{8.92^2 + 15.8^2}$$

$$= 18.2 \text{ m/s}$$

$$\theta = \tan^{-1}\left(\frac{15.8}{8.92}\right) = 60.61^\circ$$

$\therefore$  the final velocity is 18 m/s [61° below the horizontal].



a) Solve for time:

$$\Delta dy = V_{iy} \Delta t + \frac{1}{2} a_y \Delta t^2$$

$$2.5 = 4.3 \sin 42^\circ \Delta t + 4.90 \Delta t^2$$

$$0 = 4.90 \Delta t^2 + 2.877 \Delta t - 2.5 = 0$$

$$\Delta t = \frac{-2.877 \pm \sqrt{2.877^2 - 4(4.90)(-2.5)}}{2(4.90)} = \frac{-2.877 \pm 7.568}{9.80}$$

$$\Delta t = 0.479 \text{ or } -1.07$$

$\therefore$  the ball is in the air for 0.48 s.

b)  $\Delta dx = V_{ix} \Delta t = (4.3 \cos 42^\circ)(0.479 \text{ s}) = 1.53 \text{ m} \approx 1.5 \text{ m}$

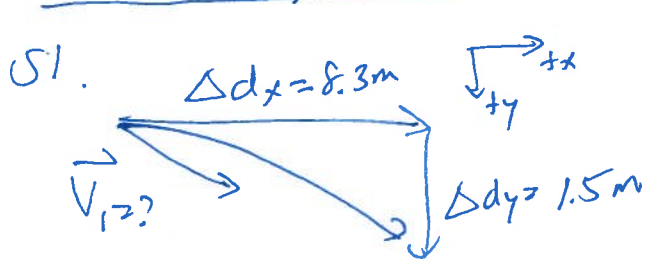
c)  $V_{2y} = ?$   $V_{2y} = V_{iy} + a_y \Delta t$   
 $= 4.3 \sin 42^\circ + (9.80)(0.479)$   
 $= 7.57$

$4.3 \cos 42^\circ = 3.196 \text{ m/s}$



$V_2 = 8.215 \text{ m/s}$   $\theta = \tan^{-1}\left(\frac{7.57}{3.196}\right) \approx 67.1^\circ$

$\therefore$  the speed of ball is 8.2 m/s as it is caught.



X	Y
$\Delta dx = 8.3m$	$V_{1y} = 0.0 m/s$
$V_x = ?$	$a_y = g = 9.80 m/s^2$
$\Delta t = ?$	$\Delta t = ?$
	$\Delta dy = 1.5m$

Solve for time:

$$\Delta dy = \frac{1}{2} a_y \Delta t^2$$

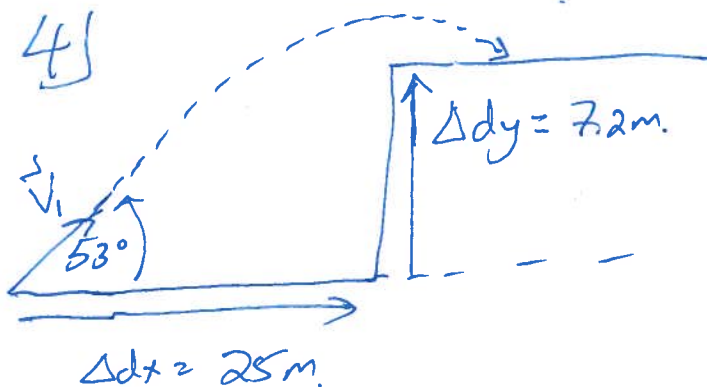
$$1.5 = \frac{1}{2} (9.80) \Delta t^2$$

$$\Delta t = \sqrt{\frac{1.5}{4.90}} = 0.553s$$

Solve for horizontal speed:

$$V_{1x} = \frac{\Delta dx}{\Delta t} = \frac{8.3m}{0.553s} = 15.0 m/s.$$

∴ the rock's initial speed is 15.0 m/s.



