## Optimization of the CMB-galaxy cross-correlation signal for studying the Integrated Sachs-Wolfe effect

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> > 15/08/2024







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1 Theoretical Aspects

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# Introduction

Theoretical Aspects

- The integrated Sachs-Wolfe (ISW) effect occurs due to time changes in gravitational potentials;
- During periods of transition from or to matter-dominated eras of the Universe, potentials change more rapidly;
- Naturally, a statistical correlation between CMB temperature maps and gravitational potentials is expected.

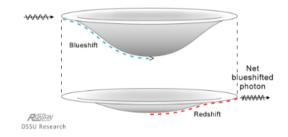


Figure 2: Illustration of the ISW effect. In this case, the gravity wells flattened, leaving a net blueshift.

References

#### The ΛCDM Model

Theoretical Aspects

To build the theoretical framework used, it is assumed

- The Universe is homogeneous and isotropic at large scales;
- Initial conditions are obtained by assuming an inflationary period when the Universe was very compact and energetic;
- Aside from baryonic matter, radiation and neutrinos, the Universe is also composed of cold dark matter and a dark energy component described by a cosmological constant Λ;

The homogeneous and isotropic background is first set up, and linear perturbations are added to it.



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#### The ΛCDM Model

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The ΛCDM model explains some important observations, such as

- The CMB and its properties;
- The accelerating expansion of the Universe;
- The Universe's large scale structure;

And made some important predictions, like

- Baryon accoustic oscillations (BAO);
- The CMB polarization and its properties.



References

## The Cosmic Microwave Background

The temperature of the Cosmic Microwave Background (CMB) can be expressed by

$$T(\mathbf{x}, \hat{\mathbf{p}}, t) = \bar{T}(t)[1 + \Theta(\mathbf{x}, \hat{\mathbf{p}}, t)]. \tag{1}$$

The temperature perturbation  $\Theta$  can be expressed in Fourier space according to

$$\Theta(\hat{\mathbf{k}}, \mu) = \sum_{\ell=0}^{\infty} (2\ell + 1)(-i)^{\ell} \Theta_{\ell}(\hat{\mathbf{k}}) \mathscr{P}_{\ell}(\mu), \tag{2}$$

where  $\mu = \hat{\mathbf{k}} \cdot \hat{\mathbf{p}}$  and  $\mathscr{P}_{\ell}$  are Legendre polynomials.



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References

## Analytical Approximation

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Working with first-order equations and the tightly coupled limit, and assuming recombination to be an instantaneous process happening at conformal time  $\eta = \eta *$ , we can obtain

$$\Theta_{\ell}(k,\eta_{0}) \approx [\Theta_{0}(k,\eta_{*}) + \Psi(k,\eta_{*})] j_{\ell}[k(\eta_{0} - \eta_{*})] 
+ i\nu_{b}(k,\eta_{*}) \left\{ j_{\ell}[k(\eta_{0} - \eta_{*})] - (\ell+1) \frac{j_{\ell}[k(\eta_{0} - \eta_{*})]}{k(\eta_{0} - \eta_{*})} \right\} 
+ \int_{0}^{\eta_{0}} d\eta e^{-\tau} [\Psi'(k,\eta) - \Phi'(k,\eta)] j_{\ell}[k(\eta_{0} - \eta)].$$
(3)

Here, the third term in the equation describes the Integrated Sachs-Wolfe effect.



References

#### **Correlation Functions**

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To calculate the CMB autocorrelation function  $C_\ell^{tt}$ , we expand  $\Theta$  in spherical harmonics

$$\Theta(\mathbf{x}, \hat{\mathbf{p}}, t) = \sum_{\ell=1}^{\ell_{\text{max}}} \sum_{m=-\ell}^{\ell} a_{\ell m}(\mathbf{x}, t) Y_{\ell m}(\hat{\mathbf{p}}), \tag{4}$$

and calculate the autocorrelation between the  $a_{\ell m}$  terms:

$$\langle a_{\ell m} a_{\ell' m'}^* \rangle = \delta_{\ell \ell'} \delta_{m m'} C_{\ell}^{tt} \tag{5}$$

Other autocorrelation spectra  $C_\ell^{xx}$  follow the same process. It is common to use  $D_\ell^{XX} = \frac{\ell(\ell+1)}{2\pi} C_\ell^{xx}$  for some spectra for better visualization.



