

Complexity and the Edge of Chaos

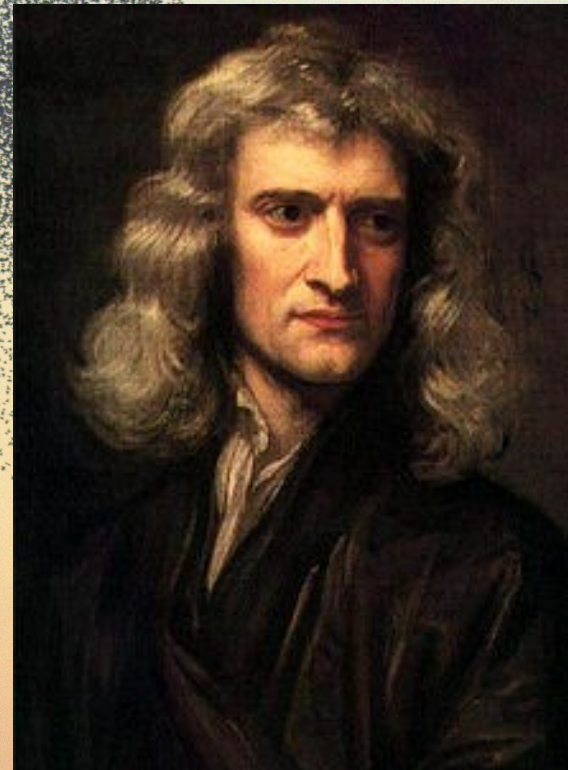
Matt Spraggs
CMG/ICSS/SHEP

Overview

- History
- Definitions and Characteristics
- Examples
- The Future

History: The Scientific Revolution

- Descartes: reductionism
- Newton: determinism



History: Laplace's Demon

- Unlimited:
 - Computational power
 - Knowledge of dynamics
 - Precision in variables
- Hence unlimited predictive power



History: Poincaré

- Three body problem
 - Aperiodic orbits
 - Some solutions
 - Sensitivity to initial conditions
- King Oscar II prize



History: The Clock Breaks Down

- Quantum Theory
 - True stochastic behaviour
- Chaos Theory
 - Sensitivity to initial conditions



History: A New Approach

- Some systems are “greater than the sum of their parts”
- Dispense with reductionism
- “What I cannot create, I do not understand.”



What is Complexity?

- Intuitive notions exist
- Many formal definitions, for example:
 - Size
 - Entropy
 - Algorithmic
- Each definition has its problems

What is Complexity?

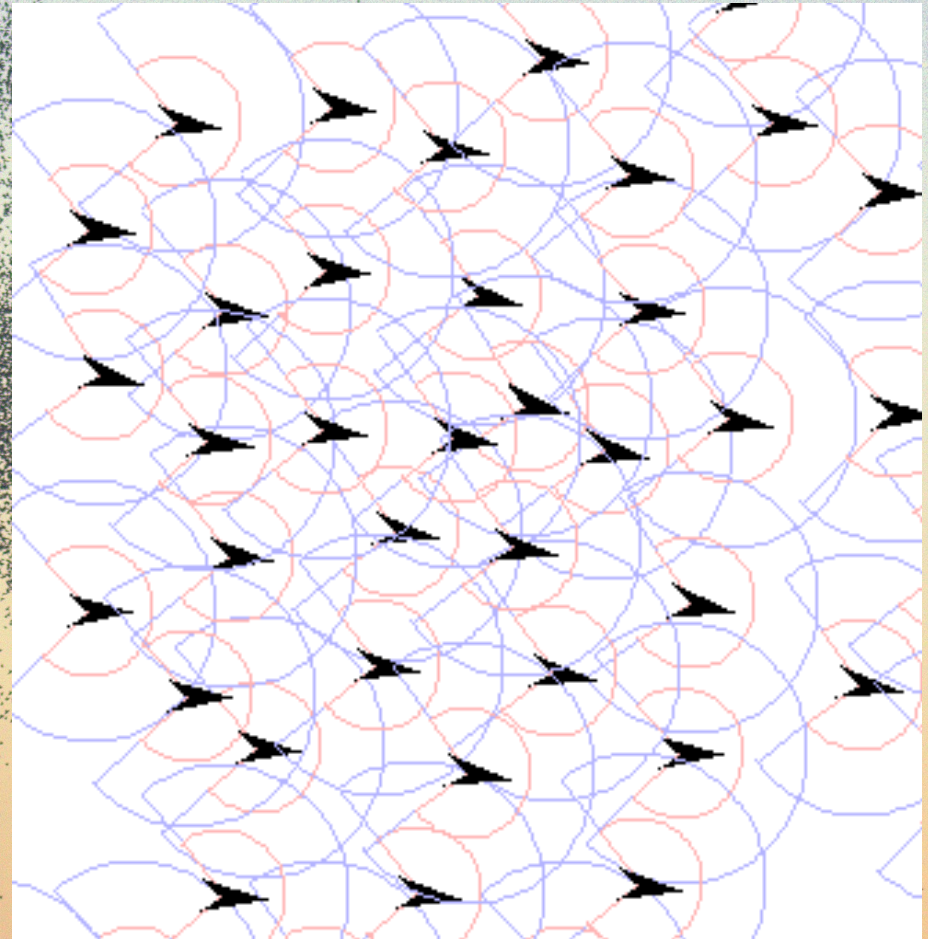
- Many interacting elements
- Sensitivity to system parameters
- Levels of behaviour/organisation
- “Emergent” group behaviour
- Self-organisation
- The “edge of chaos”

What is Complexity?

