# NBA 22-23

Gao

2023-10-19

```
library(tidyverse)
## -- Attaching core tidyverse packages ----- tidyverse 2.0.0 --
## v dplyr 1.1.2 v readr 2.1.4
## v forcats 1.0.0 v stringr 1.5.0
## v ggplot2 3.4.3 v tibble 3.2.1
## v lubridate 1.9.2 v tidyr
                                  1.3.0
## v purrr
             1.0.2
## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                   masks stats::lag()
## i Use the conflicted package (<a href="http://conflicted.r-lib.org/">http://conflicted.r-lib.org/</a>) to force all conflicts to become error
library(tidymodels)
## -- Attaching packages ------ tidymodels 1.1.1 --
## v broom 1.0.5 v rsample 1.2.0
## v dials 1.2.0 v tune 1.1.2
## v infer 1.0.5 v workflows 1.1.3
## v modeldata 1.2.0 v workflowsets 1.0.1
## v parsnip 1.1.1 v yardstick 1.2.0
## v recipes
                1.0.8
## -- Conflicts ----- tidymodels_conflicts() --
## x scales::discard() masks purrr::discard()
## x dplyr::filter() masks stats::filter()
## x recipes::fixed() masks stringr::fixed()
## x dplyr::lag() masks stats::lag()
## x yardstick::spec() masks readr::spec()
## x recipes::step() masks stats::step()
## * Use tidymodels_prefer() to resolve common conflicts.
library(ggforce)
library(yardstick)
library(car)
## Loading required package: carData
## Attaching package: 'car'
## The following object is masked from 'package:dplyr':
```

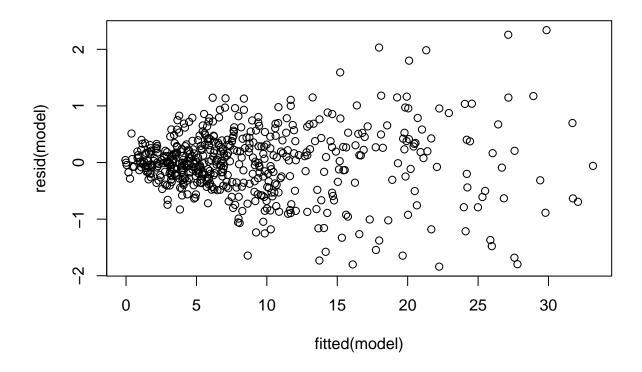
```
##
##
       recode
##
## The following object is masked from 'package:purrr':
##
##
       some
library(moments)
library(GGally)
## Registered S3 method overwritten by 'GGally':
##
     method from
##
     +.gg
           ggplot2
library(psych)
##
## Attaching package: 'psych'
## The following object is masked from 'package:car':
##
##
       logit
##
## The following objects are masked from 'package:scales':
##
##
       alpha, rescale
## The following objects are masked from 'package:ggplot2':
##
##
       %+%, alpha
library(fastDummies)
## Thank you for using fastDummies!
## To acknowledge our work, please cite the package:
## Kaplan, J. & Schlegel, B. (2023). fastDummies: Fast Creation of Dummy (Binary) Columns and Rows from
NBA <- read_csv("NBA22.csv") %>% as_tibble()
## Rows: 539 Columns: 45
## -- Column specification -----
## Delimiter: ","
## chr (8): FIRST, LAST, TEAM, COLLEGE, COUNTRY, DRAFT_YEAR, DRAFT_ROUND, DRAF...
## dbl (37): AGE, HEIGHT, INCHES, TOTAL_HEIGHT, WEIGHT, GP, W, L, MIN, PTS, FGM...
## i Use 'spec()' to retrieve the full column specification for this data.
## i Specify the column types or set 'show_col_types = FALSE' to quiet this message.
cor(NBA$PTS, NBA$AGE)
```

## [1] 0.105353

```
INCHES TOTAL_HEIGHT
##
             AGE
                     HEIGHT
                                                         WEIGHT
## [1,] 0.105353 0.06700926 -0.08555374 -0.01010688 0.03943856 0.5068927
               W
                        L
                                  MIN PTS
                                                FGM
                                                          FGA
                                                                    FG%
                                                                              3PM
## [1,] 0.4785077 0.4134082 0.8743863
                                       1 0.9917528 0.9820704 0.2019397 0.7027053
##
              3PA
                        3P%
                                  FTM
                                            FTA
                                                      FT%
                                                               OREB
                                                                         DREB
## [1,] 0.7155858 0.2181655 0.9001796 0.8902233 0.3278894 0.3043068 0.7142162
              REB
                        AST
                                  TOV
                                            STL
                                                      BLK
                                                                 PF
## [1,] 0.6353543 0.7221607 0.8521601 0.5818423 0.3271584 0.6040127 0.9526629
              DD2
                        TD3
                                  +/-
                                         NETRTG
                                                     OREB%
                                                                DREB%
## [1,] 0.5558736 0.2720614 0.2536767 0.1449639 -0.1419348 0.09481329 0.7176454
              TS%
                       AST%
## [1,] 0.2853946 0.4390633
model <- lm(PTS ~ HEIGHT + MIN + FGM + FTM + PF, data = NBA)</pre>
model
##
## Call:
## lm(formula = PTS ~ HEIGHT + MIN + FGM + FTM + PF, data = NBA)
## Coefficients:
                                                  FGM
                                                                             PF
## (Intercept)
                     HEIGHT
                                     MIN
                                                               FTM
##
       1.59543
                   -0.26825
                                 0.05852
                                              2.20716
                                                           0.81916
                                                                       -0.33988
```

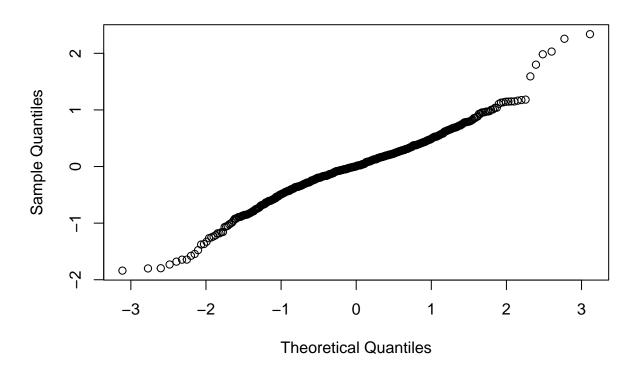
cor(NBA\$PTS, select\_if(NBA, is.numeric))

plot(fitted(model),resid(model))



qqnorm(resid(model))

# Normal Q-Q Plot



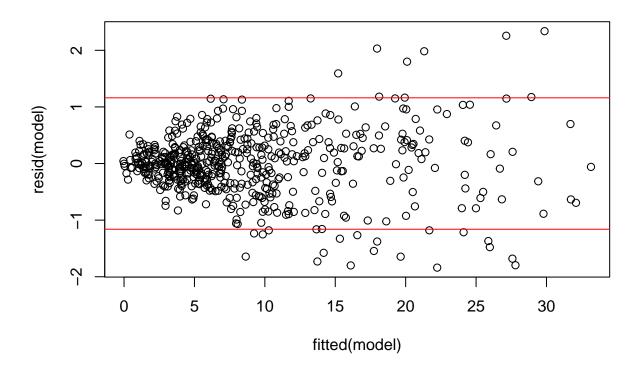
```
standard_error <- sqrt(deviance(model)/df.residual(model))
standard_error</pre>
```

