

## Projectile Motion "SIN" Problems

85-5.

$\Delta t$ (G)	$\Delta y$ (N)	$\downarrow v_i$	$\downarrow a$	$\downarrow +y$
1	30			
2	80			
3	?			

In general  $\Delta y = v_i \Delta t + \frac{1}{2} a \Delta t^2$

$$\Delta t = 1G \rightarrow 30N = v_i (1G) + \frac{a}{2} (1G)^2 \rightarrow 30 = v_i + \frac{a}{2} \quad \text{--- (1)}$$

$$\Delta t = 2G \rightarrow 80N = v_i (2G) + \frac{a}{2} (2G)^2 \rightarrow 80 = 2v_i + 2a \quad \text{--- (2)}$$

Solve for  $a$ :  $[(2) - 2 \times (1)]$ :

$$\begin{array}{r} 80 = 2v_i + 2a \\ - [60 = 2v_i + a] \\ \hline 20 = a \end{array}$$

$$a = 20 \frac{N}{G^2}$$

Solve for  $v_i$  From Eq (1):

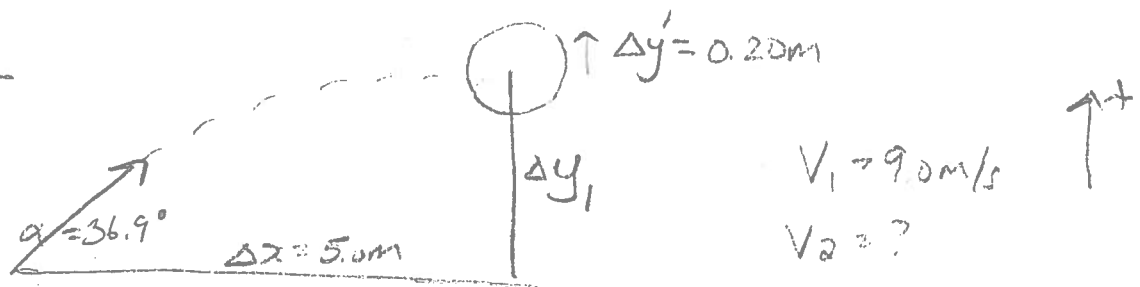
$$v_i = 30 - \frac{a}{2}$$

$$v_i = 30 - \frac{20}{2} = 20 \frac{N}{G}$$

$\Delta y_{\text{Total}}$  at  $\Delta t = 3G$ ?

$$\begin{aligned} \Delta y &= v_i \Delta t_3 + \frac{1}{2} a \Delta t_3^2 \\ &= (20 \frac{N}{G})(3G) + \frac{1}{2} (20 \frac{N}{G^2})(3G)^2 \\ &= 60N + 90N \\ &= 150N \end{aligned}$$

91-11



Solve for time of flight:

$$\Delta t = \frac{\Delta x}{V_{1x}} = \frac{5.0 \text{ m}}{9.0 \text{ m/s} \cdot \cos 36.9^\circ} = 0.6947 \text{ s}$$

Solve for original vertical displacement  $\Delta y_1$ :

$$\Delta y_1 = V_{1y} \Delta t - \frac{1}{2} g \Delta t^2$$

$$\Delta y_1 = (9.0 \text{ m/s}) (\sin 36.9^\circ) (0.6947 \text{ s}) - \frac{9.8 \text{ m/s}^2 (0.6947 \text{ s})^2}{2} = 1.3892 \text{ m}$$

Second vertical displacement  $\Delta y_2 = \Delta y_1 + 0.20 \text{ m} = 1.59 \text{ m}$

Second time of flight

$$\Delta t_2 = \frac{\Delta x}{V_2 \cos \alpha} = \frac{5.0 \text{ m}}{V_2 \cdot \cos 36.9^\circ}$$

