

3

Find the minimum of $J(x) = (2x-3)^2$, $(2, 1) = (x, J(x))$

When slope of $J(x) = (2x-3)^2 = 0$ is when the function is minimized

$$\frac{d}{dx} = (2x-3)^2 \rightarrow \text{Chain rule}$$

$$\frac{d}{dx} = 2(2x-3) \cdot 2$$

$$\frac{d}{dx} = 4(2x-3)$$

$$0 = 4(2x-3)$$

$$0 = 2x-3$$

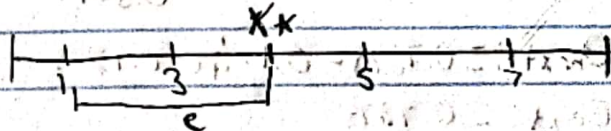
$$3 = 2x$$

$$1.5 = x$$

4A

Find AVG of $[1, 3, 5, 7] = [x_1, x_2, x_3, x_4]$

$$e = (x_i - x_*)^2$$



$$J = (x_1 - x_*)^2 + (x_2 - x_*)^2 + (x_3 - x_*)^2 + (x_4 - x_*)^2$$

$$\frac{dJ}{dx_*} = 2(x_1 - x_*) \cdot -1 + 2(x_2 - x_*) \cdot -1 + 2(x_3 - x_*) \cdot -1 + 2(x_4 - x_*) \cdot -1$$

$$0 = -2(x_1 - x_*) + (x_2 - x_*) + (x_3 - x_*) + (x_4 - x_*)$$

$$0 = x_1 + x_2 + x_3 + x_4 - 4x_*$$

$$4x_* = x_1 + x_2 + x_3 + x_4 \Rightarrow x_* = \frac{x_1 + x_2 + x_3 + x_4}{4} = \text{mean} = \frac{1+3+5+7}{4}$$

4

 $x_* = 4$

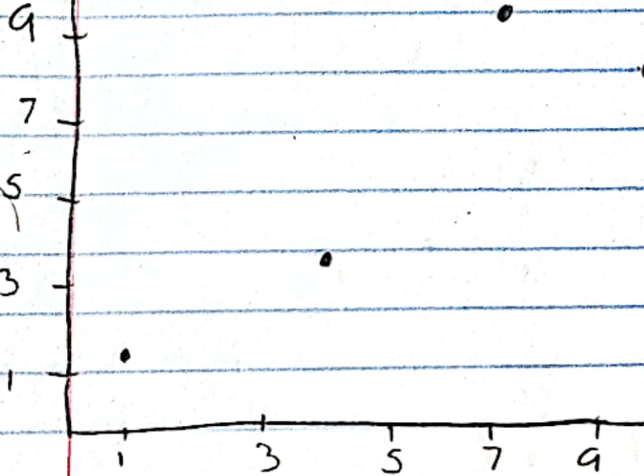
Mean = 4

4B

$$(X, y) = (1, 1.5), (4, 3.5), (7, 9), (10, 8)$$

hypothesis $h_\theta(X) = \theta X$

$$\theta_{next} := \theta_{current} - \alpha \cdot \left(\frac{1}{n} \sum x_i (\theta_{current} x_i - y_i) \right)$$



$$\theta = 1 \quad \alpha = 0.01$$

$$-0.5$$

$$-2$$

$$-1.4$$

$$-2.0$$

$$1) \theta_{next} := \theta_{current} - \alpha \cdot \left(\frac{1}{4} ((1.5-1.5) \cdot 1) + ((3.5-4.5) \cdot 4) + ((9-7) \cdot 7) + ((8-10) \cdot 10) \right)$$

