Information Retrieval Behind the Scene of Web Search

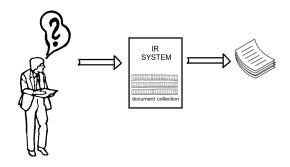
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What is Information Retrieval?

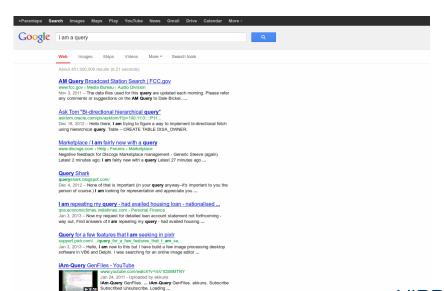


A Definition

Information retrieval (IR) is <u>finding material</u> (usually documents) of an <u>unstructured nature</u> (usually text) that satisfies an <u>information need</u> from within <u>large collections</u> (usually stored on computers).



An Example



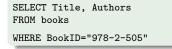


Databases vs IR: getting a book from library

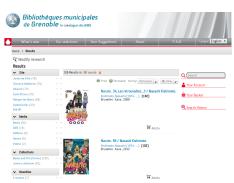
Structured Queries



Databases are fully structured, and require structured queries for retrieval.



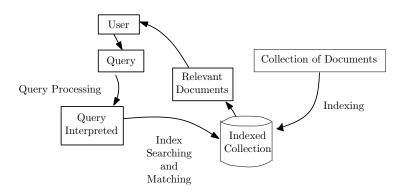
Searching by Words



IR systems require words to find results containing those words.

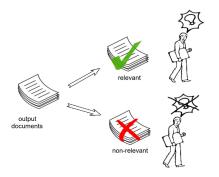


IR Procedure





How Good is a System: Relevant and Non-relevant



All that an IR system returns may not be relevant and required.

$Precision = \frac{\text{number of relevant documents retrieved}}{\text{number of all documents retrieved}}$



Ranked Retrieval

Non-ranked Retrieval



The IR system returns a bunch of documents, without any ordering.

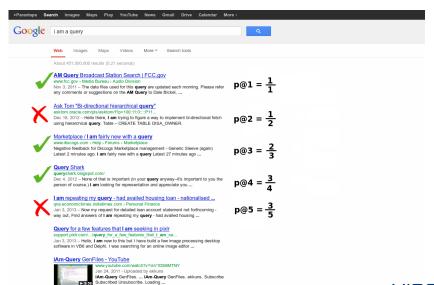
Ranked Retrieval



- The IR system returns a ranked document set.
- Documents are ranked based on score.
- Scores are given by different scoring models.



Evaluation of Ranked Retrieval Sets





Evaluation of Ranked Retrieval Sets

Average Precision

$$AP_{q_j} = \frac{1}{m_j} \sum_{k=1}^{m_j} Precision(R_{jk})$$

- $q_j \rightarrow$ given query
- $D = \{d_1, \dots d_{m_i}\} \rightarrow \text{set of retrieved documents}$
- $R_{jk} o$ is the set of ranked retrieval results from the top result until you get to document d_k

Mean Average Precision (MAP)

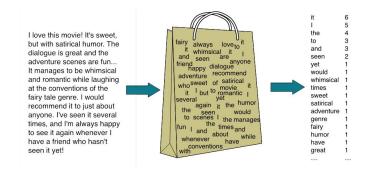
Let the query set is Q.

$$MAP = \frac{1}{|Q|} \sum_{j=1}^{|Q|} AP_{q_j}$$



Representing Text: Bag of Words

- A simplifying representation used in natural text processing
- A text (such as a sentence or a document) is represented as the bag of its words:
 - disregards: grammar, word ordering
 - · maintains: multiplicity





Text to Matrix: Count Matrix

| | Anthony and | Julius Caesar | The Tempest | Hamlet | Othello | Macbeth |
|-----------|----------------|------------------|----------------|--------|---------|---------|
| | Cleopatra | | | | | |
| anthony | 157 | 73 | 0 | 0 | 0 | 1 |
| brutus | 4 | 157 | 0 | 2 | 0 | 0 |
| caesar | 232 | 227 | 0 | 2 | 1 | 0 |
| calpurnia | 0 | 10 | 0 | 0 | 0 | 0 |
| cleopatra | 57 | 0 | 0 | 0 | 0 | 0 |
| mercy | 2 | 0 | 3 | 8 | 5 | 8 |
| worser | 2 | 0 | 1 | 1 | 1 | 5 |
| | | | | | | |

Each document is now represented as a count vector $\in \mathbb{N}^{|V|}$.

Vocabulary

Vocabulary is the set of unique words/terms present in the collection.