- Techniques
 - Agent based modelling
 - Dynamical systems theory
 - Dynamics on networks
 - Computing and simulation

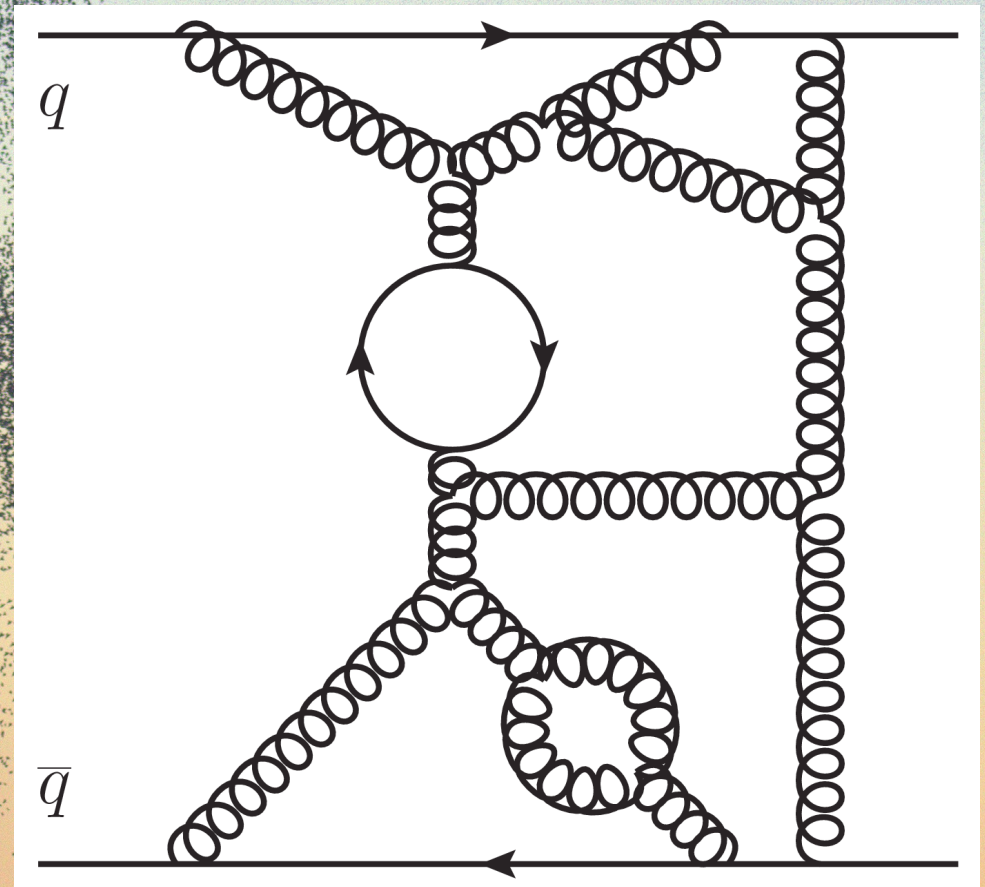
Examples: Flocking

- Boids – 1986
- Three rules
 - Avoidance
 - Cohesion
 - Alignment
- No centralised control
- Self organisation



