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Memetic Firefly Algorithm for Combinatorial Optimization

BIOMA 2012

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Bohinj, 24. May – 25. May 2012

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Motivation

- To show that memetic Firefly algorithm can also be used by solving of combinatorial optimization problems.
- To show that the memetic Firefly is comparable with the well-known heuristics for graph coloring, as Tabucol (Hertz & de Werra, 1987) and HEA (Galinier & Hao, 1999).
- To show that memetic Firefly improves the results of the EA-SAW (Eiben et al. 1998) that is well-known evolutionary algorithm for graph 3-coloring.

Characteristics of the problem

- ▣ NP-complete problem
- ▣ Constraint Optimization Problem (COP)
- ▣ The hardest instances occur near to the *phase transition* (Turner, 1988; Petford & Welsh, 1989; Hayes, 2003)
- ▣ Existing algorithms:
 - DSatur (Brelaz, 1979) greedy algorithm,
 - Tabucol (Hertz & de Werra, 1986),
 - EA with method SAW (Eiben et al. 1998),
 - HEA (Galinier & Hao, 1999).

Biological basis of Firefly Algorithm

- Firefly Algorithm (FFA) was proposed by Xin-She Yang in 2007.
- FA is inspired by the flashing behavior of fireflies

Firefly Algorithm

- Population based algorithm

Algorithm 1 Pseudo code of the MFFA algorithm

```
1:  $t = 0$ ;  $fe = 0$ ;  $found = \mathbf{FALSE}$ ;  
2:  $P^{(t)} = \text{InitializeFFA}()$ ;  $best = \emptyset$ ;  
3: while (! $\text{TerminateFFA}(fe, found)$ ) do  
4:    $fe += \text{EvaluateFFA}(P^{(t)})$ ;  
5:    $P' = \text{OrderFFA}(P^{(t)})$ ;  
6:    $found = \text{FindTheBestFFA}(P^{(t)}, best)$ ;  
7:    $P^{t+1} = \text{MoveFFA}(P^t, P')$ ;  
8:    $t = t+1$ ;  
9: end while
```

Elements of the MFFA algorithm

- ▣ **Representation:** real-valued vector $Y_i = \{w_{ij}\}$
- ▣ **InitializeFFA:** population is initialized randomly
- ▣ **EvaluateFFA:** evaluating the solution
- ▣ **OrderFFA:** forming an intermediate population
- ▣ **FindTheBestFFA:** determining the best solution in the population $P(t)$
- ▣ **MoveFFA:** moving the fireflies according to their neighbour's solutions
- ▣ **TerminateFFA:** number of function evaluations

Fitness calculation

- Attractiveness represents weights determining the order in which vertices are to be colored
- Fitness calculation consists of two steps:
 - Weights are transformed into a vertex permutation,
 - The permutation is decoded into graph 3-coloring by DSatur construction heuristic.
- Fitness function counts the number of uncolored vertices

