

INDIAN INSTITUTE OF TECHNOLOGY MADRAS  
Department of Chemical Engineering

**CH3050 Process Dynamics & Control**  
Assignment #2

Due: Monday, February 17, 2020

1. An exothermic reaction  $A \rightarrow 2B$ , takes place adiabatically in a stirred-tank reactor. This liquid reaction occurs at constant volume in a 1200-gallon reactor. The reaction is first order, irreversible with the rate constant given by  $k = 2.4 \times 10^{15} e^{-20000/T} (\text{min}^{-1})$  where  $T$  is in  $^{\circ}R$ .
  - (a) Using the information below, develop a first-principles model. State all assumptions that you make.
  - (b) Determine the steady-state exit temperature using `trim` in MATLAB.
  - (c) Derive a transfer function relating the exit temperature  $T$  to the inlet concentration  $c_{Ai}$  using MATLAB (`linmod`, `ss`, `ss2tf`). Verify your result with hand calculation.
  - (d) Compare the step response (to a 10% step in  $c_A$ ) of the non-linear and linearized systems. What is the extent of error in steady-state values?

**Steady-state conditions**

$$c_{Ai,ss} = 0.8 \text{ mol/ft}^3 \text{ and } F_{ss} = 20 \text{ gallons/min}$$

**Physical property data for the mixture**

$$T_i = 90^{\circ}\text{F}, C = 0.8 \text{ Btu/(lb } ^{\circ}\text{F)}, \rho = 52 \text{ lb / ft}^3 \text{ and } \Delta H_R = -500 \text{ kJ/mol}$$

2. (a) For a system described by the TF  $G(s) = (s+1)/(s^3+10s+31s+30)$ , write an equivalent SS description using two different methods (i) partial fraction expansion method (call this SS1) and (ii) state-transition diagram method (call this SS2). Compare SS1 and SS2 descriptions. Can you find a transformation matrix that takes SS2 to SS1? Explain.
- (b) Suppose, for a single-input two-output (SITO) system,  $y_1(t) = G_{11}u_1(t)$  and  $y_2(t) = G_{21}u_1(t)$ , where  $G_{11}(s) = \frac{4s+1}{(s+1)(s+3)}$  and  $G_{21}(s) = \frac{10s}{(s+2)(s+3)}$ . Arrive at a *minimal* order SS realization for the SITO system.
3. For the signal flow graph in Figure 1, (i) draw the block diagram relating  $R(s)$  to  $Y(s)$  and (ii) find the transfer function  $Y(s)/R(s)$ .

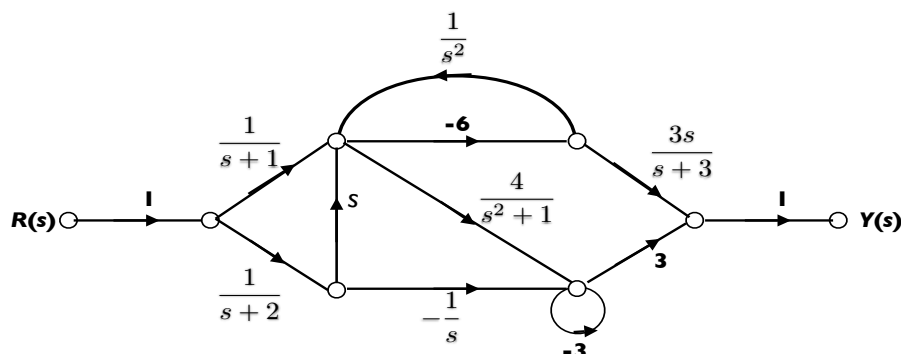


Figure 1: Signal flow graph for Q.3