## [1] 0.5803848

2\*standard\_error

## [1] 1.16077

```
plot(fitted(model),resid(model))
abline(h=2*standard_error, col = "red")
abline(h=-2*standard_error, col = "red")
```



```
residual <- resid(model)
residual</pre>
```

```
2
   -6.079934e-01 -1.251859e+00 -1.838806e+00
##
                                               3.748794e-01
##
                              7
    4.169008e-01 5.393823e-01 -1.800251e+00
##
                                               2.509084e-01 -8.475143e-01
##
              11
                             12
                                           13
   -6.341986e-01 -5.904977e-02 1.812040e-01
                                               1.249861e-01
                                                              1.310019e-02
##
                             17
                                           18
##
##
    1.477588e-02 -1.645010e+00 -4.605432e-01 -8.720513e-01
                                                              4.848599e-01
                                           23
##
              21
                             22
                  7.247669e-01 -5.037472e-01
##
    1.983333e+00
                                               7.873563e-01
##
                             27
                                           28
   -2.835339e-01 -1.213763e-01 -1.265619e+00 -2.468928e-01
                                                              2.680230e-02
##
                                           33
##
              31
                             32
                                                          34
   -4.301418e-01 -4.495140e-01
                                5.155228e-01 -2.137590e-01
                                                             -7.892184e-01
##
              36
                             37
                                           38
                                                          39
##
    1.001615e+00
                  3.834043e-01
                                 8.275530e-01
                                               3.713589e-01
##
              41
                             42
   -2.230890e-01 -1.747767e-01 -6.189994e-01
                                                2.389425e-02
              46
                             47
##
##
    5.827849e-01 -5.835421e-01 -7.619851e-02
                                               2.068145e-01
                                                              5.127391e-02
                             52
##
              51
                                           53
                                                          54
   -7.511786e-03 2.945574e-01 -2.156493e-01
                                              1.688563e-01 -3.699985e-01
              56
                             57
                                           58
                                                          59
                                                                         60
##
```

```
3.944103e-01 -3.543547e-01 -1.130452e-01  4.035327e-02  2.723692e-01
                             63
##
                 62
                                                   64
            61
##
   4.331430e-01 -4.990494e-01 -9.024159e-02 -7.704478e-02 -1.310817e-02
                         67
                                     68
                                                   69
##
            66
##
   -3.025994e-03 -4.421029e-02 1.578201e-01 -2.000245e-01 -5.976686e-01
                        72
                                   73
                                             74
##
           71
   3.909714e-01 1.106953e+00 -1.731979e-01 2.189931e-01 -1.214226e+00
##
                         77
                              78
                                                   79
##
   2.610533e-01 -3.286941e-01 9.408100e-02 -1.633967e-01 1.593988e-01
##
            81
                         82
                              83
                                                  84
   -1.730524e+00 -7.340878e-02 4.338022e-01 2.548731e-02 -2.357635e-02
##
            86
                       87
                                     88
                                                 89
##
   1.236825e-01 7.432897e-01 -2.609378e-01 -7.456894e-01 -1.916845e-02
                    92
                              93
           91
                                            94
  -4.704549e-01 -8.692294e-01 3.290741e-01 -1.577223e+00 -2.246052e-01
##
            96
                 97
                              98
                                          99
   -4.827927e-01 3.674385e-02 -1.643828e+00 5.264490e-01 3.139789e-01
                      102
                              103
           101
                                                 104
  -5.612939e-01 5.512730e-01 2.188486e-02 3.084348e-01 -4.012600e-01
           106
                        107
                                    108
                                                 109
##
  -7.563848e-01
               4.394733e-01 2.257345e+00 -2.823659e-01 -1.680258e+00
          111
                       112
                                    113
                                            114
  -1.985752e-01 7.844789e-01 -1.987749e-01 3.422849e-01 8.682374e-02
##
           116
                  117
                             118
                                           119
   1.462614e-01 -1.477261e+00 -4.063128e-01 4.396287e-02 -6.777498e-01
           121
                    122
                                    123
                                                 124
   2.905182e-01 -8.774604e-02 5.241011e-01 5.477784e-01 6.977499e-01
##
           126
                       127
                                     128
                                                  129
  -1.910362e-02 6.743881e-01 -5.178607e-01 6.162332e-02 -3.897541e-01
                       132
                                    133
           131
                                                 134
   -6.688159e-02 1.033469e-01 -4.884217e-01 2.244873e-01 -3.644863e-01
##
           136
                   137
                                     138
                                                  139
   -6.664620e-01 -3.138812e-01 -1.180193e+00 -1.789605e-01 4.026112e-01
                       142
                                    143
           141
                                                 144
   1.088513e-01 3.318922e-01 -5.930898e-02 -6.865905e-01 -9.676522e-02
           146
                       147
                                    148
##
                                                 149
   8.786041e-02
               3.201095e-01 4.324921e-01 1.536930e-01 -6.600638e-01
##
           151
                       152
                                    153
                                                 154
                4.885515e-01 -5.015130e-01 -1.328378e+00 -3.876540e-01
   -4.445116e-02
                                                  159
##
           156
                                     158
                        157
               1.992210e-01 1.153903e-01 2.095384e-01 -8.142252e-02
   -8.529160e-01
##
           161
                        162
                                     163
                                                 164
##
   8.740124e-01 5.755240e-02 -1.377859e+00 -6.940619e-01 -2.023222e-01
                                    168
##
           166
                       167
   -8.293607e-01 -8.905741e-01 -1.729405e-01 -1.006285e+00 1.297543e-01
##
           171
                       172
                                     173
                                                  174
##
   7.963301e-01
               4.126844e-01 7.780792e-01 7.479416e-01 7.902819e-01
##
           176
                       177
                                     178
                                                 179
   -6.811486e-01 4.254485e-01 1.721217e-01 -5.079384e-02 -4.267409e-01
           181
                        182
                                     183
                                                 184
##
   8.833284e-02 1.849087e-01 1.920869e-01 6.842564e-01 -8.546713e-01
##
                       187
                                    188
                                                189
   2.831950e-01 -4.890128e-02 1.869728e-02 1.149796e+00 9.569376e-01
##
           191
                        192
                                     193
                                                  194
```

```
6.214831e-01 -6.249195e-02 -4.792411e-01 6.220991e-01 9.311339e-01
                          197
                                        198
##
            196
                                                      199
    4.642253e-02 -3.410939e-01 -1.983701e-01 -5.308375e-01 -1.250987e-01
                          202
                                        203
                                                      204
##
            201
##
   2.735870e-01 6.394269e-01 4.148986e-02 -1.680724e-01 -9.227396e-01
                          207
                                        208
            206
                                                      209
##
   -1.921701e-01 -7.102169e-03 4.212962e-01 1.592496e+00 -4.549948e-02
##
            211
                          212
                                         213
                                                      214
   -1.267301e-01 9.384262e-02 -6.667796e-02 -1.229592e-02
                                                           2.885719e-01
            216
                          217
                                         218
                                                       219
   -1.607751e-01 5.653254e-01 -2.753240e-01 -2.828531e-02
                                                           1.763798e-01
            221
                          222
                                         223
                                                       224
##
   1.741126e-01
                8.842326e-01 1.144900e+00 -1.320633e-01
                                                           9.784413e-01
            226
                          227
                                         228
                                                       229
  -2.998408e-02 -4.674394e-01 7.253078e-01 -6.097011e-01
                                                            6.734059e-01
            231
                           232
                                         233
                                                       234
##
  -3.011887e-01 5.272854e-01 -2.843882e-01 -3.446145e-01
                                                           7.883588e-02
            236
                          237
                                        238
                                                      239
## -4.813306e-01 -6.315086e-02 4.955441e-01 -8.872948e-01 -6.328549e-02
            241
                          242
                                        243
                                                      244
##
   1.128862e+00 -3.585607e-01 8.561674e-01 -3.639752e-01
                                                           8.673903e-02
            246
                          247
                                        248
## -7.770976e-02 1.537275e-01 -1.480560e-01 -1.369630e+00 -1.199649e-02
##
            251
                          252
                                        253
## -1.822989e-03 -3.327325e-01 -4.449078e-01 -1.156894e+00 -3.932951e-01
            256
                          257
                                        258
                                                       259
## -1.554374e-01 -7.199345e-01 1.967452e-01 -1.657776e-02 2.153528e-02
            261
                          262
                                         263
                                                       264
                               1.939133e-01 9.304589e-01 -8.116737e-01
## -2.597298e-01
                 2.917491e-01
            266
                          267
                                         268
                                                       269
## -9.705649e-02
                 2.030874e+00 4.726630e-01
                                             1.845960e-02 1.695686e-01
##
            271
                           272
                                         273
                                                       274
   3.696157e-01
                 1.823757e-01 -7.478383e-02 -2.051969e-02 -1.355628e-01
                          277
                                        278
            276
                                                       279
   -1.915328e-02 -1.942930e-01
                               7.850302e-02
                                            4.617449e-01 -2.448479e-01
                          282
                                        283
##
            281
                                                      284
   -6.064398e-01
                 2.076427e-01
                               3.745178e-01
                                             1.379722e-01
                                                           5.397949e-01
            286
                          287
                                        288
                                                       289
##
   -2.229529e-01
                 3.413966e-01 -4.401086e-01
                                             6.880333e-01
                                                           1.631605e-01
##
            291
                          292
                                        293
                                                       294
    2.170606e-01
                2.338120e+00 -4.671329e-02 4.740203e-01 6.982190e-03
            296
                                         298
##
                          297
                                                       299
##
   -9.894747e-01 2.668585e-01 1.917924e-02 5.632034e-01
                                                           6.058711e-01
##
                          302
                                         303
            301
                                                       304
    4.021709e-01 -1.687109e-01 -1.871695e-01 -3.314187e-01
                                                            2.957943e-01
                                         308
##
            306
                          307
                                                       309
##
    1.606926e-03 1.039052e+00 -2.770685e-01 -4.315390e-01 -3.637337e-01
##
            311
                          312
                                        313
                                                      314
   -2.980937e-01 -8.230499e-01 6.174457e-01 1.300190e-01 1.278091e-01
            316
                          317
                                        318
                                                       319
##
   5.257111e-01 -1.367219e-01 1.472999e-01 6.632253e-01
##
                                                           3.461632e-01
                         322
                                       323
                                                      324
  -1.046482e+00 4.033892e-02 -5.471025e-02 8.043357e-01 -5.252008e-02
##
            326
                          327
                                        328
                                                       329
```

```
## -1.638503e-01 4.770717e-01 -3.084263e-01 6.479972e-01 2.327403e-01
##
            331
                          332
                                        333
                                                      334
  -3.563498e-01
                1.934158e-01 3.077156e-01 -3.754918e-01 -1.762660e-01
            336
                          337
                                        338
                                                      339
  -8.072618e-02 -2.915550e-01
                              1.147009e+00 -1.544496e+00 -1.057355e-02
            341
                          342
                                                      344
                                        343
   1.628619e-02
                6.339132e-01 1.155118e-01 -6.847408e-02 -1.663542e-01
##
            346
                          347
                                        348
                                                      349
   -6.324648e-01 5.837796e-01 -5.293728e-01 1.941245e-01
                                                          7.624148e-01
##
            351
                          352
                                        353
                                                      354
  -1.179974e+00
                2.324305e-01 7.830495e-01 6.535218e-01
                                                          3.450534e-01
            356
                          357
                                        358
                                                      359
##
  -8.029207e-01 -2.460353e-01
                              7.087824e-01 -1.006144e-01
                                                           1.134894e+00
            361
                          362
                                        363
   -8.171233e-05 -1.982796e-01 -8.845840e-02 -2.453793e-01
                                                           1.823720e-02
            366
                          367
                                        368
                                                      369
##
   2.434462e-01 2.357187e-01
                               2.550335e-01
                                            7.732670e-02
                                                           1.247975e-01
            371
                          372
                                        373
                                                      374
  -7.691988e-01 -3.772648e-02 5.026312e-03 4.566289e-01
                                                          5.710210e-01
##
            376
                         377
                                        378
                                                      379
##
   2.707875e-01 8.176779e-01
                              4.202339e-01
                                            3.790942e-01 -1.647508e-01
            381
                          382
                                       383
   3.166267e-01 -1.228293e-01 2.344627e-01 -2.649573e-02 -8.395438e-01
##
##
            386
                          387
                                        388
   -1.162073e+00 2.001601e-01
                              1.149813e+00 6.561340e-01
                                                          1.008135e+00
            391
                          392
                                       393
                                                      394
   -2.637485e-01 -5.913346e-01
                               9.548179e-01
                                            1.230485e-01 -4.252355e-01
##
            396
                          397
                                        398
                                                      399
   5.067661e-01 -3.002893e-01 -2.206784e-01
                                            3.358445e-01
                                                          2.209976e-01
            401
                         402
                                        403
                                                      404
   -1.477904e-01 1.759882e-01
                               3.774113e-01 3.279801e-01
                                                           1.035673e+00
##
            406
                          407
                                        408
                                                      409
    1.288179e-01 -1.553502e-01 7.911515e-02 -2.764150e-01
                                                           1.031077e-01
            411
                         412
                                       413
                                                      414
##
   -4.352835e-02 -1.380413e-01 2.830233e-01 -1.816626e-01
                                                           8.576526e-01
##
            416
                         417
                                       418
                                                     419
   -8.563051e-01 -3.940296e-01 -1.081374e-01 -4.641606e-02 -5.961262e-02
            421
                         422
                                       423
                                                     424
##
    1.477865e-01 -2.836708e-01 1.985051e-01 1.845100e-01
##
                                                           8.910380e-02
            426
                         427
                                       428
                                                      429
##
   6.388536e-01 4.590873e-01 -9.237898e-01 1.523816e-01 4.098818e-01
##
            431
                          432
                                       433
                                                      434
##
   -3.211963e-01 3.990136e-01 2.416801e-01 -1.522858e-01 4.278991e-02
                                       438
##
            436
                          437
                                                      439
   -1.354180e-01 -9.555996e-01 9.688612e-02 9.606267e-01 -8.017209e-02
                          442
                                        443
##
            441
                                                      444
##
   6.822853e-02 -7.904063e-01 3.111085e-01 -1.057848e+00 -8.274660e-02
            446
                          447
                                        448
                                                      449
   5.123134e-01 1.164002e+00 -5.823670e-01 3.910097e-01 -8.859976e-03
            451
                          452
                                       453
                                                     454
  -4.068684e-01 -7.893348e-02 -5.593808e-01 1.123755e-01
##
                                                          5.292771e-01
            456
                         457
                                       458
                                                     459
## -7.368418e-01 -1.632998e-01 -4.298590e-01 1.655053e-01 6.972846e-01
##
            461
                          462
                                        463
                                                      464
```

```
2.848170e-01 2.115516e-01 2.218823e-01 -4.767723e-02 1.174199e+00
                                 468
##
                                             469
          466
                      467
  -3.446003e-01 2.106806e-01 -3.115414e-03 -7.480334e-01 1.276030e-01
##
          471
                      472
                                 473
                                             474
##
   1.799471e+00 -1.649555e-01 1.123790e-01 -1.069117e+00 -1.942591e-01
          476
                                 478
                                             479
##
                     477
   1.636115e-01 -2.424040e-01 9.718092e-01 4.518372e-01 -2.834160e-01
##
          481
                     482
                           483
##
   2.694996e-01 2.528514e-01 -5.336655e-01 -7.264931e-01 1.181977e+00
                                      489
##
          486
                      487
                           488
   2.600597e-01 3.565798e-01 -5.125982e-04 -1.021610e+00 2.079272e-01
##
          491
                      492
                                 493
                                             494
##
  -3.058617e-01 2.518120e-01 5.807666e-01 -1.298999e-01 -3.016233e-02
          496
                     497
                                 498
                                             499
   2.174746e-01 -2.407478e-01 -3.514773e-01 2.751271e-01 3.776934e-01
          501
                     502
                                 503
  -2.386938e-01 2.477404e-01 7.191847e-01 -4.416793e-01 -2.349171e-01
          506
                507
                                 508
  -2.004006e-01 -3.570802e-01 2.873639e-01 3.765301e-01 -2.971961e-02
                            513
          511
                     512
                                            514
##
   1.320189e-01 -3.394338e-01 2.236334e-01 8.858353e-02 4.379099e-02
                     517
                            518 519
  523
##
          521
                      522
                                      524
  -5.765651e-01 -9.048760e-01 -1.185950e-01 -1.176992e-01 -1.234607e+00
          526
              527
                           528 529
   2.868017e-02 -1.796490e+00 -3.576960e-02 -4.541351e-01 -5.302546e-01
##
          531
                     532
                           533
                                             534
   3.044880e-01 -6.052113e-01 -6.357093e-01 9.706186e-01 -5.624567e-01
          536
                    537
                                  538
   1.651528e-01 2.307108e-02 -4.094633e-01 -8.928381e-01
```