$$\theta_{next} := 1 - 0.01 \cdot 1.975$$

$$\theta_{next} = 0.98125$$

$$2) \theta_{next} := 0.98125 - 0.01 \cdot 1.097$$

$$\theta_{next} = 0.9703$$

$$3) \theta_{next} := 0.9703 - 0.01 \cdot 0.6416$$

$$\theta_{next} = 0.9639$$

Repeat until $\frac{d}{dx} \approx 0$



$$\theta = 0.955$$

Problem 2 Linear regression notebook

In [1]:

```
from sklearn.linear_model import LinearRegression
from sklearn.model_selection import train_test_split
from sklearn.preprocessing import StandardScaler
from sklearn.metrics import mean_squared_error, r2_score
import matplotlib.pyplot as plt
import pandas as pd
import numpy as np
%matplotlib inline

np.random.seed(123)

df = pd.read_csv("MizzouGameData.csv")

df

X = df[['3FGPCT']]

y = df['PTS'] # target is what we are trying to predict

X_train, X_test, y_train, y_test = train_test_split(X, y, test_size = 0.20) #

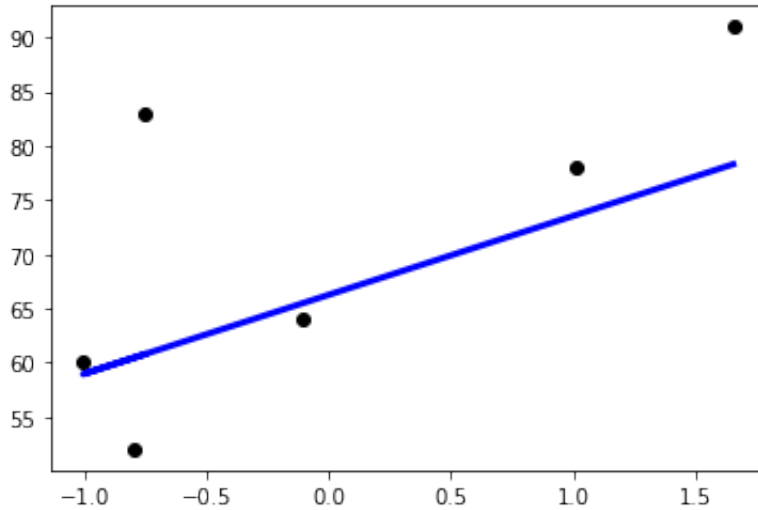
scaler = StandardScaler()
X_train = scaler.fit_transform(X_train)
X_test = scaler.fit_transform(X_test)

regression = LinearRegression().fit(X_train, y_train) # train model
y_pred = regression.predict(X_test)

# The coefficients
print("Coefficients: \n", regression.coef_)
# The mean squared error
print("Mean squared error: %.2f" % mean_squared_error(y_test, y_pred))
# The coefficient of determination: 1 is perfect prediction
print("Coefficient of determination: %.2f" % r2_score(y_test, y_pred))

plt.scatter(X_test, y_test, color="black")
plt.plot(X_test, y_pred, color="blue", linewidth=3)
plt.show()
```

```
Coefficients:  
[7.28544392]  
Mean squared error: 124.95  
Coefficient of determination: 0.33
```



Fit of model is not great but we are only using one feature so that is kinda expected

In []:

Problem 3

In [1]:

```

import numpy as np
import matplotlib.pyplot as plt
%matplotlib inline

# Function is  $y = (2x-3)^2$ 
X = np.arange(-2, 5.5, 0.5)
x_star_guess = np.arange(-2.5, 5.5, 0.5)
Y = []
e = []
J = []

#generate data for to do gradient descent on
for i in range(len(X)):
    y = (2*X[i]-3)**2
    Y.append(y)

def error_function(x, x_star):
    error = (x-x_star)**2
    return error

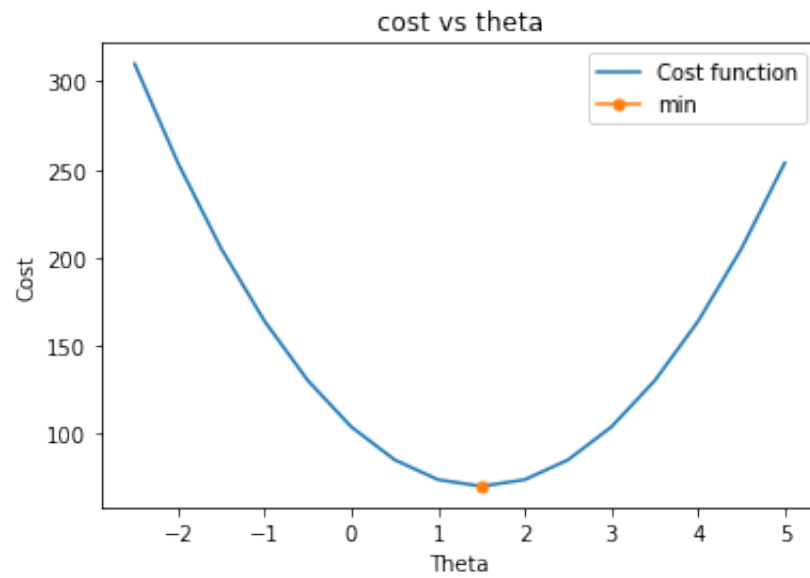
for i in range(len(x_star_guess)):
    x_star_error = []
    for j in range(len(X)):
        x_star_error.append(error_function(X[j], x_star_guess[i]))
    cost = sum(x_star_error)
    J.append(cost)

min_index = (np.where(J == min(J)))
min_J = min(J)
min_x_star = x_star_guess[min_index]

plt.xlabel("Theta")
plt.ylabel("Cost")
plt.title("cost vs theta")
plt.plot(x_star_guess, J, label='Cost function')
plt.plot(min_x_star, min_J, marker="o", markersize=5, label='min')
plt.legend()
print("The min cost of the function  $2x-3^2$  is found at theta", min_x_star)

