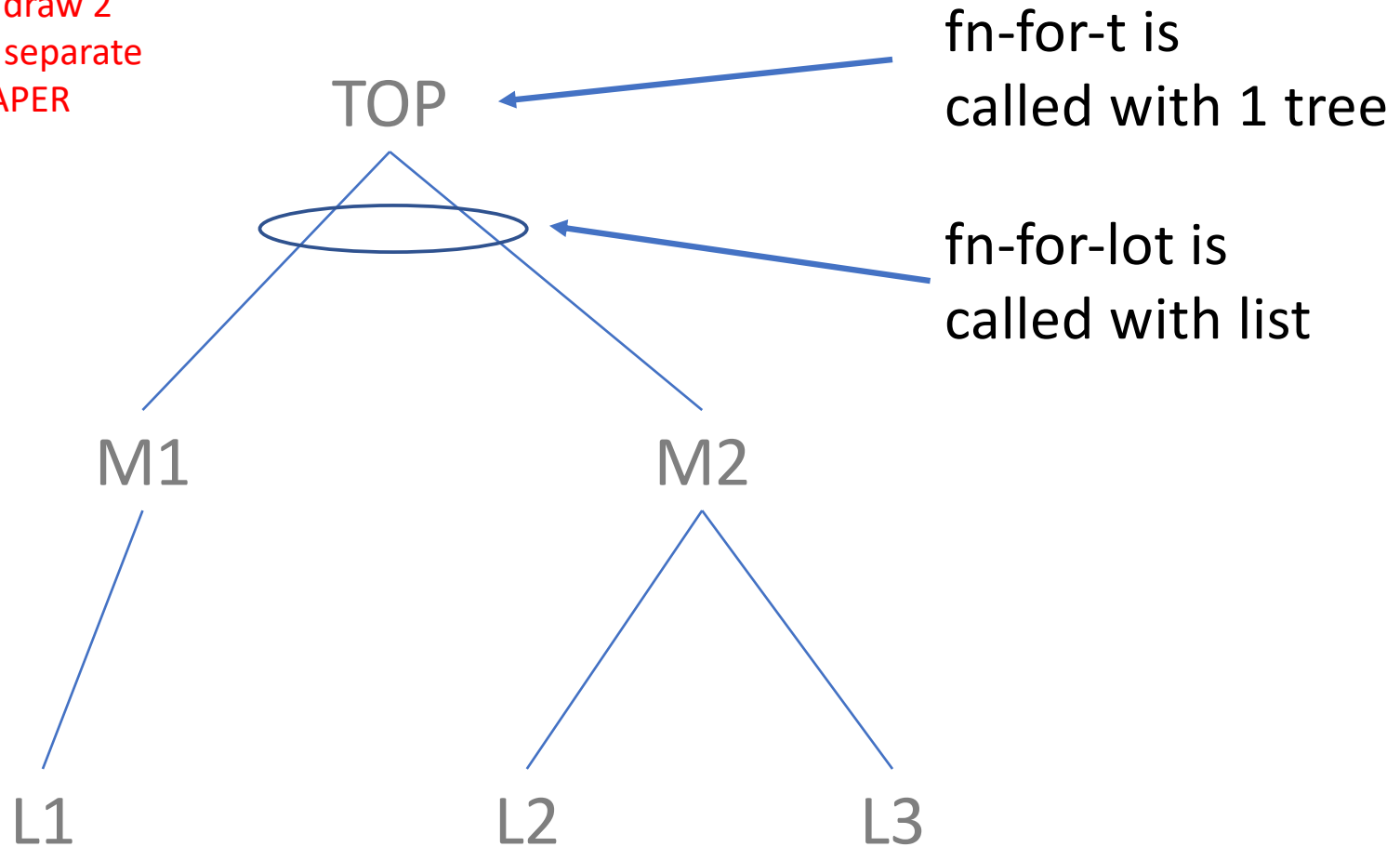


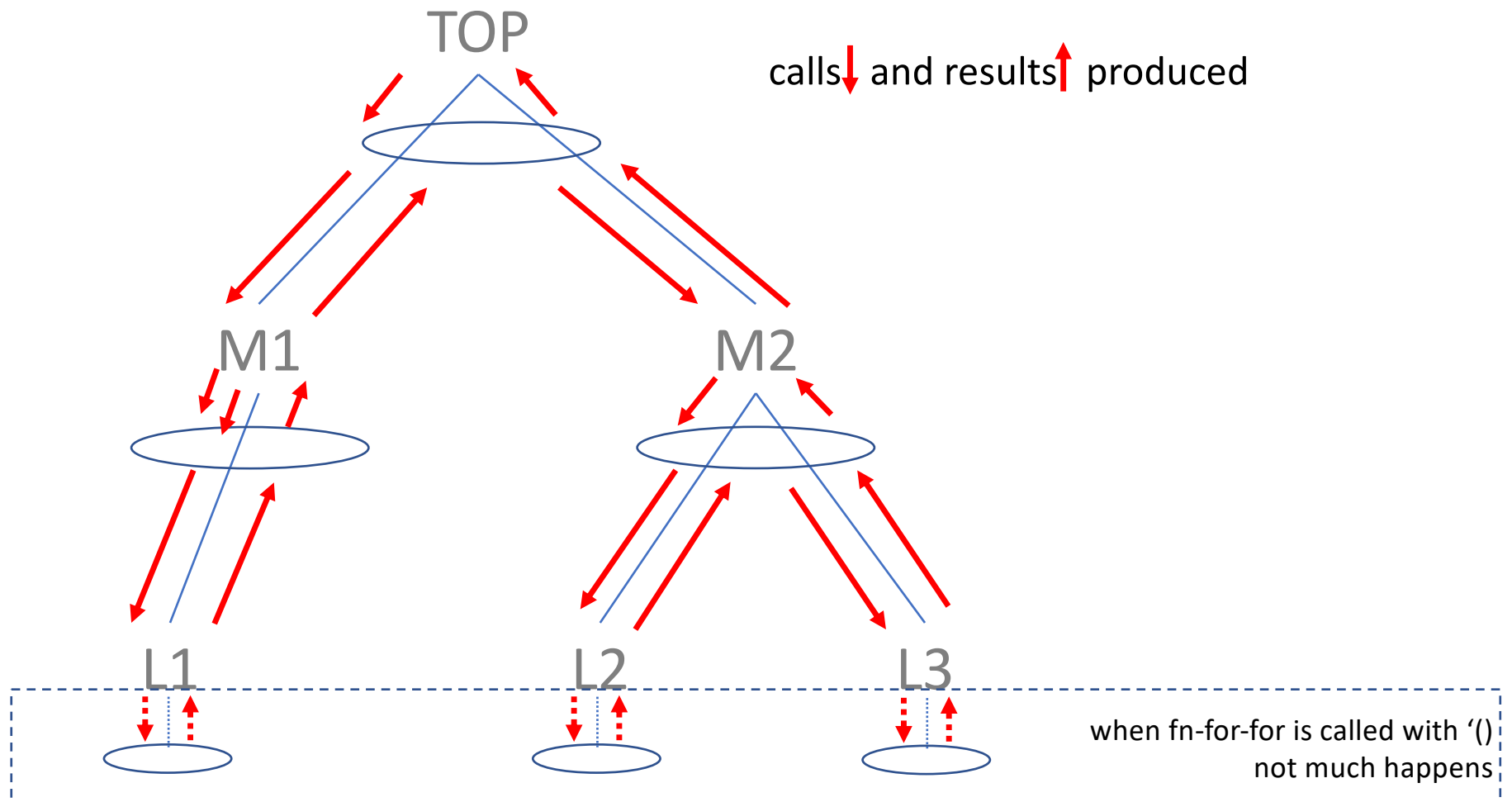
Lecture 19

