

Conceptual metaphor and graphical convention influence the interpretation of line graphs

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09/04/2019

Contents

Main analyses	1
Data wrangling	1
Analyses	12
Descriptive stats	12
Inferential stats	14
Exploratory analysis	24
Reviewer-requested additional analysis	25
Educational background	25
Speed-accuracy trade-off	35

Main analyses

This is the code used for the analysis reported in Experiment 1 of ‘Conceptual metaphor and graphical convention influence the interpretation of line graphs’.

Data wrangling

Load packages:

```
library(plyr)           # Data processing
library(tidyverse)      # Data processing
library(brms)           # Bayesian mixed models
library(ggmcnc)         # Data visualisation
library(tidybayes)      # Data visualisation
```

Get citation information for R and for the packages we use:

```
# R:
R.Version()

## $platform
## [1] "x86_64-apple-darwin17.0"
##
## $arch
## [1] "x86_64"
##
## $os
## [1] "darwin17.0"
##
```

```

## $system
## [1] "x86_64, darwin17.0"
##
## $status
## [1] ""
##
## $major
## [1] "4"
##
## $minor
## [1] "0.3"
##
## $year
## [1] "2020"
##
## $month
## [1] "10"
##
## $day
## [1] "10"
##
## $`svn rev`
## [1] "79318"
##
## $language
## [1] "R"
##
## $version.string
## [1] "R version 4.0.3 (2020-10-10)"
##
## $nickname
## [1] "Bunny-Wunnies Freak Out"

```

```

citation()

```

```

##
## To cite R in publications use:
##
##   R Core Team (2020). R: A language and environment for statistical
##   computing. R Foundation for Statistical Computing, Vienna, Austria.
##   URL https://www.R-project.org/.
##
## A BibTeX entry for LaTeX users is
##
##   @Manual{,
##     title = {R: A Language and Environment for Statistical Computing},
##     author = {{R Core Team}},
##     organization = {R Foundation for Statistical Computing},
##     address = {Vienna, Austria},
##     year = {2020},
##     url = {https://www.R-project.org/},
##   }
##
## We have invested a lot of time and effort in creating R, please cite it
## when using it for data analysis. See also 'citation("pkgname")' for

```

```
## citing R packages.
```

```
# RStudio:  
#RStudio.Version()
```

```
# plyr:  
citation('plyr')
```

```
##
```

```
## To cite plyr in publications use:
```

```
##
```

```
## Hadley Wickham (2011). The Split-Apply-Combine Strategy for Data  
## Analysis. Journal of Statistical Software, 40(1), 1-29. URL
```

```
## http://www.jstatsoft.org/v40/i01/.
```

```
##
```

```
## A BibTeX entry for LaTeX users is
```

```
##
```

```
## @Article{,  
##   title = {The Split-Apply-Combine Strategy for Data Analysis},  
##   author = {Hadley Wickham},  
##   journal = {Journal of Statistical Software},  
##   year = {2011},  
##   volume = {40},  
##   number = {1},  
##   pages = {1--29},  
##   url = {http://www.jstatsoft.org/v40/i01/},  
## }
```

```
packageVersion('plyr')
```

```
## [1] '1.8.6'
```

```
# tidyverse:  
citation('tidyverse')
```

```
##
```

```
## Wickham et al., (2019). Welcome to the tidyverse. Journal of Open  
## Source Software, 4(43), 1686, https://doi.org/10.21105/joss.01686
```

```
##
```

```
## A BibTeX entry for LaTeX users is
```

```
##
```

```
## @Article{,  
##   title = {Welcome to the {tidyverse}},  
##   author = {Hadley Wickham and Mara Averick and Jennifer Bryan and Winston Chang and Lucy D'Agostini  
##   year = {2019},  
##   journal = {Journal of Open Source Software},  
##   volume = {4},  
##   number = {43},  
##   pages = {1686},  
##   doi = {10.21105/joss.01686},  
## }
```

```
packageVersion('tidyverse')
```

```
## [1] '1.3.0'
```

```

# brms:
citation('brms')

##
## To cite brms in publications use:
##
## Paul-Christian Bürkner (2017). brms: An R Package for Bayesian
## Multilevel Models Using Stan. Journal of Statistical Software, 80(1),
## 1-28. doi:10.18637/jss.v080.i01
##
## Paul-Christian Bürkner (2018). Advanced Bayesian Multilevel Modeling
## with the R Package brms. The R Journal, 10(1), 395-411.
## doi:10.32614/RJ-2018-017
##
## To see these entries in BibTeX format, use 'print(<citation>,
## bibtex=TRUE)', 'toBibtex(.)', or set
## 'options(citation.bibtex.max=999)'.
toBibtex(citation('brms'))

## @Article{,
##   title = {{brms}: An {R} Package for {Bayesian} Multilevel Models Using {Stan}},
##   author = {Paul-Christian Bürkner},
##   journal = {Journal of Statistical Software},
##   year = {2017},
##   volume = {80},
##   number = {1},
##   pages = {1--28},
##   doi = {10.18637/jss.v080.i01},
##   encoding = {UTF-8},
## }
##
## @Article{,
##   title = {Advanced {Bayesian} Multilevel Modeling with the {R} Package {brms}},
##   author = {Paul-Christian Bürkner},
##   journal = {The R Journal},
##   year = {2018},
##   volume = {10},
##   number = {1},
##   pages = {395--411},
##   doi = {10.32614/RJ-2018-017},
##   encoding = {UTF-8},
## }
packageVersion('brms')

## [1] '2.14.4'

# ggpubr:
citation('ggpubr')

##
## To cite package 'ggpubr' in publications use:
##
## Alboukadel Kassambara (2020). ggpubr: 'ggplot2' Based Publication
## Ready Plots. R package version 0.4.0.

```

```

## https://CRAN.R-project.org/package=ggpubr
##
## A BibTeX entry for LaTeX users is
##
## @Manual{,
##   title = {ggpubr: 'ggplot2' Based Publication Ready Plots},
##   author = {Alboukadel Kassambara},
##   year = {2020},
##   note = {R package version 0.4.0},
##   url = {https://CRAN.R-project.org/package=ggpubr},
## }

packageVersion('ggpubr')

## [1] '0.4.0'

# ggcmc:
citation('ggcmc')

##
## To cite ggcmc in publications use:
##
## Xavier Fernández i Marín (2016). ggcmc: Analysis of MCMC Samples and
## Bayesian Inference. Journal of Statistical Software, 70(9), 1-20.
## doi:10.18637/jss.v070.i09
##
## A BibTeX entry for LaTeX users is
##
## @Article{,
##   title = {{ggcmc}: Analysis of {MCMC} Samples and {B}ayesian Inference},
##   author = {Xavier Fern{\a}ndez-i-Mar{\i}n},
##   journal = {Journal of Statistical Software},
##   year = {2016},
##   volume = {70},
##   number = {9},
##   pages = {1--20},
##   doi = {10.18637/jss.v070.i09},
## }

packageVersion('ggcmc')

## [1] '1.5.0'

# tidybayes:
citation('tidybayes')

##
## Kay M (2020). _tidybayes: Tidy Data and Geoms for Bayesian Models_.
## doi: 10.5281/zenodo.1308151 (URL:
## https://doi.org/10.5281/zenodo.1308151), R package version 2.3.1, <URL:
## http://mjskay.github.io/tidybayes/>.
##
## A BibTeX entry for LaTeX users is
##
## @Manual{,
##   title = {{tidybayes}: Tidy Data and Geoms for {Bayesian} Models},
##   author = {Matthew Kay},

```

```
##   year = {2020},
##   note = {R package version 2.3.1},
##   url  = {http://mjskay.github.io/tidybayes/},
##   doi  = {10.5281/zenodo.1308151},
## }
```

```
packageVersion('tidybayes')
```

```
## [1] '2.3.1'
```

Load datasets and give them shorter names for easier coding:

```
df1 <- read_csv('../data/data_viz_1.csv')
df2 <- read_csv('../data/data_viz_2.csv')
df3 <- read_csv('../data/data_viz_3.csv')
df4 <- read_csv('../data/data_viz_4.csv')
df5 <- read_csv('../data/data_viz_5.csv')
df6 <- read_csv('../data/data_viz_6.csv')
```

Disable scientific notation:

```
options("scipen" = 999)
```

Create new column in each dataset denoting experiment version:

```
df1$Version <- 1
df2$Version <- 2
df3$Version <- 3
df4$Version <- 4
df5$Version <- 5
df6$Version <- 6
```

Join data sets together:

```
df <- rbind.fill(df1, df2, df3, df4, df5, df6)
```

We noticed that some trials had response latencies of 0. Check how many response latencies of 0 there were per trial:

```
table(df$V1_FirstClick == 0)
```

```
##
## FALSE  TRUE
##   203    97
```

```
table(df$V2_FirstClick == 0)
```

```
##
## FALSE  TRUE
##   296     4
```

```
table(df$V3_FirstClick == 0)
```

```
##
## FALSE  TRUE
##   298     2
```

```
table(df$V4_FirstClick == 0)
```

```
##
## FALSE  TRUE
```

```
## 296 4
```

These zero response latencies seem to be mostly in the first trial, with some malfunctions in the other trials that can maybe be put down to software errors. Look to see if this error seems to disproportionately affect specific versions of the experiment:

```
table(df$V1_FirstClick == 0, df$Version)
```

```
##
##      1  2  3  4  5  6
## FALSE 48 49 48 50  4  4
##  TRUE  2  1  2  0 47 45
```

It seems to affect the 5th and 6th versions of the experiment mostly. See if it has anything to do with participants not answering the practice question:

```
df2 <- filter(df, is.na(Instructions))
table(df2$V1_FirstClick == 0, df2$Version)
```

```
##
##      1  2  3  4  5  6
## FALSE 1  1  2  6  2  2
##  TRUE  0  0  0  0  5  1
```

It doesn't seem to be anything to do with the practice question - there weren't actually many respondents that didn't answer the practice question. This is strange but there seems to have been a problem with the 5th and 6th versions of the experiment. We'll exclude these later.