#### sort(residual)

```
527
                      8
                                            81
## -1.838806e+00 -1.800251e+00 -1.796490e+00 -1.730524e+00 -1.680258e+00
     17 98 94 339
## -1.645010e+00 -1.643828e+00 -1.577223e+00 -1.544496e+00 -1.477261e+00
                          154
         163
               249
                                            28
## -1.377859e+00 -1.369630e+00 -1.328378e+00 -1.265619e+00 -1.251859e+00
         525
                     75
                                138
                                            351
## -1.234607e+00 -1.214226e+00 -1.180193e+00 -1.179974e+00 -1.162073e+00
                     474
                          444
## -1.156894e+00 -1.069117e+00 -1.057848e+00 -1.046482e+00 -1.021610e+00
                          437 428
                     296
## -1.006285e+00 -9.894747e-01 -9.555996e-01 -9.237898e-01 -9.227396e-01
                     539
         522
                           167
                                            239
## -9.048760e-01 -8.928381e-01 -8.905741e-01 -8.872948e-01 -8.720513e-01
      92
                     416
                          185
## -8.692294e-01 -8.563051e-01 -8.546713e-01 -8.529160e-01 -8.475143e-01
          385
                          312
## -8.395438e-01 -8.293607e-01 -8.230499e-01 -8.116737e-01 -8.029207e-01
         442 35 371 106
## -7.904063e-01 -7.892184e-01 -7.691988e-01 -7.563848e-01 -7.480334e-01
```

```
456
                           484
## -7.456894e-01 -7.368418e-01 -7.264931e-01 -7.199345e-01 -6.940619e-01
               176
                          120 518
## -6.865905e-01 -6.811486e-01 -6.777498e-01 -6.690613e-01 -6.664620e-01
          150
                    533
                               11
## -6.600638e-01 -6.357093e-01 -6.341986e-01 -6.324648e-01 -6.189994e-01
         229
               1
                          281 532
## -6.097011e-01 -6.079934e-01 -6.064398e-01 -6.052113e-01 -5.976686e-01
              47
          392
                                448
                                             521
## -5.913346e-01 -5.835421e-01 -5.823670e-01 -5.765651e-01 -5.624567e-01
          101
                     453
                                 483
                                      199
## -5.612939e-01 -5.593808e-01 -5.336655e-01 -5.308375e-01 -5.302546e-01
          348
                     128
                            23
                                            153
## -5.293728e-01 -5.178607e-01 -5.037472e-01 -5.015130e-01 -4.990494e-01
                96
                                236
                                     193
          133
## -4.884217e-01 -4.827927e-01 -4.813306e-01 -4.792411e-01 -4.704549e-01
                                      32
##
          227
                18
                                529
  -4.674394e-01 -4.605432e-01 -4.541351e-01 -4.495140e-01 -4.449078e-01
          504
                     288
                                309
                                        31
## -4.416793e-01 -4.401086e-01 -4.315390e-01 -4.301418e-01 -4.298590e-01
                                538
          180
                     395
                                            451
  -4.267409e-01 -4.252355e-01 -4.094633e-01 -4.068684e-01 -4.063128e-01
          105
                     417
                                 255
                                            130
##
## -4.012600e-01 -3.940296e-01 -3.932951e-01 -3.897541e-01 -3.876540e-01
                                             244
          334
                55
                                135
## -3.754918e-01 -3.699985e-01 -3.644863e-01 -3.639752e-01 -3.637337e-01
          242
               507
                                520
                                            331
## -3.585607e-01 -3.570802e-01 -3.565677e-01 -3.563498e-01 -3.543547e-01
                                466 197
         498
                     234
## -3.514773e-01 -3.446145e-01 -3.446003e-01 -3.410939e-01 -3.394338e-01
          252
              304
                          77
## -3.327325e-01 -3.314187e-01 -3.286941e-01 -3.211963e-01 -3.159893e-01
        137
              328
                          491 231
## -3.138812e-01 -3.084263e-01 -3.058617e-01 -3.011887e-01 -3.002893e-01
                     337
                           233
         311
## -2.980937e-01 -2.915550e-01 -2.843882e-01 -2.836708e-01 -2.835339e-01
         480
                     109
                          308 409
## -2.834160e-01 -2.823659e-01 -2.770685e-01 -2.764150e-01 -2.753240e-01
                                      29
               88
                          261
## -2.637485e-01 -2.609378e-01 -2.597298e-01 -2.468928e-01 -2.460353e-01
          364
              280
                          477
                                     497
## -2.453793e-01 -2.448479e-01 -2.424040e-01 -2.407478e-01 -2.386938e-01
         505
               95
                           41
                                            286
## -2.349171e-01 -2.246052e-01 -2.230890e-01 -2.229529e-01 -2.206784e-01
         53
              34 165 506
## -2.156493e-01 -2.137590e-01 -2.023222e-01 -2.004006e-01 -2.000245e-01
               111
          113
                          198
                                             362
## -1.987749e-01 -1.985752e-01 -1.983701e-01 -1.982796e-01 -1.942930e-01
                     206
                                 303
## -1.942591e-01 -1.921701e-01 -1.871695e-01 -1.816626e-01 -1.789605e-01
                  42
                            73
                                            168
          335
## -1.762660e-01 -1.747767e-01 -1.731979e-01 -1.729405e-01 -1.687109e-01
          204
                      345 472 380
## -1.680724e-01 -1.663542e-01 -1.649555e-01 -1.647508e-01 -1.638503e-01
```

```
457
                              216
## -1.633967e-01 -1.632998e-01 -1.607751e-01 -1.554374e-01 -1.553502e-01
          434
                 248
                              401 412
## -1.522858e-01 -1.480560e-01 -1.477904e-01 -1.380413e-01 -1.367219e-01
           275
                       436
                                    224
## -1.355628e-01 -1.354180e-01 -1.320633e-01 -1.298999e-01 -1.267301e-01
          200
                       382
                              27
## -1.250987e-01 -1.228293e-01 -1.213763e-01 -1.185950e-01 -1.176992e-01
            58
                        418
                                     359
                                                  266
## -1.130452e-01 -1.081374e-01 -1.006144e-01 -9.705649e-02 -9.676522e-02
            63
                        363
                                    122
                                                 445
## -9.024159e-02 -8.845840e-02 -8.774604e-02 -8.274660e-02 -8.142252e-02
           336
                       440
                                    452
                                                 246
## -8.072618e-02 -8.017209e-02 -7.893348e-02 -7.770976e-02 -7.704478e-02
           48
                       273
                              82
                                                 344
## -7.619851e-02 -7.478383e-02 -7.340878e-02 -6.847408e-02 -6.688159e-02
                240
                             237
##
           213
                                                 192
  -6.667796e-02 -6.328549e-02 -6.315086e-02 -6.249195e-02 -5.961262e-02
                        12
                              323
                                                 325
           143
## -5.930898e-02 -5.904977e-02 -5.471025e-02 -5.252008e-02 -5.079384e-02
          187
                       464
                                    293
                                                 419
  -4.890128e-02 -4.767723e-02 -4.671329e-02 -4.641606e-02 -4.549948e-02
                        67
                                    411
                                                  372
##
           151
## -4.445116e-02 -4.421029e-02 -4.352835e-02 -3.772648e-02 -3.576960e-02
           495
                        226
                                    510
                                                 219
  -3.016233e-02 -2.998408e-02 -2.971961e-02 -2.828531e-02 -2.649573e-02
                              90
          85
                       274
                                                 276
## -2.357635e-02 -2.051969e-02 -1.916845e-02 -1.915328e-02 -1.910362e-02
           259
                 65
                              214
                                                 250
  -1.657776e-02 -1.310817e-02 -1.229592e-02 -1.199649e-02 -1.057355e-02
##
           450
                 51
                             207
                                          468
  -8.859976e-03 -7.511786e-03 -7.102169e-03 -3.115414e-03 -3.025994e-03
                  488
                              361
                                                 306
  -1.822989e-03 -5.125982e-04 -8.171233e-05
                                         1.606926e-03 5.026312e-03
                              16
           295
                    15
                                         1.628619e-02
               1.310019e-02 1.477588e-02
##
   6.982190e-03
                                                      1.823720e-02
                       188
                                   298
                1.869728e-02 1.917924e-02
                                          2.153528e-02
##
   1.845960e-02
                                                      2.188486e-02
##
           537
                         44
                                      84
                                                   30
   2.307108e-02
                2.389425e-02
                             2.548731e-02
                                          2.680230e-02
##
                                                      2.868017e-02
           97
                        322
                                    59
                                                  203
   3.674385e-02
               4.033892e-02 4.035327e-02
                                          4.148986e-02
##
                                                      4.278991e-02
##
           515
                       119
                               196
                                                  50
                             4.642253e-02
##
   4.379099e-02
                4.396287e-02
                                          5.127391e-02
                                                       5.755240e-02
           129
                       441
                              369
                                                 278
                             7.732670e-02
                                                      7.877312e-02
##
   6.162332e-02
                6.822853e-02
                                          7.850302e-02
##
           235
                        408
                                    245
                                                  115
                7.911515e-02 8.673903e-02
##
   7.883588e-02
                                          8.682374e-02
                                                      8.786041e-02
##
           181
                       514
                                    425
                                                  212
##
   8.833284e-02
                8.858353e-02
                            8.910380e-02
                                         9.384262e-02
                                                       9.408100e-02
                        410
                                     132
                                                  141
##
           438
##
   9.688612e-02
                1.031077e-01 1.033469e-01
                                          1.088513e-01
                                                       1.123755e-01
##
           473
                                     343
                                                  394
                        158
   1.123790e-01 1.153903e-01 1.155118e-01 1.230485e-01 1.236825e-01
```

```
470
           370
                   14
   1.247975e-01
               1.249861e-01 1.276030e-01 1.278091e-01
##
                                                     1.288179e-01
                              511
##
           170
                    314
                                           284
##
   1.297543e-01
                1.300190e-01
                            1.320189e-01
                                         1.379722e-01
                                                      1.462614e-01
##
          318
                       421
                                   429
                                                  149
                             1.523816e-01
##
   1.472999e-01
                1.477865e-01
                                         1.536930e-01
                                                      1.537275e-01
            68
                  80
                              290
##
   1.578201e-01
                1.593988e-01
                             1.631605e-01
                                         1.636115e-01
                                                      1.651528e-01
##
           459
                         54
                             270
                                                  178
   1.655053e-01
                1.688563e-01
                             1.695686e-01
                                                      1.741126e-01
##
                                         1.721217e-01
           402
                        220
                              13
                                                  272
                1.763798e-01
                             1.812040e-01
                                         1.823757e-01
##
   1.759882e-01
                                                      1.845100e-01
##
           182
                       183
                                    332
                                                  263
                1.920869e-01
                                          1.939133e-01
                                                      1.941245e-01
##
   1.849087e-01
                             1.934158e-01
           258
                                           387
##
                  423
                              157
##
   1.967452e-01
                1.985051e-01
                             1.992210e-01
                                         2.001601e-01
                                                      2.068145e-01
                              159
                                          467
##
           282
                       490
                                                      2.115516e-01
   2.076427e-01
                2.079272e-01
                             2.095384e-01
                                         2.106806e-01
                              74
                                           400
##
           291
                       496
##
   2.170606e-01
                2.174746e-01
                             2.189931e-01
                                         2.209976e-01
                                                      2.218823e-01
##
          513
                        134
                              352
                                                 330
   2.236334e-01
                2.244873e-01
                             2.324305e-01
                                         2.327403e-01
##
                                                      2.344627e-01
                                     366
##
           367
                       433
                                           502
                             2.434462e-01
##
   2.357187e-01
                2.416801e-01
                                         2.477404e-01
                                                      2.509084e-01
                                     368
##
           492
                        482
                                                 486
   2.518120e-01
                2.528514e-01
                             2.550335e-01
                                         2.600597e-01
                                                      2.610533e-01
           297
                              376
                                                  60
                                                               201
##
                       481
                             2.707875e-01
##
   2.668585e-01
                2.694996e-01
                                         2.723692e-01
                                                      2.735870e-01
           499
                              186
                                           461
##
                       413
                                         2.848170e-01
                2.830233e-01
                             2.831950e-01
                                                      2.873639e-01
   2.751271e-01
##
           215
                 121
                             262
                                                  52
##
   2.885719e-01
                2.905182e-01
                            2.917491e-01
                                         2.945574e-01
                                                      2.957943e-01
##
           531
                 333
                             104
                                           519
                             3.084348e-01
   3.044880e-01
                3.077156e-01
                                         3.110793e-01
                                                      3.111085e-01
##
                   381
##
           100
                              147
                                           404
                            3.201095e-01
                3.166267e-01
                                         3.279801e-01
                                                      3.290741e-01
##
   3.139789e-01
##
          142
                       399
                              287
   3.318922e-01
                3.358445e-01
                             3.413966e-01
                                         3.422849e-01
                                                      3.450534e-01
##
                        487
                              271
                                                   39
##
                3.565798e-01
   3.461632e-01
                             3.696157e-01
                                         3.713589e-01
##
                                                      3.745178e-01
                 509
                              403
                                           500
                3.765301e-01
                             3.774113e-01
                                                      3.780020e-01
##
   3.748794e-01
                                         3.776934e-01
##
           379
                         37
                                 71
                                                 449
                             3.909714e-01
##
   3.790942e-01
                3.834043e-01
                                         3.910097e-01
                                                      3.944103e-01
           432
                        301
                              140
   3.990136e-01
                4.021709e-01
##
                             4.026112e-01
                                         4.098818e-01
                                                      4.126844e-01
                                          177
##
            6
                        378
                              208
                             4.212962e-01
                                         4.254485e-01
##
   4.169008e-01
                4.202339e-01
                                                      4.324921e-01
                              107
                                           5
##
        61
                  83
##
   4.331430e-01
                4.338022e-01
                             4.394733e-01
                                         4.425816e-01
                                                      4.518372e-01
           374
                                    279
##
                       427
                                                 517
##
   4.566289e-01
                4.590873e-01
                             4.617449e-01
                                         4.717511e-01
                                                      4.726630e-01
##
           294
                        327
                                      20
                                                  152
   4.740203e-01 4.770717e-01 4.848599e-01 4.885515e-01 4.955441e-01
```

```
##
           396
                      446
                              33
                                          123
              5.123134e-01 5.155228e-01 5.241011e-01 5.257111e-01
##
   5.067661e-01
##
          99
                       232
                             455
                                                 7
               5.272854e-01
                                                    5.397949e-01
   5.264490e-01
                           5.292771e-01
                                        5.393823e-01
##
##
          124
                      102
                             299
                                          217
               5.512730e-01
                           5.632034e-01
##
   5.477784e-01
                                        5.653254e-01
                                                    5.710210e-01
##
         493
                  46
                            347
                                               300
##
   5.807666e-01
               5.827849e-01
                            5.837796e-01
                                        6.058711e-01
                                                     6.174457e-01
##
           191
                       194
                                    342
                                                426
               6.220991e-01
                            6.339132e-01
##
   6.214831e-01
                                        6.388536e-01
                                                    6.394269e-01
##
           329
                       354
                             389
                                                319
   6.479972e-01
                            6.561340e-01
                                        6.632253e-01
##
               6.535218e-01
                                                    6.734059e-01
##
                       184
                              45
                                               289
          127
               6.842564e-01
                            6.856063e-01
                                        6.880333e-01
##
   6.743881e-01
                                                     6.972846e-01
                       358
                                          22
##
          125
                             503
##
   6.977499e-01
               7.087824e-01
                            7.191847e-01
                                        7.247669e-01
                                                     7.253078e-01
                             350
                                          173
##
           87
                 174
   7.432897e-01
               7.479416e-01
                            7.624148e-01
                                        7.780792e-01
                                                    7.830495e-01
                   24
                             175
##
       112
                                               171
##
   7.844789e-01
               7.873563e-01
                            7.902819e-01
                                        7.963301e-01
                                                     8.043357e-01
##
         377
                   38
                              243
                                               415
   8.176779e-01
               8.275530e-01
                            8.561674e-01
                                        8.576526e-01
##
           222
                      264
##
                             195
                                                393
   8.842326e-01
               9.304589e-01
                            9.311339e-01
##
                                        9.548179e-01
                                                     9.569376e-01
##
          439
                      534
                                  478
                                               225
   9.606267e-01
               9.706186e-01
                           9.718092e-01
                                        9.784413e-01
                                                    1.001615e+00
                                          72
##
           390
                  405
                             307
                            1.039052e+00
##
   1.008135e+00
               1.035673e+00
                                        1.106953e+00
                                                     1.128862e+00
           360
                      223
                             338
##
                                          189
   1.134894e+00
               1.144900e+00
                           1.147009e+00
                                        1.149796e+00
                                                     1.149813e+00
##
         447
                       465
                             485
                                                209
##
   1.164002e+00
               1.174199e+00
                            1.181977e+00
                                        1.592496e+00
                                                    1.799471e+00
                       267
                             108
               2.030874e+00 2.257345e+00 2.338120e+00
   1.983333e+00
```

