

**Question 8**
**(13 marks)**

The owners of a small family business that sells farm-fresh honey decide to advertise their produce online. A website has been created and they monitor the number of visits to the website each day for three weeks. The table below shows time series analysis of the collected data using a seven-day period.

| Week | Day       | Time (t) | Weekly mean | Visits as a percentage of the weekly mean | Deseasonalised data |
|------|-----------|----------|-------------|-------------------------------------------|---------------------|
| 1    | Monday    | 1        | 43.7        | 86.9                                      | 42.4                |
|      | Tuesday   | 2        |             | 91.5                                      | 45.3                |
|      | Wednesday | 3        |             | 77.8                                      | 45.4                |
|      | Thursday  | 4        |             | <b>A</b>                                  | 41.2                |
|      | Friday    | 5        |             | 116.7                                     | 42.6                |
|      | Saturday  | 6        |             | 125.8                                     | 42.0                |
|      | Sunday    | 7        |             | 130.4                                     | 47.0                |
| 2    | Monday    | 8        | 45.9        | 89.4                                      | 45.8                |
|      | Tuesday   | 9        |             | 85.0                                      | 44.1                |
|      | Wednesday | 10       |             | 72.0                                      | 44.1                |
|      | Thursday  | 11       |             | 76.3                                      | 46.5                |
|      | Friday    | 12       |             | 124.3                                     | 47.6                |
|      | Saturday  | 13       |             | 135.2                                     | 47.4                |
|      | Sunday    | 14       |             | 117.8                                     | 44.5                |
| 3    | Monday    | 15       | 50.9        | 92.4                                      | 52.5                |
|      | Tuesday   | 16       |             | 88.5                                      | <b>B</b>            |
|      | Wednesday | 17       |             | 74.7                                      | 50.8                |
|      | Thursday  | 18       |             | 78.7                                      | 53.1                |
|      | Friday    | 19       |             | 118.0                                     | 50.1                |
|      | Saturday  | 20       |             | 131.7                                     | 51.2                |
|      | Sunday    | 21       |             | 116.0                                     | 48.6                |

(a) Complete the following table. (2 marks)

| Day         | Monday | Tuesday | Wednesday | Thursday | Friday | Saturday | Sunday |
|-------------|--------|---------|-----------|----------|--------|----------|--------|
| Daily index | 89.6%  | 88.3%   | 74.8%     | 75.3%    | 119.7% |          |        |

(b) Determine the value of **A** in the table above. (2 marks)

(c) Given the actual website visits on Tuesday of week 3 was 45, determine the value of **B** in the table above. (2 marks)

- (d) Interpret the daily index for Friday in the context of this question. (1 mark)
- (e) Given there were 62 website visits on Friday of week 4, estimate the total of number of website visits for week 4. (2 marks)
- (f) Calculate the actual number of visits to the website on Monday of week 1. (1 mark)

The least-squares line for the deseasonalised data and time is  $y = 0.47t + 41.70$ .

- (g) Predict the number of website visits on Tuesday of week 5. (3 marks)