Create Accuracy columns denoting whether participant got answer right to each question:

```
df <- mutate(df, V1_a = ifelse(V1_r %in% 'Improving', 'right', 'wrong')) # First question
df <- mutate(df, V2_a = ifelse(V2_r %in% 'Declining', 'right', 'wrong')) # Second question
df <- mutate(df, V3_a = ifelse(V3_r %in% 'Declining', 'right', 'wrong')) # Third question
df <- mutate(df, V4_a = ifelse(V4_r %in% 'Improving', 'right', 'wrong')) # Fourth question
```

Exclude participants who got the trick question incorrect. Also, calculate how many participants remain after this exclusion, and how many participants were excluded:

```
# Original number of participants:
(old_len <- length(df$Subject))
```

```
## [1] 300
```

```
# Original number of participants remaining in each condition:
aggregate(cbind(count = Subject) ~ Version,
          data = df,
          length)
```

```
## Version count
## 1      1     50
## 2      2     50
## 3      3     50
## 4      4     50
## 5      5     51
## 6      6     49
```

```
# Exclude participants who got trick question wrong:
df <- filter(df, Trick == 'quickly')
```

```
# Number of participants remaining:
```

```
(new_len <- length(df$Subject))
```

```
## [1] 293
```

```
# Number of participants excluded:  
old_len - new_len
```

```
## [1] 7
```

Exclude rows with response latencies more than 2 standard deviations above mean. Also, calculate how many participants remain after this exclusion, and how many participants were excluded:

```
# Preliminaries:
```

```
cols <- c(df$V1_FirstClick, df$V2_FirstClick, df$V3_FirstClick, df$V4_FirstClick) # Combine values of
```

```
cols <- as.numeric(cols) # Make numeric
```

```
up_lim <- (mean(cols) + (sd(cols) * 2)) # Upper limit
```

```
# Exclude:
```

```
# First column:
```

```
df$V1_FirstClick <- as.numeric(df$V1_FirstClick) # Make numeric
```

```
df <- filter(df, V1_FirstClick < up_lim) # Filter
```

```
# Second column:
```

```
df$V2_FirstClick <- as.numeric(df$V2_FirstClick) # Make numeric
```

```
df <- filter(df, V2_FirstClick < up_lim) # Filter
```

```
# Third column:
```

```
df$V3_FirstClick <- as.numeric(df$V3_FirstClick) # Make numeric
```

```
df <- filter(df, V3_FirstClick < up_lim) # Filter
```

```
# Fourth column:
```

```
df$V4_FirstClick <- as.numeric(df$V4_FirstClick) # Make numeric
```

```
df <- filter(df, V4_FirstClick < up_lim) # Filter
```

```
# Number of participants after exclusion:
```

```
newer_len <- (length(df$Subject))
```

```
# Number of participants excluded
```

```
new_len - newer_len
```

```
## [1] 3
```

```
# 2 SDs above mean:
```

```
round(up_lim, 1)
```

```
## [1] 55.9
```

Find out info about participants:

```
# Age
```

```
df$Age <- as.numeric(df$Age) # Make numeric
```

```
range(df$Age) # Range
```

```
## [1] 24 72
```

```
round(mean(df$Age), 0) # Mean
```

```
## [1] 39
```



```
round(sd(df$Age), 0)    # Mean
```

```
## [1] 11
```

```
# Gender
```

```
(xtab <- table(df$Gender))    # Raw stats
```

```
##
```

```
##           Female           Male Non-binary/third gender
##           130           159           1
```

```
round(prop.table(xtab), 3) * 100    # Proportions (in order)
```

```
##
```

```
##           Female           Male Non-binary/third gender
##           44.8           54.8           0.3
```

```
# Number of participants remaining in each condition:
```

```
(pps <- aggregate(cbind(count = Subject) ~ Version,
  data = df,
  length))
```

```
##   Version count
```

```
## 1      1    48
## 2      2    50
## 3      3    48
## 4      4    49
## 5      5    48
## 6      6    47
```

```
# Proportions
```

```
(pps$count <- round(prop.table(pps$count), 3) * 100)
```

```
## [1] 16.6 17.2 16.6 16.9 16.6 16.2
```

Remove extraneous columns:

```
# Columns:
```

```
df <- select(df, Subject, V1_r, V1_RT = V1_FirstClick, V2_r, V2_RT = V2_FirstClick, V3_r, V3_RT = V3_Fi
```

Create AxisInversion column:

```
# Create column in df:
```

```
df <- mutate(df, AxisInversion = ifelse(df$Version %in% c(1, 2), 'normal', 'inverted'))
```

```
# Check to see if it's worked:
```

```
sample_n(df, 10) %>%
  select(Version, AxisInversion)
```

```
##   Version AxisInversion
```

```
## 1      6    inverted
## 2      3    inverted
## 3      4    inverted
## 4      6    inverted
## 5      1     normal
## 6      3    inverted
## 7      2     normal
## 8      1     normal
## 9      5    inverted
```

```
## 10      4      inverted
```

Create Orientation column:

```
# Create column in df:
df <- mutate(df, Orientation = ifelse(Version %in% c('1', '3', '5'), 'quant_y', 'quant_x'))
# Check to see if it's worked:
sample_n(df, 10) %>%
  select(Version, Orientation)
```

```
##      Version Orientation
## 1         5      quant_y
## 2         5      quant_y
## 3         4      quant_x
## 4         5      quant_y
## 5         2      quant_x
## 6         1      quant_y
## 7         3      quant_y
## 8         2      quant_x
## 9         6      quant_x
## 10        5      quant_y
```

Make data long and make valence column:

```
# Make long format:
df <- gather(df, Response, Measurement, c('V1_r', 'V2_r', 'V3_r', 'V4_r', 'V1_RT', 'V2_RT', 'V3_RT',
                                           'V4_RT'))

# Order data frame by subject column:
df <- arrange(df, Subject)

# Create column:
df <- mutate(df, Valence = ifelse(Response %in% c('V1_r', 'V2_r'), 'positive', 'negative'))

# Check to see if it's worked:
df %>% select(Subject, Response, Measurement, Valence) %>% head()
```

```
##      Subject Response Measurement  Valence
## 1         1      V1_r    Improving positive
## 2         1      V2_r    Declining positive
## 3         1      V3_r    Declining negative
## 4         1      V4_r    Improving negative
## 5         1     V1_RT          1.43 negative
## 6         1     V2_RT          1.753 negative
```

Make column for whether 'quant_y' graphs aligned with vertical valence metaphors:

```
# Create column and fill in each row as NA by default:
df$Val_Al <- NA

# Code whether graph did or did not align with valence metaphors for quant-y graphs:
df <-
  mutate(df, Val_Al = case_when(
    Version == 1 & Valence == 'positive' ~ 'yes',
    Version == 3 & Valence == 'negative' ~ 'yes',
    Version == 5 & Valence == 'positive' ~ 'yes',
    Version == 1 & Valence == 'negative' ~ 'no',
    Version == 3 & Valence == 'positive' ~ 'no',
    Version == 5 & Valence == 'negative' ~ 'no'))
```

```
# Check it's worked:
sample_n(df, 10) %>%
  select(Version, Valence, Val_Al)
```

```
##   Version  Valence Val_Al
## 1      4 negative  <NA>
## 2      6 negative  <NA>
## 3      1 negative   no
## 4      4 negative  <NA>
## 5      6 negative  <NA>
## 6      3 positive   no
## 7      6 negative  <NA>
## 8      3 negative   yes
## 9      2 negative  <NA>
## 10     5 positive   yes
```

Make Accuracy column:

```
df <-
  mutate(df, Accuracy = case_when(
    Response == 'V1_r' & Measurement == 'Declining' ~ 'wrong',
    Response == 'V2_r' & Measurement == 'Improving' ~ 'wrong',
    Response == 'V3_r' & Measurement == 'Improving' ~ 'wrong',
    Response == 'V4_r' & Measurement == 'Declining' ~ 'wrong',
    Response == 'V1_r' & Measurement == 'Improving' ~ 'right',
    Response == 'V2_r' & Measurement == 'Declining' ~ 'right',
    Response == 'V3_r' & Measurement == 'Declining' ~ 'right',
    Response == 'V4_r' & Measurement == 'Improving' ~ 'right',
    Response == 'V1_r' & Measurement == 'Neither declining or improving' ~ 'wrong',
    Response == 'V2_r' & Measurement == 'Neither declining or improving' ~ 'wrong',
    Response == 'V3_r' & Measurement == 'Neither declining or improving' ~ 'wrong',
    Response == 'V4_r' & Measurement == 'Neither declining or improving' ~ 'wrong'))

# Order data frame by subject column:
df <- arrange(df, Subject)

# Check to see if it's worked:
select(df, Subject, Response, Measurement, Accuracy) %>% head()
```

```
##   Subject Response Measurement Accuracy
## 1      1      V1_r    Improving    right
## 2      1      V2_r    Declining    right
## 3      1      V3_r    Declining    right
## 4      1      V4_r    Improving    right
## 5      1     V1_RT      1.43      <NA>
## 6      1     V2_RT      1.753      <NA>
```

Create column for x-inverted versus y-inverted graphs:

```
# Create column and fill in each row as NA by default:
df$InvertXY <- NA

# Code whether x-axis or y-axis was inverted
df <-
  mutate(df, InvertXY = case_when(
    Version == 3 ~ 'y',
```

```
Version == 4 ~ 'y',
Version == 5 ~ 'x',
Version == 6 ~ 'x'))
```

Create two separate datasets for looking at accuracy and response latency information respectively:

```
# Reduce to response latencies for use later in exploratory analysis:
df_RT <- df %>% filter(Response %in% c('V1_RT', 'V2_RT', 'V3_RT', 'V4_RT')) %>%
  mutate(Valence = case_when(
    Response == 'V1_RT' ~ 'positive',
    Response == 'V2_RT' ~ 'positive',
    Response == 'V3_RT' ~ 'negative',
    Response == 'V4_RT' ~ 'negative'
  ))

# Reduce to accuracy information for use now:
df <- df %>% filter(Response %in% c('V1_r', 'V2_r', 'V3_r', 'V4_r'))
```

Analyses

We now perform the main analyses of our study.