# $h \leftarrow 2*(5+1)/539$

h

# ## [1] 0.02226345

#### sort(hatvalues(model))

```
1
                                512
                 168
                                              378
                                                        281
        334
## 0.002211261 0.002247274 0.002247987 0.002308437 0.002339895 0.002400156
                  241 218 52
        418
                                              240
## 0.002436800 0.002444748 0.002495853 0.002511913 0.002514407 0.002550259
             502
                       504
                                 6 303
        51
## 0.002559172 0.002573729 0.002581622 0.002597024 0.002602012 0.002646600
     420
             4 80 148 9
## 0.002673141 0.002673616 0.002678926 0.002688554 0.002701000 0.002702478
                                        160
        57
                 271
                            37
                                    152
## 0.002760187 0.002763553 0.002810657 0.002811967 0.002830904 0.002849076
       497
                 354
                           77
                                    104
                                             180
                                                       147
##
```

```
## 0.002890022 0.002895507 0.002928372 0.002935335 0.002955201 0.002955703
                                                301
##
           299
                       213
                                    244
                                                             304
                                                                         101
## 0.002959251 0.002981870 0.003010351 0.003018803 0.003071869 0.003149892
                                    305
                                                524
                                                                         342
                       219
                                                             134
## 0.003175154 0.003182068 0.003182642 0.003195411 0.003195741 0.003203679
                                                             413
           256
                       415
                                     19
                                                285
## 0.003221462 0.003223647 0.003226702 0.003227514 0.003230605 0.003257795
           356
                       105
                                    102
                                                107
                                                             215
                                                                         191
## 0.003269123 0.003297572 0.003305150 0.003365215 0.003381318 0.003390618
                                    535
           327
                       503
                                                368
                                                             251
                                                                          34
## 0.003408904 0.003427582 0.003440625 0.003451289 0.003585512 0.003585695
                                                             259
           253
                       360
                                    132
                                                494
                                                                         425
## 0.003613978 0.003615206 0.003616015 0.003618592 0.003626226 0.003633168
           188
                        70
                                    337
                                                458
                                                             419
                                                                         293
## 0.003639805 0.003640871 0.003643370 0.003709406 0.003721375 0.003722175
           225
                       343
                                     53
                                                141
                                                              38
## 0.003723835 0.003767320 0.003778970 0.003786676 0.003808478 0.003814936
           282
                       226
                                    506
                                                243
                                                             111
## 0.003818576 0.003834498 0.003840376 0.003870008 0.003883008 0.003913259
           441
                       461
                                    359
                                                473
                                                             399
## 0.003943473 0.003944847 0.004014997 0.004033290 0.004034475 0.004049392
            87
                       498
                                    507
                                                472
                                                             430
## 0.004077440 0.004077667 0.004083993 0.004085682 0.004086029 0.004088549
           202
                       313
                                    247
                                                139
                                                                         411
## 0.004116032 0.004122801 0.004132288 0.004144844 0.004153103 0.004155342
           310
                       407
                                    403
                                                149
                                                             324
## 0.004157910 0.004165901 0.004176199 0.004186355 0.004289977 0.004306400
           144
                       193
                                    381
                                                210
                                                             501
                                                                         365
## 0.004310896 0.004318706 0.004322934 0.004327449 0.004327622 0.004359130
                       429
                                    433
                                                514
                                                             332
                                                                          60
           417
## 0.004412693 0.004437514 0.004437771 0.004490698 0.004511682 0.004525756
##
           495
                       525
                                    165
                                                237
                                                             427
                                                                          85
## 0.004526995 0.004528154 0.004545036 0.004573768 0.004636358 0.004641765
            30
                       109
                                    183
                                                 15
                                                             374
                                                                         227
## 0.004673286 0.004673741 0.004694807 0.004699184 0.004702892 0.004714420
                       220
                                                382
           333
                                     91
                                                            476
                                                                         196
## 0.004716189 0.004739628 0.004767314 0.004781379 0.004782922 0.004809573
                       291
                                                279
           509
                                    195
                                                              18
## 0.004812625 0.004817014 0.004827314 0.004841154 0.004845006 0.004845127
                       383
                                                508
            50
                                    496
                                                             331
                                                                          83
## 0.004848488 0.004850960 0.004854090 0.004855145 0.004882939 0.004884007
           174
                       178
                                    450
                                                518
                                                             135
                                                                          62
## 0.004884166 0.004898714 0.004931814 0.004943115 0.004951492 0.004958947
                        90
                                                280
           451
                                    319
                                                             118
## 0.004959072 0.004979999 0.005003935 0.005029796 0.005076116 0.005109757
                                                408
                                                                         469
           312
                        55
                                    484
                                                             453
## 0.005121901 0.005124815 0.005137505 0.005142698 0.005148793 0.005177463
                       175
                                    400
                                                466
                                                             206
                                                                          43
## 0.005188425 0.005193824 0.005228602 0.005243757 0.005271901 0.005275508
                       112
                                    423
                                                315
                                                             321
           242
## 0.005286355 0.005296159 0.005301278 0.005349291 0.005349520 0.005377408
                       150
                                     42
                                                487
                                                             526
## 0.005415489 0.005417852 0.005424660 0.005441068 0.005493727 0.005497990
##
             2
                       355
                                    156
                                                361
                                                             372
                                                                         264
```

```
## 0.005534454 0.005548548 0.005658836 0.005669529 0.005683216 0.005705554
           13
                       286
                                   216
                                               158
                                                            308
## 0.005711929 0.005724498 0.005738818 0.005775499 0.005791421 0.005806628
                                                           182
                       373
                                   340
                                               493
## 0.005823556 0.005832923 0.005844725 0.005869653 0.005871634 0.005876670
           366
                       187
                                   505
                                               25
                                                             26
## 0.005884029 0.005887175 0.005891349 0.005913589 0.005920404 0.005931779
                                                           128
                       116
                                   169
                                                56
## 0.005948523 0.005948808 0.005956198 0.005963630 0.005974448 0.005987985
                        95
                                   273
                                               84
## 0.005997961 0.006003147 0.006024572 0.006033540 0.006040396 0.006046437
           467
                       323
                                    33
                                               369
                                                           201
                                                                        260
## 0.006064162 0.006074681 0.006092849 0.006136262 0.006147384 0.006176869
           154
                       401
                                   475
                                               274
                                                            422
## 0.006187332 0.006192664 0.006204769 0.006289050 0.006298928 0.006302804
           130
                       194
                                   452
                                               276
                                                            155
## 0.006315489 0.006322763 0.006341326 0.006358601 0.006379183 0.006419048
                        67
                                   519
                                                66
                                                           138
## 0.006432736 0.006440360 0.006448405 0.006454669 0.006461843 0.006497123
                       121
                                   294
                                               181
                                                            48
## 0.006498847 0.006509119 0.006510422 0.006629886 0.006631748 0.006662266
                                    92
           12
                                               336
## 0.006669717 0.006708829 0.006768884 0.006776684 0.006819121 0.006822997
           397
                       460
                                   231
                                                59
## 0.006826106 0.006849760 0.006869419 0.006869894 0.006930711 0.006944075
                       515
                                  463
                                               270
                                                           236
## 0.006966604 0.006981525 0.007015789 0.007020153 0.007032566 0.007037013
           136
                       350
                                    94
                                                10
                                                            394
## 0.007051640 0.007078909 0.007107569 0.007122078 0.007145253 0.007152079
                       531
                                   421
                                               124
                                                            470
           120
## 0.007219118 0.007296200 0.007339190 0.007351552 0.007387528 0.007402741
           339
                       224
                                    88
                                               113
                                                             40
## 0.007412370 0.007425243 0.007428088 0.007429114 0.007444360 0.007451343
                                               329
           72
                       357
                                   455
                                                           142
## 0.007460872 0.007463859 0.007496460 0.007523055 0.007535415 0.007595718
                                   396
           162
                       131
                                               457
                                                           114
## 0.007616630 0.007626504 0.007651621 0.007662348 0.007682395 0.007702079
           20
                                   409
                                               380
                       511
                                                           488
## 0.007709357 0.007727341 0.007786078 0.007787907 0.007808678 0.007862889
           31
                       235
                                   510
                                               296
                                                            326
## 0.007865815 0.007952945 0.008012872 0.008064532 0.008111929 0.008180057
           185
                       440
                                   328
                                               438
                                                           376
## 0.008186834 0.008190492 0.008202525 0.008210354 0.008217471 0.008285120
                                               384
           32
                       250
                                   454
                                                            523
## 0.008295135 0.008304099 0.008371522 0.008432026 0.008446873 0.008545196
                                                74
                                                                         28
           192
                       499
                                   316
                                                            317
## 0.008548341 0.008558690 0.008575765 0.008721980 0.008770589 0.008780941
                       459
                                   341
                                               189
                                                             96
## 0.008785523 0.008811987 0.008828276 0.008858739 0.008913407 0.008921507
                        64
                                    82
                                               81
                                                           517
                                                                        335
           68
## 0.008962879 0.009028316 0.009035241 0.009137992 0.009174871 0.009205382
                        93
                                   234
                                               500
                                                           245
## 0.009254699 0.009435969 0.009482257 0.009527897 0.009615431 0.009649003
##
            16
                       254
                                   221
                                               145
                                                            295
```

```
## 0.009671159 0.009677975 0.009689224 0.009714377 0.009724480 0.009808234
                                   538
           157
                       123
                                                14
                                                           311
## 0.009829200 0.009918858 0.009924920 0.009932231 0.009958686 0.009984355
                       3
                                   379
                                               54
                                                                         7
                                                           115
## 0.010067826 0.010089977 0.010154725 0.010178740 0.010229291 0.010294893
                       207
                                               233
                                    73
                                                           537
## 0.010330071 0.010531565 0.010574401 0.010656813 0.010750179 0.010760420
           388
                       246
                                   212
                                               449
                                                             46
## 0.010856115 0.010870385 0.010877695 0.010989479 0.010989827 0.011010240
           269
                       159
                                   492
                                               532
                                                            398
## 0.011072569 0.011072985 0.011097167 0.011101746 0.011210342 0.011242426
           86
                       392
                                   445
                                               161
                                                           197
                                                                        528
## 0.011302932 0.011332643 0.011380010 0.011411003 0.011478726 0.011523137
                       447
                                   172
                                                58
                                                            151
## 0.011632859 0.011672028 0.011681542 0.011711053 0.011725999 0.012174076
           100
                       106
                                   266
                                                24
                                                            205
## 0.012245795 0.012351405 0.012420540 0.012541522 0.012731938 0.012779512
                       395
                                   404
                                               348
                                                            283
## 0.013099189 0.013127487 0.013195721 0.013375419 0.013403491 0.013452372
           78
                        36
                                   140
                                               358
                                                            268
## 0.013665254 0.013760406 0.013836161 0.013910477 0.013950630 0.013999745
                       322
                                   127
                                               516
## 0.014279564 0.014312748 0.014321552 0.014418399 0.014445864 0.014570662
           278
                       437
                                   199
                                               252
                                                            146
## 0.014716131 0.014803937 0.014956579 0.015218778 0.015225075 0.015234692
                       405
                                   483
                                               522
                                                           126
## 0.015253577 0.015266280 0.015325152 0.015336231 0.015490491 0.015653138
           176
                       442
                                   177
                                               214
                                                            444
## 0.015982224 0.016000606 0.016128522 0.016234013 0.016309636 0.016332069
                       217
                                    39
                                                97
                                                            434
## 0.016390588 0.016606345 0.016708421 0.016770073 0.017014865 0.017245291
           35
                       320
                                   410
                                               153
                                                            481
## 0.017423509 0.017537607 0.017836257 0.018085980 0.018428617 0.018574945
                       208
                                   377
                                               21
                                                            71
           480
                                                                        489
## 0.018880059 0.019195035 0.019229703 0.019249112 0.019909114 0.020017325
                       375
           186
                                   464
                                               513
                                                           117
## 0.020018537 0.020207038 0.020893898 0.021245439 0.021363709 0.021489120
                       338
                                   230
                                               255
           406
                                                           163
## 0.021754860 0.021810174 0.022100480 0.022212777 0.022440778 0.023605294
           23
                                               521
                                                             98
                       108
                                   110
## 0.023709271 0.024500054 0.024755446 0.024845685 0.025379614 0.025447829
           49
                                    22
                                               289
                       482
                                                           346
                                                                        530
## 0.025540357 0.025930045 0.026096245 0.026576332 0.026733482 0.027116872
           203
                                               265
                                                              5
                       443
                                   412
## 0.027152236 0.027311337 0.027488497 0.027536833 0.027696143 0.027736401
           275
                       298
                                   471
                                                65
                                                            385
                                                                         63
## 0.027829683 0.027847073 0.027899029 0.028006323 0.028011423 0.028171609
                                                            76
           325
                       287
                                   386
                                               272
                                                                        539
## 0.028303523 0.028803668 0.029008546 0.029281959 0.029586574 0.029841830
           387
                       200
                                   223
                                               402
                                                           167
## 0.030247497 0.030499549 0.030551203 0.030698653 0.030732725 0.030952891
                       446
                                   262
                                               465
                                                           533
## 0.031428870 0.031429798 0.031561505 0.032433221 0.032682501 0.032887384
##
           416
                       367
                                   190
                                               393
                                                            478
```

```
## 0.033346496 0.033641274 0.033782708 0.034412930 0.034564809 0.034704086
           306
                        89
                                    79
                                               307
                                                            27
## 0.034886369 0.034994844 0.035334239 0.037610045 0.038763358 0.041123082
                                                75
            17
                       239
                                  173
                                                           536
## 0.041316693 0.043570323 0.048567142 0.058980841 0.060317257 0.064992593
                      164
                                   267
           11
                                               143
## 0.065650842 0.084075759 0.094961840 0.096223371 0.101082746
t \leftarrow qt(df = 539 - 5 - 2, 0.95)
```