#### Cosmic Variance

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The low number of  $a_{\ell m}$  coefficients for lower multipoles  $\ell$  leads to a high uncertainty in this region called cosmic variance

$$\left(\frac{\Delta C_{\ell}^{XX}}{C_{\ell}^{XX}}\right)_{CV} = \sqrt{\frac{2}{2\ell+1}}$$
(6)

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#### Planck 2018

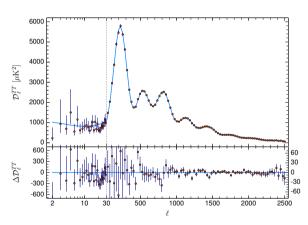


Figure 3: Planck 2018 CMB temperature power spectrum.

Parameter	Best-fit		
$\Omega_b h^2$	$0.02237 \pm 0.00015$		
$\Omega_c h^2$	$0.1200 \pm 0.0012$		
$100\Theta_{MC}$	$1.04092 \pm 0.00031$		
au	$0.0544 \pm 0.0073$		
$\ln{(10^{10}A_s)}$	$3.044 \pm 0.014$		
$n_s$	$0.9649 \pm 0.042$		
$\Omega_m$	$0.3153 \pm 0.0073$		
$H_0$	$67.36 \pm 0.54  \text{km/s/Mpc}$		
$\sigma_8$	$0.8111 \pm 0.0060$		

Table 1: Best-fit values of cosmological parameters reported in Planck 2018 results using TT+TE+EE+lowE and gravitational lensing data.

## The Matter Power Spectrum

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To calculate a cross-correlation function, we need the 3D matter power spectrum P(k, z), defined by

$$\langle \delta(\mathbf{k}, z) \delta^*(\mathbf{k}', z) \rangle = (2\pi)^3 P(k, z) \delta_D(\mathbf{k} - \mathbf{k}')$$
 (7)

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Throughout this project, we have used CAMB's implementation of the HALOFIT model to calculate the matter power spectrum.

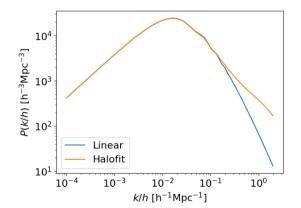


Figure 4: Matter power spectrum calculated using both a linear approximation and the so-called HALOFIT model.

References

## The Cross-correlation Spectrum

To trace the matter density anisotropies, we used galaxy contrast maps, which can be calculated using

$$\delta_g(\mathbf{k}) = \frac{\rho_g(\mathbf{k}) - \bar{\rho}_g}{\bar{\rho}_g} \tag{8}$$

It is assumed that  $\delta_g = b_g \delta$ , where  $b_g$  is the bias factor, which we assume to be a slowly varying function of redshift.

The cross-correlation function  $C_\ell^{tg}$  can then be calculated with

$$\langle a_{\ell m}^t a_{\ell' m'}^g \rangle = C_{\ell}^{tg} \delta_{\ell \ell'} \delta_{mm'} \tag{9}$$



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#### Analytical Formula

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Given fields x and y, representing either the ISW contribution to the CMB temperature (x, y = t) or the galaxy contrast (x, y = g), we can calculate the associated auto- or cross-correlation spectra using [1]

$$C_{\ell}^{xy} = \frac{2}{\pi} \int dk k^2 W_{\ell}^{x}(k) W_{\ell}^{y}(k) P(k), \tag{10}$$

with

$$W_{\ell}^{t} = -3\Omega_{m} \left(\frac{H_{0}}{k}\right)^{2} \int dz \frac{\mathrm{d}[(1+z)D(z)]}{\mathrm{d}z} j_{\ell}[k\chi(z)] \tag{11}$$

$$W_{\ell}^{g} = \int dz b_{g}(z) \frac{\mathrm{d}N}{\mathrm{d}z} D(z) j_{\ell}[k\chi(z)]$$
 (12)



#### ISW Contribution: Temperature Autocorrelation

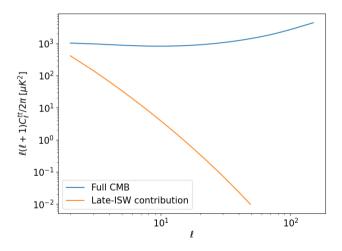


Figure 5: CMB autocorrelation comparison between full spectrum and ISW contribution.



