

33°

52'

37''S

151°

06'

04''E

10

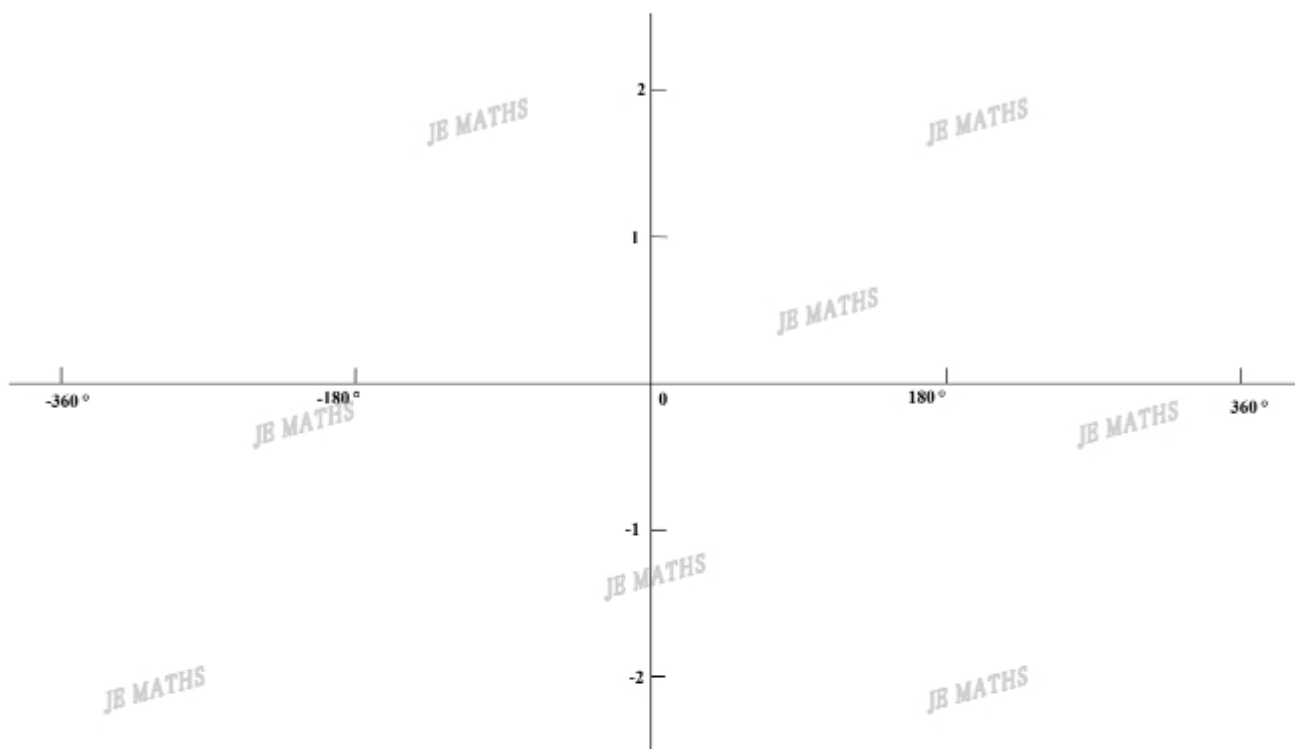
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MATHS

Plot 4 basic trig graphs:

1. Plot $y = \sin x$ and $y = \operatorname{cosec} x$ on the same given number plane for $-360^\circ \leq x \leq 360^\circ$.

x	-360°	-270°	-180°	-90°	0°	90°	180°	270°	360°
$y = \sin x$									
$y = \operatorname{cosec} x$									



- (b) Find the domain and range by filling the table below:

	$y = \sin x$	$y = \operatorname{cosec} x$
Domain	---	-----
Range	--	----

2. Simplify the following by using the **odd** symmetry property:

$\sin(-x) = -\sin x$ and $\operatorname{cosec}(-x) = -\operatorname{cosec} x$, and then check them on the graph in Q1.