Descriptive stats

Look at Accuracy overall:

```
(xtab <- table(df$Accuracy))

##
## right wrong
## 736 424

round(prop.table(xtab), 3) * 100

##
## right wrong
## 63.4 36.6
```

Look at descriptive stats for Accuracy as a function of AxisInversion:

```
(xtab <- table(df$AxisInversion, df$Accuracy))

##
## right wrong
## inverted 431 337
## normal 305 87

round(prop.table(xtab, 1), 3) * 100

##
## right wrong
## inverted 56.1 43.9
## normal 77.8 22.2
```

People were more likely to get the answers to the questions right if the graph was normal and not inverted.

Look at descriptive stats for Accuracy as a function of Orientation:

```
(xtab <- table(df$Orientation, df$Accuracy))
```

```
##
##           right wrong
## quant_x   419   165
## quant_y   317   259
```

```
round(prop.table(xtab, 1), 3) * 100
```

```
##
##           right wrong
## quant_x   71.7  28.3
## quant_y   55.0  45.0
```

Contrary to our predictions, speakers were more likely to get the answer right if quantity was on the x-axis, and time on the y-axis.

Look at Accuracy as a function of Valence:

```
(xtab <- table(df$Valence, df$Accuracy))
```

```
##
##           right wrong
## negative   313   267
## positive   423   157
```

```
round(prop.table(xtab, 1), 3) * 100
```

```
##
##           right wrong
## negative   54.0  46.0
## positive   72.9  27.1
```

Look at descriptive stats for Accuracy as a function of Val_Al:

```
(xtab <- table(df$Val_Al, df$Accuracy))
```

```
##
##           right wrong
## no       125   163
## yes      192    96
```

```
round(prop.table(xtab, 1), 3) * 100
```

```
##
##           right wrong
## no       43.4  56.6
## yes      66.7  33.3
```

For graphs depicting quantity on the y-axis, people were more likely to get the answer right if the graph they looked at aligned with vertical valence metaphors.

Get accuracy information for each graph type that was relevant to our hypotheses (Trend was not considered here):

```
# Positive valence:
positive <- df %>% filter(Valence == 'positive')           # Filter to positive valence
(positive <- table(positive$Accuracy, positive$Version))    # Get raw N
```

```
##
##           1  2  3  4  5  6
```

```
##   right 94 95 30 90 48 66
##   wrong  2  5 66  8 48 28

round(prop.table(positive, 2) * 100, 1) # Proportions

##
##           1    2    3    4    5    6
##   right 97.9 95.0 31.2 91.8 50.0 70.2
##   wrong  2.1  5.0 68.8  8.2 50.0 29.8

# Negative valence:
negative <- df %>% filter(Valence == 'negative') # Filter to negative valence
(negative <- table(negative$Accuracy, negative$Version)) # Get raw N

##
##           1  2  3  4  5  6
##   right 54 62 50 60 41 46
##   wrong 42 38 46 38 55 48

round(prop.table(negative, 2) * 100, 1) # Proportions

##
##           1    2    3    4    5    6
##   right 56.2 62.0 52.1 61.2 42.7 48.9
##   wrong 43.8 38.0 47.9 38.8 57.3 51.1
```

Inferential stats

Run Model 1, which tests the effect of axis inversion, quantity mapping, and valence on response accuracy.

```
# Run chains in parallel:
options(mc.cores = parallel::detectCores())

# Turn variables into factors:
df$Accuracy <- factor(df$Accuracy, levels = c('wrong', 'right'))
df$AxisInversion <- as.factor(df$AxisInversion)
df$Orientation <- as.factor(df$Orientation)
df$Valence <- as.factor(df$Valence)

# Set prior:
my_priors <- c(prior(normal(0, 2), class = b),
               prior(normal(0, 2), class = 'sd'))

# Set controls:
my_controls <- list(adapt_delta = 0.99,
                   max_treedepth = 13)

# Run model:
xmdl <- brm(Accuracy ~ AxisInversion + Orientation + Valence +
            (1 + Valence|Subject),
            data = df,
            family = bernoulli,
            init = 0,
            chains = 4,
            warmup = 2000,
            iter = 4000,
            prior = my_priors,
```

```

      control = my_controls,
      seed = 13)

# Summary of model:
summary(xmdl)

## Family: bernoulli
## Links: mu = logit
## Formula: Accuracy ~ AxisInversion + Orientation + Valence + (1 + Valence | Subject)
## Data: df (Number of observations: 1160)
## Samples: 4 chains, each with iter = 4000; warmup = 2000; thin = 1;
##          total post-warmup samples = 8000
##
## Group-Level Effects:
## ~Subject (Number of levels: 290)
##
##           Estimate Est.Error 1-95% CI u-95% CI Rhat
## sd(Intercept)          3.80      0.46    2.97    4.76 1.00
## sd(Valencepositive)     3.64      0.45    2.81    4.60 1.00
## cor(Intercept,Valencepositive) -0.84    0.06   -0.93   -0.70 1.00
##
##           Bulk_ESS Tail_ESS
## sd(Intercept)       1764    3435
## sd(Valencepositive)  1938    3512
## cor(Intercept,Valencepositive) 1968    3423
##
## Population-Level Effects:
##           Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
## Intercept          0.44      0.36   -0.29    1.14 1.00    2370    3241
## AxisInversionnormal  2.68      0.45    1.85    3.61 1.00    2595    3906
## Orientationquant_y  -1.81      0.36   -2.52   -1.12 1.00    2882    4251
## Valencepositive      1.50      0.35    0.85    2.23 1.00    2517    3149
##
## Samples were drawn using sampling(NUTS). For each parameter, Bulk_ESS
## and Tail_ESS are effective sample size measures, and Rhat is the potential
## scale reduction factor on split chains (at convergence, Rhat = 1).

# Get odds:
round(exp(summary(xmdl)$fixed[2, 1]), 2) # AxisInversion

## [1] 14.63

round(exp(summary(xmdl)$fixed[3, 1]), 2) # Orientation

## [1] 0.16

round(exp(summary(xmdl)$fixed[4, 1]), 2) # Valence

## [1] 4.5

# Posterior predictive checks:
# pp_check(xmdl)

Run leave-one-out cross-validation comparing intercept-only model with models with predictors left in:

# Run models to compare:

# Run intercept-only model:
#xmdl_null <- brm(Accuracy ~ 1 +

```

```

#           (1 + Valence/Subject),
#           data = df,
#           family = bernoulli,
#           chains = 4,
#           warmup = 2000,
#           init = 0,
#           iter = 4000,
#           sample_prior = "yes",
#           control = my_controls,
#           seed = 13)

# Run AxisInversion-only model:
#xmdl_axis <- brm(Accuracy ~ AxisInversion +
#           (1 + Valence/Subject),
#           data = df,
#           family = bernoulli,
#           init = 0,
#           chains = 4,
#           warmup = 2000,
#           iter = 4000,
#           prior = my_priors,
#           control = my_controls,
#           seed = 13)

# Run Orientation-only model:
#xmdl_orient <- brm(Accuracy ~ Orientation +
#           (1 + Valence/Subject),
#           data = df,
#           family = bernoulli,
#           init = 0,
#           chains = 4,
#           warmup = 2000,
#           iter = 4000,
#           prior = my_priors,
#           control = my_controls,
#           seed = 13)

# Run Valence-only model:
#xmdl_val <- brm(Accuracy ~ Valence +
#           (1 + Valence/Subject),
#           data = df,
#           family = bernoulli,
#           init = 0,
#           chains = 4,
#           warmup = 2000,
#           iter = 4000,
#           prior = my_priors,
#           control = my_controls,
#           seed = 13)

# Calculate LOO for each model:
#loo(xmdl_null)

```



```

#loo(xmdl_axis)
#loo(xmdl_orient)
#loo(xmdl_val)

# Compare null model with AxisInversion model:
#loo_compare(xmdl_null, xmdl_axis)

# Compare null model with Orientation model:
#loo_compare(xmdl_null, xmdl_orient)

# Compare null model with Valence model:
#loo_compare(xmdl_null, xmdl_val)

```

Run Model 2, which tests the effect of vertical valence alignment on response accuracy.

```

# Filter to graphs with quantity on the y-axis:
df_y <- df %>% filter(Orientation == 'quant_y')

# Create copies of relevant predictors:
df_y$AxisInversion_c <- factor(df_y$AxisInversion, levels = c('normal', 'inverted'))
df_y$Valence_c <- factor(df_y$Valence, levels = c('positive', 'negative'))
df_y$Accuracy <- factor(df_y$Accuracy, levels = c('wrong', 'right'))

# Deviation code these predictors:
contrasts(df_y$AxisInversion_c) <- contr.sum(2) / 2
contrasts(df_y$Valence_c) <- contr.sum(2) / 2

# Run model:
y_md1 <- brm(Accuracy ~ AxisInversion_c * Valence_c +
              (1 + Valence_c|Subject),
              data = df_y,
              family = bernoulli,
              init = 0,
              chains = 4,
              warmup = 2000,
              iter = 4000,
              prior = my_priors,
              control = my_controls,
              seed = 13)

```

```
## Compiling Stan program...
```

```
## recompiling to avoid crashing R session
```

```
## Start sampling
```

```

# Posterior predictive checks:
# pp_check(y_md1)

```

```

# Summary of model:
summary(y_md1)

```

```

## Family: bernoulli
## Links: mu = logit
## Formula: Accuracy ~ AxisInversion_c * Valence_c + (1 + Valence_c | Subject)
## Data: df_y (Number of observations: 576)