While waiting, draw 2
copies of this on separate
sheets on PAPER



typical structural recursion

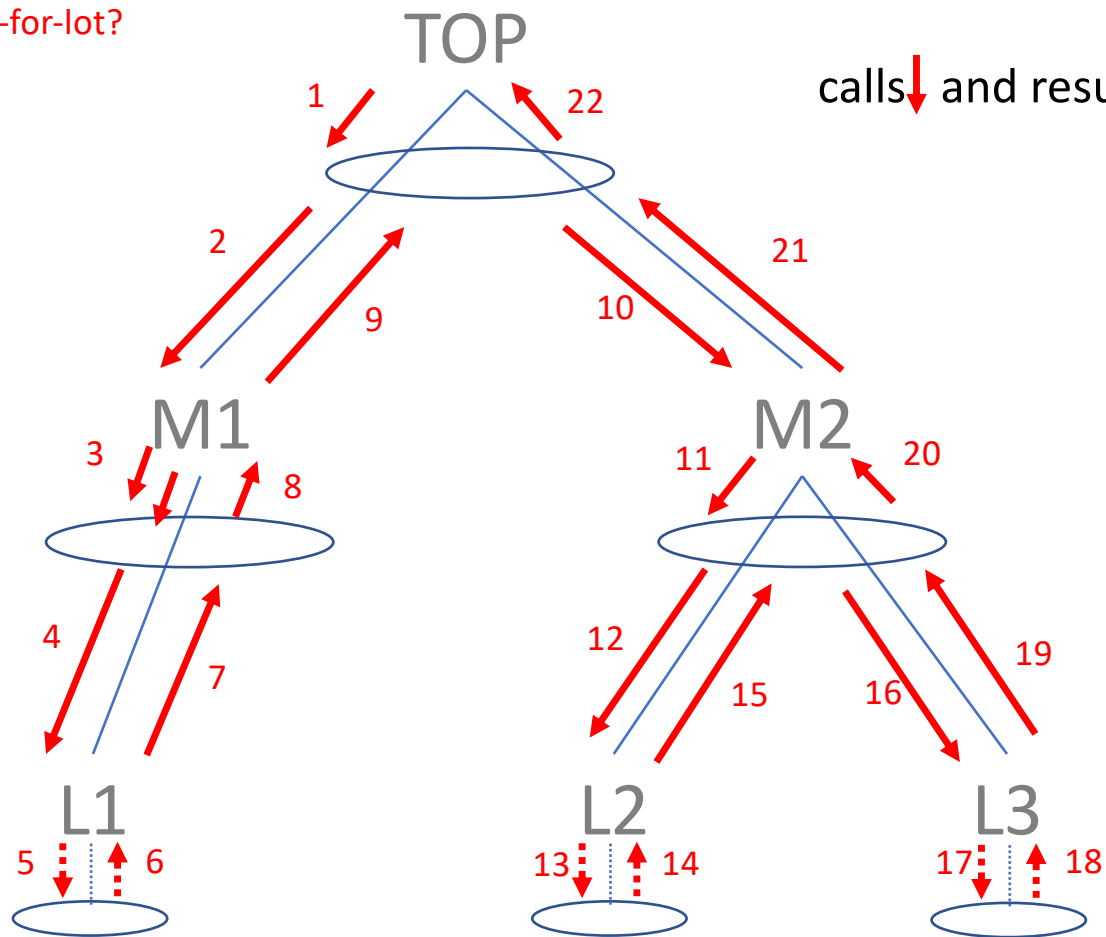
calls↓ and results↑ produced



What is value of path at each call to fn-for-lot?

