

Day 1 13 pg 22-25 p<sup>#</sup> 1-3 pg 25 5<sup>#</sup> / 10 pg 29

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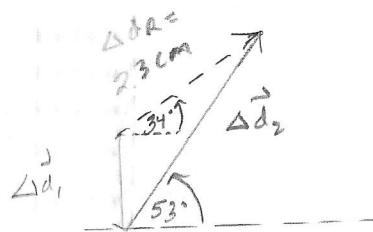
1.  $\Delta \vec{d}_1 = 1.2 \text{ km [S]}$

$\Delta \vec{d}_2 = 3.1 \text{ km [E } 53^\circ \text{ N]}$

$\Delta \vec{d}_R = ?$

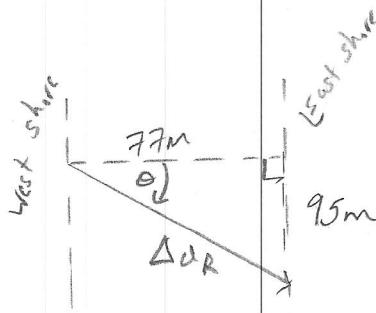
analysis:  $\Delta \vec{d}_R = \Delta \vec{d}_1 + \Delta \vec{d}_2$

Scale: 1 cm = 1 km



$\therefore \Delta \vec{d}_R = 2.3 \text{ km [E } 34^\circ \text{ N]}$

2.  $\Delta \vec{d}_R = ?$



$\Delta d_R = \sqrt{77^2 + 95^2} = 122.3 \text{ km}$

$\theta = \tan^{-1}\left(\frac{95}{77}\right) = 50.97^\circ$

$\therefore \Delta \vec{d}_R = 122 \text{ km [E } 51^\circ \text{ S]}$

3.  $\Delta \vec{d}_1 = 65 \text{ km [N } 32^\circ \text{ E]}$

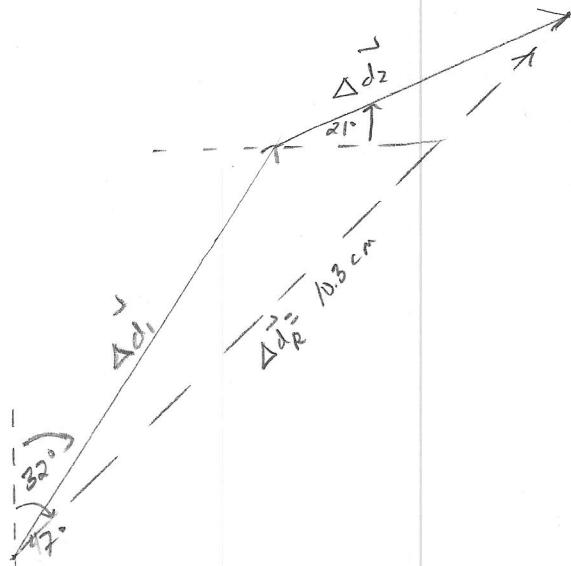
$\Delta \vec{d}_2 = 42 \text{ km [E } 21^\circ \text{ N]}$

$\Delta \vec{d}_R = ?$

analysis:  $\Delta \vec{d}_R = \Delta \vec{d}_1 + \Delta \vec{d}_2$



Scale: 1 cm = 10 km



$\Delta \vec{d}_R = 103 \text{ km [N } 47^\circ \text{ E]}$

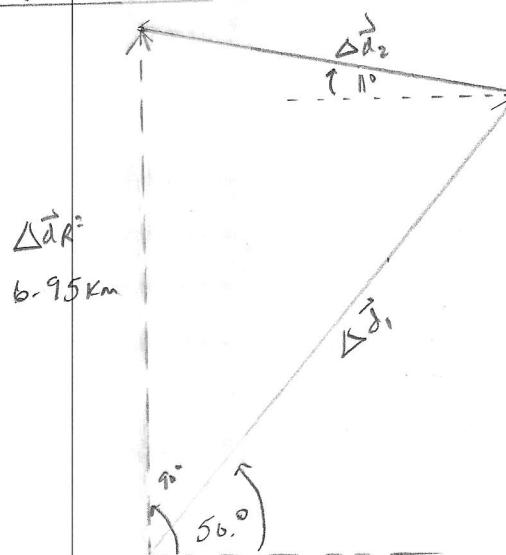
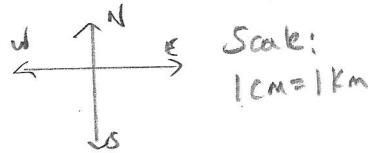
or  $\approx 1.0 \times 10^2 \text{ km [N } 47^\circ \text{ E]} \quad (\text{to 2 sig digits})$