```

```

## Samples: 4 chains, each with iter = 4000; warmup = 2000; thin = 1;
##       total post-warmup samples = 8000
##
## Group-Level Effects:
## ~Subject (Number of levels: 144)
##
##           Estimate Est.Error l-95% CI u-95% CI Rhat Bulk_ESS
## sd(Intercept)      2.51      0.38    1.85    3.31 1.00    2911
## sd(Valence_c1)      3.49      0.62    2.38    4.81 1.00    2862
## cor(Intercept,Valence_c1) -0.18    0.24   -0.60    0.33 1.00    2529
##
##           Tail_ESS
## sd(Intercept)      4343
## sd(Valence_c1)      4572
## cor(Intercept,Valence_c1) 3919
##
## Population-Level Effects:
##
##           Estimate Est.Error l-95% CI u-95% CI Rhat Bulk_ESS
## Intercept          1.29      0.32    0.68    1.94 1.00    5229
## AxisInversion_c1    3.55      0.66    2.32    4.90 1.00    5421
## Valence_c1          2.09      0.54    1.04    3.19 1.00    6171
## AxisInversion_c1:Valence_c1 4.78    1.05    2.78    6.90 1.00    5817
##
##           Tail_ESS
## Intercept          5420
## AxisInversion_c1    5975
## Valence_c1          6030
## AxisInversion_c1:Valence_c1 5598
##
## Samples were drawn using sampling(NUTS). For each parameter, Bulk_ESS
## and Tail_ESS are effective sample size measures, and Rhat is the potential
## scale reduction factor on split chains (at convergence, Rhat = 1).

# Get odds:
round(exp(summary(y_mdl)$fixed[4, 1]), 2)

## [1] 118.53

# Get posterior samples:
myposts <- posterior_samples(y_mdl) %>%
  select(b_Intercept, b_AxisInversion_c1, b_Valence_c1, `b_AxisInversion_c1:Valence_c1`)

# Save samples for different columns:
intercept <- myposts$b_Intercept
axis_coef <- myposts$b_AxisInversion_c1
val_coef <- myposts$b_Valence_c1
interaction_coef <- myposts$b_AxisInversion_c1:Valence_c1

# Normal, positive graphs:
normal_positive <- (intercept +
  (+0.5) * axis_coef +
  (+0.5) * val_coef +
  (+0.5) * (+0.5) * interaction_coef)
round(quantile(normal_positive, 0.025), 2)

## 2.5%
## 3.77

```

```

round(quantile(normal_positive, 0.975), 2)

## 97.5%
## 7.08

# Normal, negative graphs:
normal_negative <- (intercept +
  (+0.5) * axis_coef +
  (-0.5) * val_coef +
  (+0.5) * (-0.5) * interaction_coef)
round(quantile(normal_negative, 0.025), 2)

## 2.5%
## -0.29

round(quantile(normal_negative, 0.975), 2)

## 97.5%
## 2.08

# Inverted, positive graphs:
inverted_positive <- (intercept +
  (-0.5) * axis_coef +
  (+0.5) * val_coef +
  (-0.5) * (+0.5) * interaction_coef)
round(quantile(inverted_positive, 0.025), 2)

## 2.5%
## -1.39

round(quantile(inverted_positive, 0.975), 2)

## 97.5%
## 0.06

# Inverted, negative graphs:
inverted_negative <- (intercept +
  (-0.5) * axis_coef +
  (-0.5) * val_coef +
  (-0.5) * (-0.5) * interaction_coef)
round(quantile(inverted_negative, 0.025), 2)

## 2.5%
## -1.16

round(quantile(inverted_negative, 0.975), 2)

## 97.5%
## 0.48

Run LOO-CV on model 2:

# Run models to compare:

# Run intercept-only model:
#y_mdl_null <- brm(Accuracy ~ 1 +
#                  (1 + Valence_c/Subject),
#                  data = df_y,
#                  family = bernoulli,

```

```

#           init = 0,
#           chains = 4,
#           warmup = 2000,
#           iter = 4000,
#           sample_prior = "yes",
#           control = my_controls,
#           seed = 13)

# Calculate LOO for each model:
#loo(y_mdl_null)
#loo(y_mdl)

# Compare null model with interaction model:
#loo(y_mdl_null, y_mdl)

```

Create table summary of model 1:

```

# Make table of fixed effects:
summary1 <- tibble(
  "Predictors" = c('Axis Orientation',
                   'Quantity Mapping',
                   'Valence'),
  "Estimate" = c(round(summary(xmdl)$fixed[2, 1], 2),
                 round(summary(xmdl)$fixed[3, 1], 2),
                 round(summary(xmdl)$fixed[4, 1], 2)),
  "Std. Error" = c(round(summary(xmdl)$fixed[2, 2], 2),
                   round(summary(xmdl)$fixed[3, 2], 2),
                   round(summary(xmdl)$fixed[4, 2], 2)),
  "Lower" = c(round(summary(xmdl)$fixed[2, 3], 2),
              round(summary(xmdl)$fixed[3, 3], 2),
              round(summary(xmdl)$fixed[4, 3], 2)),
  "Upper" = c(round(summary(xmdl)$fixed[2, 4], 2),
              round(summary(xmdl)$fixed[3, 4], 2),
              round(summary(xmdl)$fixed[4, 4], 2))

# Factorise predictor column and re-order levels:
summary1$Predictors <- factor(summary1$Predictors, levels = c('Valence', 'Quantity Mapping', 'Axis Orientation'))

```

Create table summary of model 2:

```

# Make table of fixed effects:
summary2 <- tibble(
  "Predictors" = c("Axis Orientation",
                   "Valence",
                   "Axis Orientation x Valence"),
  "Estimate" = c(round(summary(y_mdl)$fixed[2, 1], 1),
                 round(summary(y_mdl)$fixed[3, 1], 1),
                 round(summary(y_mdl)$fixed[4, 1], 2)),
  "Std. Error" = c(round(summary(y_mdl)$fixed[2, 2], 2),
                   round(summary(y_mdl)$fixed[3, 2], 2),
                   round(summary(y_mdl)$fixed[4, 2], 2)),
  "Lower" = c(round(summary(y_mdl)$fixed[2, 3], 2),
              round(summary(y_mdl)$fixed[3, 3], 2),
              round(summary(y_mdl)$fixed[4, 3], 2)),
  "Upper" = c(round(summary(y_mdl)$fixed[2, 4], 2),
              round(summary(y_mdl)$fixed[3, 4], 2),
              round(summary(y_mdl)$fixed[4, 4], 2))

```

```

round(summary(y_mdl)$fixed[3, 4], 2),
round(summary(y_mdl)$fixed[4, 4], 2)))

# Factorise predictor column:
summary2$Predictors <- factor(summary2$Predictors, levels = c("Axis Orientation x Valence", "Valence",

Wrangle outputs from model 1 for plotting:

# Convert output of model 1 into tibble:
xtrans <- ggs(xmdl)

## Warning in custom.sort(D$Parameter): NAs introduced by coercion
# Filter xmdl_trans to parameter rows and change name of Parameter column to match table summary (above)
xmdl_trans <- xtrans %>%
  filter(Parameter %in% c('b_AxisInversionnormal', 'b_Orientationquant_y', 'b_Valencepositive')) %>%
  rename(Predictors = Parameter)

# Change name of predictor levels:
xmdl_trans$Predictors <- revalue(xmdl_trans$Predictors, c("b_AxisInversionnormal" = "Axis Orientation",
                                                         "b_Orientationquant_y" = "Quantity Mapping",
                                                         "b_Valencepositive" = "Valence"))

Wrangle outputs from model 2 for plotting:

# Convert output of model 2 into tibble:
ytrans <- ggs(y_mdl)

## Warning in custom.sort(D$Parameter): NAs introduced by coercion
# Filter xmdl_trans_2 to interaction row:
xmdl_trans_2 <- ytrans %>%
  filter(Parameter %in% c('b_AxisInversion_c1', "b_Valence_c1", 'b_AxisInversion_c1:Valence_c1')) %>%
  rename(Predictors = Parameter)

# Change name of predictor levels:
xmdl_trans_2$Predictors <- revalue(xmdl_trans_2$Predictors, c('b_AxisInversion_c1' = 'Axis Orientation',
                                                             'b_Valence_c1' = 'Valence',
                                                             "b_AxisInversion_c1:Valence_c1" = "Axis O:

Make plot showing posterior distributions for model 1 (inspired by https://osf.io/atr57/):

# Combine point estimates with posterior samples:
posterior <- merge(summary1, xmdl_trans, by = 'Predictors')

# Re-order levels:
posterior$Predictors <- factor(posterior$Predictors, levels = c("Valence", "Quantity Mapping", "Axis Or:

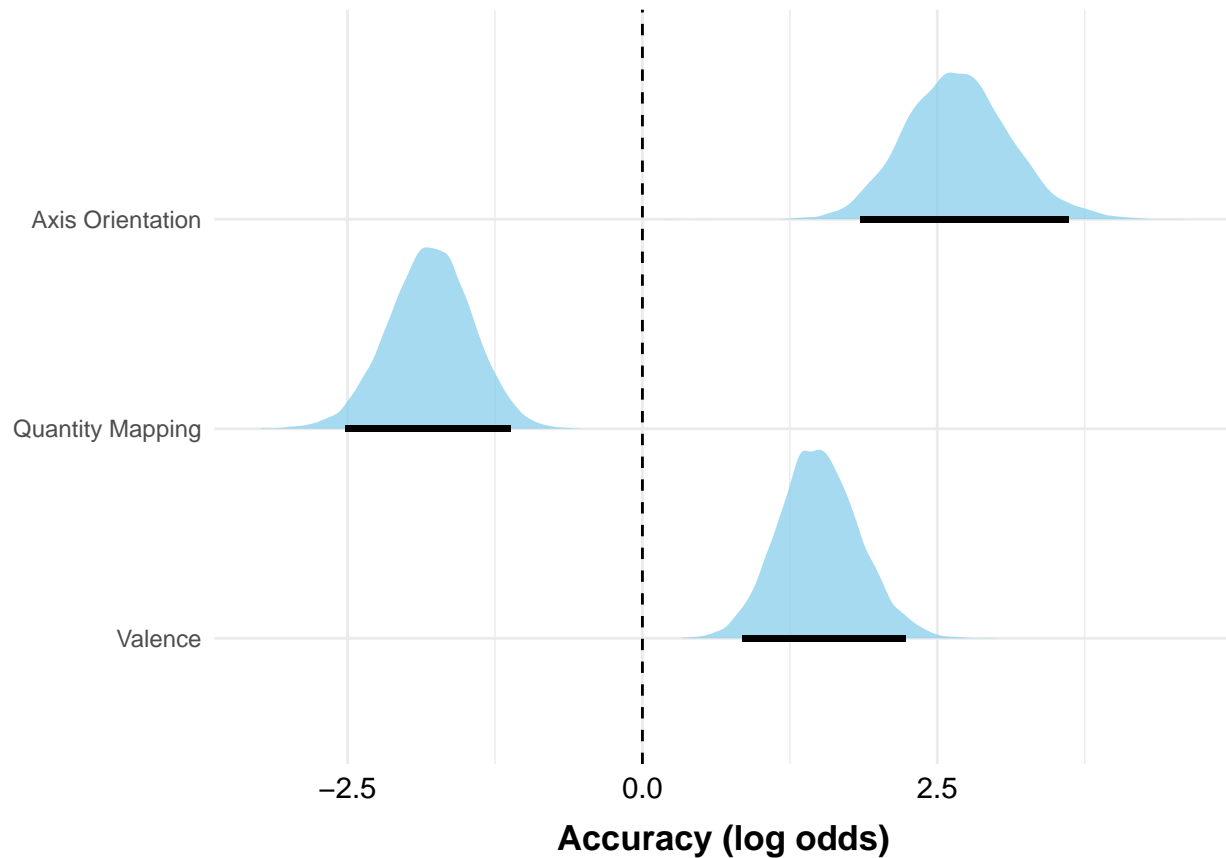
# Make plot:
posterior %>%
  ggplot(aes(x = value, y = Predictors, fill = Predictors, xmin = Lower, xmax = Upper)) +
  stat_slab(alpha = 0.75) +
  geom_linerange(size = 1) +
  theme_minimal() +
  geom_vline(xintercept = 0,
            color = "black",
            linetype = 2) +