typical structural recursion

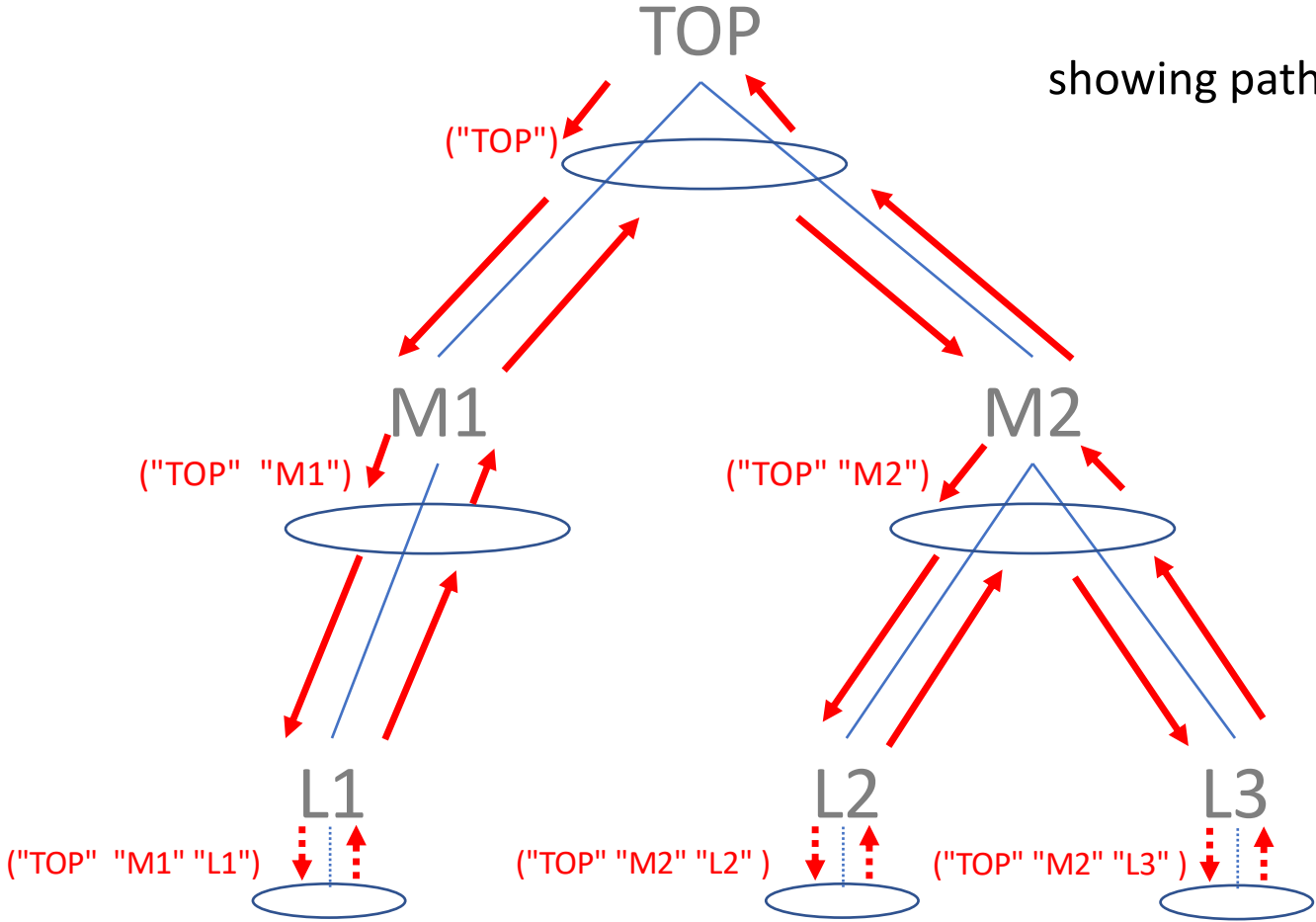
calls↓ and results↑ produced



path; names of parents to here

With path accumulator

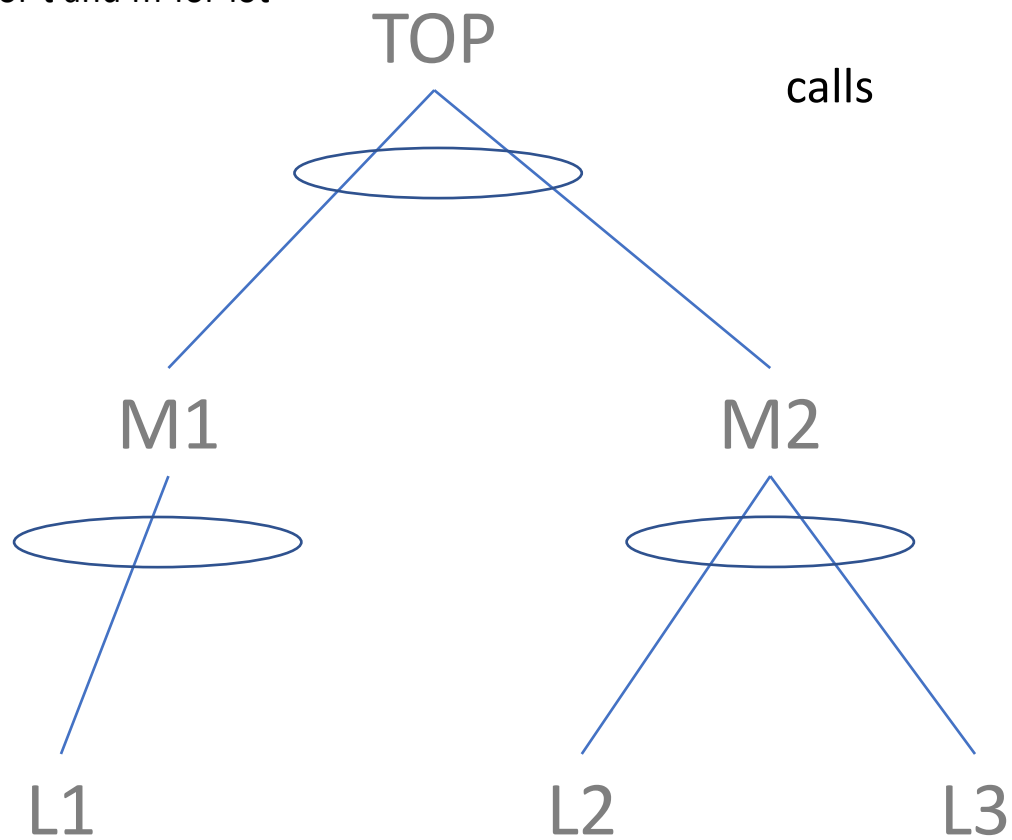
showing path at each call to fn-for-lot



tree worklist at fn-for-t and fn-for-lot