For example: {anthony, brutus, caesar...}



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Term Frequency

- The term frequency $tf_{t,d}$ of term t in document d is defined as the number of times that t occurs in d.
- A document with tf = 10 occurrences of a term is more relevant than a document with tf = 1 occurrence of the term.
 - Relevance does not increase proportionally with term frequency.
- The frequency of the term in the collection...
 - Some terms are rare (e.g. EPISTEMOPHOBIA).
 - Some terms are frequent (e.g. INFORMATION)
 - Rare terms are more informative than frequent terms.
 - Rare terms should have higher weights than frequent terms.



Document Frequency

- We want:
 - higher weights for rare terms like EPISTEMOPHOBIA.
 - lower (but positive) weights for frequent terms like INFORMATION.
- The document frequency df_t of a term t is the number of documents in the collection that t occurs in.
- Rare terms will have lower df than frequent terms.
- df_t is an inverse measure of the informativeness of term t.



Inverse Document Frequency

Inverse document frequency idf_t of term t is:

$$Idf_t = \log \frac{N}{df_t}$$

(N is the number of documents in the collection.)

- idf_t is a measure of the informativeness of the term.
- In the query "epistemophobia information", idf weighting increases the relative weight of EPISTEMOPHOBIA and decreases the relative weight of INFORMATION.



TF-IDF Scoring

 The tf-idf weight of a document d w.r.t a query term t is the product of its tf_{t,d} and idf_d.

$$score_{tf-idf}(t,d) = (tf_{t,d}).\left(\log \frac{N}{df_t}\right)$$

- The tf-idf score:
 - increases with the number of occurrences of t within d. (term frequency)
 - increases with the rarity of the term in the collection. (inverse document frequency)
- One of the classical weighting scheme in information retrieval.



Weight Matrix

| | Anthony and Cleopatra | Julius Caesar | The Tempest | Hamlet | Othello | Macbeth |
|-----------|-----------------------------|------------------|----------------|--------|---------|---------|
| anthony | 157 | 73 | 0 | 0 | 0 | 1 |
| brutus | 4 | 157 | 0 | 2 | 0 | 0 |
| caesar | 232 | 227 | 0 | 2 | 1 | 0 |
| calpurnia | 0 | 10 | 0 | 0 | 0 | 0 |
| cleopatra | 57 | 0 | 0 | 0 | 0 | 0 |
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. . .



Weight Matrix

| | Anthony and Cleopatra | Julius Caesar | The Tempest | Hamlet | Othello | Macbeth |
|--------------------|-----------------------------|------------------|----------------|-------------|-------------|-------------|
| anthony | 5.25 | 3.18 | 0.0 | 0.0 | 0.0 | 0.35 |
| brutus | 1.21 | 6.10 | 0.0 | 1.0 | 0.0 | 0.0 |
| caesar | 8.59 | 2.54 | 0.0 | 1.51 | 0.25 | 0.0 |
| calpurnia | 0.0 | 1.54 | 0.0 | 0.0 | 0.0 | 0.0 |
| cleopatra | 2.85 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| mercy | 1.51 | 0.0 | 1.90 | 0.12 | 5.25 | 0.88 |
| worser | 1.37 | 0.0 | 0.11 | 4.15 | 0.25 | 1.95 |
| cleopatra mercy | 2.85 1.51 | 0.0 | 0.0 1.90 | 0.0 0.12 | 0.0 5.25 | 0.0 0.88 |

. . .

Each document is now represented as a real-valued vector of tf-idf weights $\in \mathbb{R}^{|V|}$.

 $V \implies$ the vocabulary of the collection under consideration



Vector Space Model

- The Vector Space Model is an algebraic model for representing text documents as vectors
- In this model:
 - Each document d of a collection C is represented with a vector $\vec{d} \in \mathbb{R}^{|V|}$
 - ullet Dimension of the vector $ec{d}$ is the size of the vocabulary |V|
 - Vector space constructed is a space of terms in which each dimension is associated with a term of the collection
- To score documents w.r.t queries:
 - **Q** Each query q is similarly represented by a vector $\vec{q} \in \mathbb{R}^{|V|}$ of same dimension
 - Rank documents according to their similarity to the query.
- Cosine similarity is used to measure similarity between query and document.

$$\mathit{score}_{\mathit{vspace}}(q,d) = \cos(ec{q},ec{d}) = rac{ec{q}.ec{d}}{|ec{q}|.|ec{d}|}$$



BM25

Key Idea

A term appearing in a small distinct number of documents with high frequency is far more important than the terms appearing in a large number of documents with very low frequency.

Elite Terms for a Document

Terms having a high term frequency in the document in question but low document frequency.