```

The min cost of the function $2x-3^2$ is found at theta [1.5]



Problem 4a

In [2]:

```

nums = [1, 3, 5, 7]
x_star_guess = np.arange(-10, 20, 1)
e = []
J = []

def error_function(x, x_star):
    error = (x-x_star)**2
    return error

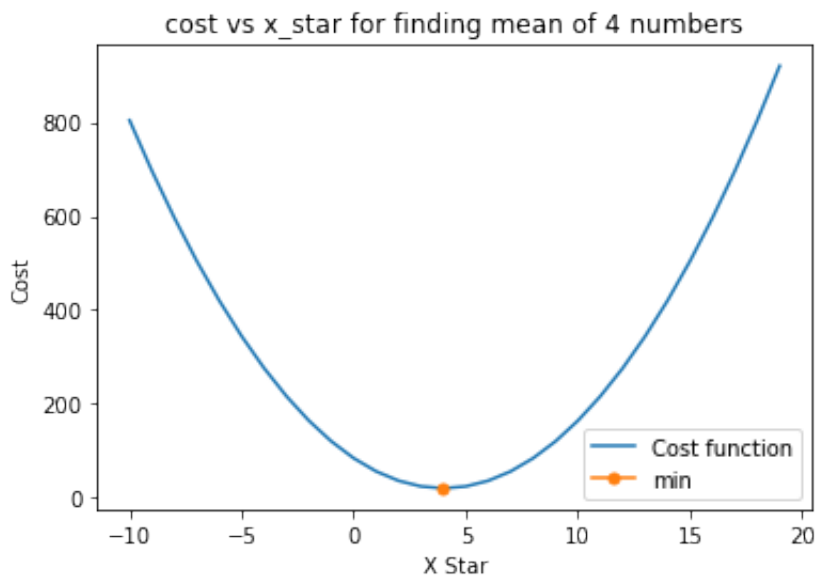
for i in range(len(x_star_guess)):
    x_star_error = []
    for j in range(len(nums)):
        x_star_error.append(error_function(nums[j], x_star_guess[i]))
    cost = sum(x_star_error)
    J.append(cost)

min_index = (np.where(J == min(J)))
min_J = min(J)
min_x_star = x_star_guess[min_index]

plt.xlabel("X Star")
plt.ylabel("Cost")
plt.title("cost vs x_star for finding mean of 4 numbers")
plt.plot(x_star_guess,J,label='Cost function')
plt.plot(min_x_star, min_J , marker="o", markersize=5, label='min')
plt.legend()
plt.show()

print("The min aka the mean is %d" %min_x_star)