tail recursion with worklist

calls



tree worklist at fn-for-t and fn-for-lot

tail recursion with worklist

()
TOP

calls

(M1 M2)

M2

M1

M2 ()

L1 M2

L2 L3

M2

L1

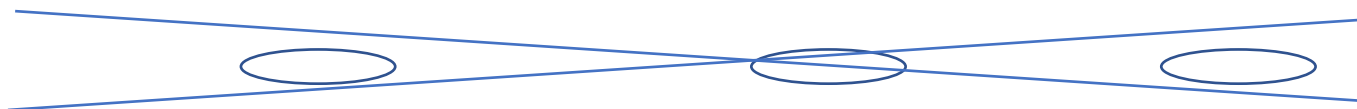
L3

L2

L3

() L3

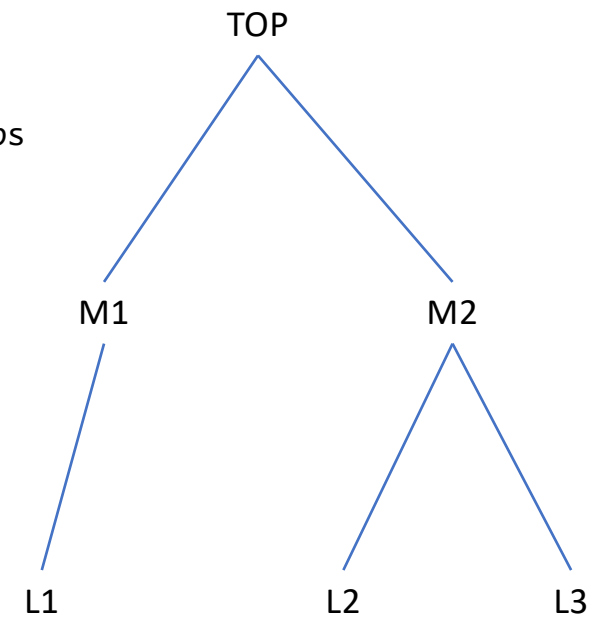
()