Moving the fireflies

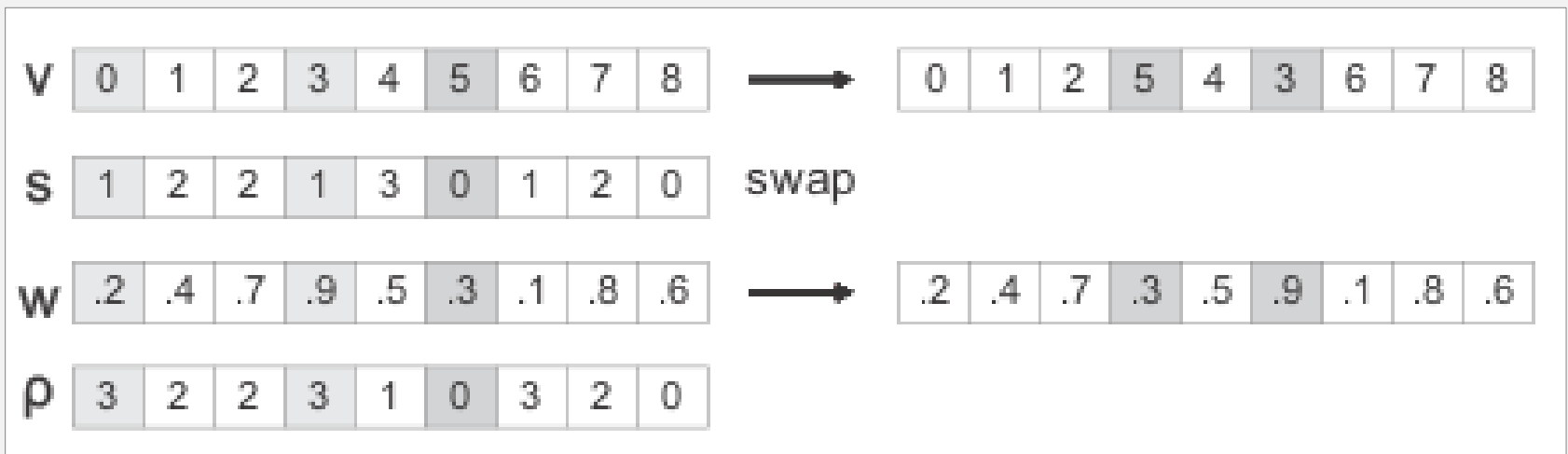
- Calculation of the new position:

$$\mathbf{w}_i = \mathbf{w}_i + \beta_0 \mathbf{e}^{-\gamma r_{i,j}^2} (\mathbf{w}_j - \mathbf{w}_i) + \alpha \left(rand(0,1) - \frac{1}{2} \right)$$

- \mathbf{w}_i : i -th firefly.
 - \mathbf{w}_j : j -th firefly.
 - β : beta parameter.
 - α : alfa parameter.
 - γ : gama parameter.
 - $rand(0,1)$ The random value in the range $[0,1]$.
- Stochastic large distance exploration