$$1. \Delta \vec{d}_1 = 7.81 \text{ km} [E 50^\circ N]$$

$$\Delta \vec{d}_2 = 5.10 \text{ km} [W 11^\circ N]$$

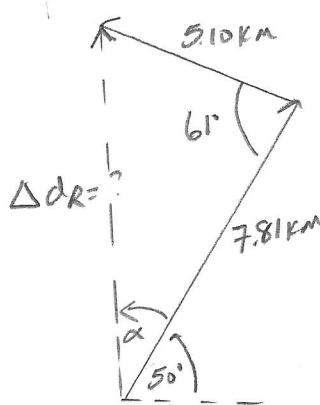
$$\Delta \vec{d}_R = ?$$

analysis:  $\Delta \vec{d}_R = \Delta \vec{d}_1 + \Delta \vec{d}_2$



$$\therefore \Delta \vec{d}_R = 6.95 \text{ km} [N]$$

b)



$$\begin{aligned} \Delta d_R &= \sqrt{7.81^2 + 5.10^2 - 2(7.81)(5.10) \cos 61^\circ} \\ &= 6.96 \text{ km} \end{aligned}$$

$$\frac{\sin \alpha}{5.10} = \frac{\sin 61^\circ}{6.96}$$

$$\therefore \alpha = \sin^{-1} \left( \frac{(5.10)(\sin 61^\circ)}{(6.96)} \right) = 39.89^\circ \approx 39.9^\circ$$

$$\therefore \Delta \vec{d}_R = 6.96 \text{ km} [E 89.9^\circ N] \approx 6.96 \text{ km} [N]$$

$$c) \% \text{ diff} = \frac{|\text{calc 1} - \text{calc 2}|}{\left( \frac{\text{calc 1} + \text{calc 2}}{2} \right)} \times 100\% =$$

$$\times 100\% = \frac{|6.95 - 6.96|}{\left( \frac{6.95 + 6.96}{2} \right)} \times 100\% = 0.14\%$$

The two methods agree to within 0.14%. This is excellent agreement; the two values are the same within reasonable measurement error.

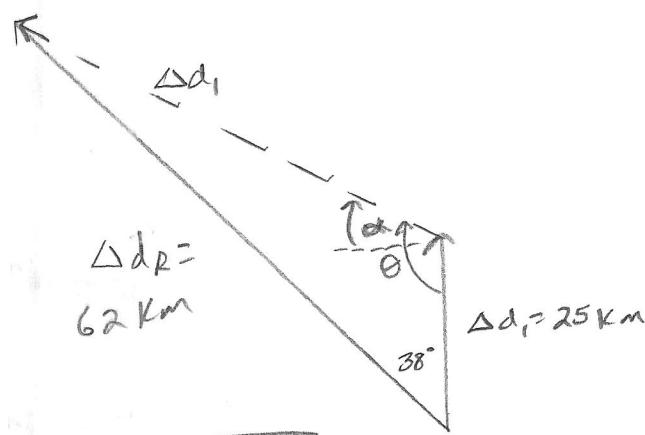
16]

$$\Delta \vec{d}_1 = 25 \text{ km [N]}$$

$$\Delta \vec{d}_R = 62 \text{ km [N} 38^\circ \text{W}]$$

$$\Delta \vec{d}_2 = ?$$

analysis:  $\Delta \vec{d}_2 = \Delta \vec{d}_R - \Delta \vec{d}_1$



$$\Delta d_1 = \sqrt{25^2 + 62^2 - 2(62)(25)\cos 38^\circ}$$

$$= 45.0 \text{ km}$$

$$\frac{\sin \theta}{62} = \frac{\sin 38}{45.0} \rightarrow \theta = \sin^{-1} \left( \frac{62 \sin 38}{45.0} \right) = 57.99^\circ$$

$$\text{But } \theta \text{ is obtuse, so } \theta = 180^\circ - 57.99^\circ$$

$$= 122.0^\circ$$

Find angle  $\alpha$  from west direction

$$\therefore \alpha = 122.0^\circ - 90^\circ = 32.0^\circ$$

$$\boxed{\Delta \vec{d}_1 = 45 \text{ km [W} 32^\circ \text{N]}}$$