## Simpson's Paradox

In early August 2021, Public Health England released national statistics on the Delta variant of COVID-19, reporting both the number of positive cases and deaths, classified by vaccination status. Some of this data is summarized in the table below:

Group	Vaccinated	Unvaccinated
Cases	117,3115	151,3054
Deaths	481	253
Mortality Rate	0.41%	0.17%

- 1. Does this provide evidence that the vaccine actually **increases** likelihood of mortality?
- 2. What are some possible explanations for this pattern?

The report also included data on the age group of cases.

## ${\bf Under~50}$

Group	Vaccinated, < 50	Unvaccinated, $< 50$
Cases	89,3807	147,3612
Deaths	21	48
Mortality Rate	0.02%	0.03%

## Over 50

	Group	Vaccinated, $\geq 50$	Unvaccinated, $\geq 50$
	Cases	27,307	3,3440
	Deaths	460	205
N	Mortality Rate	1.68%	5.96%

This is an example of **Simpson's Paradox**:

$$A = Death$$
  $B = Vaccinated$   $C = Over 50$ 

Then

$$P(A|B,C) < P(A|B^c,C) \quad \text{and} \quad P(A|B,C^c) < P(A|B^c,C^c)$$

But

$$P(A|B) > P(A|B^c)$$