Clicker

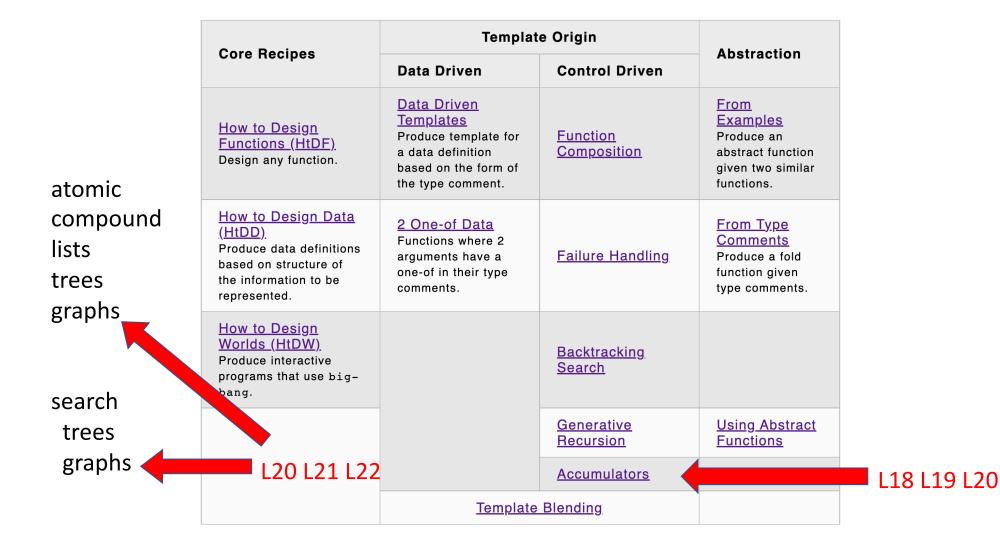
I thought the midterm was:

- A. Easier than expected
- B. About as hard as expected
- C. Harder than expected

Clicker

I should have:

- A. Completed fewer practice exams than I did
- B. Completed the same number of practice exams as I did
- C. Completed more practice exams than I did



Accumulators

- accumulate information from prior recursive calls
- three categories
 - preserve context from prior recursive calls
 - result so far

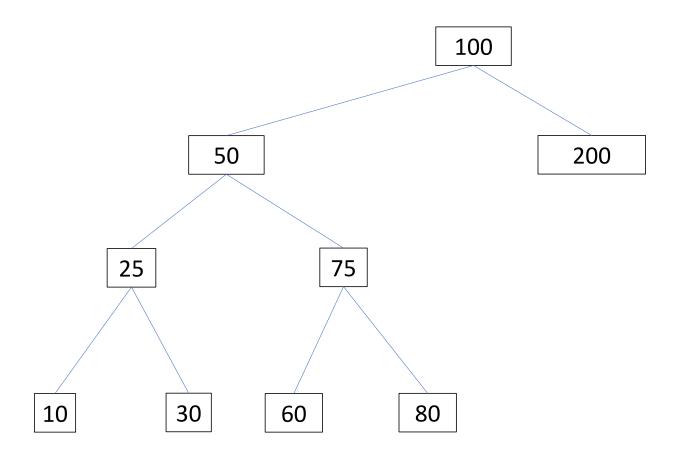
these overlap some

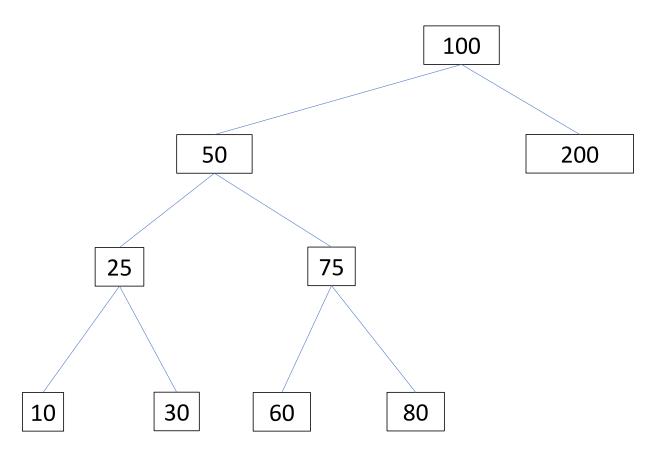
worklist next lecture

accumulator design recipe (htdf + this)