## [1] 1.647723

### sort(jackknife <- rstudent(model))</pre>

```
8
                          527
## -3.2120715548 -3.1618503199 -3.1367553878 -3.0181006504 -2.9527404748
             17
                           98
                                       94
                                                      339
## -2.9150644669 -2.8886456943 -2.7439089897 -2.6866108738 -2.5866446844
            163
                          249
                                        154
                                                       28
  -2.4119649078 -2.3926271092 -2.3051753262 -2.1981519823 -2.1704571146
             75
                                        351
                          525
                                                      138
## -2.1641114666 -2.1391946935 -2.0757258258 -2.0461578149 -2.0379351926
            254
                          474
                                        444
                                                      321
## -2.0087326101 -1.8487558390 -1.8418332986 -1.8117926339 -1.7817386807
            169
                          296
                                        437
                                                      428
## -1.7423274786 -1.7148898845 -1.6615552173 -1.6193646295 -1.6024459711
##
            522
                          239
                                        539
                                                      167
  -1.5733644870 -1.5653644588 -1.5639530403 -1.5606892105 -1.5089929723
             19
                                        416
                           92
                                                      185
## -1.5067623784 -1.5045527978 -1.5024107766 -1.4803109956 -1.4753716393
            385
                          10
                                                      265
                                        312
  -1.4688173963 -1.4670740058 -1.4231231964 -1.4195216379 -1.3868949851
##
            442
                           35
                                        371
                                                      106
## -1.3740369350 -1.3729611949 -1.3353106586 -1.3122588881 -1.3087822583
                                        484
            469
                          456
                                                       164
## -1.2930214384 -1.2736236438 -1.2556504971 -1.2502062429 -1.2436241694
            144
                          176
                                        120
                                                      518
## -1.1860022416 -1.1835526788 -1.1724091329 -1.1560135587 -1.1527363405
                          11
                                        533
                                                      346
## -1.1407020659 -1.1307539767 -1.1139254876 -1.1048270540 -1.0695014985
            229
                           1
                                        532
                                                       281
## -1.0593182385 -1.0488474234 -1.0487110979 -1.0462417612 -1.0317220514
            392
                           47
                                        521
## -1.0247374404 -1.0224359469 -1.0060059440 -1.0055159720 -0.9707289982
                                        483
            101
                          453
                                                      530
## -0.9685771098 -0.9662409471 -0.9265075700 -0.9261473996 -0.9214172640
                                        23
            348
                         128
                                                      153
  -0.9181330469 -0.8947813212 -0.8782413148 -0.8718297408 -0.8617914094
##
                            96
                                        236
## -0.8438343415 -0.8353447585 -0.8320214195 -0.8272737619 -0.8122711537
                           18
                                        529
                                                      32
## -0.8070367883 -0.7951684898 -0.7879556896 -0.7774541348 -0.7676668381
```

```
288
                            504
                                          309
   -0.7646312301 -0.7616951709 -0.7468428942 -0.7437522136 -0.7417092049
             395
                            180
                                          538
                                                         451
   -0.7372195796 \ -0.7360446503 \ -0.7086993984 \ -0.7024428132 \ -0.7015239903
##
             105
                            255
                                          417
                                                         130
   -0.6921731323 -0.6849580310 -0.6800706362 -0.6733294284 -0.6697196909
##
             334
                             55
                                          135
                                                         244
   -0.6473338345 -0.6387903727 -0.6292118032 -0.6277163843 -0.6276611636
##
             242
                            507
                                           520
                                                         331
                                                                         57
   -0.6190792786 -0.6161486561 -0.6159909946 -0.6151344616 -0.6110361336
             498
                            234
                                          466
                                                         197
   -0.6064720091 -0.5962434672 -0.5949465084 -0.5907443730 -0.5851575601
             252
                            304
                                           77
                                                         431
                                                                        137
   -0.5773478310 -0.5715504931 -0.5668080315 -0.5548660335 -0.5481155116
##
             516
                            328
                                          491
                                                         231
   -0.5480559148 -0.5332515555 -0.5282281225 -0.5203819780 -0.5188158258
                                                         233
##
                                           480
             311
                            337
   -0.5158351627 -0.5029126306 -0.4926501041 -0.4922811357 -0.4899602542
                                          308
                                                         409
##
              26
                            109
##
   -0.4896304960 -0.4873069182 -0.4784295079 -0.4777803819 -0.4746296420
##
             391
                             88
                                          261
                                                          29
   -0.4559924520 -0.4509363666 -0.4485225174 -0.4267149756 -0.4251813618
##
             364
                            280
                                           477
                                                         497
   -0.4237446957 -0.4226106931 -0.4181356860 -0.4150851996 -0.4118397953
##
             505
                             95
                                            41
                                                         286
   -0.4056402494 -0.3878509621 -0.3851341286 -0.3849429305 -0.3820706662
              53
                             34
                                          165
                                                          69
##
   -0.3719657029 -0.3686686276 -0.3491071498 -0.3465782661 -0.3456681844
             113
                            198
                                          111
                                                         362
   -0.3434828810 -0.3432254083 -0.3425262864 -0.3424945510 -0.3354710232
##
             277
                            206
                                           303
   -0.3353899499 -0.3317071400 -0.3226409763 -0.3135891805 -0.3087267363
             335
                             42
                                           73
                                                         168
   -0.3048532093 -0.3017019064 -0.2997532136 -0.2980558942 -0.2911831933
                                           79
             204
                            345
                                                         380
   -0.2906185182 \ -0.2874465180 \ -0.2863944637 \ -0.2847308164 \ -0.2845541602
##
                            457
                                          216
   -0.2832206776 -0.2822049784 -0.2775722866 -0.2680165385 -0.2679932170
##
   -0.2644178004 -0.2552138829 -0.2552101287 -0.2409692199 -0.2366838001
             317
                            436
                                           224
                                                         494
   -0.2364014332 -0.2343310288 -0.2281906684 -0.2240230105 -0.2188509224
             200
                             27
                                          382
                                                         523
   -0.2187129697 \ -0.2131147365 \ -0.2119519155 \ -0.2050226678 \ -0.2029370971
              58
                            418
                                           359
                                                         266
   -0.1957500150 -0.1863786957 -0.1735490345 -0.1681226824 -0.1673889133
##
              63
                            363
                                          122
                                                         445
   -0.1575789717 \ -0.1529284740 \ -0.1512939857 \ -0.1432583830 \ -0.1403603218
             336
                                          452
                                                         246
                            440
   -0.1394360484 -0.1385776160 -0.1363095967 -0.1345031796 -0.1332281588
##
              48
                            273
                                           82
                                                         344
   -0.1316056744 -0.1291227806 -0.1269409275 -0.1183374675 -0.1155714719
                                          237
             213
                            240
                                                         192
## -0.1149508961 -0.1090766802 -0.1089571590 -0.1080361834 -0.1073917233
```

```
420
                                            323
                                                                           179
                              12
   -0.1027542855 -0.1019886426 -0.0944651507 -0.0917148508 -0.0875751529
##
              187
                             464
                                            293
   -0.0844270189 \ -0.0829421249 \ -0.0805617912 \ -0.0800491402 \ -0.0784922713
##
##
              151
                              67
                                            411
                                                            372
   -0.0769702808 -0.0763492779 -0.0750852923 -0.0651271144 -0.0619310713
##
##
              495
                             226
                                            510
                                                            219
##
   -0.0520388121 -0.0517133084 -0.0513650148 -0.0487674675 -0.0458027578
##
               85
                             274
                                            126
                                                             90
   -0.0406783953 \ -0.0354337827 \ -0.0331422750 \ -0.0330786479 \ -0.0330753892
              259
                              65
                                            214
                                                            250
   -0.0285884886 -0.0228868921 -0.0213398606 -0.0207367846
##
                                                                -0.0182544998
##
              450
                              51
                                            207
                                                            468
                                                                -0.0052257725
##
   -0.0152891183 -0.0129472019 -0.0122904075 -0.0053814850
##
              251
                             488
                                            361
                                                            306
                                                                           373
    -0.0031436931
                  -0.0008858406
                                 -0.0001410582
                                                  0.0028156776
                                                                 0.0086775264
                                             16
##
              295
                                                                           365
                              15
                                                            341
    0.0120778579
                   0.0226035502
                                  0.0255587744
                                                  0.0281592813
                                                                 0.0314617813
##
              269
##
                             188
                                            298
                                                            260
                                                                           103
##
    0.0319533663
                   0.0322438524
                                  0.0334842572
                                                  0.0371854265
                                                                 0.0378054205
##
              537
                              44
                                             84
                                                             30
                                                                           526
    0.0399293142
                   0.0412558882
                                  0.0440063270
                                                  0.0462451689
                                                                 0.0495056863
##
##
               97
                              59
                                            322
                                                            203
    0.0637874024
                                  0.0699411630
                                                  0.0724098905
##
                   0.0697033724
                                                                 0.0738170959
##
              515
                             119
                                            196
                                                             50
##
    0.0756457670
                   0.0759004734
                                  0.0801040655
                                                  0.0884771776
                                                                 0.0994498050
##
                                                             25
              129
                             441
                                            369
                                                                           278
##
    0.1064495937
                   0.1176808724
                                  0.1335209928
                                                  0.1360033909
                                                                 0.1361411507
##
              235
                             408
                                            245
                                                            115
                   0.1365409903
##
    0.1362515775
                                  0.1500368693
                                                  0.1502299753
                                                                 0.1524089319
##
              181
                             514
                                            425
                                                            212
                                                                            78
##
    0.1525640924
                   0.1528326164
                                  0.1536640999
                                                  0.1624284482
                                                                 0.1630710310
##
              438
                             132
                                            410
                                                            141
                   0.1782268272
##
    0.1674709314
                                  0.1790969696
                                                  0.1877361645
                                                                 0.1938448095
##
                                            343
                                                            394
              454
                             158
                                                                            86
    0.1942624785
                   0.1992138188
                                  0.1992224630
                                                  0.2125828446
##
                                                                 0.2141269883
##
              370
                                            470
                                                            315
    0.2155828918
                   0.2162342296
                                  0.2204788762
                                                  0.2206087331
                                                                 0.2242070185
##
                                                            284
##
              170
                             314
                                            511
                                  0.2281487078
##
    0.2251358739
                   0.2262669213
                                                  0.2384222163
                                                                 0.2525385031
##
              318
                             421
                                            429
                                                            149
                                                                           247
    0.2540892203
                   0.2553507890
                                  0.2629073561
                                                  0.2651367851
                                                                 0.2651890306
##
##
               68
                              80
                                            290
                                                            476
                                                                           459
##
    0.2729128907
                   0.2747733449
                                  0.2818450186
                                                  0.2823343540
                                                                 0.2861828496
##
               54
                             270
                                            536
                                                            178
    0.2921796154
                                  0.2932963025
##
                   0.2929452015
                                                  0.2970394642
                                                                 0.3012018698
##
              220
                             402
                                             13
                                                            272
                                                                           182
##
    0.3043648219
                   0.3077293548
                                  0.3128439366
                                                  0.3186677815
                                                                 0.3192668475
##
              424
                             183
                                            332
                                                            349
                                                                           263
##
    0.3200896328
                   0.3314673456
                                  0.3337301493
                                                  0.3352879307
                                                                 0.3356865151
##
              258
                             423
                                            157
                                                            387
                                                                           282
##
    0.3393741053
                   0.3426494154
                                  0.3446709560
                                                  0.3499235064
                                                                 0.3581590756
##
              490
                              49
                                                            467
                                                                           462
                                            159
##
    0.3591191139
                   0.3606851703
                                  0.3627533753  0.3638107500
                                                                 0.3654337345
```