(a) $\sin(-45^\circ) =$

—
—

(b) $\sin(-120^\circ) =$

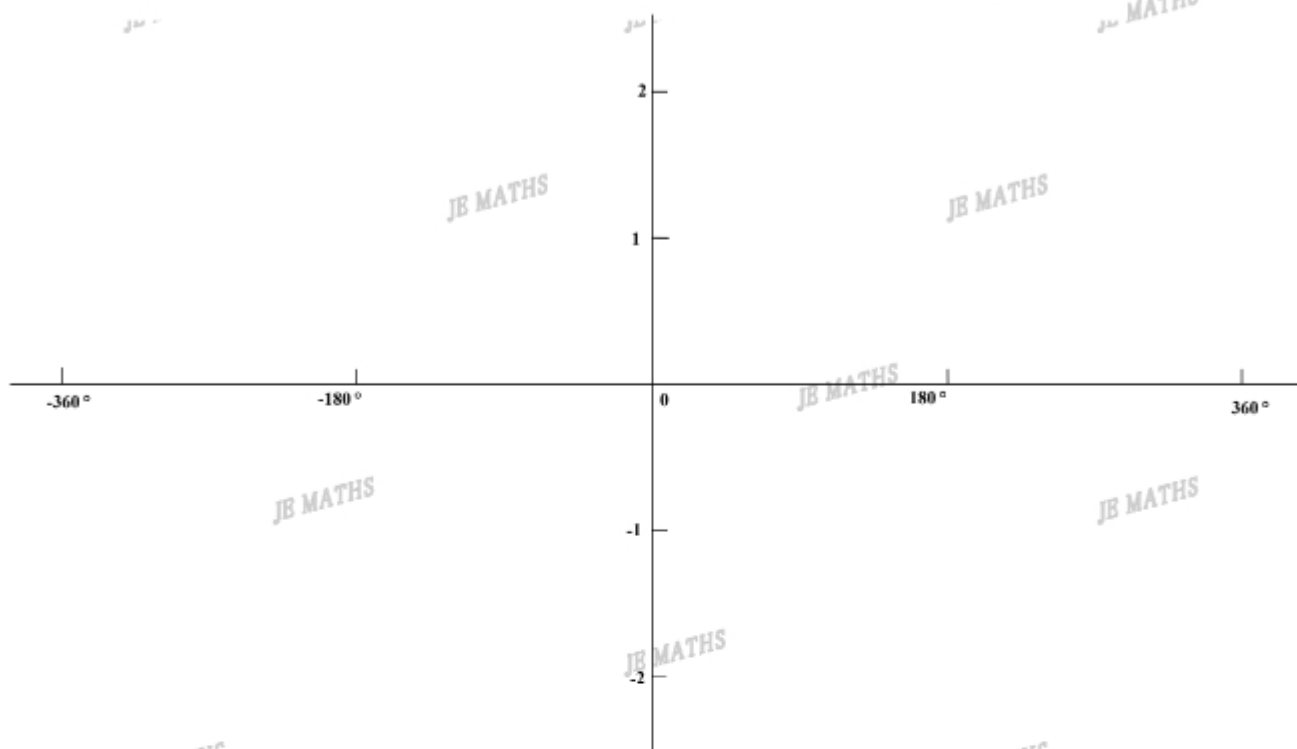
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—

(c) $\operatorname{cosec}(-240^\circ) =$

(d) $\operatorname{cosec}(-321^\circ) =$

3. (a) Plot $y = \cos x$ and $y = \sec x$ on the same given number plane for $-360^\circ \leq x \leq 360^\circ$.

x	-360°	-270°	-180°	-90°	0°	90°	180°	270°	360°
$y = \cos x$									
$y = \sec x$									



- (b) Find the domain and range by filling the table below:

	$y = \cos x$	$y = \sec x$
Domain		
Range		

4. Simplify the following by using the **even** symmetry property:

$\cos(-x) = \cos x$ and $\sec(-x) = \sec x$, and then check them on the graph in Q3.

(a) $\cos(-62^\circ) =$

-

-

(b) $\cos(-100^\circ) =$

(c) $\sec(-249.2^\circ) =$

-

-

(d) $\sec(-310^\circ 01') =$

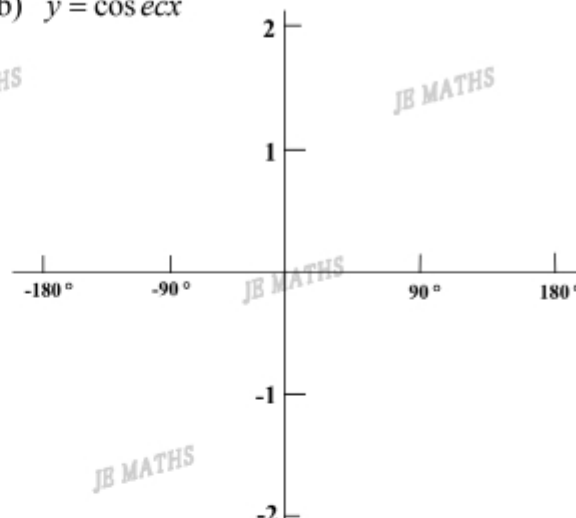
- Sketch 4 basic trig graphs:

5. Sketch the following 4 trig functions for $-180^\circ \leq x \leq 180^\circ$.

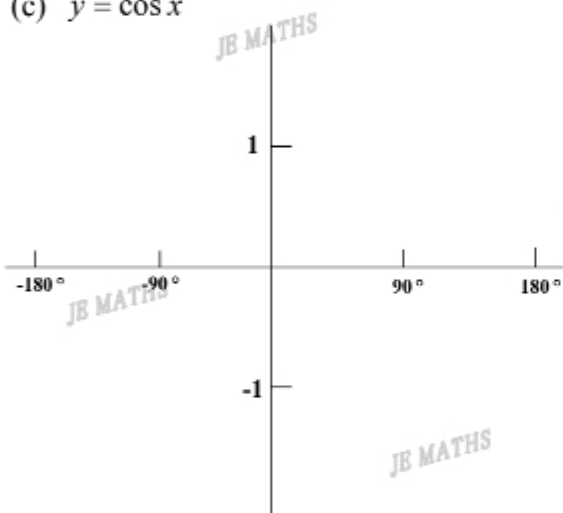
(a) $y = \sin x$



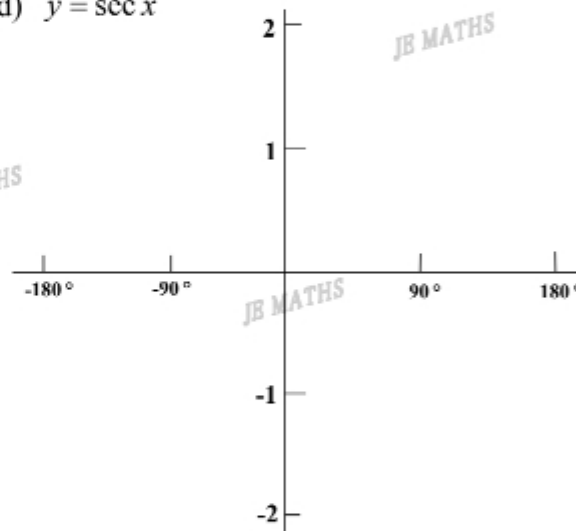
(b) $y = \cos x$



(c) $y = \cos x$



(d) $y = \sec x$



6. Simplify:

(a) $\cos(-x) + \cos(-x)$

—
—

(b) $\cos ec(-x) \times \cos ec(-x)$

—
—

(c) $\frac{\sin(-x)}{\cos(-x)}$

—
—

(d) $\frac{\cos ec(-x)}{\sec(-x)}$

—
—

- **Symmetry property:** $\sin(x - \theta) = -\sin(\theta - x)$ and $\cos(x - \theta) = \cos(\theta - x)$

7. Simplify:

(a) $\sin(x - 360^\circ)$

(b) $\cos(x - 180^\circ)$

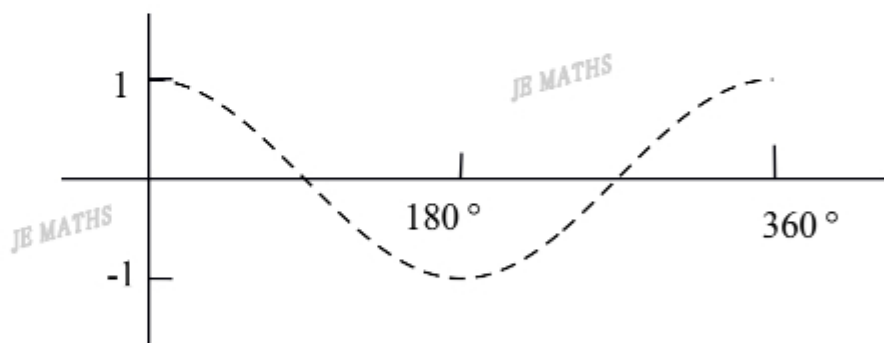
(c) $\frac{\sin(x - 180^\circ)}{\cos(-x)}$