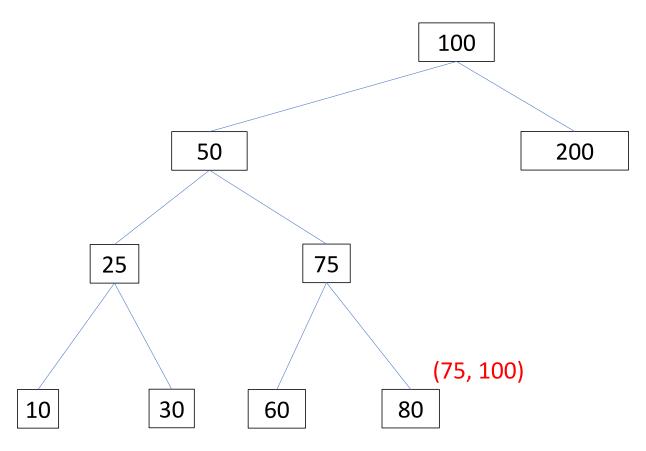
- templating:
 - recursive template wrapped in local and top-level function
 - add acc(umulator) parameter(s) to inner function
 - add acc after all ... (can use better name)
 - add (... acc) in recursive call
 - add ... in trampoline
- work out example progression of recursive calls
- wish for what the accumulator should be at the end
- work backward through progression to get accumulator at each step
- design type and invariant (may need a new data definition)
- initialize invariant, preserve invariant, exploit invariant
- test and debug

```
(@htdf sequence?)
(@signature (listof Natural) -> Boolean)
;; produces true if every element of lon is 1 greater than prior element
(check-expect (sequence? (list))
                                      true)
(check-expect (sequence? (list 2))
                                       true)
(check-expect (sequence? (list 2 3 4)) true)
(check-expect (sequence? (list 3 5 6)) false)
(check-expect (sequence? (list 2 3 4 7 5)) false)
(@template-origin (listof Natural) accumulator)
(define (sequence? lon0)
 ;; prev is Natural
 ;; invariant: the element of lon0 immediately before (first lon)
 ;; (sequence? (list 2 3 4 7 5))
 ;; (sequence? (list 3 4 7 5) 2)
 ;; (sequence? (list
                         4 7 5) 3)
 :: (sequence? (list
                       7 5) 4) ==> false
 (local [(define (sequence? lon prev)
            (cond [(empty? lon) true]
                  [else
                  (if (= (first lon) (+ 1 prev)) ;exploit (use)
                       (sequence? (rest lon)
                                  (first lon))
                                                 ;preserve
                       false))))
   (if (empty? lon0)
                                     ; if original list is empty, we can't
                                     ;initialize accumulator, so special case
       true
       (sequence? (rest lon0)
                   (first lon0)))) ; initialize
```





Why is 80 OK here? What range of numbers is OK here?



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```
(@htdf bst?)
(@signature BinaryTree -> Boolean)
;; produce true if bt satisfies binary search tree invariants
(check-expect (bst? BT1) true)
(check-expect (bst? BT2) false)
(check-expect (bst? BT3) false)
(check-expect (bst? BT4) false)
(check-expect (bst? BT5) false)
(@template-origin BinaryTree accumulator)
(define (bst? bt0)
  ;; lower is Integer
  ;; lower bound of key at current node
       initially -inf.0 is reset on recursions down a right branch
  ;; upper is Integer
      upper bound of key at current node
      initially +inf.0 is reset on recursions down a left branch
  ;;
  (local [(define (bst? bt lower upper)
            (cond [(false? bt) true]
                  [else
                   (and (< lower (node-k bt) upper)</pre>
                                                                      ;exploit
                        (bst? (node-l bt) lower
                                                        (node-k bt)) ;preserve
                        (bst? (node-r bt) (node-k bt) upper))]))] ;preserve
    (bst? bt0 -inf.0 +inf.0))):
                                                                      ;initialize
                              ;NOTE that we would never expect you to have
;;
                                    already known about these two constants!
;;
```