```



The min aka the mean is 4

Problem 4b

In [3]:

```
from mpl_toolkits import mplot3d

X = np.array([1, 4, 7, 10])

Y = np.array([1.5, 3.5, 9, 8])

m = 1
c = 0

M = []
C = []
J = []

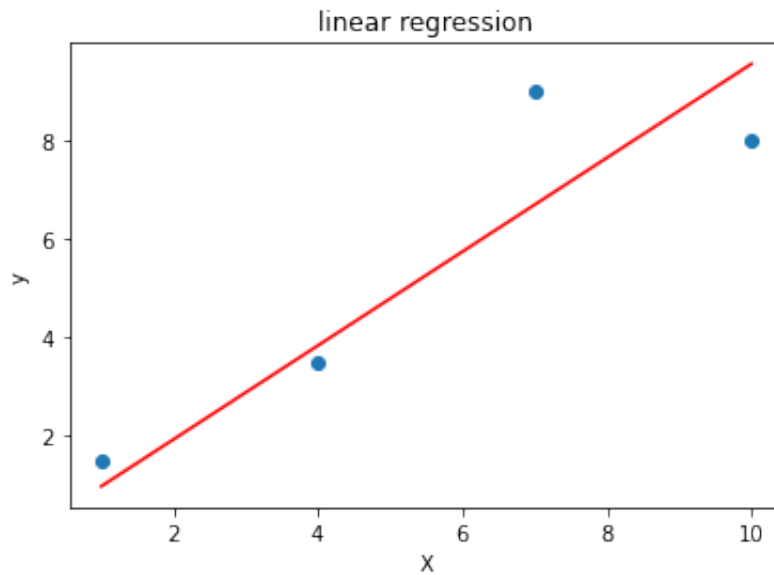
L = 0.0001 # The learning Rate
epochs = 1000 # The number of iterations to perform gradient descent

n = float(len(X)) # Number of elements in X

def cost_fun(y,y_hat,x):
    J = ((y-y_hat)*x)
    return J

# Performing Gradient Descent
for i in range(epochs):
    Y_pred = m*X + c # The current predicted value of Y
    D_m = (-1/n) * sum(X * (Y - Y_pred)) # Derivative wrt m
    D_c = (-1/n) * sum(Y - Y_pred) # Derivative wrt c
    m = m - L * D_m # Update m
    c = c - L * D_c # Update c
    M.append(m)
    C.append(c)
    total_cost = cost_fun(Y,Y_pred,X)
    total_cost = sum(total_cost)
    J.append(total_cost)

Y_pred = m*X + c
#print (m, c)
plt.scatter(X, Y)
plt.plot([min(X), max(X)], [min(Y_pred), max(Y_pred)], color='red') # regres
plt.xlabel('X')
plt.ylabel('Y')
plt.title('linear regression')
plt.show()
print("slope equals", m)
print("bias equals", c)
```

slope equals 0.9537790462397807
bias equals 0.01851484803581841

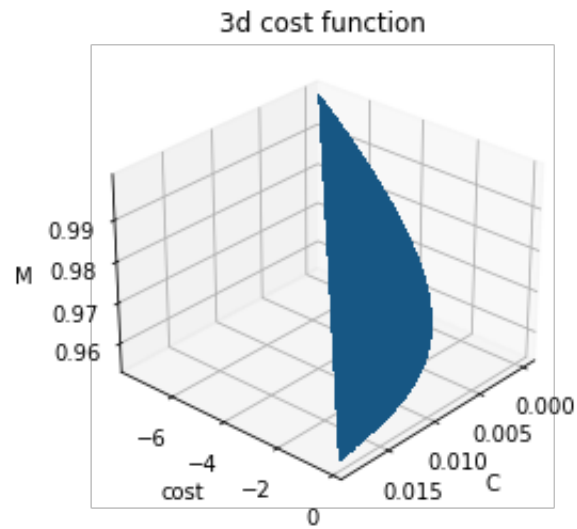
In [4]:

```
%matplotlib notebook

ax = plt.axes(projection='3d')

print("J is minimized when m is {} and when c is {}".format(m,c))

surf = ax.plot_trisurf(C, J, M, linewidth=0, antialiased=False)
ax.set_xlabel('C', fontsize=10)
ax.set_ylabel('cost', fontsize=10)
ax.set_zlabel('M', fontsize=10)
ax.set_title("3d cost function")
```



J is minimized when m is 0.9537790462397807 and when c is 0.01851484803581841

Out[4]: Text(0.5, 0.92, '3d cost function')

In []:

In []:

In []: