Optimization of the CMB-galaxy cross-correlation signal for studying the Integrated Sachs-Wolfe effect

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1 Theoretical Aspects

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Introduction

Theoretical Aspects

- The integrated Sachs-Wolfe (ISW) effect occurs due to time changes in gravitational potentials;
- During periods of transition from or to matter-dominated eras of the Universe, potentials change more rapidly;
- Naturally, a statistical correlation between CMB temperature maps and gravitational potentials is expected.

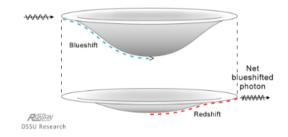


Figure 2: Illustration of the ISW effect. In this case, the gravity wells flattened, leaving a net blueshift.

The ΛCDM Model

Theoretical Aspects

To build the theoretical framework used, it is assumed

- The Universe is homogeneous and isotropic at large scales;
- Initial conditions are obtained by assuming an inflationary period when the Universe was very compact and energetic;
- The Universe is composed of baryonic matter, radiation, neutrinos, cold dark matter and a dark energy component described by a cosmological constant Λ;

The homogeneous and isotropic background is first set up, and linear perturbations are added to it.



The Perturbed Metric

Theoretical Aspects

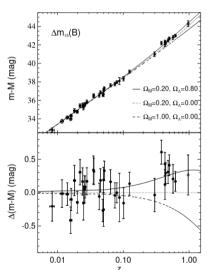
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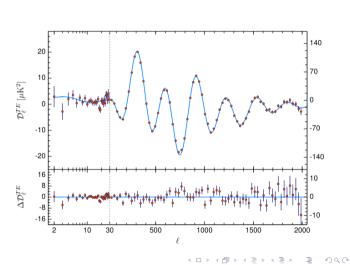
We express the perturbed metric with two functions $\Psi(\mathbf{x},t)$ and $\Phi(\mathbf{x},t)$

$$\begin{cases} g_{00} = -1 - 2\Psi(\mathbf{x}, t), \\ g_{0i} = g_{i0} = 0, \\ g_{ij} = a^{2}(t)\delta_{ij}[1 + 2\Phi(\mathbf{x}, t)]. \end{cases}$$
 (1)

The ΛCDM Model

Theoretical Aspects





The Cosmic Microwave Background

The temperature of the Cosmic Microwave Background (CMB) can be expressed by

$$T(\mathbf{x}, \hat{\mathbf{p}}, t) = \bar{T}(t)[1 + \Theta(\mathbf{x}, \hat{\mathbf{p}}, t)]. \tag{2}$$

The temperature perturbation Θ can be expressed in Fourier space according to

$$\Theta(\hat{\mathbf{k}}, \mu) = \sum_{\ell=0}^{\infty} (2\ell + 1)(-i)^{\ell} \Theta_{\ell}(\hat{\mathbf{k}}) \mathscr{P}_{\ell}(\mu), \tag{3}$$

where $\mu = \hat{\mathbf{k}} \cdot \hat{\mathbf{p}}$ and \mathscr{P}_{ℓ} are Legendre polynomials.



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Analytical Approximation

Theoretical Aspects

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Working with first-order equations and the tightly coupled limit, and assuming recombination to be an instantaneous process happening at conformal time $\eta = \eta *$, we can obtain

$$\Theta_{\ell}(k,\eta_{0}) \approx [\Theta_{0}(k,\eta_{*}) + \Psi(k,\eta_{*})] j_{\ell}[k(\eta_{0} - \eta_{*})]
+ i \nu_{b}(k,\eta_{*}) \left\{ j_{\ell}[k(\eta_{0} - \eta_{*})] - (\ell + 1) \frac{j_{\ell}[k(\eta_{0} - \eta_{*})]}{k(\eta_{0} - \eta_{*})} \right\}
+ \int_{0}^{\eta_{0}} d\eta e^{-\tau} [\Psi'(k,\eta) - \Phi'(k,\eta)] j_{\ell}[k(\eta_{0} - \eta)].$$
(4)

Here, the third term in the equation describes the Integrated Sachs-Wolfe effect.



Correlation Functions

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To calculate the CMB autocorrelation function C_{ℓ}^{tt} , we expand Θ in spherical harmonics

$$\Theta(\mathbf{x}, \hat{\mathbf{p}}, t) = \sum_{\ell=1}^{\ell_{\text{max}}} \sum_{m=-\ell}^{\ell} a_{\ell m}(\mathbf{x}, t) Y_{\ell m}(\hat{\mathbf{p}}),$$
 (5)

and calculate the autocorrelation between the $a_{\ell m}$ terms:

$$\langle a_{\ell m} a_{\ell' m'}^* \rangle = \delta_{\ell \ell'} \delta_{m m'} C_{\ell}^{tt} \tag{6}$$

Other autocorrelation spectra C_ℓ^{xx} follow the same process. It is common to use $D_\ell^{XX} = \frac{\ell(\ell+1)}{2\pi} C_\ell^{xx}$ for some spectra for better visualization. We can also write

$$C_{\ell}^{tt} = \frac{1}{2\ell + 1} \sum_{m = -\ell}^{\ell} a_{\ell m} a_{\ell' m'}^* \tag{7}$$



Cosmic Variance

The low number of $a_{\ell m}$ coefficients for lower multipoles ℓ leads to a high uncertainty in this region called cosmic variance

$$\left(\frac{\Delta C_{\ell}^{XX}}{C_{\ell}^{XX}}\right)_{CV} = \sqrt{\frac{2}{2\ell+1}}$$
(8)

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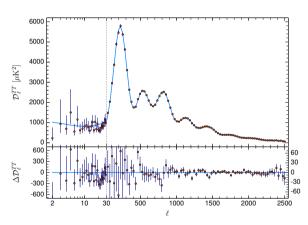


Figure 3: Planck 2018 CMB temperature power spectrum.

Parameter	Best-fit		
$\Omega_b h^2$	0.02237 ± 0.00015		
$\Omega_c h^2$	0.1200 ± 0.0012		
$100\Theta_{MC}$	1.04092 ± 0.00031		
au	0.0544 ± 0.0073		
$\ln{(10^{10}A_s)}$	3.044 ± 0.014		
n_s	0.9649 ± 0.042		
Ω_m	0.3153 ± 0.0073		
H_0	$67.36 \pm 0.54 \text{ km/s/Mpc}$		
σ_8	0.8111 ± 0.0060		

Table 1: Best-fit values of cosmological parameters reported in Planck 2018 results using TT+TE+EE+lowE and gravitational lensing data.

The Matter Power Spectrum

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To calculate a cross-correlation function, we need the 3D matter power spectrum P(k, z), defined by

$$\langle \delta(\mathbf{k}, z) \delta^*(\mathbf{k}', z) \rangle = (2\pi)^3 P(k, z) \delta_D(\mathbf{k} - \mathbf{k}')$$

We have used CAMB's implementation of the HALOFIT model to calculate the matter power spectrum.

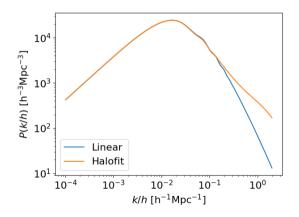


Figure 4: Matter power spectrum calculated using both a linear approximation and the HALOFIT model.

The Cross-correlation Spectrum

To trace the matter density anisotropies, we used galaxy contrast maps, which can be calculated using

$$\delta_g(\mathbf{n}) = \frac{N_g(\mathbf{n}) - \bar{N}_g}{\bar{N}_g} \tag{9}$$

It is assumed that $\delta_g = b_g \delta$, where b_g is the bias factor, which we assume to be a slowly varying function of redshift.

The galaxy autocorrelation $C_\ell^{\rm gg}$ and cross-correlation function $C_\ell^{\rm tg}$ can then be calculated with

$$\langle a_{\ell m}^t a_{\ell' m'}^g \rangle = C_{\ell}^{tg} \delta_{\ell \ell'} \delta_{mm'} \qquad \langle a_{\ell m}^g a_{\ell' m'}^g \rangle = C_{\ell}^{gg} \delta_{\ell \ell'} \delta_{mm'}$$
 (10)



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Analytical Formula

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Given fields x and y, representing either the ISW contribution to the CMB temperature (x, y = t) or the galaxy contrast (x, y = g), we can calculate the associated auto- or cross-correlation spectra using [1]

$$C_{\ell}^{xy} = \frac{2}{\pi} \int dk k^2 W_{\ell}^{x}(k) W_{\ell}^{y}(k) P(k), \tag{11}$$

with

$$W_{\ell}^{t} = -3\Omega_{m} \left(\frac{H_{0}}{k}\right)^{2} \int dz \frac{\mathrm{d}[(1+z)D(z)]}{\mathrm{d}z} j_{\ell}[k\chi(z)] \tag{12}$$

$$W_{\ell}^{g} = \int dz b_{g}(z) \frac{\mathrm{d}N}{\mathrm{d}z} D(z) j_{\ell}[k\chi(z)]$$
 (13)



ISW Contribution: Temperature Autocorrelation

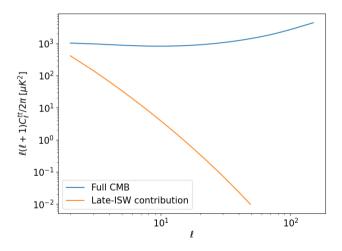


Figure 5: CMB autocorrelation comparison between full spectrum and ISW contribution.



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ISW Contribution: Galaxy Autocorrelation and Cross-correlation

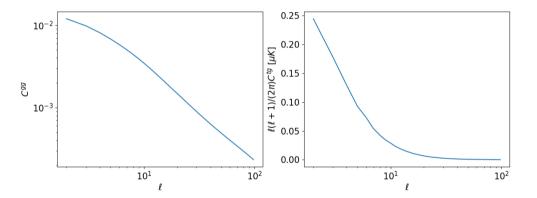


Figure 6: Galaxy autocorrelation spectrum (left) and late-ISW contribution to the galaxy-CMB cross-correlation (right).



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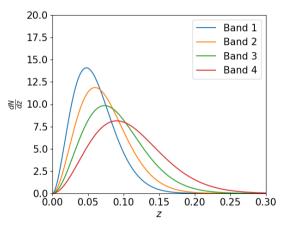
Selection Function Parametrization

The function $\frac{dN}{dz}$ in equation (13) is called the selection function. We are assuming its parametrization to be [2]

$$\frac{\mathrm{d}N}{\mathrm{d}z} \left(z | \lambda, \beta, z_0 \right) dz = \frac{\beta}{\Gamma(\lambda)} \left(\frac{z}{z_0} \right)^{\beta \lambda - 1} \exp \left[-\left(\frac{z}{z_0} \right)^{\beta} \right] d\left(\frac{z}{z_0} \right) \tag{14}$$

We have explored how to maximize the cross-correlation signal using an idealized selection function.

2MASS Bands Comparison



Band	z_0	β	λ
1	0.043	1.825	1.524
2	0.054	1.800	1.600
3	0.067	1.765	1.636
4	0.084	1.723	1.684

Table 2: Parameter values for the 4 bands of the 2MASS catalog.

Figure 7: Selection function calculated for the 4 bands of the 2MASS catalog.



Exploring the Parameter Space

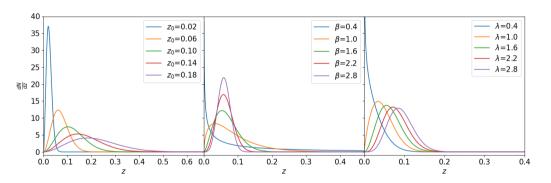


Figure 8: Selection function calculated for various parameter values.



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Null Hypothesis

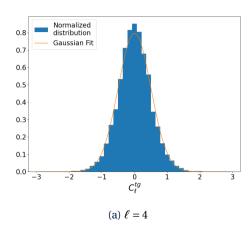
For the process of finding a galaxy survey with an idealized selection function, we first needed an estimation for the probability of C_ℓ^{tg} being 0, which would be our null hypothesis. The following process was used:

- Synthesize multiple uncorrelated CMB temperature and galaxy contrast maps using HEALPix;
- Calculate the cross-correlation C_ℓ^{tg} for each pair of uncorrelated maps at each multipole;
- For each multipole ℓ , a histogram of C_{ℓ}^{tg} was produced;
- Each histogram was fit with Gaussian distributions with average $\mu=\mu_\ell\approx 0$ and $\sigma^2=\sigma_\ell^2.$

The null hypothesis is compatible with $\Omega_m = 1$.



Synthesized Maps' Histograms



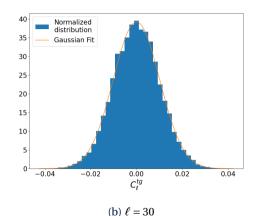


Figure 9: Distribution of cross-correlation values on different multipoles for 10^4 maps synthesized with null cross-correlation.



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Null Hypothesis

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For f_ℓ corresponding to the Gaussian fit made for the multipole ℓ

$$f_{\ell}(C_{\ell}^{tg}) = \frac{1}{\sqrt{2\pi\sigma_{\ell}^2}} \exp\left[-\frac{1}{2} \left(\frac{C_{\ell}^{tg} - \mu_{\ell}}{\sigma_{\ell}}\right)^2\right],\tag{15}$$

we have defined the null hypothesis probability distribution to be

$$P_{\text{null}} = \prod_{\ell=2}^{\ell_{\text{max}}} f_{\ell}(C_{\ell}^{tg}) \tag{16}$$

Exploring the Parameter Space

For various points (β, z_0, λ) in the parameter space, we have calculated the ratio $P_{\rm null}(\beta, z_0, \lambda)/P_{\rm null}^{\rm 2MASS}$ and produced the heat maps in Figure 10.

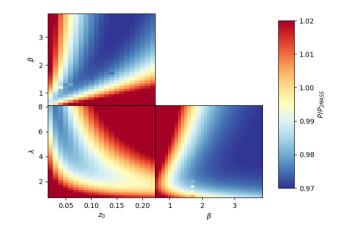


Figure 10: Heat maps used to explore the parameter space.

Minimizer

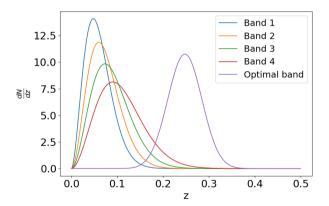
The heat maps provided initial points to run an algorithm that minimizes $P_{\text{null}}(z_0, \beta, \lambda)$. The point found that minimizes the null hypothesis probability in that region of the parameter space was

$$(\beta, z_0, \lambda) = (3.088, 0.1508, 4.9401) \tag{17}$$



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Properties of the Minimum



The selection function found is deeper than that of 2MASS band 1. It does not favor galaxies at $z^* = 0.63$, the estimated redshift at which the accelerated expansion started.

Figure 11: Selection functions comparison.



Properties of the Minimum

The selection function found reduces the maximum value of the cross-correlation function, but its peak is at higher redshifts ($\ell \approx 10$), reducing the influence of cosmic variance in the signal.

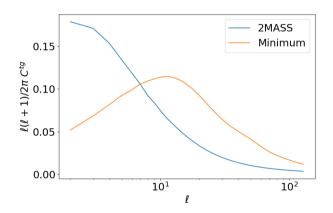


Figure 12: Theoretical cross-correlation spectrum comparison.



Discussion

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- The ratio $P_{\rm null}(z_0,\beta,\lambda)/P_{\rm null}^{\rm 2MASS}=0.971$ for the minimum;
- Despite the small statistical gain, this optimal selection function yields reasonably better results for constraints on Ω_m , as will be discussed;
- A similar work has reported a small preference towards the non-null signal with changes to the depth of the survey and fainter magnitude limits [3].



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WMAP Data

The CMB temperature maps used in this project are the ones provided by WMAP9 [4].

- Three frequency bands were used, which are named bands Q (40GHz), V (60GHz) and W (90GHz);
- The temperature intensity maps' noise power can be well modeled as uncorrelated Gaussian fluctuations;
- Despite having a lower resolution (0.3°) compared to Planck's (0.083°), this project focuses on lower multipoles;
- We have combined both maps' masks and used it for analysing each one, resulting in a fraction $f_{\text{sky}} = 0.7$.



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WMAP Data

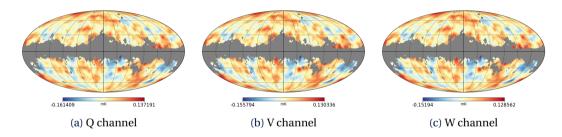


Figure 13: Mollweide projection of three (Q, V, W) WMAP9 CMB temperature (in mK) maps in galactic coordinates with an $f_{\rm skv} = 0.70$ mask applied

2MASS Catalog

Wide sky coverage is a very influential aspect of studying cross-correlation spectra, and the 2MASS catalog contains raw imaging data covering 99.998% of the sky [5], which was the dataset used.

- We have used the K_s (2.16 μ m) band of the Extended Source Catalog (XSC);
- The data of the K_s band obtained from a 20 mag aperture (K_{20}) were corrected for galactic extinction, and the remaining data was further divided into 4 bands: Bands 1 (12.0 < K'_{20} < 12.5), 2 (12.5 < K'_{20} < 13.0), 3 (13.0 < K'_{20} < 13.5) and 4 (13.5 < K'_{20} < 14.0);
- Each band has a different selection function, as shown in Figure 7.



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2MASS Catalog

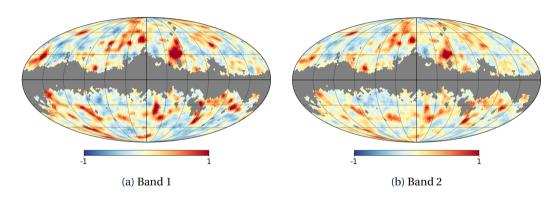


Figure 14: Mollweide projection of the 2MASS-XSC galaxy contrast maps in galactic coordinates with the combined 2MASS+WMAP mask applied ($f_{skv} = 0.70$).



2MASS Catalog

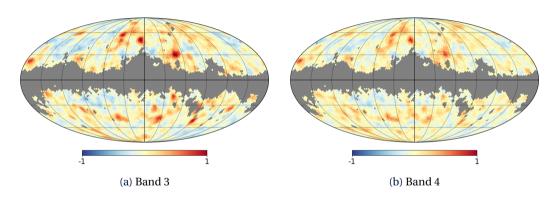


Figure 15: Mollweide projection of the 2MASS-XSC galaxy contrast maps in galactic coordinates with the combined 2MASS+WMAP mask applied ($f_{skv} = 0.70$).



Correlation Spectra Estimator

To estimate the correlation spectra that describe the pixelized maps d with primordial signal s and noise n (with S and N being the corresponding covariance matrices), we could use the following likelihood function.

$$\mathcal{L} = P(\mathbf{d}|\mathbf{C}) = \frac{1}{(2\pi)^{n_{\text{dim}}/2} |\mathbf{C}|^{1/2}} \exp\left(-\frac{1}{2}\mathbf{d}^T \mathbf{C}^{-1} \mathbf{d}\right), \qquad \mathbf{C} = \mathbf{S} + \mathbf{N}$$
 (18)

With a prior $\pi(S)$ we can use Bayes' Theorem to obtain

$$P(\mathbf{C}|\mathbf{d}) \propto \pi(\mathbf{S})P(\mathbf{d}|\mathbf{C})$$
 (19)



Correlation Spectra Estimator

If we can sample from P(C|s,d) and P(s|C,d). Then we iterate

$$\mathbf{s}^{i+1} \leftarrow P(\mathbf{s}|\mathbf{C}^i, d) \tag{20}$$
$$\mathbf{C}^{i+1} \leftarrow P(\mathbf{C}|\mathbf{s}^{i+1}, d), \tag{21}$$

$$\mathbf{C}^{i+1} \leftarrow P(\mathbf{C}|\mathbf{s}^{i+1}, d), \tag{21}$$

to obtain a sample of $\{(\mathbf{s}^i, \mathbf{C}^i)\}$.



References

The Blackwell-Rao Estimator

We can then use the Blackwell-Rao estimator to obtain an approximation for $P(C_{\ell}|\mathbf{d})$

$$P(C_{\ell}|\mathbf{d}) \approx \frac{1}{N_G} \sum_{i=1}^{N_G} P(C_{\ell}|\sigma_{\ell}^i), \tag{22}$$

where

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$$\sigma_{\ell}^{i} = \frac{1}{2\ell + 1} \sum_{m=-\ell}^{\ell} \mathbf{s}_{\ell m} \mathbf{s}_{\ell m}^{\dagger}.$$
 (23)

We then maximize the probability $P(C_{\ell}|\mathbf{d})$ to obtain the best-fit C_{ℓ} .



Matrices Used

In this work, **s** and **S** are defined by

$$\mathbf{s}^{T} = (s_{00}^{tg}, s_{01}^{tg}, s_{11}^{tg}, \dots, s_{\ell_{max}0}^{tg}, \dots, s_{\ell_{max}\ell_{max}}^{tg}), \tag{24}$$

$$\mathbf{S} = \operatorname{diag}(S_0^{tg}, S_1^{tg}, S_1^{tg}, \dots, S_{\ell_{\max}}^{tg}, \dots, S_{\ell_{\max}}^{tg}), \tag{25}$$

where

$$\mathbf{s}_{\ell m}^{tg} = \begin{pmatrix} a_{\ell m}^{t} \\ a_{\ell m}^{g} \end{pmatrix}, \qquad \mathbf{S}_{\ell}^{tg} = \begin{pmatrix} C_{\ell}^{tt} & C_{\ell}^{tg} \\ C_{\ell}^{tg} & C_{\ell}^{gg} \end{pmatrix}. \tag{26}$$



Correlation Spectra Obtained

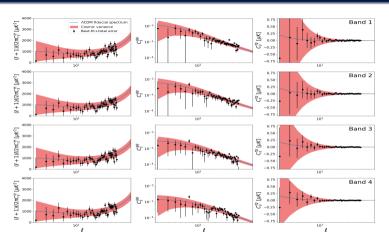


Figure 16: Comparison between theoretical correlation spectra and the ones estimated from WMAP and 2MASS.



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Monte Carlo Markov Chains

Theoretical Aspects

By defining the likelihood $\mathcal{L}(C_\ell|\theta)$ and the prior $p(\theta)$, one can use Markov chains to obtain samples of each parameter in θ following the posterior

$$P(\theta|C_{\ell}) = \mathcal{L}(C_{\ell}|\theta)p(\theta) \tag{27}$$

Joint posteriors can be easily obtained from each parameter sample, strongly simplifying data analysis for multiple parameter models.



Planck Likelihoods

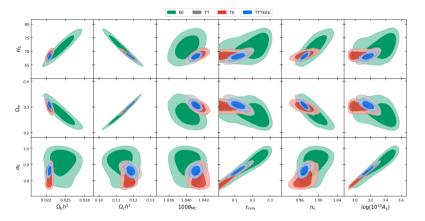


Figure 17: Joint posterior distributions of cosmological parameters using Planck's CMB temperature (T) and polarization (E) data.



References

Likelihood Profiling

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The likelihood of each point in the spectrum was assumed to be Gaussian

$$\mathcal{L}(C_{\ell, \text{ theo}}^{xy} | C_{\ell, \text{ data}}^{xy}) = \frac{1}{\sigma_{\ell} \sqrt{2\pi}} \exp \left[-\frac{1}{2} \left(\frac{C_{\ell, \text{ data}}^{xy} - C_{\ell, \text{ theo}}^{xy}}{\sigma_{\ell}} \right)^{2} \right]. \tag{28}$$

We are varying only Ω_m , so $C_{\ell, \, \text{theo}}^{xy}$ is a functions of only Ω_m . The likelihood of a full spectrum is

$$\mathcal{L}(\Omega_m | C_{\text{data}}^{\text{xy}}) = \prod_{\ell=2}^{\ell_{\text{max}}} \mathcal{L}(C_{\ell, \text{ theo}}^{\text{xy}} | C_{\ell, \text{ data}}^{\text{xy}}). \tag{29}$$

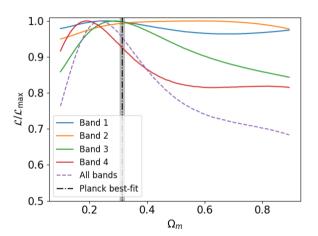
The $C^{tg} + C^{gg}$ joint-likelihood is

$$\mathcal{L}(\Omega_m|C_{\text{data}}^{tg}, C_{\text{data}}^{\text{gg}}) = \mathcal{L}(\Omega_m|C_{\text{data}}^{tg})\mathcal{L}(\Omega_m|C_{\text{data}}^{\text{gg}}). \tag{30}$$



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Results for 2MASS



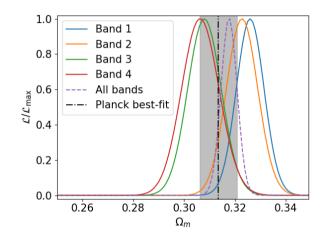
- All curves are compatible with Planck;
- Not much constraining power on Ω_m ;
- Bands 3 and 4 which have the deepest selection functions – have the most constraining power amongst all 4.

Figure 18: C^{tg} only likelihood profiles.



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Results for 2MASS



- All likelihoods are compatible with Planck;
- Very high constraining power on Ω_m when C^{gg} is introduced, comparable to Planck's;
- No significant difference in constraining power between each band.

Figure 19: Joint likelihood profiles



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Forecast for the Optimized Band

To estimate the behavior of a survey that follows our idealized selection function in this analysis, we have produced two synthetic cross-correlation spectra using that selection function. Both use the Λ CDM model with Planck's best-fit parameters, only differing in Ω_m :

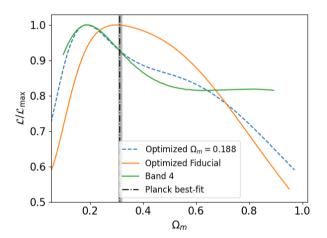
- One of the datasets was produced using Plancks best-fit of $\Omega_m = 0.3153$;
- The other dataset was produced using $\Omega_m = 0.188$, the value that maximizes the likelihood of band 4 for the C^{tg} only likelihood.

Band 4's errors were used as estimated for both synthetic datasets.

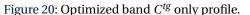


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Forecast for the Optimized Band



- Constraining power still low;
- Reasonable improvement in the constraining power.





Discussion

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- The optimized band being deeper than 2MASS means errors on the spectra should be lower, meaning the errors used are overestimated, which indicates the constraints could be better for a real survey following our optimized selection function;
- The optimized band was not found by optimizing the Ω_m constraints, but rejecting the null cross-correlation hypothesis. $\Omega_m = 1$ leads to $C_\ell^{tg} = 0$, and the fast decrease in likelihood for higher Ω_m is noticeable.

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Conclusions

- We have obtained the likelihood profiles for Ω_m obtained from cross-correlation data by studying the ISW effect;
- The constraints obtained using only C^{tg} were not strong, but can be used as a complement to other datasets for a combined analysis;
- In the 2MASS catalog, the 2 deepest bands bands 3 and 4 yielded better constraining power;
- The Planck collaboration also studied the ISW effect using the cross-correlation spectrum[6], obtaining significantly better results with deeper surveys (SDSS[7] and Planck's Kappa map).



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Conclusions

- An optimized band capable of maximizing the ISW signal was obtained, prioritizing galaxies at higher redshifts and increasing the cross-correlation signal in a region less affected by cosmic variance;
- The likelihoods obtained for artificial data calculated using the optimized band improved the constraints on Ω_m ;
- Combining different matter tracers leads to improved results overall.





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Extra Content

Discussão de Future prospects



Extra Content

More extras



Bibliography I

Theoretical Aspects

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