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#### ISW Contribution: Galaxy Autocorrelation and Cross-correlation

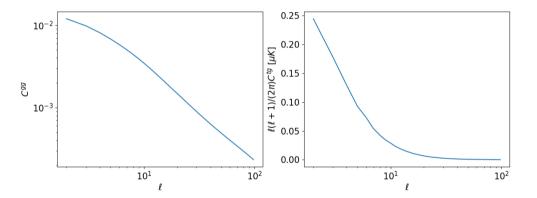


Figure 6: Galaxy autocorrelation spectrum (left) and late-ISW contribution to the galaxy-CMB cross-correlation (right).



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#### **Selection Function Parametrization**

The function  $\frac{dN}{dz}$  in equation (12) is called the selection function. We are assuming its parametrization to be [2]

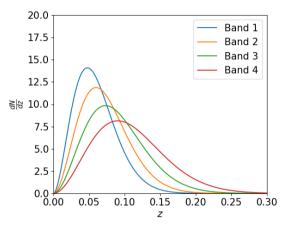
$$\frac{\mathrm{d}N}{\mathrm{d}z} \left( z | \lambda, \beta, z_0 \right) dz = \frac{\beta}{\Gamma(\lambda)} \left( \frac{z}{z_0} \right)^{\beta \lambda - 1} \exp \left[ -\left( \frac{z}{z_0} \right)^{\beta} \right] d\left( \frac{z}{z_0} \right) \tag{13}$$

We have explored how to maximize the cross-correlation signal using an idealized selection function.



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#### 2MASS Bands Comparison



Band	$z_0$	β	λ
1	0.043	1.825	1.524
2	0.054	1.800	1.600
3	0.067	1.765	1.636
4	0.084	1.723	1.684

Table 2: Parameter values for the 4 bands of the 2MASS catalog.

Figure 7: Selection function calculated for the 4 bands of the 2MASS catalog.



## Exploring the Parameter Space

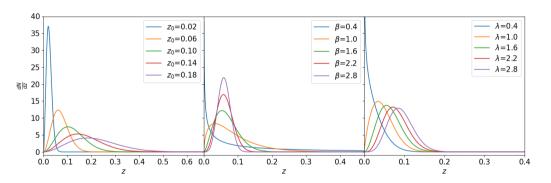


Figure 8: Selection function calculated for various parameter values.



## Null Hypothesis

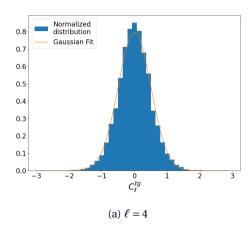
For the process of finding a galaxy survey with an idealized selection function, we first needed an estimation for the probability of  $C_\ell^{tg}$  being 0, which would be our null hypothesis. The following process was used:

- Synthesize multiple uncorrelated CMB temperature and galaxy contrast maps using HEALPix;
- Calculate the cross-correlation  $C_\ell^{tg}$  for each pair of uncorrelated maps at each multipole;
- For each multipole  $\ell$ , a histogram of  $C_{\ell}^{tg}$  was produced;
- Each histogram was fit with Gaussian distributions with average  $\mu=\mu_\ell\approx 0$  and  $\sigma^2=\sigma_\ell^2.$

The null hypothesis is compatible with  $\Omega_m = 1$ .