X	Y
$V_{1x} = V_1 \cos 53$	$V_{1y} = V_1 \sin 53$
$\Delta t_1 = 2.1s$	$\Delta t_1 = 2.1s$
$\Delta dx_1 = 25m$	$\Delta dy_1 = 7.2m$
	$\Delta t_2 = ?$

a)  $V_{1x} = \frac{\Delta dx_1}{\Delta t_1} = \frac{25m}{2.1s} = 11.90 m \rightarrow V_1 \cos 53 = 11.90m$

$$V_1 = \frac{11.90m}{\cos 53} = 19.8 m/s$$

Find time to land on building:

b)  $\Delta t_2 = ?$   $\Delta dy_2 = V_{1y} \sin 53 \Delta t_2 - \frac{1}{2} (9.80) \Delta t_2^2$

$$7.2 = 19.8 \sin 53 \Delta t_2 - 4.90 \Delta t_2^2$$

$$0 = -4.90 \Delta t_2^2 + 19.8 \sin 53 \Delta t_2 - 7.2$$

$$\Delta t_2 = \frac{-19.8 \sin 53 \pm \sqrt{19.8^2 \sin^2 53 - 4(-4.90)(-7.2)}}{2(-4.90)} = \frac{-15.798 \pm 10.414}{-9.80} = 0.549s \text{ or } 2.675s$$

c) Find horizontal range.

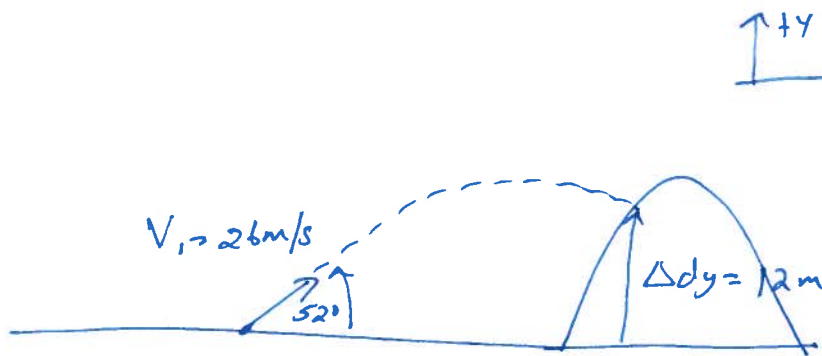
$$\begin{aligned}\Delta d_x &= V_1 \cos 53 \cdot \Delta t_2 \\ &= (19.8 \text{ m/s}) (\cos 53) (2.67 \text{ s}) \\ &= \boxed{31.8 \text{ m}}\end{aligned}$$

c.) Find height of ball at time  $\Delta t_1 = 2.1 \text{ s}$ .

$$\begin{aligned}\Delta d_y &= V_1 \sin 53 \Delta t_1 - \frac{1}{2} (9.80) \Delta t_1^2 \\ &= (19.8 \text{ m/s}) (\sin 53) (2.1 \text{ s}) - 4.90 (2.1 \text{ s})^2 \\ &= 11.567 \text{ m}\end{aligned}$$

$$\therefore \text{Clearance} = 11.567 \text{ m} - 7.2 \text{ m} = \boxed{4.4 \text{ m}}$$

5]



x	y
$V_{1x} = 26 \cos 52$	$V_{1y} = 26 \sin 52$
$\Delta d_x = ?$	$a_y = 9 \text{ m/s}^2 - 3.7 \text{ m/s}^2$
$\Delta t = ?$	$\Delta d_y = 12 \text{ m}$
	$\Delta t = ?$
	$\Delta d_{y \max} = ?$

a) Max height  $V_{2y} = 0$

$$\Delta d_{y \max} = \frac{V_{2y}^2 - V_{1y}^2}{2a_y} = \frac{0 - (26 \sin 52 \text{ m/s})^2}{2(-3.7 \text{ m/s}^2)} = 56.7 \text{ m}$$

