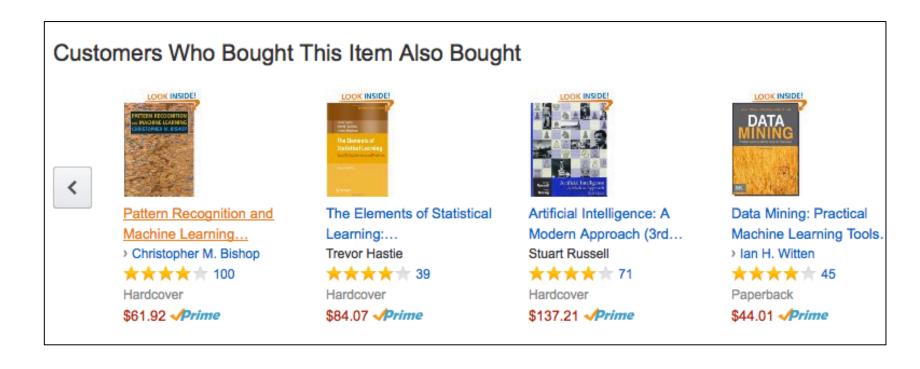
# Collaborative Filtering

EECS 349 Machine Learning
Recitation
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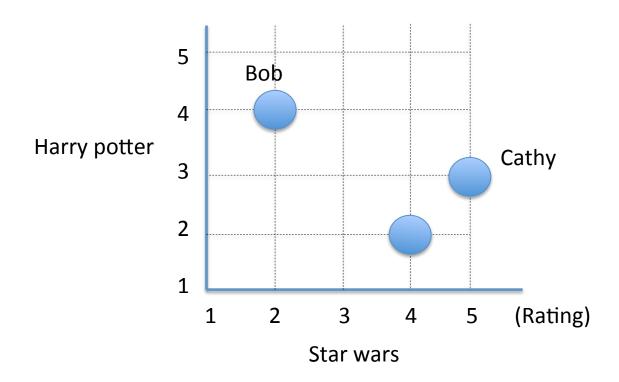
# Collaborative Filtering

- Recommendation system
  - Search for a user that is similar to you
  - You might like the item the user likes.



### How do we find a user who is similar?

- Distance (or similarity) measure
  - N-dimensional space



# Which similarity measure to use?

- p-norm
  - Manhattan
  - Euclidian
- Pearson Correlation
- Cosine Similarity

### Who is the most similar to John?

#### Example #1

	Inception	Begin again	Once
Brian	5	2	2
Bob	1	4	4
Cathy	2	3	3
John	5	1	2

#### - Manhattan Distance:

(John, Brian) = 
$$0 + 1 + 0 = 1$$
  
(John, Bob) =  $4 + 3 + 2 = 9$   
(John, Cathy) =  $3 + 2 + 1 = 6$ 

Q: Does Manhattan Distance measure similarities properly in this data set?

### Who is the most similar to Adam?

#### Example #2

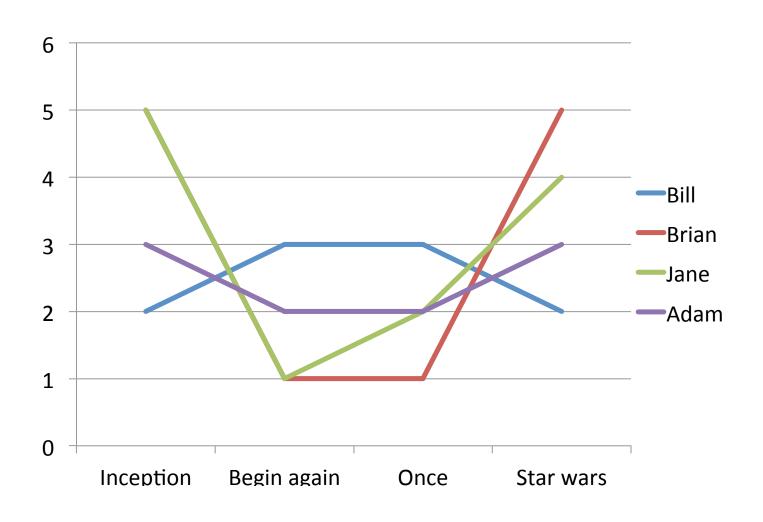
	Inception	Begin again	Once	Star wars
Bill	2	3	3	2
Brian	5	1	1	5
Jane	5	1	2	4
Adam	3	2	2	3

- Manhattan Distance:

Q: Does Manhattan Distance measure similarities properly in this data set?

