

## Delaunay Triangulation

Generated by Doxygen 1.8.5

Wed Nov 25 2015 16:50:57



# Contents

<b>1</b>	<b>Class Index</b>	<b>1</b>
1.1	Class List . . . . .	1
<b>2</b>	<b>Class Documentation</b>	<b>3</b>
2.1	Delaunay3d Class Reference . . . . .	3
2.1.1	Member Function Documentation . . . . .	4
2.1.1.1	bowyer_watson . . . . .	4
2.1.1.2	check_face_tet . . . . .	4
2.1.1.3	compute_circumcircle . . . . .	4
2.1.1.4	compute_jacobian . . . . .	4
2.1.1.5	cross_product3 . . . . .	4
2.1.1.6	det4 . . . . .	4
2.2	Face Struct Reference . . . . .	5
2.2.1	Detailed Description . . . . .	5
2.3	Tet Class Reference . . . . .	5
2.3.1	Detailed Description . . . . .	5
2.4	Walkdata Struct Reference . . . . .	6
2.4.1	Detailed Description . . . . .	6
	<b>Index</b>	<b>7</b>



# Chapter 1

## Class Index

### 1.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

<a href="#">Delaunay3d</a>	3
<a href="#">Face</a>	5
<a href="#">Tet</a>	5
<a href="#">Walkdata</a>	6



## Chapter 2

# Class Documentation

## 2.1 Delaunay3d Class Reference

### Public Member Functions

- **Delaunay3d** (Matrix< double > \*\_points, int num\_points)
- **Delaunay3d** (const [Delaunay3d](#) &other)
- [Delaunay3d](#) & **operator=** (const [Delaunay3d](#) &other)
- void **setup** (Matrix< double > \*\_points, int num\_points)
- double **l2norm** (const vector< double > &a)
- double **dot** (const vector< double > &a, const vector< double > &b)
- void **compute\_jacobian** ([Tet](#) &elem)
- void **cross\_product3** (vector< double > &c, const vector< double > &a, const vector< double > &b)
- void **compute\_circumsphere** ([Tet](#) &elem)
- double **det4** (int ielem, int i, const vector< double > &r) const
- int **find\_containing\_tet** (const vector< double > &r, int startelement) const
- int **check\_face\_tet** (const [Tet](#) &elem, const [Face](#) &face) const
- void **compute\_circumcircle** ([Tet](#) &elem)
- void **bowyer\_watson** ()
- void **clear** ()  
*Reset the [Delaunay3d](#) object, except for input data.*
- void **writeGmsh2** (string mfile)
- [Walkdata](#) **find\_containing\_tet\_and\_barycentric\_coords** (const vector< double > &rr, int startelement) const
- void **compute\_jacobians** ()
- bool **detect\_negative\_jacobians** ()

### Public Attributes

- Matrix< double > **points**
- std::vector< Point > [nodes](#)  
*List of nodes in the Delaunay graph.*
- std::vector< [Tet](#) > [elems](#)  
*List of all elements ([tetrahedra](#)) in the Delaunay graph.*
- std::vector< int > [badelems](#)  
*Collection of 'bad elements', that are to be removed while adding a point; its are integers that index members index [elems](#).*
- std::vector< [Face](#) > [faces](#)  
*List of all [faces](#) in the Delaunay graph.*

- `std::vector< int >` **voidpoly**

*Collection of faces that bounds the void obtained after removing bad elements while adding a point; its members are integers that index **faces**.*

- `Matrix< double >` **jacobians**
- `int` **npoints**

## 2.1.1 Member Function Documentation

### 2.1.1.1 `void Delaunay3d::bowyer_watson ( )`

Computes the Delaunay triangulation (tetrahedralization, in this case). Make sure 'points' has space for three more points when passing to this sub. 'N' is the actual number of real points. First, find the element containing the new point

Second, search among neighbors for other triangles whose circumcircles contain this point

Third, store the faces that will be obtained after removal of bad triangles

Delete faces which are between two bad elements. NOTE: This is one place that is inefficient because of use of array stacks (`std::vectors`) as it needs deletion of arbitrary members.

Fourth, delete bad elements. This is another place where array stacks (vectors) of elems, badelems etc make the program slower.