b)  $\Delta t = ?$   $\Delta d_y = V_{1y} \Delta t + \frac{1}{2} a_y \Delta t^2$

$$12 = 26 \sin 52 \Delta t + \frac{1}{2} (-3.7) \Delta t^2$$

$$1.85 \Delta t^2 - 20.49 \Delta t + 12 = 0$$

$$\Delta t = \frac{20.49 \pm \sqrt{20.49^2 - 4(1.85)(12)}}{2(1.85)}$$

$$\Delta t = \frac{20.49 \pm 18.19}{3.7}$$

$$= \boxed{10.45 \text{ s}} \text{ OR } 0.620 \text{ s}$$

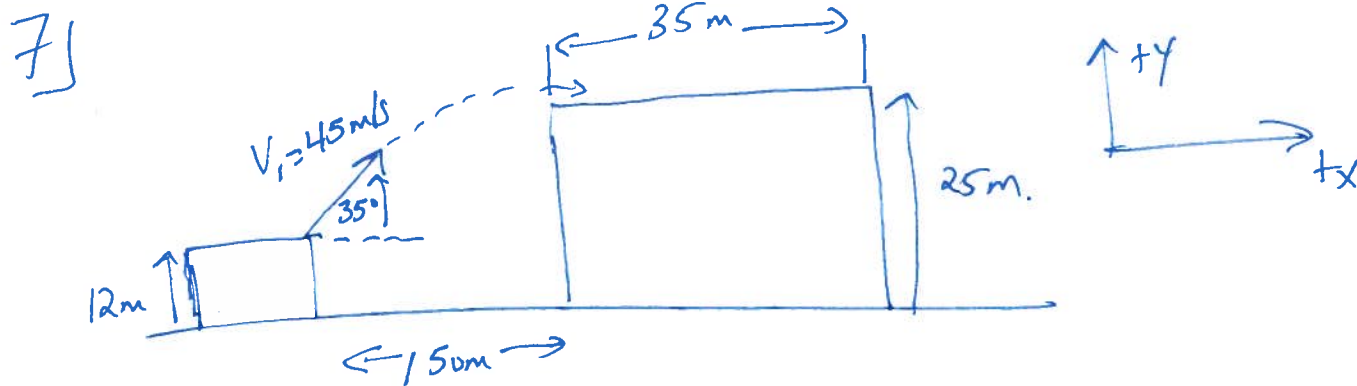
$\therefore$  it passes through a height of 12.0 m at two times. The first time it occurs after the



c) Solve for range:

$$\begin{aligned}\Delta d_x &= V_x \Delta t \\ &= (26 \cos 52)(10.45 \text{ s}) \\ &= 167.3 \text{ m}\end{aligned}$$

∴ the max height of the rock is 57m.  
The time of flight is  $1.0 \times 10^1 \text{ s}$  and the range is  $1.7 \times 10^2 \text{ m}$ .



Solve for time of flight to reach building.

$$\begin{aligned}V_{ix} &= 45 \cos 35^\circ \\ \Delta d_x &= 150 \text{ m} \\ \Delta t &= ?\end{aligned}$$

$$\Delta t = \frac{\Delta d_x}{V_{ix}} = \frac{150 \text{ m}}{45 \cos 35^\circ} = 4.069 \text{ s}$$

Solve for max height and time to reach max height.

$$\begin{aligned}\Delta d_{y \max} &= ? \\ V_{2y} &= 0.0 \\ \Delta d_y &= \frac{V_{2y}^2 - V_{1y}^2}{2a_y} = \frac{0 - (45 \sin 35^\circ)^2}{2(-9.80)} \\ &= 33.99 \text{ m}\end{aligned}$$

$$\begin{aligned}V_{1y} &= 45 \sin 35^\circ \\ a_y &= g = -9.80 \text{ m/s}^2\end{aligned}$$

∴ max height from ground =

$$33.99 \text{ m} + 12 \text{ m} = 45.99 \approx 46 \text{ m}$$

$$\Delta t = ? \quad \Delta t = \frac{V_{2y} - V_{1y}}{a_y} = \frac{0 - 45 \sin 35^\circ}{-9.80} = 2.634 \text{ s}$$

From this we can see the snowball will rise and land on the building on the way down

Solve for time to reach a height of 25m (13m above launch point) 7/7

$$13 = V_i \sin 35^\circ \Delta t + \frac{1}{2} a_y \Delta t^2$$

$$13 = 45 \sin 35^\circ \Delta t - 4.90 \Delta t^2$$

$$4.90 \Delta t^2 - 25.81 \Delta t + 13 = 0$$

$$\Delta t = \frac{25.81 \pm \sqrt{25.81^2 - 4(4.9)(13)}}{2(4.90)} = \frac{25.81 \pm 20.28}{9.80} = 0.564s \text{ or } 4.70s$$

$\therefore$  at time 4.70s it is at roof height of the second building.

The final check is to make sure it has not overshoot the building.

$$\Delta x = (45 \cos 35^\circ)(4.70s) = 173.4m - 150m = 23.4m$$

horizontal  
start of building  
↓ 2

Since the second building is 35m wide the snowball will land on the roof!!