Different users may use different rating scales

### Let's see correlations between users



### **Pearson Correlation**

- Measure of correlation between two variables
- Pearson correlation coefficient
  - Range (-1, 1)
  - 1 indicates perfect correlation.

$$sim(\mathbf{u}, \mathbf{v}) = \frac{\sum_{i \in C} (r_{\mathbf{u},i} - \bar{r}_{\mathbf{u}})(r_{\mathbf{v},i} - \bar{r}_{\mathbf{v}})}{\sqrt{\sum_{i \in C} (r_{\mathbf{u},i} - \bar{r}_{\mathbf{u}})^2} \sqrt{\sum_{i \in C} (r_{\mathbf{v},i} - \bar{r}_{\mathbf{v}})^2}},$$

- >> import scipy.stats
- >> scipy.stats.pearsonr(array1, array2)

### Who is the most similar to Adam?

#### Example #2

	Inception	Begin again	Once	Star wars
Bill	2	3	3	2
Brian	5	1	1	5
Jane	5	1	2	4
Adam	3	2	2	3

- Pearson Correlation:

Q: Does Pearson Correlation measure similarities properly in this data set?

# How to predict ratings to unrated items

- K- Nearest Neighbor Collaborative Filtering
  - Pick k users that had similar preferences to those of current user
  - Factors the relative proximity of k nearest neighbors
  - You need to do experiments to find optimal k value.

# Let's practice k-NN CF (k=1)

#### Example #1

	Inception	Begin again	Once	Star wars
Brian	5	2	2	4
Bob	1	4	4	2
Cathy	2	3	3	1
John	5	1	2	?

#### Manhattan Distance:

(John, Brian) = 0 + 1 + 0 = 1(John, Bob) = 4 + 3 + 2 = 9(John, Cathy) = 3 + 2 + 1 = 6

# Let's practice k-NN CF (k=1)

#### Example #2

	Inception	Begin again	Once	Star wars	Avatar
Brian	2	3	3	2	4
Bob	5	1	1	5	2
Cathy	5	1	2	4	1
John	3	2	2	3	?

Manhattan Distance:

$$(John, Brian) = 1 + 1 + 1 + 1 = 4$$
  
 $(John, Bob) = 2 + 1 + 1 + 2 = 6$ 

$$(John, Cathy) = 1 + 1 + 1 + 1 = 4$$

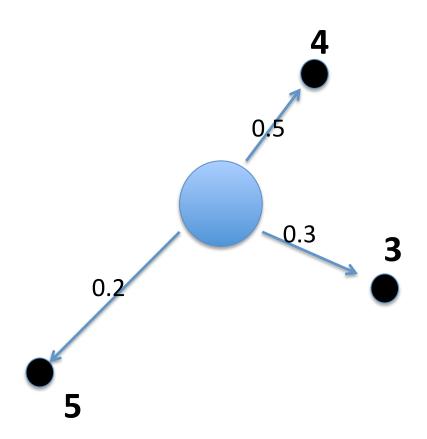
**Pearson Correlation Coefficient** 

$$(John, Brian) = -1$$

$$(John, Bob) = 1$$

$$(John, Cathy) = 0.94$$

## When $K \ge 2$



### Item-based CF

#### Example #1

	Inception	Begin again	Once
Brian	5	2	2
Bob	1	4	4
Cathy	2	3	3
John	5	1	2

#### - Manhattan Distance:

(Once, Inception) = 3 + 3 + 1 + 3 = 10(Once, Begin again) = 0+0+0+1=1

# Let's practice k-NN CF (k=1)

#### Example #1

	Inception	Begin again	Once	Star wars
Brian	5	2	2	4
Bob	1	4	4	2
Cathy	2	3	3	1
John	5	1	2	?

#### Manhattan Distance:

```
(Star wars, Inception) = 1 + 1 + 1 = 3
(Star wars, Begin again) = 1 + 2 + 2 = 5
(Star wars, Once) = 2+2+2=6
```

# Dealing with missing values

Example #2

	Inception	Begin again	Once	Star wars	Avatar
Brian	2	?	3	?	4
Bob	5	1	1	5	2
Cathy	5	?	2	2	1
John	5	?	2	3	?

# Dealing with missing values

Example #2

•	Inception	Begin again	Once	Star wars	Avatar
Brian	2	0	3	0	4
Bob	5	1	1	5	2
Cathy	5	0	2	2	1
John	5	0	2	3	?

### Make a decision

- Which distance measure to use?
- How many neighbors to pick?
- How to weight neighbors chosen?
- User-based or item-based?
- How to deal with missing values?
  - Discard data related to unrated items?
  - Fill Zero or average value?
  - Other advanced imputation technique?