Fifth, add new elements; these are formed by the faces in voidpoly and the new point. Also correspondingly update 'faces'.

### 2.1.1.2 `int Delaunay3d::check_face_tet ( const Tet & elem, const Face & face ) const` `[inline]`

Returns the local face number (number of node opposite to the face) of elem's face that is the same as the second argument. If no faces of elem match, it returns -1.

### 2.1.1.3 `void Delaunay3d::compute_circumcircle ( Tet & elem )`

Computes circumcentre and circumradius of a **tetrahedron**. NOTE: The tetrahedron's jacobian (2\*volume) should be stored in `[elem.D](&ref D)` beforehand. The center and radius of the circumsphere are calculated as follows. The circumcenter is

$$\mathbf{O} = \frac{|\mathbf{a}^2(\mathbf{b} \times \mathbf{c}) + \mathbf{b}^2(\mathbf{c} \times \mathbf{a}) + \mathbf{c}^2(\mathbf{a} \times \mathbf{b})|}{12V}$$

and the radius  $R = |\mathbf{O}|$ .

### 2.1.1.4 `void Delaunay3d::compute_jacobian ( Tet & elem )`

Computes 6\*volume of any tetrahedron.

### 2.1.1.5 `void Delaunay3d::cross_product3 ( vector< double > & c, const vector< double > & a, const vector< double > & b )` `[inline]`

Computes cross product c of two 3-vectors a and b.

### 2.1.1.6 `double Delaunay3d::det4 ( int ielem, int i, const vector< double > & r ) const`

Calculates the jacobian of the tetrahedron formed by point r and a face of tetrahedron ielem. The face is selected by i between 0 and 3. **Face** i is the face opposite to local node i of the tetrahedron.

The documentation for this class was generated from the following file:



- /home/aditya/Myprojects/amovemesh/include/abowyerwatson3d.hpp

## 2.2 Face Struct Reference

```
#include <abowyerwatson3d.hpp>
```

### Public Attributes

- int **p** [3]
- int **elem** [2]

### 2.2.1 Detailed Description

Structure for triangular face.

The documentation for this struct was generated from the following file:

- /home/aditya/Myprojects/amovemesh/include/abowyerwatson3d.hpp

## 2.3 Tet Class Reference

```
#include <abowyerwatson3d.hpp>
```

### Public Member Functions

- **Tet** (const [Tet](#) &other)

### Public Attributes

- int [p](#) [4]  
*Indices of vertices.*
- Point [centre](#)  
*Coords of circumcenter of the tet.*
- int [surr](#) [4]  
*Indices of surrounding tets. Note that the neighbor corresponding to surr[3] is opposite the vertex p[3].*
- double [D](#)  
*6\*volume of tet.*
- double [radius](#)  
*Radius of circumcircle of tet.*

### 2.3.1 Detailed Description

Class representing a tetrahedron.

The documentation for this class was generated from the following file:

- /home/aditya/Myprojects/amovemesh/include/abowyerwatson3d.hpp

## 2.4 Walkdata Struct Reference

```
#include <abowyerwatson3d.hpp>
```

### Public Attributes

- int **elem**
- double **areacoords** [4]

#### 2.4.1 Detailed Description

Intended to encapsulate data required by 'walk-through' algorithms. Not needed for mesh generation, but in independent application of the walk-through subroutine `find_containing_triangle_and_area_coords()`.

The documentation for this struct was generated from the following file:

- `/home/aditya/Myprojects/amovemesh/include/abowyerwatson3d.hpp`

# Index

bowyer\_watson  
Delaunay3d, [4](#)

check\_face\_tet  
Delaunay3d, [4](#)

compute\_circumcircle  
Delaunay3d, [4](#)

compute\_jacobian  
Delaunay3d, [4](#)

cross\_product3  
Delaunay3d, [4](#)

Delaunay3d, [3](#)  
    bowyer\_watson, [4](#)  
    check\_face\_tet, [4](#)  
    compute\_circumcircle, [4](#)  
    compute\_jacobian, [4](#)  
    cross\_product3, [4](#)  
    det4, [4](#)

det4  
Delaunay3d, [4](#)

Face, [5](#)

Tet, [5](#)

Walkdata, [6](#)