## Synthesized Maps' Histograms



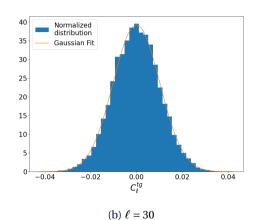


Figure 9: Distribution of cross-correlation values on different multipoles for  $10^4$  maps synthesized with null cross-correlation.



## Null Hypothesis

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For  $f_\ell$  corresponding to the Gaussian fit made for the multipole  $\ell$ 

$$f_{\ell}(C_{\ell}^{tg}) = \frac{1}{\sqrt{2\pi\sigma_{\ell}^2}} \exp\left[-\frac{1}{2} \left(\frac{C_{\ell}^{tg} - \mu_{\ell}}{\sigma_{\ell}}\right)^2\right],\tag{14}$$

we have defined the null hypothesis probability distribution to be

$$P_{\text{null}} = \prod_{\ell=2}^{\ell_{\text{max}}} f_{\ell}(C_{\ell}^{tg}) \tag{15}$$

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## Exploring the Parameter Space

For various points  $(\beta, z_0, \lambda)$  in the parameter space, we have calculated the ratio  $P_{\rm null}(\beta, z_0, \lambda)/P_{\rm null}^{\rm 2MASS}$  and produced the heat maps in Figure 10.

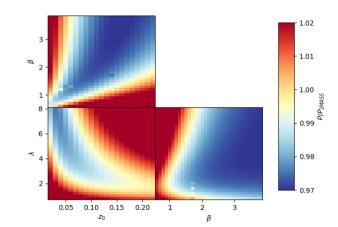


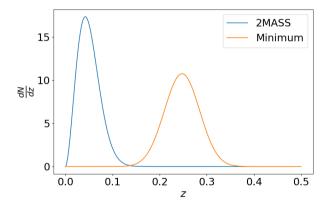
Figure 10: Heat maps used to explore the parameter space.

#### Minimizer

The heat maps provided initial points to run an algorithm that minimizes  $P_{\text{null}}(z_0, \beta, \lambda)$ . The point found that minimizes the null hypothesis probability in that region of the parameter space was

$$(\beta, z_0, \lambda) = (3.088, 0.1508, 4.9401) \tag{16}$$

#### Properties of the Minimum



The selection function found is deeper than that of 2MASS band 1. It does not favor galaxies at  $z^* = 0.63$ , the estimated redshift at which the accelerated expansion started.

Figure 11: Selection functions comparison.



#### Properties of the Minimum

The selection function found reduces the maximum value of the cross-correlation function, but its peak is at higher redshifts ( $\ell \approx 10$ ), reducing the influence of cosmic variance in the signal.

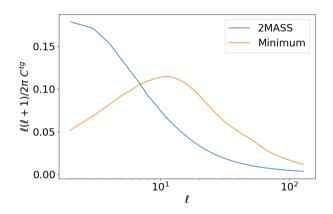


Figure 12: Theoretical cross-correlation spectrum comparison.



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#### Discussion

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- The ratio  $P_{\rm null}(z_0,\beta,\lambda)/P_{\rm null}^{\rm 2MASS}=0.971$  for the minimum;
- Despite the small statistical gain, this optimal selection function yields reasonably better results for constraints on  $\Omega_m$ , as will be discussed;
- A similar work has reported a small preference towards the non-null signal with changes to the depth of the survey and fainter magnitude limits [3].



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#### WMAP Data

The CMB temperature maps used in this project are the ones provided by WMAP9 [4].

- Three frequency bands were used, which are named bands Q (40GHz), V (60GHz) and W (90GHz);
- The temperature intensity maps' noise power can be well modeled as uncorrelated Gaussian fluctuations;
- Despite having a lower resolution (0.3°) compared to Planck's (0.083°), this project focuses on lower multipoles;
- We have combined both maps' masks and used it for analysing each one, resulting in a fraction  $f_{\text{sky}} = 0.7$ .