```

```

theme(axis.text.x = element_text(size = 10.5,
                                   colour = 'black'),
      axis.title.x = element_text(size = 13,
                                   face = "bold",
                                   vjust = -0.7),
      axis.title.y = element_blank(),
      legend.position = "none") +
scale_fill_manual(values = c("skyblue", "skyblue", "skyblue")) +
scale_x_continuous(name = "Accuracy (log odds)",
                   breaks = seq(-5, 10, 2.5))

```



```

# Save plot as PDF:
ggsave('../table_creation/E1_model1.pdf', width = 6, height = 5)

```

Make plot showing posterior distributions for model 2 (inspired by <https://osf.io/atr57/>):

```

# Combine point estimates with posterior samples:
posterior2 <- merge(summary2, xmdl_trans_2, by = 'Predictors')

# Re-order levels:
posterior2$Predictors <- factor(posterior2$Predictors, levels = c("Axis Orientation x Valence", "Valence"))

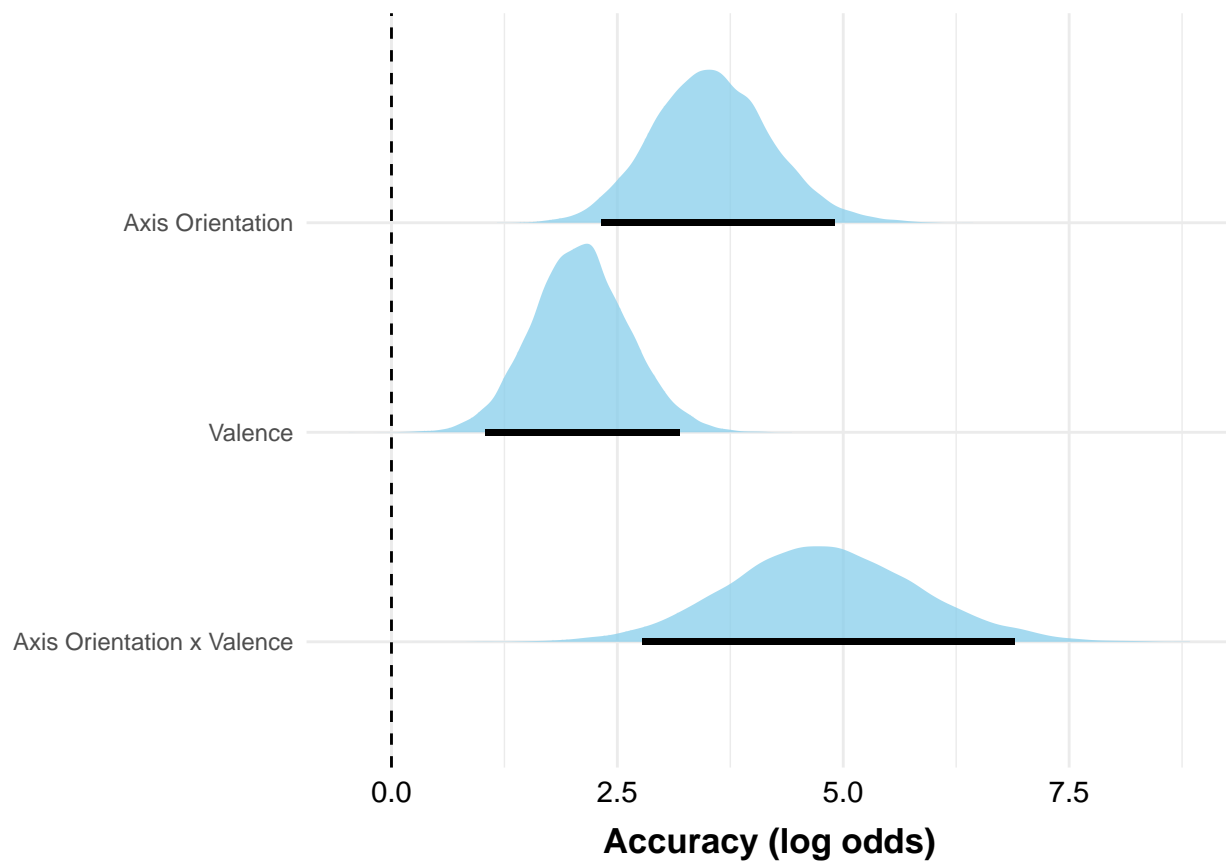
# Make plot:
posterior2 %>%
  ggplot(aes(x = value, y = Predictors, fill = Predictors, xmin = Lower, xmax = Upper)) +
  stat_slab(alpha = 0.75) +
  theme_minimal() +

```

```

geom_linerange(size = 1) +
geom_vline(xintercept = 0,
           color = "black",
           linetype = 2) +
theme(axis.text.x = element_text(size = 10.5,
                                   colour = 'black'),
      axis.title.x = element_text(size = 13,
                                   face = "bold",
                                   vjust = -0.7),
      axis.title.y = element_blank(),
      legend.position = "none") +
scale_fill_manual(values = c("skyblue", "skyblue", "skyblue")) +
scale_x_continuous(name = "Accuracy (log odds)",
                   breaks = seq(-5, 15, 2.5))

```



```

# Save plot as PDF:
ggsave('../table_creation/E1_model2.pdf', width = 6, height = 4)

```

Save table summaries:

```

# Remove lower and upper 95% interval values:
summary1 <- summary1 %>% select(-Lower, -Upper)           # Model 1
summary2 <- summary2 %>% select(-Lower, -Upper)           # Model 2

# Save summary of model 1 as CSV:
write_csv(summary1, '../table_creation/E1_model1.csv')

```

```
# Save summary of model 2 as CSV:
write_csv(summary2, '../table_creation/E1_model2.csv')
```

Get accuracy proportions for each graph type:

```
# Normal graphs:
(xtab <- df_y %>%
  filter(AxisInversion == 'normal') %>%
  with(table(Accuracy, Valence)))
```

```
##           Valence
## Accuracy negative positive
##   wrong         42         2
##   right         54        94
```

```
round(prop.table(xtab, 2) * 100, 1)
```

```
##           Valence
## Accuracy negative positive
##   wrong      43.8      2.1
##   right      56.2     97.9
```

```
# Inverted graphs:
(xtab <- df_y %>%
  filter(AxisInversion == 'inverted') %>%
  with(table(Accuracy, Valence)))
```

```
##           Valence
## Accuracy negative positive
##   wrong      101      114
##   right       91       78
```

```
round(prop.table(xtab, 2) * 100, 1)
```

```
##           Valence
## Accuracy negative positive
##   wrong      52.6     59.4
##   right      47.4     40.6
```

Exploratory analysis

First, check whether axis inversion effect was stronger for y-axis graphs than x-axis graphs:

```
(xtab <- table(df$Accuracy, df$AxisInversion, df$Orientation))
```

```
## , , = quant_x
##
##
##           inverted normal
##   wrong      122      43
##   right      262     157
##
## , , = quant_y
##
##
##           inverted normal
##   wrong      215      44
##   right      169     148
```



```
round(prop.table(xtab, c(2, 3)), 3) * 100
```

```
## , , = quant_x
##
##          inverted normal
## wrong      31.8    21.5
## right      68.2    78.5
##
## , , = quant_y
##
##          inverted normal
## wrong      56.0    22.9
## right      44.0    77.1
```

For inverted graphs, check effects of time axis versus quantity axis being subverted:

```
# Filter dataset to inverted graphs and add column to mark whether quantity or time is subverted:
df %>%
  filter(AxisInversion == 'inverted') %>%
  mutate(WhichSubvert = case_when(
    Orientation == 'quant_y' & InvertXY == 'y' ~ 'quant',
    Orientation == 'quant_x' & InvertXY == 'x' ~ 'quant',
    Orientation == 'quant_y' & InvertXY == 'x' ~ 'time',
    Orientation == 'quant_x' & InvertXY == 'y' ~ 'time')) %>%
  with(print(table(Accuracy, WhichSubvert))) %>%
  prop.table(2) %>%
  round(3) * 100
```

```
##          WhichSubvert
## Accuracy quant time
## wrong      188    149
## right      192    239
##
##          WhichSubvert
## Accuracy quant time
## wrong      49.5   38.4
## right      50.5   61.6
```

Check response latencies for participants responding to graphs mapping quantity information onto the x-axis versus the y-axis:

```
df_RT %>%
  group_by(Orientation) %>%
  summarise(mean(as.numeric(Measurement)))

## `summarise()` ungrouping output (override with `.groups` argument)

## # A tibble: 2 x 2
##   Orientation `mean(as.numeric(Measurement))`
##   <chr>                                <dbl>
## 1 quant_x                                5.48
## 2 quant_y                                3.75
```

Reviewer-requested additional analysis

Educational background We now look at the effect of educational background on responses.