The heuristical swap local search

- Improving the current solution
- Using the heuristical swap unary operator



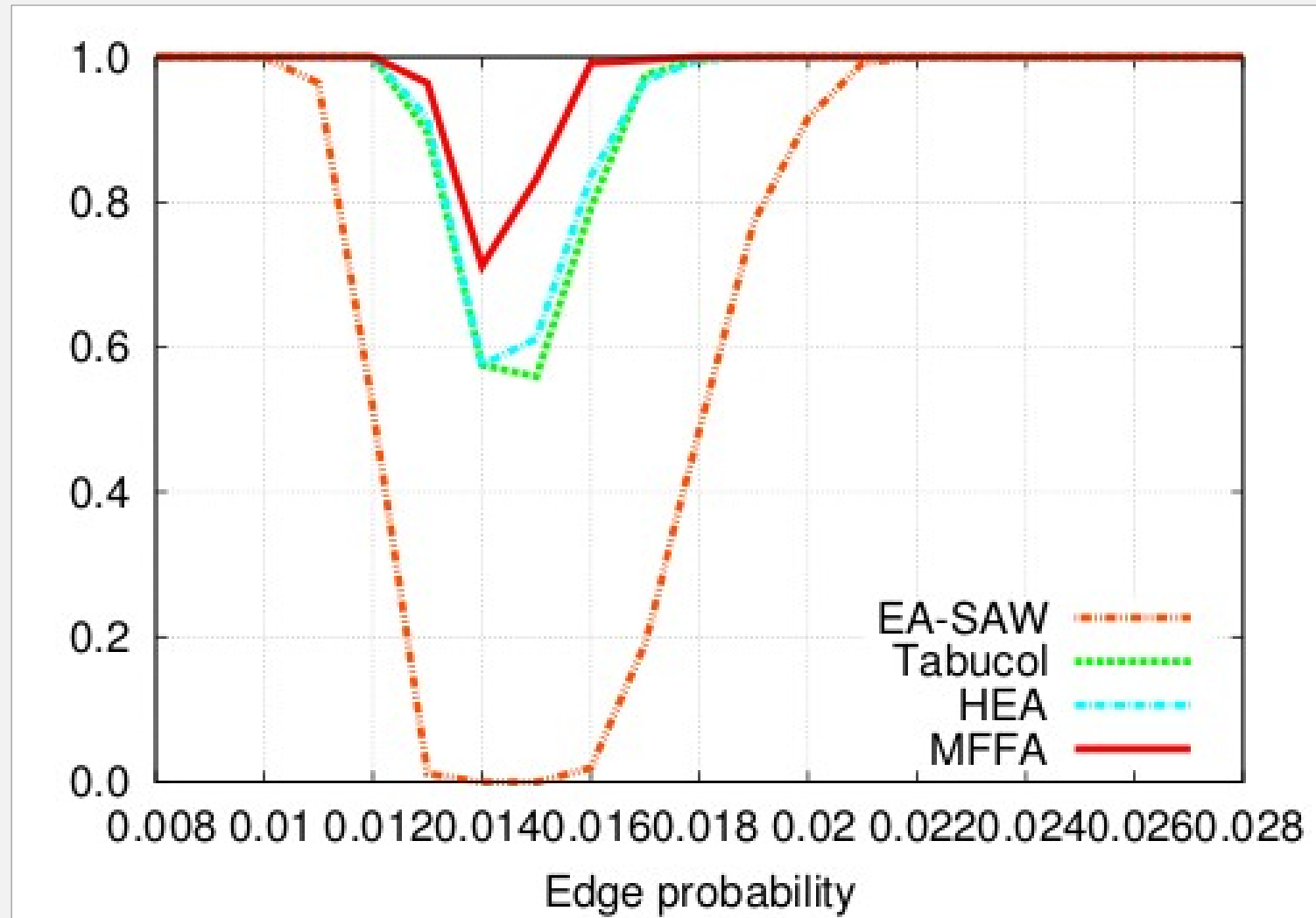
Experiments and results

- Comparison with:
 - Tabucol (Hertz & de Werra, 1986),
 - EA with method SAW (Eiben & al. 1998),
 - HEA (Galinier & Hao, 1999).
- All implementations can be downloaded from Internet
- Characteristics of MFFA:
 - Population size: $NP=500$,
 - Number of objective function evaluations: $FES=300,000$,
 - Number of runs: 25,
 - $\alpha =0.1$, $\beta =0.1$, $\gamma =0.8$.
- Measures:
 - Success rate (SR),
 - Average number of function evaluation (AES).