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#### WMAP Data

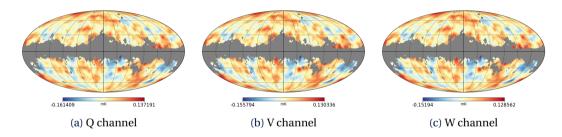


Figure 13: Mollweide projection of three (Q, V, W) WMAP9 CMB temperature (in mK) maps in galactic coordinates with an  $f_{\rm skv} = 0.70$  mask applied

## 2MASS Catalog

Wide sky coverage is a very influential aspect of studying cross-correlation spectra, and the 2MASS catalog contains raw imaging data covering 99.998% of the sky [5], which was the dataset used.

- We have used the  $K_s$  (2.16  $\mu$ m) band of the Extended Source Catalog (XSC);
- The data of the  $K_s$  band obtained from a 20 mag aperture ( $K_{20}$ ) were corrected for galactic extinction, and the remaining data was further divided into 4 bands: Bands 1 (12.0 <  $K'_{20}$  < 12.5), 2 (12.5 <  $K'_{20}$  < 13.0), 3 (13.0 <  $K'_{20}$  < 13.5) and 4 (13.5 <  $K'_{20}$  < 14.0);
- Each band has a different selection function, as shown in Figure 7.



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## 2MASS Catalog

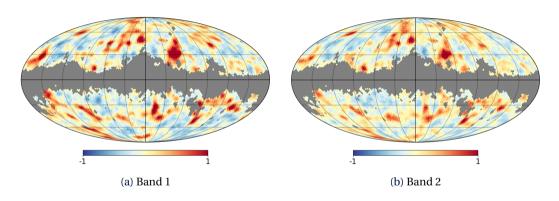


Figure 14: Mollweide projection of the 2MASS-XSC galaxy contrast maps in galactic coordinates with the combined 2MASS+WMAP mask applied ( $f_{skv} = 0.70$ ).



#### 2MASS Catalog

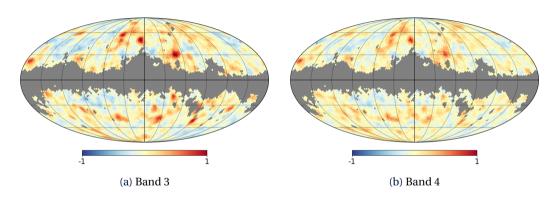


Figure 15: Mollweide projection of the 2MASS-XSC galaxy contrast maps in galactic coordinates with the combined 2MASS+WMAP mask applied ( $f_{skv} = 0.70$ ).



#### Correlation Spectra Estimator

To estimate the correlation spectra that describe the pixelized maps d with primordial signal s and noise n (with S and N being the corresponding covariance matrices), we could use the following likelihood function.

$$\mathcal{L} = P(\mathbf{d}|\mathbf{C}) = \frac{1}{(2\pi)^{n_{\text{dim}}/2} |\mathbf{C}|^{1/2}} \exp\left(-\frac{1}{2}\mathbf{d}^T \mathbf{C}^{-1}\mathbf{d}\right). \tag{17}$$

With a prior  $\pi(S)$  we can use Bayes' Theorem to obtain

$$P(\mathbf{C}|\mathbf{d}) \propto \pi(\mathbf{S})P(\mathbf{d}|\mathbf{C})$$
 (18)



## Correlation Spectra Estimator

If we can sample from P(C|s,d) and P(s|C,d). Then we iterate

$$\mathbf{s}^{i+1} \leftarrow P(\mathbf{s}|\mathbf{C}, d) \tag{19}$$
$$\mathbf{C}^{i+1} \leftarrow P(\mathbf{C}|\mathbf{s}, d), \tag{20}$$

$$\mathbf{C}^{i+1} \leftarrow P(\mathbf{C}|\mathbf{s}, d),\tag{20}$$

to obtain a sample of  $\{(\mathbf{s}^i, \mathbf{C}^i)\}$ .