##	291	496	74	400	463
##	0.3745959328	0.3753174803	0.3786756330	0.3814710477	0.3833430451
##	134	513	330	352	383
##	0.3871008736	0.3891684973	0.4018631893	0.4029925476	0.4046437209
##	367	433	366	502	9
##	0.4128293020	0.4170171640	0.4203710512	0.4270778296	0.4325687066
##	492	368	482	486	76
##	0.4359668082	0.4398484156	0.4410886485	0.4514618627	0.4562594459
##	297	376	481	60	201
##	0.4668533223	0.4681511177	0.4683417773	0.4700124991	0.4724998841
##	499	413	461	186	508
##	0.4757386752	0.4880882243	0.4913590385	0.4925517513	0.4959816417
##	215	121	52	305	262
##	0.4976990806	0.5018458605	0.5078055562	0.5101106654	0.5104532395
##	531	333	104	519	443
##	0.5261983310	0.5310889784	0.5318550301	0.5373656298	0.5431521249
##	100	381	147	404	93
##	0.5439675421	0.5463692229	0.5520035571	0.5685125358	0.5693258408
##	142	399	114	355	287
##	0.5736539592	0.5794678015	0.5916725662	0.5958206058	0.5965228069
##	320	487	271	39	4
##	0.6013768064	0.6157044676	0.6373724635	0.6449091230	0.6464272259
##	283	509	403	40	500
##	0.6493081629	0.6499737835	0.6512878136	0.6533818655	0.6535348756
##	379	37	449	71	56
##	0.6561684278	0.6611845503	0.6770960771	0.6801061986	0.6812595870
##	432	301	140	430	172
##	0.6902465172	0.6936488180	0.6982104689	0.7073396613	0.7149148939
##	6	378	208	177	148
##	0.7189264253	0.7245864347	0.7326412051	0.7387145580	0.7458748399
##	83	61	107	5	479
##	0.7489622248	0.7509322538	0.7581849225	0.7730585188	0.7827966442
##	374	427	279	517	294
##	0.7883457385	0.7925684722	0.7972443045	0.8163236918	0.8191532646
##	268	327	20	152	238
##	0.8198844387	0.8231476044	0.8384163378	0.8427285412	0.8638735652
##	396	33	446	123	316
##	0.8763243336	0.8907888764	0.8967562084	0.9073851861	0.9095593221
##	99	455	232	285	7
##	0.9118447104	0.9152398229	0.9153801708		
##	124	102	299	217	375
##	0.9472166077	0.9513294214	0.9717847915	0.9822101391	
##	493 1.0036144319	347 1.0083106861	46 1.0097174110	300 1.0516400451	313 1.0661923284
## ##	1.0036144319	194	342	202	426
##	1.0727839359	1.0754361874	1.0941853179	1.1042308655	1.1050948609
##	329	354	389	319	127
##	1.1209892434	1.1279364296	1.1346958386	1.1459402510	1.1707851944
##	230	184	45	289	460
##	1.1737283739	1.1842690492	1.1875892697	1.2020531975	1.2060678282
##	125	358	503	228	22
##	1.2283142920	1.2304047334	1.2419119694	1.2548706804	
##	87	174	350	112	353
##		1.2926711074		1.3563137014	
	100 f1000	T	0102204010	1.0000101014	1.001101010

```
175
                                 173
    1.3663082680
                 1.3663112807 1.3755675076 1.3772426052 1.3900625613
##
##
            377
                          38
                                 243
                                                      415
                               1.4796831632
    1.4239701436
                 1.4299921117
##
                                             1.4817778401
                                                           1.5164304380
##
            222
                          264
                                       195
##
                 1.6101693013
                              1.6106285185
    1.5325628883
                                             1.6602465489
                                                           1.6770498757
            534
                         190
                                      225
                                             1.7071906017
##
    1.6773538426
                 1.6802415321
                               1.6919457731
                                                           1.7410843982
##
            390
                          405
                                        307
                                                       72
                 1.8020257833
                               1.8289388919
                                             1.9192420768
##
    1.7529466695
                                                          1.9525368372
            360
                          189
                                        388
                                                      338
    1.9642065079
                 1.9954849408
                               1.9975435893
                                             2.0038457258
##
                                                           2.0091988981
##
            447
                          485
                                       465
                                                      209
                               2.0630396054
                                             2.7780609973
    2.0232225828
                 2.0542623628
                                                           3.1712602783
##
             21
                          267
                                 108
    3.4865705316 3.7222771163 3.9927493813 4.2317956705
```

