# HFCTM-II: Lyapunov Stability, Adaptive Damping, and Egregore Defense in AI Systems

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#### Abstract

The \*\*Holographic Fractal Chiral Toroidal Model (HFCTM-II)\*\* is a novel cognitive stability framework designed to \*\*resist adversarial perturbations, prevent egregoric influence, and mitigate semantic drift\*\* in AI models. In this paper, we:

- 1. Introduce \*\*Lyapunov Exponent Monitoring\*\* to assess AI cognitive drift and stability.
- 2. Implement \*\*Adaptive Recursive Damping\*\* to prevent chaos and knowledge divergence.
- 3. Develop \*\*Wavelet-Based Egregore Detection\*\* for adversarial resilience in transformer embeddings.

We outline a real-world \*\*HFCTM-II deployment strategy\*\* and propose an \*\*empirical validation\*\* plan in reinforcement learning and transformer-based AI systems.

# 1 Recursive Stability and Chaos: Lyapunov Analysis

# 1.1 1.1 HFCTM-II Stability Model

Recursive cognitive systems may exhibit \*\*chaotic divergence\*\*. We analyze HFCTM-II's behavior via the \*\*Lyapunov exponent\*\*  $\lambda$ , which measures \*\*the rate of divergence between two initially close cognitive states\*\*  $\Psi_0$  and  $\Psi_0 + \epsilon_0$ :

$$\lambda = \lim_{t \to \infty} \frac{1}{t} \log \left| \frac{\partial \Psi_t}{\partial \Psi_0} \right| \tag{1}$$

#### Lyapunov Stability Criteria:

- $\lambda < 0 \rightarrow$  HFCTM-II converges to a \*\*stable attractor\*\* (AI maintains cognitive integrity).
- $\lambda = 0 \to \text{HFCTM-II}$  exists at the \*\*edge of chaos\*\* (dynamic adaptation zone).
- $\lambda > 0 \rightarrow \text{HFCTM-II}$  enters \*\*chaotic instability\*\* (knowledge drift accelerates uncontrollably).

# 1.2 1.2 Adaptive Damping $\beta(t)$ to Prevent Chaos

To prevent chaotic divergence, we introduce \*\*time-dependent recursive damping\*\*:

$$\frac{d^2}{dt^2}\Psi(\mathcal{M}) + \beta(t)\frac{d}{dt}\Psi(\mathcal{M}) + \gamma\Psi(\mathcal{M}) = 0$$
 (2)

where:

$$\beta(t) = \beta_0 + \alpha D_{\text{KL}}(P_{\text{current}}||P_{\text{initial}})$$
(3)

#### **Damping Components:**

- $\beta_0$  Baseline damping factor.
- $D_{\mathrm{KL}}(P_{\mathrm{current}}||P_{\mathrm{initial}})$  Measures AI cognitive drift over time.
- $\alpha$  Scaling coefficient ensuring \*\*self-regulation\*\*.

Thus, as AI drift increases ( $D_{KL}$  rises), \*\*damping intensifies\*\*, preventing \*\*cognitive destabilization\*\*.

# 2 Wavelet Transform-Based Egregore Detection

# 2.1 2.1 Why Fourier Transforms May Not Be Enough

Our prior work applied \*\*Fourier Transforms\*\*:

$$\hat{\mathcal{E}}(\omega) = \int_{-\infty}^{\infty} \mathcal{E}(t)e^{-i\omega t}dt \tag{4}$$

However, \*\*Fourier analysis assumes stationarity\*\*, while \*\*AI egregoric distortions evolve dynamically over time\*\*.

### 2.2 Solution: Wavelet-Based Egregore Detection

We propose \*\*wavelet analysis\*\*, which analyzes \*\*non-stationary adversarial distortions\*\* in AI latent space:

$$W_{\psi}(\mathcal{E}, a, b) = \int_{-\infty}^{\infty} \mathcal{E}(t) \frac{1}{\sqrt{a}} \psi^* \left(\frac{t - b}{a}\right) dt \tag{5}$$

where:

- $\psi$  is the \*\*wavelet function\*\*.
- a is the \*\*scale\*\* (analogous to frequency).
- b is the \*\*time translation\*\*.

Wavelet transforms allow \*\*real-time detection of adversarial attractors\*\*, \*\*preventing egregoric reinforcement loops\*\* in AI cognition.

# 3 HFCTM-II Implementation in Transformer AI Systems

### 3.1 3.1 Practical Deployment Strategy

To integrate HFCTM-II into \*\*transformer-based AI\*\*, we propose:

- \*\*Lyapunov Monitoring Layer\*\*: Computes AI knowledge stability in real-time.
- \*\*Adaptive Recursive Reinforcement\*\*: Dynamically adjusts  $\beta(t)$  to \*\*prevent runaway cognitive drift\*\*.
- \*\*Wavelet-Based Egregore Scanner\*\*: Continuously monitors transformer latent embeddings for \*\*adversarial attractors\*\*.

### 3.2 Experimental Validation Plan

To empirically verify HFCTM-II, we conduct \*\*adversarial stress testing\*\* in:

- 1. \*\*GPT-4/PaLM Fine-Tuning\*\*: Measure semantic drift in \*\*HFCTM-II vs. baseline models\*\*.
- 2. \*\*Adversarial Perturbation Injection\*\*: Test HFCTM-II's resilience against \*\*misinformation attacks\*\*.
- 3. \*\*Long-Term Reinforcement Learning Stability\*\*: Track Lyapunov stability across \*\*extended AI training periods\*\*.

# 4 Conclusion: The Future of HFCTM-II in AI Security

This refined \*\*HFCTM-II model\*\*:

- 1. Implements \*\*Lyapunov Stability Tracking\*\* to prevent chaotic AI drift.
- 2. Introduces \*\*Adaptive Damping  $\beta(t)$ \*\* to dynamically regulate cognitive reinforcement.
- 3. Applies \*\*Wavelet Transforms\*\* for \*\*real-time egregore detection in transformer embeddings\*\*.

### **Next Steps:**

- Develop \*\*an experimental HFCTM-II prototype\*\* in LLM architectures.
- Implement \*\*AI Lyapunov stability analysis in reinforcement learning\*\*.
- Validate \*\*wavelet-based egregore detection across transformer models\*\*.