First, look at demographic information:

```
(xtab <- table(df$Ed))

##
##               Associate degree in college (2-year)
##                                           144
##               Bachelor's degree in college (4-year)
##                                           540
##               Doctoral degree
##                                           20
## High school graduate (high school diploma or equivalent including GED)
##                                           120
##               Less than high school degree
##                                           12
##               Master's degree
##                                           140
##               Professional degree (JD, MD)
##                                           12
##               Some college but no degree
##                                           172
```

```
round(prop.table(xtab) * 100, 1)

##
##               Associate degree in college (2-year)
##                                           12.4
##               Bachelor's degree in college (4-year)
##                                           46.6
##               Doctoral degree
##                                           1.7
## High school graduate (high school diploma or equivalent including GED)
##                                           10.3
##               Less than high school degree
##                                           1.0
##               Master's degree
##                                           12.1
##               Professional degree (JD, MD)
##                                           1.0
##               Some college but no degree
##                                           14.8
```

Look at how accuracy varies according to education level:

```
(xtab <- table(df$Ed, df$Accuracy))           # Raw stats

##
##                                     wrong
## Associate degree in college (2-year)      46
## Bachelor's degree in college (4-year)    187
## Doctoral degree                          8
## High school graduate (high school diploma or equivalent including GED)  45
## Less than high school degree              8
## Master's degree                          48
## Professional degree (JD, MD)              6
## Some college but no degree                76
##
```

```
##
## Associate degree in college (2-year) right 98
## Bachelor's degree in college (4-year) 353
## Doctoral degree 12
## High school graduate (high school diploma or equivalent including GED) 75
## Less than high school degree 4
## Master's degree 92
## Professional degree (JD, MD) 6
## Some college but no degree 96
```

```
(xtab <- round(prop.table(xtab, 1), 3) * 100) # Proportions
```

```
##
## wrong
## Associate degree in college (2-year) 31.9
## Bachelor's degree in college (4-year) 34.6
## Doctoral degree 40.0
## High school graduate (high school diploma or equivalent including GED) 37.5
## Less than high school degree 66.7
## Master's degree 34.3
## Professional degree (JD, MD) 50.0
## Some college but no degree 44.2
##
## right
## Associate degree in college (2-year) 68.1
## Bachelor's degree in college (4-year) 65.4
## Doctoral degree 60.0
## High school graduate (high school diploma or equivalent including GED) 62.5
## Less than high school degree 33.3
## Master's degree 65.7
## Professional degree (JD, MD) 50.0
## Some college but no degree 55.8
```

Look at how response time varied according to education level:

```
df_RT %>%
  group_by(Ed) %>%
  summarise(mean(as.numeric(Measurement))) %>%
  arrange(desc(`mean(as.numeric(Measurement))`))
```

```
## `summarise()` ungrouping output (override with `.groups` argument)
```

```
## # A tibble: 8 x 2
## Ed `mean(as.numeric(Measur~
## <chr> <dbl>
## 1 Doctoral degree 6.45
## 2 Associate degree in college (2-year) 6.05
## 3 Bachelor's degree in college (4-year) 4.49
## 4 Less than high school degree 4.45
## 5 High school graduate (high school diploma or equiv~ 4.39
## 6 Some college but no degree 4.37
## 7 Master's degree 4.10
## 8 Professional degree (JD, MD) 1.92
```

Run Model 1 but with an interaction with Ed entered for each of the predictors, to see if Education modulates any of the effects:

```
# Turn variables into factors:
df$Ed <- factor(df$Ed)
```

```
# Run model:
```

```
xmdl <- brm(Accuracy ~ (AxisInversion * Ed) +
            (Orientation * Ed) +
            (Valence * Ed) +
            (1 + Valence|Subject),
            data = df,
            family = bernoulli,
            init = 0,
            chains = 4,
            warmup = 2000,
            iter = 4000,
            prior = my_priors,
            control = my_controls,
            seed = 13)
```

```
# Summary of model:
summary(xmdl)
```

```
## Family: bernoulli
## Links: mu = logit
## Formula: Accuracy ~ (AxisInversion * Ed) + (Orientation * Ed) + (Valence * Ed) + (1 + Valence | Subject)
## Data: df (Number of observations: 1160)
## Samples: 4 chains, each with iter = 4000; warmup = 2000; thin = 1;
##          total post-warmup samples = 8000
##
## Group-Level Effects:
## ~Subject (Number of levels: 290)
##
```

	Estimate	Est.Error	l-95% CI	u-95% CI	Rhat
sd(Intercept)	4.13	0.48	3.26	5.15	1.00
sd(Valencepositive)	3.94	0.47	3.08	4.90	1.00
cor(Intercept,Valencepositive)	-0.82	0.06	-0.92	-0.68	1.00

```
## Bulk_ESS Tail_ESS
## sd(Intercept)      2338    4117
## sd(Valencepositive) 2598    4558
## cor(Intercept,Valencepositive) 2084    3727
##
## Population-Level Effects:
##
```

	Estimate
Intercept	0.54
AxisInversionnormal	2.79
EdBachelorsdegreeincollege4Myer	-0.02
EdDoctoraldegree	0.27
EdHighschoolgraduatehighschooldiplomaorequivalentincludingGED	-0.94
EdLessthanhighschooldegree	-1.00
EdMastersdegree	0.18
EdProfessionaldegreeJDMD	-0.60
EdSomecollegebutnodegree	-0.21
Orientationquant_y	-2.16
Valencepositive	1.81
AxisInversionnormal:EdBachelorsdegreeincollege4Myer	0.14
AxisInversionnormal:EdDoctoraldegree	-0.00

## AxisInversionnormal:EdHighschoolgraduatehighschooldiplomaorequivalentincludingGED	-0.00
## AxisInversionnormal:EdLessthanhighschooldegree	-0.32
## AxisInversionnormal:EdMastersdegree	0.06
## AxisInversionnormal:EdProfessionaldegreeJDMD	1.00
## AxisInversionnormal:EdSomecollegebutnodegree	0.36
## EdBachelorsdegreeincollege4Myer:Orientationquant_y	0.55
## EdDoctoraldegree:Orientationquant_y	0.28
## EdHighschoolgraduatehighschooldiplomaorequivalentincludingGED:Orientationquant_y	0.34
## EdLessthanhighschooldegree:Orientationquant_y	-0.73
## EdMastersdegree:Orientationquant_y	-0.17
## EdProfessionaldegreeJDMD:Orientationquant_y	-0.61
## EdSomecollegebutnodegree:Orientationquant_y	0.33
## EdBachelorsdegreeincollege4Myer:Valencepositive	-0.34
## EdDoctoraldegree:Valencepositive	0.07
## EdHighschoolgraduatehighschooldiplomaorequivalentincludingGED:Valencepositive	1.20
## EdLessthanhighschooldegree:Valencepositive	-0.86
## EdMastersdegree:Valencepositive	0.23
## EdProfessionaldegreeJDMD:Valencepositive	0.24
## EdSomecollegebutnodegree:Valencepositive	-1.00
##	Est.Error
## Intercept	0.64
## AxisInversionnormal	0.77
## EdBachelorsdegreeincollege4Myer	0.78
## EdDoctoraldegree	1.47
## EdHighschoolgraduatehighschooldiplomaorequivalentincludingGED	1.04
## EdLessthanhighschooldegree	1.61
## EdMastersdegree	0.99
## EdProfessionaldegreeJDMD	1.77
## EdSomecollegebutnodegree	1.00
## Orientationquant_y	0.71
## Valencepositive	0.65
## AxisInversionnormal:EdBachelorsdegreeincollege4Myer	0.90
## AxisInversionnormal:EdDoctoraldegree	2.03
## AxisInversionnormal:EdHighschoolgraduatehighschooldiplomaorequivalentincludingGED	1.20
## AxisInversionnormal:EdLessthanhighschooldegree	1.76
## AxisInversionnormal:EdMastersdegree	1.19
## AxisInversionnormal:EdProfessionaldegreeJDMD	1.69
## AxisInversionnormal:EdSomecollegebutnodegree	1.10
## EdBachelorsdegreeincollege4Myer:Orientationquant_y	0.84
## EdDoctoraldegree:Orientationquant_y	1.55
## EdHighschoolgraduatehighschooldiplomaorequivalentincludingGED:Orientationquant_y	1.14
## EdLessthanhighschooldegree:Orientationquant_y	1.68
## EdMastersdegree:Orientationquant_y	1.09
## EdProfessionaldegreeJDMD:Orientationquant_y	1.73
## EdSomecollegebutnodegree:Orientationquant_y	1.02
## EdBachelorsdegreeincollege4Myer:Valencepositive	0.76
## EdDoctoraldegree:Valencepositive	1.47
## EdHighschoolgraduatehighschooldiplomaorequivalentincludingGED:Valencepositive	1.01
## EdLessthanhighschooldegree:Valencepositive	1.62
## EdMastersdegree:Valencepositive	0.96
## EdProfessionaldegreeJDMD:Valencepositive	1.67
## EdSomecollegebutnodegree:Valencepositive	0.92
##	1-95% CI
## Intercept	-0.70

## AxisInversionnormal	1.29
## EdBachelorsdegreeincollege4Myer	-1.52
## EdDoctoraldegree	-2.60
## EdHighschoolgraduatehighschooldiplomaorequivalentincludingGED	-2.93
## EdLessthanhighschooldegree	-4.23
## EdMastersdegree	-1.75
## EdProfessionaldegreeJDMD	-4.01
## EdSomecollegebutnodegree	-2.17
## Orientationquant_y	-3.56
## Valencepositive	0.56
## AxisInversionnormal:EdBachelorsdegreeincollege4Myer	-1.62
## AxisInversionnormal:EdDoctoraldegree	-4.02
## AxisInversionnormal:EdHighschoolgraduatehighschooldiplomaorequivalentincludingGED	-2.35
## AxisInversionnormal:EdLessthanhighschooldegree	-3.79
## AxisInversionnormal:EdMastersdegree	-2.24
## AxisInversionnormal:EdProfessionaldegreeJDMD	-2.29
## AxisInversionnormal:EdSomecollegebutnodegree	-1.81
## EdBachelorsdegreeincollege4Myer:Orientationquant_y	-1.07
## EdDoctoraldegree:Orientationquant_y	-2.71
## EdHighschoolgraduatehighschooldiplomaorequivalentincludingGED:Orientationquant_y	-1.91
## EdLessthanhighschooldegree:Orientationquant_y	-4.03
## EdMastersdegree:Orientationquant_y	-2.33
## EdProfessionaldegreeJDMD:Orientationquant_y	-4.02
## EdSomecollegebutnodegree:Orientationquant_y	-1.70
## EdBachelorsdegreeincollege4Myer:Valencepositive	-1.88
## EdDoctoraldegree:Valencepositive	-2.80
## EdHighschoolgraduatehighschooldiplomaorequivalentincludingGED:Valencepositive	-0.77
## EdLessthanhighschooldegree:Valencepositive	-4.04
## EdMastersdegree:Valencepositive	-1.66
## EdProfessionaldegreeJDMD:Valencepositive	-2.99
## EdSomecollegebutnodegree:Valencepositive	-2.79
##	u-95% CI
## Intercept	1.79
## AxisInversionnormal	4.32
## EdBachelorsdegreeincollege4Myer	1.52
## EdDoctoraldegree	3.17
## EdHighschoolgraduatehighschooldiplomaorequivalentincludingGED	1.11
## EdLessthanhighschooldegree	2.18
## EdMastersdegree	2.15
## EdProfessionaldegreeJDMD	2.87
## EdSomecollegebutnodegree	1.79
## Orientationquant_y	-0.80
## Valencepositive	3.12
## AxisInversionnormal:EdBachelorsdegreeincollege4Myer	1.90
## AxisInversionnormal:EdDoctoraldegree	3.99
## AxisInversionnormal:EdHighschoolgraduatehighschooldiplomaorequivalentincludingGED	2.36
## AxisInversionnormal:EdLessthanhighschooldegree	3.10
## AxisInversionnormal:EdMastersdegree	2.42
## AxisInversionnormal:EdProfessionaldegreeJDMD	4.32
## AxisInversionnormal:EdSomecollegebutnodegree	2.60
## EdBachelorsdegreeincollege4Myer:Orientationquant_y	2.18
## EdDoctoraldegree:Orientationquant_y	3.32
## EdHighschoolgraduatehighschooldiplomaorequivalentincludingGED:Orientationquant_y	2.55
## EdLessthanhighschooldegree:Orientationquant_y	2.52

## EdMastersdegree:Orientationquant_y	1.98
## EdProfessionaldegreeJDMD:Orientationquant_y	2.82
## EdSomecollegebutnodegree:Orientationquant_y	2.31
## EdBachelorsdegreeincollege4Myer:Valencepositive	1.12
## EdDoctoraldegree:Valencepositive	2.93
## EdHighschoolgraduatehighschooldiplomaorequivalentincludingGED:Valencepositive	3.15
## EdLessthanhighschooldegree:Valencepositive	2.30
## EdMastersdegree:Valencepositive	2.12
## EdProfessionaldegreeJDMD:Valencepositive	3.55
## EdSomecollegebutnodegree:Valencepositive	0.78
##	Rhat
## Intercept	1.00
## AxisInversionnormal	1.00
## EdBachelorsdegreeincollege4Myer	1.00
## EdDoctoraldegree	1.00
## EdHighschoolgraduatehighschooldiplomaorequivalentincludingGED	1.00
## EdLessthanhighschooldegree	1.00
## EdMastersdegree	1.00
## EdProfessionaldegreeJDMD	1.00
## EdSomecollegebutnodegree	1.00
## Orientationquant_y	1.00
## Valencepositive	1.00
## AxisInversionnormal:EdBachelorsdegreeincollege4Myer	1.00
## AxisInversionnormal:EdDoctoraldegree	1.00
## AxisInversionnormal:EdHighschoolgraduatehighschooldiplomaorequivalentincludingGED	1.00
## AxisInversionnormal:EdLessthanhighschooldegree	1.00
## AxisInversionnormal:EdMastersdegree	1.00
## AxisInversionnormal:EdProfessionaldegreeJDMD	1.00
## AxisInversionnormal:EdSomecollegebutnodegree	1.00
## EdBachelorsdegreeincollege4Myer:Orientationquant_y	1.00
## EdDoctoraldegree:Orientationquant_y	1.00
## EdHighschoolgraduatehighschooldiplomaorequivalentincludingGED:Orientationquant_y	1.00
## EdLessthanhighschooldegree:Orientationquant_y	1.00
## EdMastersdegree:Orientationquant_y	1.00
## EdProfessionaldegreeJDMD:Orientationquant_y	1.00
## EdSomecollegebutnodegree:Orientationquant_y	1.00
## EdBachelorsdegreeincollege4Myer:Valencepositive	1.00
## EdDoctoraldegree:Valencepositive	1.00
## EdHighschoolgraduatehighschooldiplomaorequivalentincludingGED:Valencepositive	1.00
## EdLessthanhighschooldegree:Valencepositive	1.00
## EdMastersdegree:Valencepositive	1.00
## EdProfessionaldegreeJDMD:Valencepositive	1.00
## EdSomecollegebutnodegree:Valencepositive	1.00
##	Bulk_ESS
## Intercept	3532
## AxisInversionnormal	3934
## EdBachelorsdegreeincollege4Myer	3280
## EdDoctoraldegree	6921
## EdHighschoolgraduatehighschooldiplomaorequivalentincludingGED	4287
## EdLessthanhighschooldegree	10210
## EdMastersdegree	4006
## EdProfessionaldegreeJDMD	11182
## EdSomecollegebutnodegree	4031
## Orientationquant_y	3749

## Valencepositive	3633
## AxisInversionnormal:EdBachelorsdegreeincollege4Myer	4221
## AxisInversionnormal:EdDoctoraldegree	14748
## AxisInversionnormal:EdHighschoolgraduatehighschooldiplomaorequivalentincludingGED	5103
## AxisInversionnormal:EdLessthanhighschooldegree	11036
## AxisInversionnormal:EdMastersdegree	5514
## AxisInversionnormal:EdProfessionaldegreeJDMD	11289
## AxisInversionnormal:EdSomecollegebutnodegree	5113
## EdBachelorsdegreeincollege4Myer:Orientationquant_y	3533
## EdDoctoraldegree:Orientationquant_y	8191
## EdHighschoolgraduatehighschooldiplomaorequivalentincludingGED:Orientationquant_y	4486
## EdLessthanhighschooldegree:Orientationquant_y	9975
## EdMastersdegree:Orientationquant_y	4149
## EdProfessionaldegreeJDMD:Orientationquant_y	11538
## EdSomecollegebutnodegree:Orientationquant_y	4426
## EdBachelorsdegreeincollege4Myer:Valencepositive	3698
## EdDoctoraldegree:Valencepositive	7934
## EdHighschoolgraduatehighschooldiplomaorequivalentincludingGED:Valencepositive	4769
## EdLessthanhighschooldegree:Valencepositive	10399
## EdMastersdegree:Valencepositive	4465
## EdProfessionaldegreeJDMD:Valencepositive	11708
## EdSomecollegebutnodegree:Valencepositive	3943
##	Tail_ESS
## Intercept	5491
## AxisInversionnormal	5709
## EdBachelorsdegreeincollege4Myer	4482
## EdDoctoraldegree	6001
## EdHighschoolgraduatehighschooldiplomaorequivalentincludingGED	5771
## EdLessthanhighschooldegree	6103
## EdMastersdegree	4896
## EdProfessionaldegreeJDMD	5635
## EdSomecollegebutnodegree	5308
## Orientationquant_y	5221
## Valencepositive	4761
## AxisInversionnormal:EdBachelorsdegreeincollege4Myer	5443
## AxisInversionnormal:EdDoctoraldegree	5028
## AxisInversionnormal:EdHighschoolgraduatehighschooldiplomaorequivalentincludingGED	6300
## AxisInversionnormal:EdLessthanhighschooldegree	6608
## AxisInversionnormal:EdMastersdegree	5879
## AxisInversionnormal:EdProfessionaldegreeJDMD	6415
## AxisInversionnormal:EdSomecollegebutnodegree	6120
## EdBachelorsdegreeincollege4Myer:Orientationquant_y	5484
## EdDoctoraldegree:Orientationquant_y	6621
## EdHighschoolgraduatehighschooldiplomaorequivalentincludingGED:Orientationquant_y	5409
## EdLessthanhighschooldegree:Orientationquant_y	5899
## EdMastersdegree:Orientationquant_y	5378
## EdProfessionaldegreeJDMD:Orientationquant_y	6518
## EdSomecollegebutnodegree:Orientationquant_y	4797
## EdBachelorsdegreeincollege4Myer:Valencepositive	4906
## EdDoctoraldegree:Valencepositive	5735
## EdHighschoolgraduatehighschooldiplomaorequivalentincludingGED:Valencepositive	5979
## EdLessthanhighschooldegree:Valencepositive	6405
## EdMastersdegree:Valencepositive	5677
## EdProfessionaldegreeJDMD:Valencepositive	6395


```
## EdSomecollegebutnodegree:Valencepositive
##
## Samples were drawn using sampling(NUTS). For each parameter, Bulk_ESS
## and Tail_ESS are effective sample size measures, and Rhat is the potential
## scale reduction factor on split chains (at convergence, Rhat = 1).
```

```
# Posterior predictive checks:
# pp_check(xmdl)
```

None of the interactions with the Ed predictor were significant (their 95% credible intervals all contained zero).