Test problems

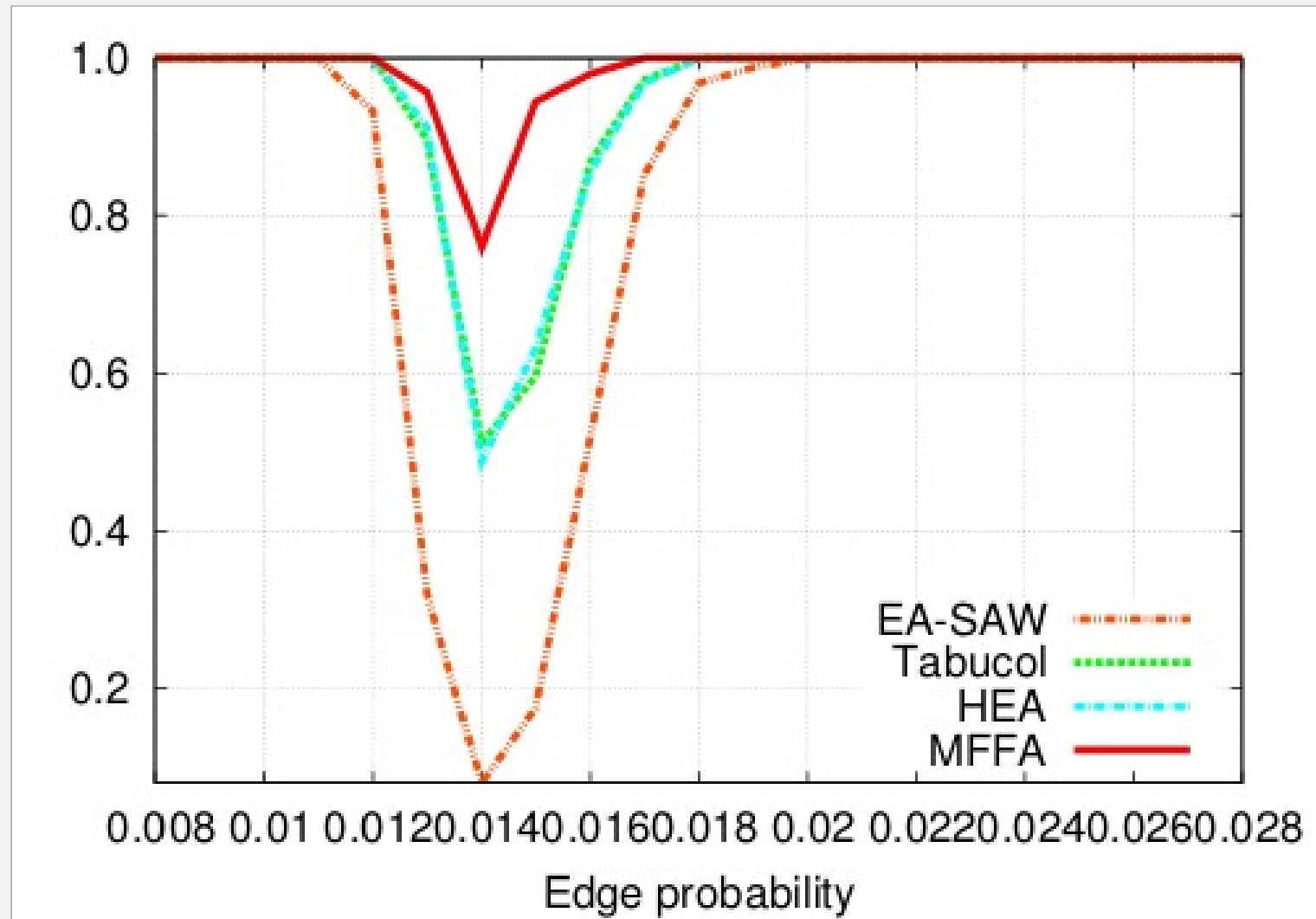
- Random graphs generated by Culberson's graph generator with following characteristics:
 - **types:** equi-partite, uniform, flat;
 - **sizes:** $n=500$ (also medium-scale graphs);
 - **edge density:** $p=0.008\dots0.028$ in steps of 0.001;
 - **seed:** $s=1\dots10$.
- Capture the phenomenon of *phase transition*, where graphs are really hard to color
- Phase transition occurs when $p=0.014$