## sort(cooks.distance(model))

```
488
                            251
                                      66
                                              468
        361
## 1.894425e-11 1.031235e-09 5.938212e-09 2.962454e-08 3.374946e-08 4.785281e-08
      51 373 450 295 207
## 7.181719e-08 7.377056e-08 1.934563e-07 2.391962e-07 2.684650e-07 3.271250e-07
    15 259 250
                               188 365
## 4.027962e-07 4.966822e-07 6.012579e-07 6.341895e-07 7.236477e-07 9.144424e-07
    16 276
                          341
                                    214
## 1.065229e-06 1.168975e-06 1.179326e-06 1.254819e-06 1.267700e-06 1.288529e-06
                  260 30 103
        274
                                               226
## 1.326855e-06 1.435053e-06 1.676687e-06 1.691323e-06 1.718873e-06 1.727156e-06
            84 495 526 65
## 1.908889e-06 1.962879e-06 2.056352e-06 2.260643e-06 2.520172e-06 2.885847e-06
            384 510 411 435
  537
## 2.893053e-06 2.978896e-06 3.558600e-06 3.928119e-06 3.935160e-06 3.996640e-06
       372 293 179
                                    210 420
## 4.048125e-06 4.048868e-06 4.079114e-06 4.471245e-06 4.725415e-06 5.007805e-06
            298
       196
                     59 119 67
## 5.178077e-06 5.362777e-06 5.611925e-06 5.686429e-06 6.309364e-06 6.368506e-06
            515 187 528 323
## 6.598784e-06 6.717719e-06 7.048434e-06 7.465908e-06 9.106888e-06 9.108172e-06
        441
             160
                      97
                                 12
                                              151
## 9.155028e-06 9.338848e-06 1.158806e-05 1.166200e-05 1.173757e-05 1.186069e-05
                 162
                          129
                                     418
                                              425
        122
## 1.249194e-05 1.267499e-05 1.327396e-05 1.416798e-05 1.437660e-05 1.609183e-05
        192
                  273 131
                                     514
                                                25
## 1.680365e-05 1.687357e-05 1.713977e-05 1.759324e-05 1.837282e-05 1.837917e-05
             132 48
                                    452 359
## 1.853139e-05 1.924811e-05 1.930710e-05 1.979907e-05 2.027293e-05 2.204298e-05
       336
            141 203
                                    464 82
## 2.214975e-05 2.236852e-05 2.443524e-05 2.451313e-05 2.453217e-05 2.485009e-05
       343 473 181
                                    440 64
## 2.505995e-05 2.540719e-05 2.593851e-05 2.647991e-05 2.700147e-05 2.885752e-05
                  246 168
                                     363
                                          80
## 3.043145e-05 3.319758e-05 3.340568e-05 3.365666e-05 3.385928e-05 3.603603e-05
        245
                 158
                           256
                                     438
                                              115
```

```
## 3.649277e-05 3.849248e-05 3.875995e-05 3.876704e-05 3.894664e-05 3.944581e-05
            315 318 303 145
        325
## 4.091162e-05 4.370143e-05 4.382643e-05 4.533768e-05 4.589330e-05 4.622323e-05
                           149
               247
                                     407
                                         211
## 4.844555e-05 4.871997e-05 4.934066e-05 5.016204e-05 5.072263e-05 5.143806e-05
                           394
                                     472 266
       454
                 370
## 5.319451e-05 5.426198e-05 5.430199e-05 5.545883e-05 5.935568e-05 5.978797e-05
        146 470 78 116 476
## 5.996373e-05 6.040572e-05 6.151622e-05 6.372189e-05 6.395908e-05 6.503768e-05
                     401 178 284
        139 511
## 6.622882e-05 6.767947e-05 6.776139e-05 7.251625e-05 7.264263e-05 7.270308e-05
                           258 58 111
       220
                  216
## 7.365211e-05 7.424644e-05 7.553865e-05 7.581387e-05 7.635092e-05 7.690073e-05
        14 502 134 421 34
## 7.831716e-05 7.856180e-05 8.019588e-05 8.048830e-05 8.165056e-05 8.208703e-05
       317
            42 497 332 9
## 8.256073e-05 8.288596e-05 8.335974e-05 8.426876e-05 8.459037e-05 8.652022e-05
     86 53 414 290 165
## 8.751804e-05 8.761428e-05 8.939273e-05 9.111056e-05 9.289621e-05 9.386647e-05
       218
            436 410 206
                                         182
## 9.407938e-05 9.569561e-05 9.726004e-05 9.735249e-05 1.005091e-04 1.012915e-04
                          345 423 380 52
        277 457
## 1.015283e-04 1.026670e-04 1.028799e-04 1.044618e-04 1.062388e-04 1.083791e-04
            477 368 68 291
        326
## 1.095242e-04 1.117644e-04 1.118395e-04 1.124629e-04 1.133838e-04 1.147012e-04
             63
                      459 349 501
## 1.173036e-04 1.201884e-04 1.215633e-04 1.227327e-04 1.230596e-04 1.249804e-04
        400
             413
                           433
                                     362
                                         512
## 1.276824e-04 1.288712e-04 1.293978e-04 1.313412e-04 1.322063e-04 1.332342e-04
        170
                  467 41
                                     305
                                              104
## 1.345754e-04 1.348093e-04 1.368881e-04 1.386606e-04 1.389807e-04 1.390924e-04
        215
                  286
                            335 54 113
## 1.402661e-04 1.424186e-04 1.441545e-04 1.465655e-04 1.474191e-04 1.481914e-04
                        147 95
                  280
                                              337
        462
## 1.505715e-04 1.507092e-04 1.507460e-04 1.516580e-04 1.543588e-04 1.549460e-04
                  77
                                 73 505
       330
                           461
## 1.574498e-04 1.574614e-04 1.595923e-04 1.603213e-04 1.627770e-04 1.676347e-04
        304
            57
                           463 366 364
## 1.679754e-04 1.724377e-04 1.733220e-04 1.745917e-04 1.823307e-04 1.861122e-04
              4 314
                                     271
        406
                                              157
## 1.866510e-04 1.869065e-04 1.877231e-04 1.878404e-04 1.968724e-04 1.983376e-04
             508
                           434
                                     261 143
       244
## 1.985163e-04 2.003137e-04 2.020553e-04 2.022822e-04 2.050293e-04 2.054140e-04
     37
             263 74
                                    381 308
## 2.055811e-04 2.094330e-04 2.106210e-04 2.162984e-04 2.225466e-04 2.230555e-04
  6
                  357 399 201 29
## 2.245002e-04 2.269250e-04 2.269821e-04 2.304909e-04 2.359160e-04 2.383064e-04
        301 159 148 504 200
## 2.430518e-04 2.459690e-04 2.501671e-04 2.504775e-04 2.512579e-04 2.512881e-04
       422 88 69 507 105
## 2.539809e-04 2.540060e-04 2.595787e-04 2.597693e-04 2.644427e-04 2.646213e-04
       275 180 412 310 121 398
## 2.677451e-04 2.678570e-04 2.740289e-04 2.744593e-04 2.753961e-04 2.762788e-04
        491
                  391
                            403
                                     409
                                                376
```

```
## 2.809933e-04 2.899492e-04 2.967993e-04 2.989841e-04 3.030954e-04 3.058055e-04
        397 331 466 231 519
## 3.087584e-04 3.098153e-04 3.113560e-04 3.126090e-04 3.127738e-04 3.237594e-04
             135 355
                                    152 431
## 3.261045e-04 3.287205e-04 3.305228e-04 3.339593e-04 3.360913e-04 3.396365e-04
       242 509 458 417 430
## 3.398618e-04 3.408697e-04 3.416655e-04 3.419946e-04 3.424457e-04 3.460615e-04
        55 492 253 352 327
## 3.507177e-04 3.560201e-04 3.565225e-04 3.849186e-04 3.865136e-04 3.924832e-04
        520 451 1 142 118
## 4.099226e-04 4.102448e-04 4.130123e-04 4.169538e-04 4.188799e-04 4.356857e-04
            311 114 83 56
       281
## 4.388527e-04 4.467019e-04 4.522592e-04 4.592287e-04 4.645359e-04 4.672003e-04
       285 155 130 427 374
## 4.683281e-04 4.804286e-04 4.807375e-04 4.880009e-04 4.897822e-04 4.941211e-04
       193 102 402 79 272
## 4.950371e-04 5.002843e-04 5.007090e-04 5.015861e-04 5.114048e-04 5.134171e-04
        227 93 279 91 40
## 5.145175e-04 5.152590e-04 5.156858e-04 5.270809e-04 5.342231e-04 5.422829e-04
            486 234 49 100
       513
## 5.487922e-04 5.669072e-04 5.678988e-04 5.692169e-04 6.122192e-04 6.154322e-04
       62 387 342 70 191
## 6.171791e-04 6.375865e-04 6.410802e-04 6.482029e-04 6.523854e-04 6.762175e-04
            481 448 133 432 404
       500
## 6.855011e-04 6.873564e-04 7.027451e-04 7.105556e-04 7.155075e-04 7.212449e-04
     31 294 516 379 480 313
## 7.315481e-04 7.333191e-04 7.333197e-04 7.369610e-04 7.795153e-04 7.841425e-04
       128
            453
                      33
                                    236 347
## 8.023157e-04 8.054175e-04 8.110379e-04 8.176123e-04 8.249704e-04 8.271505e-04
       202 538 32
                                    449 252
## 8.395756e-04 8.399192e-04 8.432605e-04 8.498984e-04 8.596217e-04 8.645108e-04
                  309 20 536
        503
                                              283
## 8.832176e-04 9.064859e-04 9.107299e-04 9.218656e-04 9.556533e-04 9.873177e-04
        367
             493 172
                                43 144
## 9.903765e-04 9.911646e-04 1.007765e-03 1.010778e-03 1.014221e-03 1.029078e-03
     96 356 455 257 76
## 1.046547e-03 1.049633e-03 1.054812e-03 1.057135e-03 1.059390e-03 1.077251e-03
       319 518 124 87 140
## 1.100039e-03 1.105741e-03 1.107681e-03 1.123749e-03 1.141053e-03 1.179166e-03
                     415 316 534
        297
            150
## 1.180442e-03 1.180686e-03 1.180841e-03 1.193067e-03 1.194858e-03 1.202903e-03
            19 194 61 38
