## Examples of regression estimators with different rho functions

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Here are some examples illustrating the use of lmrobdetMM() and lmrobdetDCML() with different choices of rho functions (bisquare, optimal and modified optimal).

First, we load the library:

```
library(RobStatTM)
```

The first example uses the coleman data available in the robustbase package. By default lmrobdetMM uses a bisquare rho tuned to 85% asymptotic efficiency for Gaussian errors. The default breakdown point is 50%.

```
data(coleman, package = "robustbase")
coef(m2 <- lmrobdetMM(Y ~ ., data = coleman))</pre>
## (Intercept)
                    salaryP
                               fatherWc
                                                        teacherSc
                                             sstatus
                                                                    motherLev
## 29.48394602 -1.65635168 0.08326375
                                         0.66565464
                                                      1.17784872 -4.00376846
coef(m0 \leftarrow lm(Y \sim ., data = coleman))
## (Intercept)
                                                       teacherSc
                    salaryP
                               fatherWc
                                             sstatus
                                                                    motherLev
## 19.94856503 -1.79333327 0.04360156 0.55576006 1.11016839 -1.81092194
To use the optimal or modified optimal rho (also with default asymptotic efficiency of 85%), we use
coef(m4 <- lmrobdetMM(Y ~ ., data = coleman, control = lmrobdet.control(family = "modified.optimal")))</pre>
## (Intercept)
                    salaryP
                               fatherWc
                                             sstatus
                                                        teacherSc
                                                                    motherLev
## 29.75770013 -1.69734324 0.08511131 0.66615071 1.18378682 -4.06634517
coef(m5 <- lmrobdetMM(Y ~ ., data = coleman, control = lmrobdet.control(family = "optimal")))</pre>
## Warning in lmrob.fit(X, y, control, init = S.init, mf = mf): M-step did NOT
## converge. Returning unconverged 1M-estimate
## (Intercept)
                    salaryP
                               fatherWc
                                             sstatus
                                                       teacherSc
                                                                    motherLev
## 30.45276762 -1.69449992 0.09009071 0.67811958 1.21315201 -4.34422411
```

## DCML

The DCML estimator is "between" the MM one and the LS one, as expected:

The algorithm failed to converge when using the optimal rho.

```
coef(m1 <- lmrobdetDCML(Y ~ ., data = coleman))</pre>
## (Intercept)
                                                                    motherLev
                    salaryP
                               fatherWc
                                             sstatus
                                                       teacherSc
## 25.3586308
                -1.7156144
                              0.0661046
                                           0.6181107
                                                       1.1485680
                                                                   -3.0550719
coef(m2)
## (Intercept)
                    salaryP
                               fatherWc
                                             sstatus
                                                       teacherSc
                                                                    motherLev
## 29.48394602 -1.65635168 0.08326375 0.66565464 1.17784872 -4.00376846
```

```
coef(m0)
## (Intercept)
                                                       teacherSc
                   salaryP
                               fatherWc
                                             sstatus
                                                                   motherLev
## 19.94856503 -1.79333327
                            0.04360156  0.55576006  1.11016839  -1.81092194
Similarly, when we use a non-bisquare rho function:
coef(m10 <- lmrobdetDCML(Y ~ ., data = coleman, control = lmrobdet.control(family = "modified.optimal")</pre>
## (Intercept)
                   salaryP
                               fatherWc
                                             sstatus
                                                       teacherSc
                                                                   motherLev
                                         0.61929745
                                                     1.15254084 -3.10907260
## 25.59439462 -1.73808443 0.06749327
coef(m4)
## (Intercept)
                                                       teacherSc
                   salaryP
                               fatherWc
                                             sstatus
                                                                   motherLev
## 29.75770013 -1.69734324 0.08511131 0.66615071
                                                     1.18378682 -4.06634517
coef(m0)
## (Intercept)
                   salaryP
                               fatherWc
                                            sstatus
                                                       teacherSc
                                                                   motherLev
## 19.94856503 -1.79333327
                             0.04360156 0.55576006
                                                     1.11016839 -1.81092194
```

## Unintuitive behaviour of modified.optimal

A behaviour that appears to be unintuitive is that as we increase the desired asymptotic efficiency, the estimators computed with the optimal / modified optimal rho do not seem to get closer to the least squares one.

When using the bisquare family of rho, as we increase the desired asymptotic efficiency, the MM-estimator approaches the least squares one. For example

```
coef(m2.eff <- lmrobdetMM(Y ~ ., data = coleman, control = lmrobdet.control(efficiency = 0.9999)))</pre>
## (Intercept)
                    salaryP
                               fatherWc
                                             sstatus
                                                       teacherSc
                                                                    motherLev
## 20.49300018 -1.78830691 0.04578737 0.56128534 1.11334086 -1.93145829
coef(m0)
## (Intercept)
                    salaryP
                               fatherWc
                                             sstatus
                                                        teacherSc
                                                                    motherLev
## 19.94856503 -1.79333327
                             0.04360156
                                                      1.11016839 -1.81092194
                                         0.55576006
Something similar happens for the DCML estimator based on an MM-estimator computed with a bisquare
rho function, which seems to be identical to the least squares estimator:
coef(m3 <- lmrobdetDCML(Y ~ ., data = coleman, control = lmrobdet.control(efficiency = 0.9999)))</pre>
## (Intercept)
                    salaryP
                               fatherWc
                                             sstatus
                                                       teacherSc
                                                                    motherLev
## 19.94856503 -1.79333327 0.04360156 0.55576006 1.11016839 -1.81092194
However, if we use a modified optimal rho, the results are very different:
coef(m7 <- lmrobdetMM(Y ~ ., data = coleman, control = lmrobdet.control(family = "modified.optimal",</pre>
    efficiency = 0.9999)))
## (Intercept)
                                                       teacherSc
                   salaryP
                               fatherWc
                                             sstatus
                                                                    motherLev
## 34.25477283 -1.61792045 0.08544125 0.67387777 1.11029441 -4.56713985
coef(m6 <- lmrobdetDCML(Y ~ ., data = coleman, control = lmrobdet.control(family = "modified.optimal",</pre>
    efficiency = 0.9999)))
## (Intercept)
                    salaryP
                               fatherWc
                                             sstatus
                                                       teacherSc
                                                                    motherLev
```

```
## 27.82362671 -1.69677471 0.06663283 0.62077968 1.11023776 -3.32812247 coef(m0)
```

## (Intercept) salaryP fatherWc sstatus teacherSc motherLev ## 19.94856503 -1.79333327 0.04360156 0.55576006 1.11016839 -1.81092194