Influence of the edge density 1/3



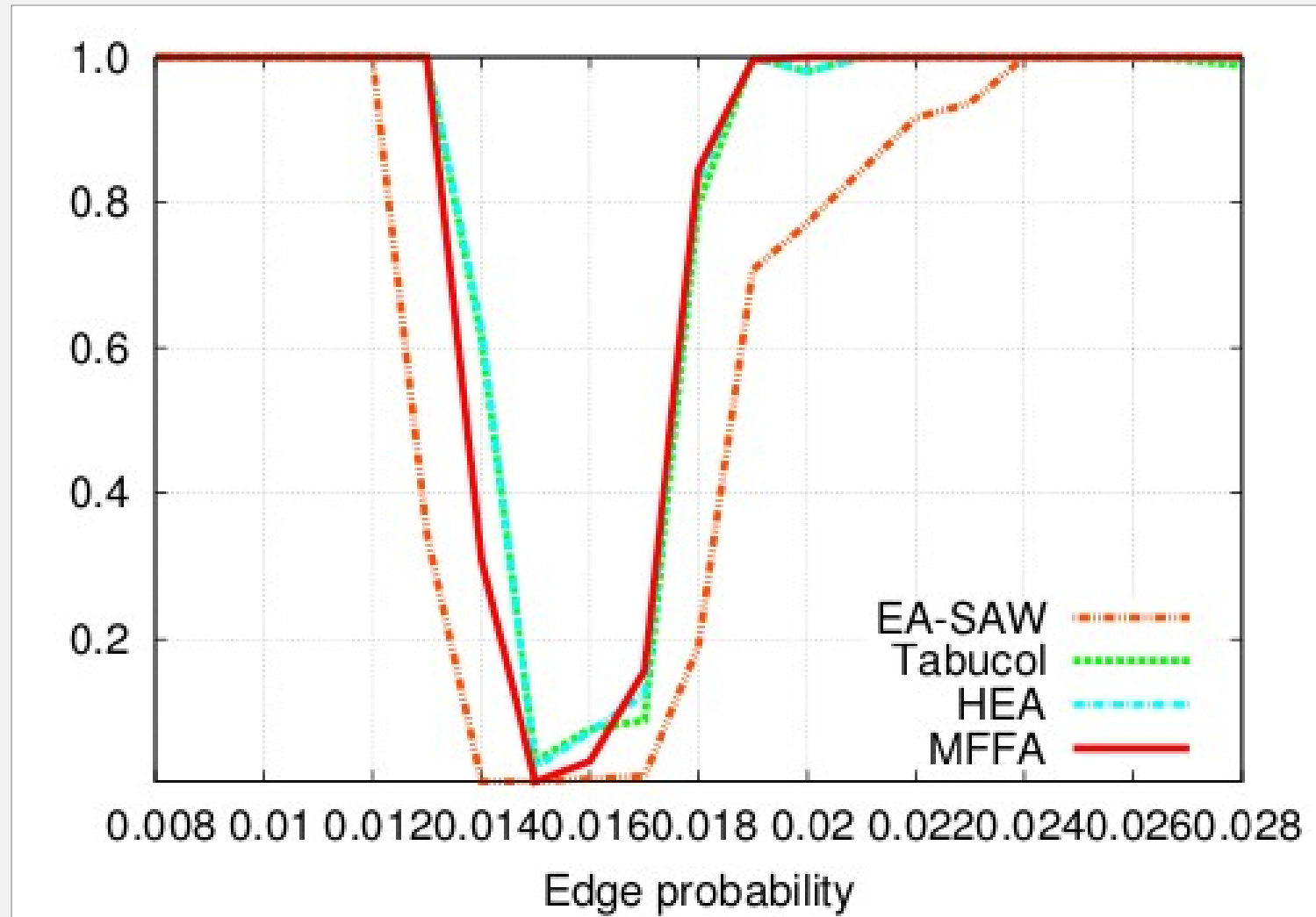
□ SR by uniform graphs.

Influence of the edge density 2/3



□ SR by equi-partite graphs.

Influence of the edge density 3/3



□ SR by flat graphs.

Discussion

- Exploration of search space depends on the best solution, i.e. elitism is used.
- The heuristic swap local search improves the current solutions
- α parameter determines the size of the randomness move within the search space
- Self-adaptation of the α parameter could improve the results of MFFA

Conclusion

- The results of MFFA is comparable with the results of Tabucol and HEA on medium-scale graphs
- MFFA improves results of EA-SAW by solving of all three type of medium-scale graphs
- As a result, MFFA could be successfully applied to solving of graph 3-coloring problem
- In the future, tests on large-scale graphs (1,000 vertices) would be conducted