arb arity tree structural recursion templates

```
(define-struct node (name subs))  
;; Tree is (make-node String (listof Tree))  
;; interp. a bare bones arbitrary arity tree, each node has a name and subs
```

```
(define (fn-for-tree t)  
  (local [(define (fn-for-t t)  
            (local [(define name (node-name t)) ;unpack the fields  
                    (define subs (node-subs t))] ;for convenience  
  
              (... name (fn-for-lot subs))))]  
  
    (define (fn-for-lot lot)  
      (cond [(empty? lot) (...)]  
            [else  
             (... (fn-for-t (first lot))  
                   (fn-for-lot (rest lot))))]))]  
  
  (fn-for-t t)))
```

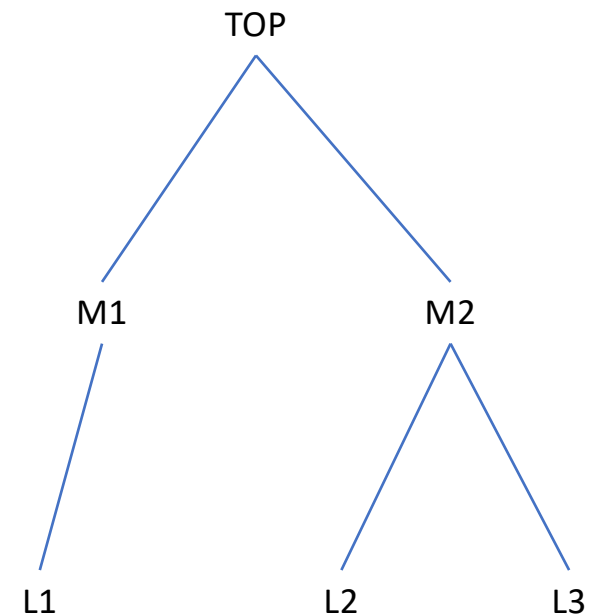


structural recursion with path accumulator.

```
(@template Tree (listof Tree) accumulator)

(define (find-path t n)
  ;; path is (listof String); names of ... grandparent, parent trees
  ;;                               (builds along recursive calls)
  (local [(define (fn-for-t t path)
            (local [(define name (node-name t))
                    (define subs (node-subs t))
                    (define npath (append path (list name)))]
              (if (string=? name n)
                  npath
                  (fn-for-lot subs npath))))
          (define (fn-for-lot lot path)
            (cond [(empty? lot) false]
                  [else
                   (local [(define try (fn-for-t (first lot) path))]
                     (if (not (false? try))
                         try
                         (fn-for-lot (rest lot) path))))])
          (fn-for-t t empty)))]

  (fn-for-t t empty)))
```



tail recursion with worklist

```
(@template backtracking Tree (listof Tree) accumulator)
```

```
;; Tail recursion
(define (find-tree t to)
  ;; todo is (listof Tree); worklist of pending trees to visit
  (local [(define (fn-for-t t t-wl)
            (local [(define name (node-name t)) ;unpack the fields
                    (define subs (node-subs t))] ;for convenience
              (if (string=? name to)
                  t
                  (fn-for-lot (append subs t-wl))))))

            (define (fn-for-lot t-wl)
              (cond [(empty? t-wl) false]
                    [else
                     (fn-for-t (first t-wl)
                               (rest t-wl))]))])

  (fn-for-t t empty)))
```