Run Model 2, which tests the effect of vertical valence alignment on response accuracy, except this time, include an interaction with Ed to see if this modulates the effects:

```
# Create copies of relevant predictors:
df_y$Ed_c <- as.factor(df_y$Ed)
contrasts(df_y$Ed_c) <- contr.sum(8) / 2

# Run model:
y_mdl <- brm(Accuracy ~ (AxisInversion_c * Valence_c) * Ed_c +
              (1 + Valence_c|Subject),
              data = df_y,
              family = bernoulli,
              init = 0,
              chains = 4,
              warmup = 2000,
              iter = 4000,
              prior = my_priors,
              control = my_controls,
              seed = 13)
```

```
## Compiling Stan program...
```

```
## Start sampling
```

```
# Posterior predictive checks:
# pp_check(y_mdl)
```

```
# Summary of model:
summary(y_mdl)
```

```
## Family: bernoulli
## Links: mu = logit
## Formula: Accuracy ~ (AxisInversion_c * Valence_c) * Ed_c + (1 + Valence_c | Subject)
## Data: df_y (Number of observations: 576)
## Samples: 4 chains, each with iter = 4000; warmup = 2000; thin = 1;
##          total post-warmup samples = 8000
##
## Group-Level Effects:
## ~Subject (Number of levels: 144)
##
```

	Estimate	Est.Error	1-95% CI	u-95% CI	Rhat	Bulk_ESS
sd(Intercept)	2.75	0.39	2.06	3.57	1.00	3240
sd(Valence_c1)	3.73	0.63	2.61	5.06	1.00	3153
cor(Intercept,Valence_c1)	-0.21	0.23	-0.62	0.27	1.00	2229

```
## Tail_ESS
## sd(Intercept) 5273
```

```

## sd(Valence_c1)          4628
## cor(Intercept,Valence_c1) 4072
##
## Population-Level Effects:
##
##               Estimate Est.Error 1-95% CI u-95% CI Rhat
## Intercept          1.21      0.43    0.40    2.08 1.00
## AxisInversion_c1    3.77      0.75    2.39    5.28 1.00
## Valence_c1          2.10      0.63    0.89    3.36 1.00
## Ed_c1              -0.37      1.38   -3.10    2.33 1.00
## Ed_c2               0.72      0.99   -1.23    2.65 1.00
## Ed_c3               0.37      1.69   -2.89    3.71 1.00
## Ed_c4               0.31      1.28   -2.21    2.81 1.00
## Ed_c5              -0.62      1.76   -4.11    2.80 1.00
## Ed_c6               0.55      1.27   -1.93    3.02 1.00
## Ed_c7              -0.61      1.68   -3.89    2.62 1.00
## AxisInversion_c1:Valence_c1 4.86      1.11    2.75    7.03 1.00
## AxisInversion_c1:Ed_c1 0.55      1.76   -2.93    3.94 1.00
## AxisInversion_c1:Ed_c2 -0.05      1.45   -2.92    2.83 1.00
## AxisInversion_c1:Ed_c3 -0.37      1.86   -4.01    3.38 1.00
## AxisInversion_c1:Ed_c4 -0.27      1.65   -3.53    3.04 1.00
## AxisInversion_c1:Ed_c5 0.09      1.88   -3.57    3.76 1.00
## AxisInversion_c1:Ed_c6 -0.09      1.65   -3.28    3.18 1.00
## AxisInversion_c1:Ed_c7 0.23      1.88   -3.48    4.01 1.00
## Valence_c1:Ed_c1    -0.18      1.64   -3.38    3.04 1.00
## Valence_c1:Ed_c2     0.66      1.30   -1.83    3.23 1.00
## Valence_c1:Ed_c3     0.58      1.78   -2.95    4.00 1.00
## Valence_c1:Ed_c4     0.40      1.55   -2.57    3.46 1.00
## Valence_c1:Ed_c5    -0.80      1.83   -4.35    2.75 1.00
## Valence_c1:Ed_c6    -0.68      1.52   -3.64    2.29 1.00
## Valence_c1:Ed_c7     0.10      1.82   -3.46    3.65 1.00
## AxisInversion_c1:Valence_c1:Ed_c1 -0.60      1.84   -4.15    2.93 1.00
## AxisInversion_c1:Valence_c1:Ed_c2 -1.01      1.72   -4.36    2.41 1.00
## AxisInversion_c1:Valence_c1:Ed_c3 -1.17      1.89   -4.92    2.48 1.00
## AxisInversion_c1:Valence_c1:Ed_c4 -0.28      1.82   -3.79    3.33 1.00
## AxisInversion_c1:Valence_c1:Ed_c5 -0.49      1.91   -4.20    3.21 1.00
## AxisInversion_c1:Valence_c1:Ed_c6 0.00      1.85   -3.61    3.58 1.00
## AxisInversion_c1:Valence_c1:Ed_c7 -0.72      1.94   -4.54    3.09 1.00
##
##               Bulk_ESS Tail_ESS
## Intercept          5431    5727
## AxisInversion_c1    5544    6084
## Valence_c1          5968    6233
## Ed_c1              6863    5542
## Ed_c2              5084    5944
## Ed_c3              9866    6080
## Ed_c4              6734    6495
## Ed_c5             10334    6394
## Ed_c6              6828    5850
## Ed_c7              9538    6090
## AxisInversion_c1:Valence_c1 6660    6199
## AxisInversion_c1:Ed_c1  9799    5811
## AxisInversion_c1:Ed_c2  6957    6424
## AxisInversion_c1:Ed_c3 12949    6718
## AxisInversion_c1:Ed_c4  9485    5650
## AxisInversion_c1:Ed_c5 13421    6507

```

```
## AxisInversion_c1:Ed_c6          9004      6629
## AxisInversion_c1:Ed_c7          12187     5824
## Valence_c1:Ed_c1                11271     6110
## Valence_c1:Ed_c2                 7103     6025
## Valence_c1:Ed_c3                13088     5969
## Valence_c1:Ed_c4                 9439     6498
## Valence_c1:Ed_c5                11815     6635
## Valence_c1:Ed_c6                 9483     6651
## Valence_c1:Ed_c7                12665     6635
## AxisInversion_c1:Valence_c1:Ed_c1 13421     6723
## AxisInversion_c1:Valence_c1:Ed_c2  9483     6718
## AxisInversion_c1:Valence_c1:Ed_c3 15087     5296
## AxisInversion_c1:Valence_c1:Ed_c4 13741     6566
## AxisInversion_c1:Valence_c1:Ed_c5 14307     6366
## AxisInversion_c1:Valence_c1:Ed_c6 13595     6596
## AxisInversion_c1:Valence_c1:Ed_c7 13965     5555
##
```

Samples were drawn using sampling(NUTS). For each parameter, Bulk_ESS and Tail_ESS are effective sample size measures, and Rhat is the potential scale reduction factor on split chains (at convergence, Rhat = 1).

None of the interactions with the Ed predictor were significant (their 95% credible intervals all contained zero).

Speed-accuracy trade-off We now test the possibility that there was a speed-accuracy trade-off in responses. First, we need to do some wrangling to ensure the reaction time data are in the same dataframe as the accuracy data:

```
# Create new dataframe called `df_acc` with relevant columns from default dataframe `df`:
df_acc <- df %>% select(Subject, Version, Response, Accuracy)

# Change values in Response column so they match values in `df_RT` (reaction time) dataframe:
df_acc$Response[df_acc$Response == "V1_r"] <- "V1_RT"
df_acc$Response[df_acc$Response == "V2_r"] <- "V2_RT"
df_acc$Response[df_acc$Response == "V3_r"] <- "V3_RT"
df_acc$Response[df_acc$Response == "V4_r"] <- "V4_RT"

# Merge `df_acc` and `df_RT` dataframes, arrange by Subject column, and select relevant columns:
df_acc <- merge(df_acc, df_RT, by = c('Subject', 'Version', 'Response')) %>%
  arrange(Subject) %>%
  select(Subject, AxisInversion, Orientation, Valence, Accuracy = Accuracy.x, Measurement)
```

Look at the mean reaction times for incorrect and correct responses:

```
df_acc %>%
  group_by(Accuracy) %>%
  summarise(mean(as.numeric(Measurement)))

## `summarise()` ungrouping output (override with `.groups` argument)
## # A tibble: 2 x 2
##   Accuracy `mean(as.numeric(Measurement))`
##   <fct>          <dbl>
## 1 wrong          4.77
## 2 right          4.53
```

Incorrect responses were more likely to be slower, which is the opposite of what we'd expect from a speed-

accuracy trade-off.

Now, look at this solely for graphs that plotted quantity on the y-axis:

```
df_x <- df_acc %>% filter(Orientation == 'quant_x')
df_x %>% group_by(Accuracy) %>% summarise(mean(as.numeric(Measurement)))
```

```
## `summarise()` ungrouping output (override with `.groups` argument)
```

```
## # A tibble: 2 x 2
##   Accuracy `mean(as.numeric(Measurement))`
##   <fct>                                <dbl>
## 1 wrong                                6.08
## 2 right                                5.24
```

Even for these graphs, correct responses were more likely to be quicker than incorrect responses.