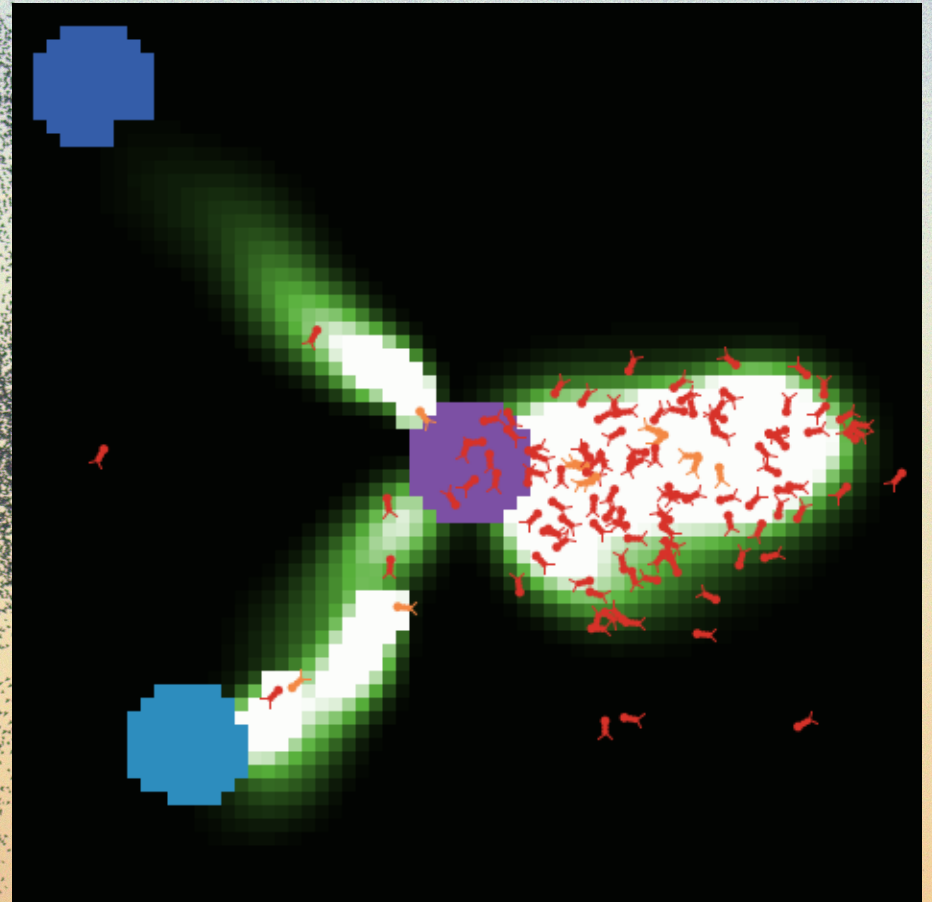
Examples: Lattice QCD

- Quarks and gluons
- Nonlinear Lagrangian
- Complex phenomena:
 - Hadrons
 - Asymptotic freedom
 - Confinement and hadronization



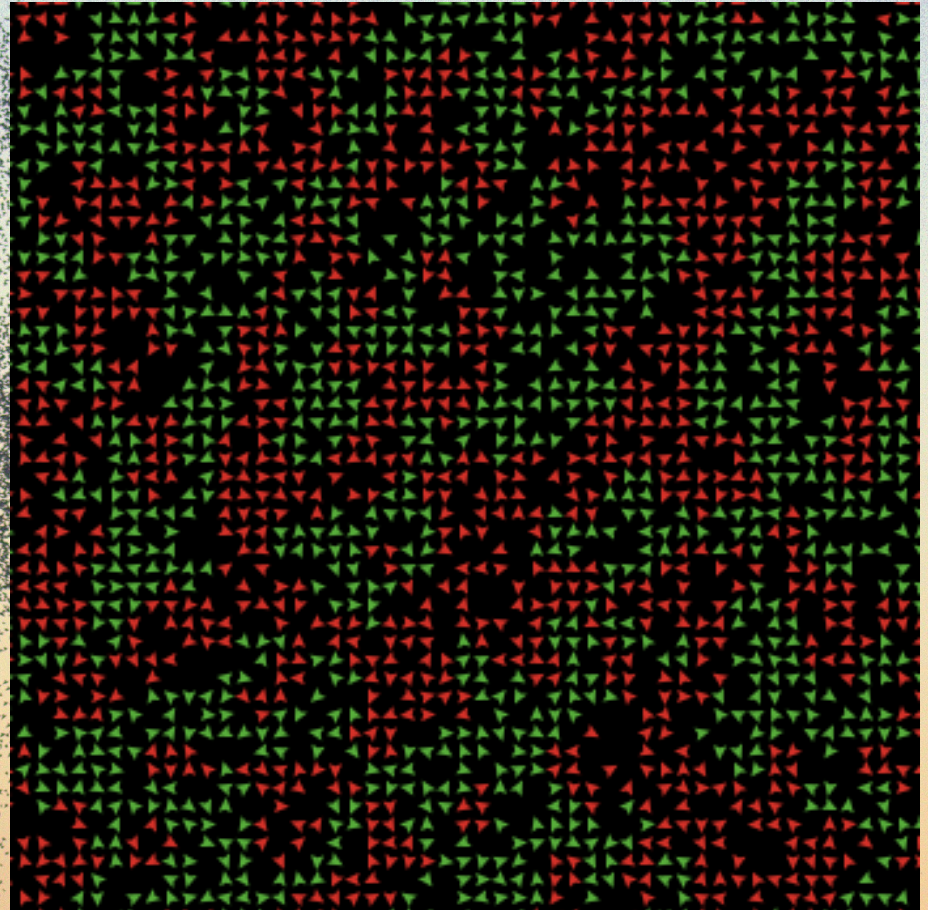
Examples: Foraging

- How do ants find food?
- Simple rules, complex behaviour
- Decentralised



Examples: Segregation

- Schelling model
- Agents are tolerant
 - E.g. 30% of neighbours must be like ourselves
- Segregation
 - Highly mixed configuration improbable



The Future

- A young discipline
- Increasing computing power
- “I think the next century will be the century of complexity.”