To score a document d for a word t in query q:

- the importance of term t in document d is proportional to the term frequency of t in d
- the importance of term t is inversely proportional to the document frequency of t
- the score is weighted by the number of occurrences of the term t inside the query q itself

Key Idea

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Elite Terms for a Document

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BM25 equation

$$score_{BM25}(q,d) = \sum_{t \in q \cap d} \underbrace{\frac{(k_1 + 1) \times tf_t^d}{k_1 \left((1 - b) + b \frac{f_d}{f_{aVg}} \right) + tf_t^d}_{\text{term frequency}}} \underbrace{ \ln \left(\frac{N - df_t + 0.5}{df_t + 0.5} \right)}_{\text{document frequency}} \underbrace{\frac{(k_3 + 1) \times tf_t^q}{k_3 + tf_t^q}}_{\text{key frequency}}$$



Probabilistic Approach

- Given a query and a collection of documents, a system must determine how well the documents satisfy the query.
 - An IR system makes an uncertain guess of whether a document satisfies the query.
- Probability theory provides a principled foundation for such reasoning under uncertainty.
 - Probabilistic models exploit this foundation to estimate how likely it is that a document is relevant to a query.



Probabilistic Approach

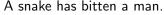
- Assume binary notion of relevance: $R_{d,q}$ is a random variable, such that
 - $R_{d,q} = 1$ if document d is relevant w.r.t query q
 - $R_{d,a} = 0$ otherwise
- Probabilistic ranking orders documents decreasingly by their estimated probability of relevance w.r.t. query: P(R = 1|q, d)
- Assume that the relevance of each document is independent of the relevance of other documents.
- The score is:

$$\mathit{score}_{\mathit{prob}}(q,d) = \log \prod_{t \in q} P(R=1|q,d) = \sum_{t \in q} \log P(R=1|q,d)$$



Information-Based Models







A snake has bitten a man. A man has bitten a snake.

Surprisal of a message

Measure of information content called the self-information or surprisal of a message m:

$$I(m) = -\log[P(m)]$$



Information-Based Model

The more a word deviates in a document from its average behavior in the collection, the more likely it is *significant* for this particular document.

word behaves in a document as expected in collection \implies word has high probability (p) of occurrence in the document \implies information it brings to the document $(-\log p)$ is small

Similarly, if a word has a low probability of occurrence in the document \implies high information content.

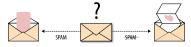
Information Model Equation

$$\mathit{score}_{\mathsf{info}}(q,d) = \sum_{t \in q \cap d} \mathit{tf}_t^q \{ -\log P(X_t \geq \mathit{tf}_t^d | \lambda_t) \}$$



Using Machine Learning

• Document classification: a mail $\vec{d} \rightarrow \{spam, good\}$



- \vec{d} : count vector or tf.idf vector
- Can we do same for retrieval? $\vec{d} \rightarrow \{relevant, not\}$
 - assume we have labels for learning, i.e. if \vec{d} is relevant or not





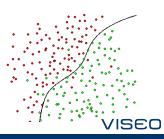


- Wrong feature set:
 - word or feature "obama"
 - highly relevant for query "44th US president"
 - useless for query "area of a parallelogram"
 - can classify for one particular query
 - solution? separate classifier for every query?



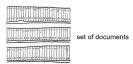
Learning to Rank

- Utilize the query, along with documents, as feature: a consistent feature set across all the queries
- Transform feature set: $f(q \times d) = \vec{X} \rightarrow \{relevant, not\}$
 - example features that have the same effect for any query:
 - BM25 score of query q against document d
 - tf.idf score of query q against document d
 - various count statistics of query words within documents:
 - e.g. number of query words in the title
 - and more...
 - Refer to LETOR features
- Training data: {R, X}
 - $R = \{-1, +1\}$: is **d** is relevant to **q**
 - X: is (d, q) pairs
- Learn any standard classifier
- Three types of learning to rank: pointwise, pairwise, listwise



Experimental Setup

Test Collection





set of queries



relevancy judgement or 'qrels'

Testing Platform

- Different modules (e.g. indexing, query processing matching) are implemented.
- Some popular scoring models are implemented.
- Anyone can customize the platform at code level to implement any new developments.
- Mostly open source and free.



Some Information...

Popular IR Platforms

- Terrier IR Platform. Written in Java, and is developed at the School of Computing Science, University of Glasgow.
 Ref: http://terrier.org/.
- Indri (Lemur). Written C++, and is developed at the Center for Intelligent Information Retrieval, University of Massachusetts and the Language Technologies Institute, Carnegie Mellon University.

Ref: https://www.lemurproject.org/indri/.

Popular Test Collections

- Text REtrieval Conference (TREC).
 - Ref: http://trec.nist.gov/.
- Cross-Language Evaluation Forum (CLEF).
 Ref: http://www.clef-initiative.eu/



It's the beginning

Further Readings:

- Introduction to Information Retrieval. Manning, Raghavan, Schütz
 - Freely available: https://nlp.stanford.edu/IR-book/
- Recherche d'information: Applications, modles et algorithmes
 - Data mining, dcisionnel et big data. *Massih-R Amini, Eric Gaussier*





Thank you!

Questions, Comments...