References

### The Blackwell-Rao Estimator

We can then use the Blackwell-Rao estimator to obtain an approximation for  $P(C_{\ell}|\mathbf{d})$ 

$$P(C_{\ell}|\mathbf{d}) \approx \frac{1}{N_G} \sum_{i=1}^{N_G} P(C_{\ell}|\sigma_{\ell}^i), \tag{21}$$

where

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$$\sigma_{\ell}^{i} = \frac{1}{2\ell + 1} \sum_{m=-\ell}^{\ell} \mathbf{s}_{\ell m} \mathbf{s}_{\ell m}^{\dagger}.$$
 (22)

We then maximize the probability  $P(C_{\ell}|\mathbf{d})$  to obtain the best-fit  $C_{\ell}$ .



#### **Matrices Used**

In this work, **s** and **S** are defined by

$$\mathbf{s}^T = (s_{00}^{tg}, s_{01}^{tg}, s_{11}^{tg}, \dots, s_{\ell_{max}0}^{tg}, \dots, s_{\ell_{max}\ell_{max}}^{tg}), \tag{23}$$

$$\mathbf{S} = \text{diag}(S_0^{tg}, S_1^{tg}, S_1^{tg}, \dots, S_{\ell_{\text{max}}}^{tg}, \dots, S_{\ell_{\text{max}}}^{tg}), \tag{24}$$

where

$$\mathbf{s}_{\ell m}^{tg} = \begin{pmatrix} a_{\ell m}^{t} \\ a_{\ell m}^{g} \end{pmatrix}, \qquad \mathbf{s}_{\ell}^{tg} = \begin{pmatrix} C_{\ell}^{tt} & C_{\ell}^{tg} \\ C_{\ell}^{tg} & C_{\ell}^{gg} \end{pmatrix}. \tag{25}$$



# Correlation Spectra Obtained

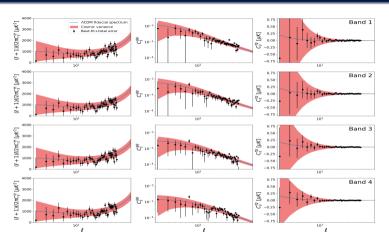


Figure 16: Comparison between theoretical correlation spectra and the ones estimated from WMAP and 2MASS.



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### Monte Carlo Markov Chains

By using the likelihood  $\mathcal{L}(C_{\ell}|\theta)$  of the data  $C_{\ell}$  being described by a parameter combination  $\theta$ , one can use Markov chains to obtain samples of each parameter in  $\theta$  following the posterior distribution

$$P(\theta|C_{\ell}) = \mathcal{L}(C_{\ell}|\theta)p(\theta) \tag{26}$$

Joint posteriors can be easily obtained from each parameter sample, strongly simplifying data analysis for multiple parameter models.



### Planck Likelihoods

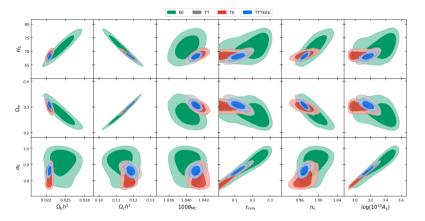


Figure 17: Joint posterior distributions of cosmological parameters using Planck's CMB temperature (T) and polarization (E) data.



# Likelihood Profiling

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To analyze the data, we have opted to profile the likelihood functions applied to  $\Omega_m$ . The likelihood of each point in the spectrum was assumed to be Gaussian

$$\mathcal{L}(C_{\ell, \text{ theo}}^{xy} | C_{\ell, \text{ data}}^{xy}) = \frac{1}{\sigma_{\ell} \sqrt{2\pi}} \exp \left[ -\frac{1}{2} \left( \frac{C_{\ell, \text{ data}}^{xy} - C_{\ell, \text{ theo}}^{xy}}{\sigma_{\ell}} \right)^{2} \right]. \tag{27}$$

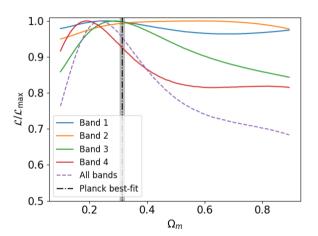
We are varying only  $\Omega_m$ , so  $C_{\ell,\, {\rm theo}}^{xy}$  is a functions of only  $\Omega_m$ . The likelihood of a full spectrum is

$$\mathcal{L}(\Omega_m | C_{\text{data}}^{\text{xy}}) = \prod_{\ell=2}^{\ell_{\text{max}}} \mathcal{L}(C_{\ell, \text{ theo}}^{\text{xy}} | C_{\ell, \text{ data}}^{\text{xy}}).$$
 (28)

