For the second-order source extension, we examine the symbols as pairs rather than individually, observing the dependencies and relationships between the symbols. As in the previous question, we need to identify all the pairs that exist within the image. Therefore, we will look at the neighbor of each pixel to see which pairs are present.

## Identification of discrete symbols:

We will look for horizontal and vertical pairs (all neighboring pixels).

Two variables will be needed to store all the pairs, as well as code to generate them.

## The variables:

```
orizodia_zeugaria = containers.Map('KeyType', 'char', 'ValueType',
  'double');
katheta_zeugaria = containers.Map('KeyType', 'char', 'ValueType',
  'double');
```

The method of creating pairs:

```
for i = 1:row
   for j = 1:(col - 1)
orizodio zeugari = [image(i, j), image(i, j + 1)];
```

Where in the loop, it takes the pixel where the counter is located and pairs it with the next one in the row. In the same way, we create the vertical pair:

```
for i = 1:(row - 1)
    for j = 1:col
katheto_zeugari= [image(i, j), image(i + 1, j)];
```

Let's proceed with finding the probabilities. As we did in **Question 1**, we will divide each horizontal pair by the total number of horizontal pairs, and similarly for each vertical pair.

```
orizodies_pithanotites = zeros(1, length(horizontal_keys));
for i = 1:length(horizontal_keys)
    arithos_emfaniseon = orizodia_zeugaria(horizontal_keys{i});
    pithanotita = arithos_emfaniseon / sinolika_orizodia_zeugaria;
    orizodies_pithanotites(i) = pithanotita;
```

Αρχικά δημιουργούμε το array orizodies\_pithanotites στο οποίο θα αποθηκεύετε η First, we create the orizodies\_pithanotites array, where the probability of each pair will be stored. Then, the loop counts how many times each pair appears in the image and stores the result in the variable arithmos\_emfaniseon. Finally, we calculate the probability as mentioned above and store the result in the array. We use the same method to find the vertical probabilities.

The results we obtain:

```
17 102: 0.00013423 238 221: 0.0037919
                                                                     kathetes pithanotites:
orizodies pithanotites:
                                                                      0 0: 0.081139
                          17 119: 0.00010067
                                              238 238: 0.015839
0 0: 0.078926
                          17 136: 0.00010067
                                                                     0 102: 0.0001005
                                              238 255: 0.0013758
0 119: 3.3557e-05
                          17 153: 3.3557e-05
                                                                      0 17: 0.012831
0 136: 6.7114e-05
                                               255 170: 3.3557e-05
                          17 17: 0.046846
                                                                      0 34: 0.0012395
0 17: 0.013255
                                               255 187: 6.7114e-05
                          17 170: 6.7114e-05
                                                                      0 51: 0.00040201
0 34: 0.0020134
                                               255 221: 0.00016779
                         17 34: 0.014564
                                                                      0 68: 0.00026801
0 51: 0.00057047
                                               255 238: 0.0014094
                         17 51: 0.0029195
                                                                      0 85: 3.3501e-05
  68: 0.00040268
                                               255 255: 0.0014765
                         17 68: 0.0014765
                                                                      102 17: 0.000134
0 85: 0.00026846
                                               34 0: 0.0013423
                          17 85: 0.00067114
                                                                      102 34: 0.00036851
102 17: 0.00030201
                                               34 102: 0.0007047
                          170 17: 3.3557e-05
                                                                      102
                                                                           51: 0.0015745
    34: 0.00067114
102
                                               34 119: 0.00053691
                          170
                               51: 0.00016779
                                                                            68: 0.0036181
                                                                      102
102 51: 0.0018121
                                               34 136: 0.00020134
                          170 68: 0.0002349
                                                                           85: 0.016549
                                                                      102
102 68: 0.0058725
                                               34 153: 0.00016779
                          170 85: 0.00053691
                                                                      102 102: 0.070117
102 85: 0.018725
                                               34 17: 0.015369
                          170 102: 0.00067114
                                                                     102 119: 0.015645
102 102: 0.059832
                                               34 187: 0.00016779
                          170 119: 0.0012752
                                                                     102 136: 0.0026466
102 119: 0.018926
                                               34 204: 3.3557e-05
                          170 136: 0.0030872
                                                                      102 153: 0.001072
102 136: 0.004698
                          170 153: 0.009094
                                               34 34: 0.032248
                                                                      102 170: 0.00056951
102 153: 0.0018121
                          170 170: 0.015168
                                               34 51: 0.011913
                                                                      102 187: 0.00063652
102 170: 0.0004698
                          170 187: 0.0069799
                                                                      102 204: 0.0001675
                                               34 68: 0.0037248
102
    187: 0.00020134
                          170 204: 0.0013423
                                                                      102 221: 0.0001005
                                               34 85: 0.0015101
102 204: 0.00010067
                          170 221: 0.00033557
                                                                     102 238: 0.0001005
                                               51 0: 0.00033557
119
    17: 0.00020134
                          170 238: 0.00010067
                                                                     102 255: 3.3501e-05
                                               51 102: 0.0016443
    34: 0.00040268
119
                          187 34: 3.3557e-05
                                                                      119 34: 0.000134
                                               51 119: 0.00050336
119 51: 0.00097315
                          187
                                51: 3.3557e-05
                                                                      119
                                                                           51: 0.00043551
                                               51 136: 0.00053691
119 68: 0.0023154
                          187
                                68: 6.7114e-05
                                                                      119
                                                                           68: 0.0017755
                                               51 153: 0.00026846
119 85: 0.005302
                          187 85: 0.00016779
                                                                           85: 0.0047236
                                                                      119
                                               51 17: 0.0035906
119 102: 0.016913
                          187 102: 0.00040268
                                                                      119 102: 0.015779
                                               51 170: 0.00010067
119 119: 0.041309
                          187 119: 0.00040268
                                                                     119 119: 0.050151
                                                51 187: 3.3557e-05
119 136: 0.017416
                          187 136: 0.0009396
                                                                     119 136: 0.013367
                                                51 204: 3.3557e-05
119 153: 0.0042953
                          187 153: 0.0018456
                                                                      119 153: 0.0024456
                                               51 221: 3.3557e-05
119 170: 0.0010067
                          187 170: 0.0068792
                                                                      119 170: 0.00063652
119 187: 0.00050336
                          187 187: 0.014463
                                               51 34: 0.013792
                                                                      119 187: 0.00056951
                          187 204: 0.0068121
119 204: 6.7114e-05
                                               51 51: 0.024933
                                                                      119 204: 0.00020101
                          187 221: 0.00087248
119 221: 0.00013423
                                               51 68: 0.012315
                                                                      119 221: 0.0001005
119 238: 3.3557e-05
                          187 238: 0.00010067
                                                                     119 238: 0.000134
                                               51 85: 0.0039597
119 255: 3.3557e-05
                          204 68: 3.3557e-05
                                                                     119 255: 3.3501e-05
                                               68 0: 6.7114e-05
                          204 85: 0.00013423
                                                                     136 17: 3.3501e-05
136 17: 6.7114e-05
                                               68 102: 0.005604
                          204 102: 6.7114e-05
                                                                           34: 3.3501e-05
                                                                      136
136
    34: 0.00016779
                                               68 119: 0.0022148
                          204 119: 0.00020134
                                                                      136
                                                                           51: 0.000134
136 51: 0.00063758
                                               68 136: 0.00057047
                          204 136: 3.3557e-05
                                                                      136
                                                                           68: 0.00036851
136
     68: 0.00083893
                                               68 153: 0.00036913
                                                                      136 85: 0.001541
                          204 153: 0.00073826
136
    85: 0.0023826
                                               68 17: 0.0014094
                          204 170: 0.0017785
                                                                     136 102: 0.0047236
136 102: 0.0060738
                                               68 170: 0.0002349
                          204 187: 0.0060738
                                                                     136 119: 0.015578
136 119: 0.014698
                                               68 187: 3.3557e-05
                          204 204: 0.017685
                                                                     136 136: 0.056348
136 136: 0.050805
                                               68 204: 3.3557e-05
                          204 221: 0.0063758
136 153: 0.017215
                                                                      136 153: 0.013568
                                              68 238: 3.3557e-05
                           204 238: 0.00050336
                                                                      136 170: 0.0020101
136 170: 0.0024161
                                               68 34: 0.0033221
                           204 255: 0.00010067
                                                                      136 187: 0.001005
136 187: 0.0010738
                                              68 51: 0.01349
                          221 68: 3.3557e-05
                                                                      136 204: 0.00030151
136 204: 0.00030201
                          221 85: 6.7114e-05
                                              68 68: 0.034933
                                                                      136 221: 0.0001005
136 221: 0.00016779
                          221 119: 0.00013423 68 85: 0.014362
                                                                     136 238: 0.000134
136 255: 3.3557e-05
                          221 136: 0.00010067
                                               85 102: 0.019597
                                                                     136 255: 0.0001675
153
    17: 3.3557e-05
                          221 153: 0.00036913
                                                                      153 34: 6.7002e-05
                                              85 119: 0.005302
153
     34: 0.00010067
                          221 170: 0.00030201
                                                                      153
                                                                           51: 3.3501e-05
                                               85 136: 0.0020134
     51: 0.00033557
                          221 187: 0.00090604
                                                                      153
                                                                           68: 0.000134
                                               85 153: 0.00057047
153
     68: 0.00073826
                          221 204: 0.0056376
                                                                           85: 0.00036851
                                                                      153
                                              85 17: 0.00040268
153
    85: 0.0007047
                          221 221: 0.013926
                                                                     153 102: 0.00063652
                                               85 170: 0.00040268
153 102: 0.001745
                          221 238: 0.0044295
                                                                     153 119: 0.0035176
153 119: 0.0051007
                                               85 187: 3.3557e-05
                          221 255: 0.00013423
                                                                      153 136: 0.018392
                                               85 204: 0.00016779
153 136: 0.015705
                          238 102: 3.3557e-05
                                                                      153 153: 0.034405
153 153: 0.029966
                                               85 221: 3.3557e-05
                          238 119: 6.7114e-05
                                                                      153 170: 0.0068342
                                              85 238: 3.3557e-05
153 170: 0.010034
                           238 136: 3.3557e-05
                                                                      153 187: 0.001474
153 187: 0.0019463
                                              85 34: 0.0011409
                          238 153: 0.00010067
                                                                      153 204: 0.00093802
153 204: 0.00067114
                         238 170: 0.00020134 85 51: 0.004698
                                                                      153 221: 0.00023451
                         238 187: 0.00030201 85 68: 0.014128
153 221: 0.00020134
                                                                     153 238: 0.0001675
    0: 0.014396
                         $ 238 204: 0.00077181 85 85: 0.04198
                                                                   fx 153 255: 6.7002e-05
```

```
255 153: 3.3501e-05
17 0: 0.012261
                      255 170: 6.7002e-05
 17 102: 0.00043551
 17 119: 0.00020101
                      255 221: 0.0001005
 17 136: 0.00026801
                      255 238: 0.0022111
 17 153: 0.0001005
                      255 255: 0.00073702
 17 17: 0.050452
                      34 0: 0.001005
 17 170: 6.7002e-05
                      34 102: 0.001005
 17 187: 3.3501e-05
                      34 119: 0.00040201
 17 34: 0.013333
                      34 136: 0.00036851
 17 51: 0.0025461
                      34 153: 0.00033501
 17 68: 0.001273
                      34 17: 0.012998
 17 85: 0.00053601
                      34 170: 0.00020101
 170 34: 3.3501e-05
                      34 187: 0.0001675
 170 51: 3.3501e-05
                      34 204: 0.000134
 170 68: 0.0001005
 170 85: 0.00033501
                      34 34: 0.036147
 170 102: 0.000134
                      34 51: 0.01196
 170 119: 0.00067002
                      34 68: 0.0025796
 170 136: 0.0022111
                      34 85: 0.0011725
 170 153: 0.010519
                      51 0: 0.00020101
 170 170: 0.016918
                      51 102: 0.001407
 170 187: 0.0060302
                      51 119: 0.00073702
 170 204: 0.0013735
                      51 136: 0.00020101
 170 221: 0.00040201
                      51 153: 0.00033501
 170 238: 0.0001675
                      51 17: 0.0029816
 170 255: 0.0001005
                      51 170: 0.00023451
 187
      85: 3.3501e-05
 187 102: 6.7002e-05
                      51 187: 6.7002e-05
 187 119: 0.00023451
                      51 204: 0.0001005
 187 136: 0.00060302
                      51 221: 0.0001005
 187 153: 0.0024121
                      51 238: 3.3501e-05
 187 170: 0.0079732
                      51 34: 0.012228
 187 187: 0.013635
                      51 51: 0.028978
 187 204: 0.0059296
                      51 68: 0.012127
 187 221: 0.001474
                      51 85: 0.0023451
 187 238: 0.00050251
                      68 102: 0.0025796
 187 255: 0.00020101
                      68 119: 0.001407
 204 102: 6.7002e-05
                      68 136: 0.00073702
 204 119: 3.3501e-05
                      68 153: 0.00050251
 204 136: 0.00043551
                      68 17: 0.00093802
 204 153: 0.001072
 204 170: 0.0022446
                      68 170: 0.00020101
 204 187: 0.0073702
                      68 187: 0.00023451
 204 204: 0.01675
                      68 204: 0.000134
 204 221: 0.0046566
                      68 221: 0.0001675
 204 238: 0.001005
                      68 238: 0.0001005
 204 255: 0.00020101
                      68 34: 0.0024791
 221
      85: 6.7002e-05
                      68 51: 0.011926
 221 119: 3.3501e-05
                      68 68: 0.041876
 221 136: 6.7002e-05
                      68 85: 0.013568
 221 153: 0.000134
                      85 102: 0.016583
 221 170: 0.00067002
                      85 119: 0.0024121
 221 187: 0.0013735
                      85 136: 0.00134
 221 204: 0.0068342
 221 221: 0.012898
                      85 153: 0.00040201
 221 238: 0.0036516
                      85 17: 0.00030151
 221 255: 0.00030151
                      85 170: 0.00040201
 238 85: 3.3501e-05
                      85 187: 0.00023451
 238 119: 3.3501e-05
                      85 204: 0.0001005
 238 153: 0.000134
                      85 221: 0.0001005
 238 170: 6.7002e-05
                      85 238: 0.0001005
 238 187: 0.00026801
                      85 34: 0.0016415
 238 204: 0.00087102
                      85 51: 0.0041876
 238 221: 0.0055946
                      85 68: 0.013032
 238 238: 0.014171
f 238 255: 0.0013065 85 85: 0.049514
```