Solve for  $V_2$ :

$$\Delta y_2 = V_{2y} \Delta t - \frac{1}{2} g \Delta t^2$$

$$1.59 \text{ m} = \frac{1}{2} \sin 36.9^\circ \left( \frac{5.0 \text{ m}}{V_2 \cos 36.9^\circ} \right) - \frac{9.8 \text{ m/s}^2}{2} \left( \frac{5.0 \text{ m}}{V_2 \cos 36.9^\circ} \right)^2$$

$$1.59 \text{ m} = 3.754 \text{ m} - \frac{191.557 \text{ m}^{3/2}}{V_2^2}$$

$$-2.164 \text{ m} = -\frac{191.557 \text{ m}^{3/2}}{V_2^2}$$

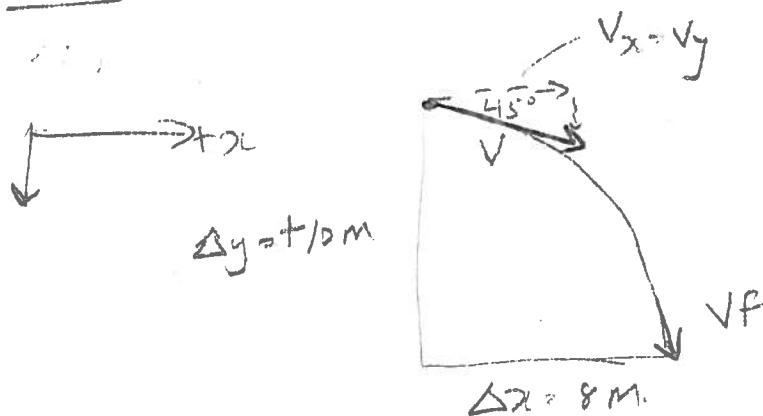
$$V_2 = 9.409 \text{ m/s}$$

$$\% \text{ increase} = \frac{V_2 - V_1}{V_1} \times 100\%$$

$$= \frac{9.409 - 9.0}{9.0} \times 100\%$$

$$= 4.5\%$$

94-21



\* by symmetry final velocity is the same as initial velocity

$$\Delta y = v_y \Delta t + \frac{1}{2} g \Delta t^2 \quad \text{--- (1)}$$

$$\Delta x = v_x \Delta t \quad \text{--- (2)} \quad \text{but } v_x = v_y \text{ at that point}$$

$$\therefore \Delta t = \frac{\Delta x}{v_x} = \frac{\Delta x}{v_y} \quad \text{--- (2b)}$$

Substitute (2b) into (1) to solve for  $\Delta t$ :

$$\Delta y = v_y \Delta t + \frac{1}{2} g \Delta t^2$$

$$\Delta y = v_y \cdot \frac{\Delta x}{v_y} + \frac{1}{2} g \Delta t^2$$

$$10\text{m} = 8\text{m} + \frac{1}{2} (9.8 \frac{\text{m}}{\text{s}^2}) \Delta t^2$$

$$2\text{m} = 4.9 \frac{\text{m}}{\text{s}^2} \cdot \Delta t^2$$

$$\Delta t = 0.639\text{s}$$

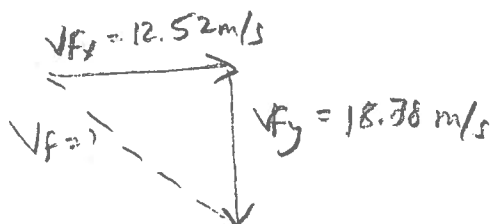
Solve for  $v_x + v_y$ :

$$v_x = \frac{\Delta x}{\Delta t} = \frac{8\text{m}}{0.639\text{s}} = 12.52\text{m/s} \quad v_y = v_x = 12.52\text{m/s}$$

Solve for  $v_f$ :

$$v_{fy} = v_y + g \Delta t = 12.52\text{m/s} + (9.8 \frac{\text{m}}{\text{s}^2})(0.639\text{s}) = 18.78\text{m/s}$$

$$v_{fx} = v_x = 12.52\text{m/s}$$



$$v_f = \sqrt{12.52^2 + 18.78^2} = 22.6\text{m/s}$$