The  $C^{tg} + C^{gg}$  joint-likelihood is

$$\mathcal{L}(\Omega_m|C_{\text{data}}^{tg}, C_{\text{data}}^{\text{gg}}) = \mathcal{L}(\Omega_m|C_{\text{data}}^{tg})\mathcal{L}(\Omega_m|C_{\text{data}}^{\text{gg}}). \tag{29}$$

### **Results for 2MASS**

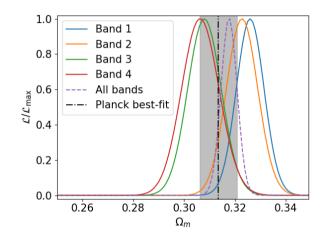


- All curves are compatible with Planck;
- Not much constraining power on  $\Omega_m$ ;
- Bands 3 and 4 which have the deepest selection functions – have the most constraining power amongst all 4.

Figure 18:  $C^{tg}$  only likelihood profiles.



### **Results for 2MASS**



- All likelihoods are compatible with Planck;
- Very high constraining power on  $\Omega_m$  when  $C^{gg}$  is introduced, comparable to Planck's;
- No significant difference in constraining power between each band.

Figure 19: Joint likelihood profiles



# Forecast for the Optimized Band

To estimate the behavior of a survey that follows our idealized selection function in this analysis, we have produced two synthetic cross-correlation spectra using that selection function. Both use the  $\Lambda$ CDM model with Planck's best-fit parameters, only differing in  $\Omega_m$ :

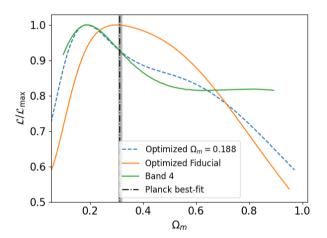
- One of the datasets was produced using Plancks best-fit of  $\Omega_m = 0.3153$ ;
- The other dataset was produced using  $\Omega_m = 0.188$ , the value that maximizes the likelihood of band 4 for the  $C^{tg}$  only likelihood.

Band 4's errors were used as estimated for both synthetic datasets.

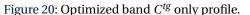


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## Forecast for the Optimized Band



- Constraining power still low;
- Reasonable improvement in the constraining power.





#### Discussion

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- The optimized band being deeper than 2MASS means errors on the spectra should be lower, meaning the errors used are overestimated, which indicates the constraints could be better for a real survey following our optimized selection function;
- The optimized band was not found by optimizing the  $\Omega_m$  constraints, but rejecting the null cross-correlation hypothesis.  $\Omega_m = 1$  leads to  $C_\ell^{tg} = 0$ , and the fast decrease in likelihood for higher  $\Omega_m$  is noticeable.

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### Conclusions

- We have obtained the likelihood profiles for  $\Omega_m$  obtained from cross-correlation data by studying the ISW effect;
- The constraints obtained using only  $C^{tg}$  were not strong, but can be used as a complement to other datasets for a combined analysis;
- In the 2MASS catalog, the 2 deepest bands bands 3 and 4 yielded better constraining power;
- The Planck collaboration also studied the ISW effect using the cross-correlation spectrum[6], obtaining significantly better results with deeper surveys (SDSS[7] and Planck's Kappa map).



#### Conclusions

- An optimized band capable of maximizing the ISW signal was obtained, prioritizing galaxies at higher redshifts and increasing the cross-correlation signal in a region less affected by cosmic variance;
- The likelihoods obtained for artificial data calculated using the optimized band improved the constraints on  $\Omega_m$ ;
- Combining different matter tracers leads to improved results overall.

Thank You

### Extra Content

Discussão de Future prospects



## Extra Content

More extras



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Theoretical Aspects

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