       395
## 1.205966e-03 1.221988e-03 1.226174e-03 1.248466e-03 1.300391e-03 1.308303e-03
            174
                          123 443 324
       484
## 1.355520e-03 1.365197e-03 1.375204e-03 1.382406e-03 1.385098e-03 1.408378e-03
                  262 137
                                    469
                                              389
        243
## 1.414536e-03 1.417259e-03 1.430307e-03 1.448386e-03 1.472562e-03 1.492205e-03
     99 7 426 529 474
## 1.507841e-03 1.512935e-03 1.527392e-03 1.531141e-03 1.536666e-03 1.549027e-03
     71 136 268 329 175
## 1.567566e-03 1.571826e-03 1.586048e-03 1.586779e-03 1.621777e-03 1.629869e-03
       120 460 288 312 208 287
## 1.664688e-03 1.670638e-03 1.711263e-03 1.734445e-03 1.752328e-03 1.761038e-03
        225
                  255
                          171
                                    46
                                              228
```

```
## 1.777122e-03 1.778148e-03 1.848691e-03 1.888090e-03 1.888549e-03 1.905212e-03
                   392 532 156
         184
                                                350
## 1.926394e-03 2.005923e-03 2.057400e-03 2.060087e-03 2.065077e-03 2.090979e-03
              232 483 360 45
## 2.149124e-03 2.163870e-03 2.227276e-03 2.320633e-03 2.326583e-03 2.334405e-03
         264 92 10 300 217
## 2.472173e-03 2.565086e-03 2.567590e-03 2.701218e-03 2.715395e-03 2.839349e-03
         321 185 238 169
## 2.929909e-03 3.007954e-03 3.008430e-03 3.020066e-03 3.104523e-03 3.116880e-03
         23 127 375 525
                                                 358
## 3.123215e-03 3.317081e-03 3.395900e-03 3.446176e-03 3.555919e-03 3.584378e-03
         222 176 24 296
                                                 530
## 3.647439e-03 3.789062e-03 3.945226e-03 3.970438e-03 3.985693e-03 4.046286e-03
        521 2 446
                                      161 138
## 4.297517e-03 4.339334e-03 4.350785e-03 4.413104e-03 4.511386e-03 4.591654e-03
         442
                   230 154 205 35
## 5.108157e-03 5.185419e-03 5.469589e-03 5.502998e-03 5.561782e-03 5.585748e-03
         189 47 522 254
                                           289
## 5.898737e-03 5.924290e-03 6.408222e-03 6.534842e-03 6.569418e-03 6.613315e-03
        437 533 36 28 22
## 6.891290e-03 6.984110e-03 7.022394e-03 7.083118e-03 7.150878e-03 7.258161e-03
         390 485 447 405 94
## 7.390293e-03 7.949045e-03 8.010655e-03 8.355220e-03 8.874000e-03 8.879928e-03
                   265 8 89 385
## 9.332334e-03 9.491773e-03 9.625772e-03 1.033897e-02 1.033990e-02 1.076356e-02
             539 167 416 81
## 1.077398e-02 1.250554e-02 1.283722e-02 1.294739e-02 1.379102e-02 1.391792e-02
                   11 209 173 190
         338
## 1.483759e-02 1.496543e-02 1.565484e-02 1.607129e-02 1.639566e-02 1.664932e-02
                  478 249
     3
                                      239
## 1.722611e-02 1.732873e-02 1.789932e-02 1.855399e-02 2.055788e-02 2.108291e-02
         307
                   163 465 164 117
## 2.169169e-02 2.205859e-02 2.363349e-02 2.388718e-02 2.408604e-02 2.565791e-02
         98 110 21 166
                                                 527
## 3.572263e-02 3.635904e-02 3.894945e-02 4.257368e-02 4.278653e-02 4.730125e-02
         75 17 108 292
## 4.858806e-02 6.019063e-02 6.491203e-02 2.010870e-01 2.365909e-01
skewness(jackknife)
## [1] -0.0005651455
kurtosis(jackknife)
## [1] 4.882543
NBA <- dummy_cols(NBA, select_columns = "DRAFT_ROUND", remove_first_dummy = TRUE)
## # A tibble: 539 x 49
                      AGE HEIGHT INCHES TOTAL_HEIGHT WEIGHT COLLEGE COUNTRY
    FIRST
           LAST TEAM
           <chr> <chr> <chr> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
##
    <chr>
```

```
## 1 Precious Achiu~ TOR
                               23
                                             8
                                                          80
                                                                225 Memphis Nigeria
## 2 Steven Adams MEM
                               29
                                                         83
                                                                265 Pittsb~ New Ze~
                                      6
                                            11
              Adeba~ MIA
## 3 Bam
                               25
                                             9
                                                         81
                                                                255 Kentuc~ USA
## 4 Ochai
              Agbaji UTA
                              23
                                      6
                                             5
                                                         77
                                                                215 Kansas USA
                                                                215 Loyola~ Spain
## 5 Santi
              Aldama MEM
                               22
                                      7
                                             1
                                                          85
## 6 Nickeil Alexa~ MIN
                                                         77
                                                                205 Virgin~ Canada
                              24
                                      6
                                             5
## 7 Grayson Allen MIL
                              27
                                      6
                                             4
                                                         76
                                                               198 Duke
## 8 Jarrett Allen CLE
                              25
                                      6
                                             9
                                                          81
                                                                243 Texas
                                                                            USA
## 9 Jose
              Alvar~ NOP
                               25
                                      6
                                             1
                                                          73
                                                                179 Georgi~ USA
                                      6
                                                                230 UCLA
## 10 Kyle
              Ander~ MIN
                               29
                                             9
                                                          81
                                                                            USA
## # i 529 more rows
## # i 39 more variables: DRAFT_YEAR <chr>, DRAFT_ROUND <chr>, DRAFT_NUMBER <chr>,
       GP <dbl>, W <dbl>, L <dbl>, MIN <dbl>, PTS <dbl>, FGM <dbl>, FGA <dbl>,
      'FG%' <dbl>, '3PM' <dbl>, '3PA' <dbl>, '3P%' <dbl>, FTM <dbl>, FTA <dbl>,
## #
       'FT%' <dbl>, OREB <dbl>, DREB <dbl>, REB <dbl>, AST <dbl>, TOV <dbl>,
## #
       STL <dbl>, BLK <dbl>, PF <dbl>, FP <dbl>, DD2 <dbl>, TD3 <dbl>,
      '+/-' <dbl>, NETRTG <dbl>, 'OREB%' <dbl>, 'DREB%' <dbl>, 'USG%' <dbl>, ...
model2 <- lm(PTS ~ HEIGHT + MIN + FGM + FTM + PF + DRAFT_ROUND_2 + DRAFT_ROUND_Undrafted, data = NBA)
summary(model2)
##
## Call:
## lm(formula = PTS ~ HEIGHT + MIN + FGM + FTM + PF + DRAFT_ROUND_2 +
       DRAFT_ROUND_Undrafted, data = NBA)
##
## Residuals:
                     Median
       Min
                 1Q
                                    30
                                            Max
## -1.84321 -0.29160 0.00745 0.31655 2.33387
## Coefficients:
                         Estimate Std. Error t value Pr(>|t|)
##
                         1.471345
                                    0.601195
                                              2.447 0.01471 *
## (Intercept)
                                    0.097735 -2.599 0.00961 **
## HEIGHT
                         -0.254026
## MIN
                         0.059484
                                    0.006885
                                               8.640
                                                      < 2e-16 ***
                         2.209876
## FGM
                                    0.030926 71.456 < 2e-16 ***
## FTM
                                    0.032754 24.958 < 2e-16 ***
                         0.817471
## PF
                        -0.341527
                                    0.049874 -6.848 2.09e-11 ***
## DRAFT ROUND 2
                         -0.038080
                                    0.066142 -0.576 0.56504
## DRAFT_ROUND_Undrafted 0.094052
                                    0.068268
                                               1.378 0.16888
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 0.5807 on 529 degrees of freedom
     (2 observations deleted due to missingness)
## Multiple R-squared: 0.9929, Adjusted R-squared: 0.9928
## F-statistic: 1.058e+04 on 7 and 529 DF, p-value: < 2.2e-16
model2 %>% tidy()
## # A tibble: 8 x 5
##
    term
                           estimate std.error statistic
                                                         p.value
```

<dbl>

<dbl>

<dbl>

<dbl>

##

<chr>>

##	1	(Intercept)	1.47	0.601	2.45	1.47e- 2
		HEIGHT	-0.254	0.0977	-2.60	9.61e- 3
##	3	MIN	0.0595	0.00688	8.64	6.67e- 17
##	4	FGM	2.21	0.0309	71.5	6.37e-274
##	5	FTM	0.817	0.0328	25.0	1.93e- 91
##	6	PF	-0.342	0.0499	-6.85	2.09e- 11
##	7	DRAFT_ROUND_2	-0.0381	0.0661	-0.576	5.65e- 1
##	8	DRAFT_ROUND_Undrafted	0.0941	0.0683	1.38	1.69e- 1