(d) $\frac{\sin(-x) \cos(x - 180^\circ)}{\cos(-x) \sin(x - 180^\circ)}$

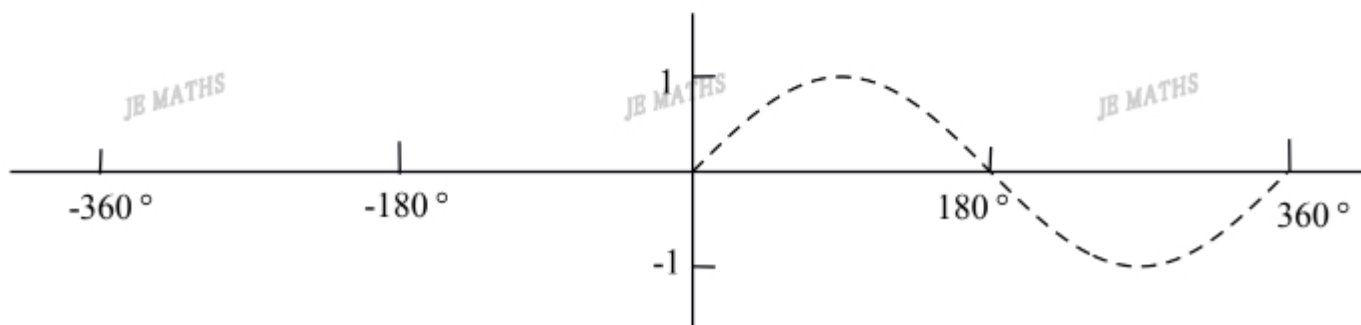
- **Reflect in the x, y-axis:**

8. Sketch the following trig graphs from the basic graph, for $0 \leq x \leq 360^\circ$.

(a) $y = -\cos x$



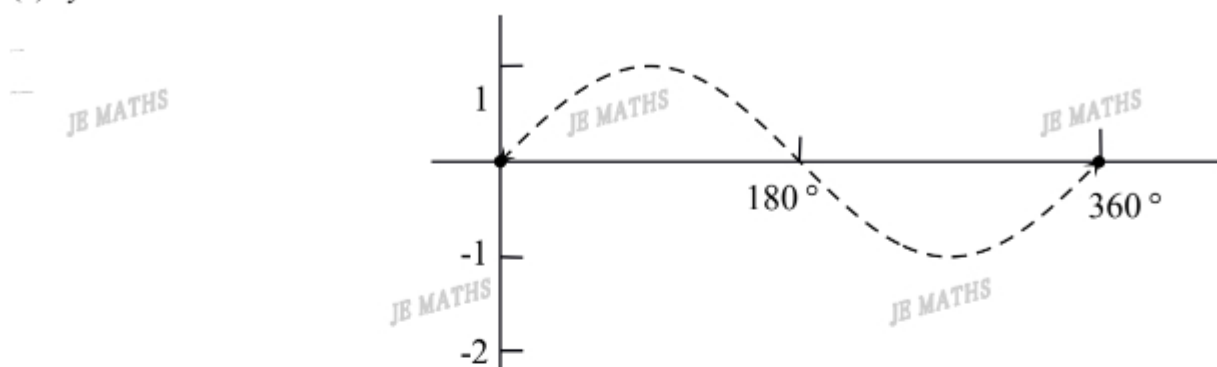
(b) $y = \sin(-x)$



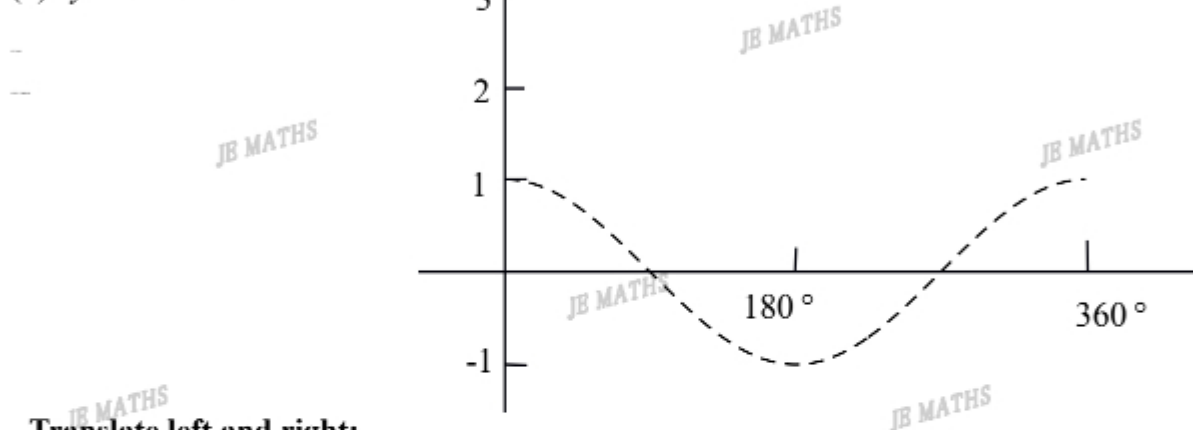
- Translate up and down:

9. Sketch the following trig graphs from the basic graph, for $0 \leq x \leq 360^\circ$.

(a) $y = \sin x - 1$

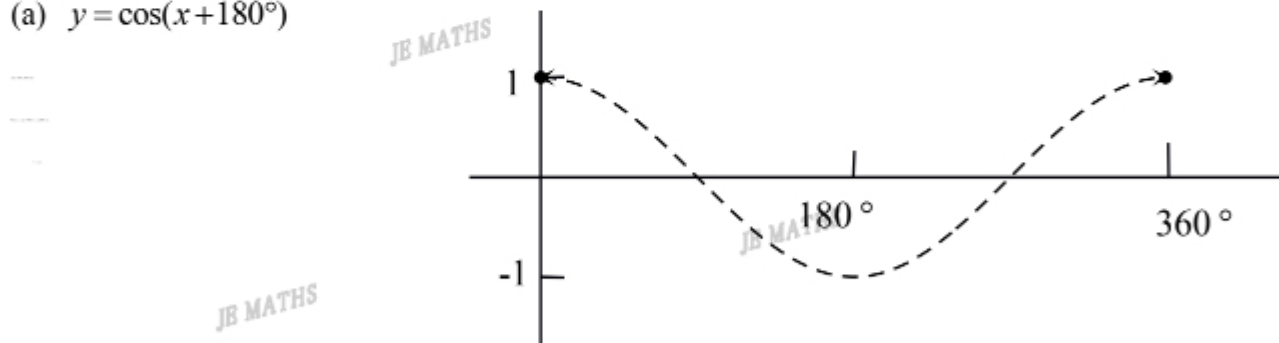


(b) $y = 2 + \cos x$

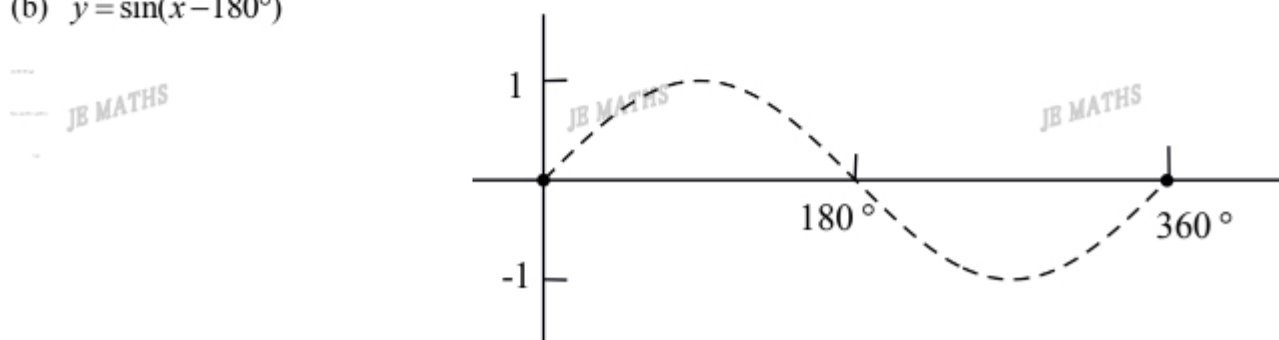
**- Translate left and right:**

10. Sketch the following trig graphs from the basic graph, for $0 \leq x \leq 360^\circ$.

(a) $y = \cos(x + 180^\circ)$



(b) $y = \sin(x - 180^\circ)$

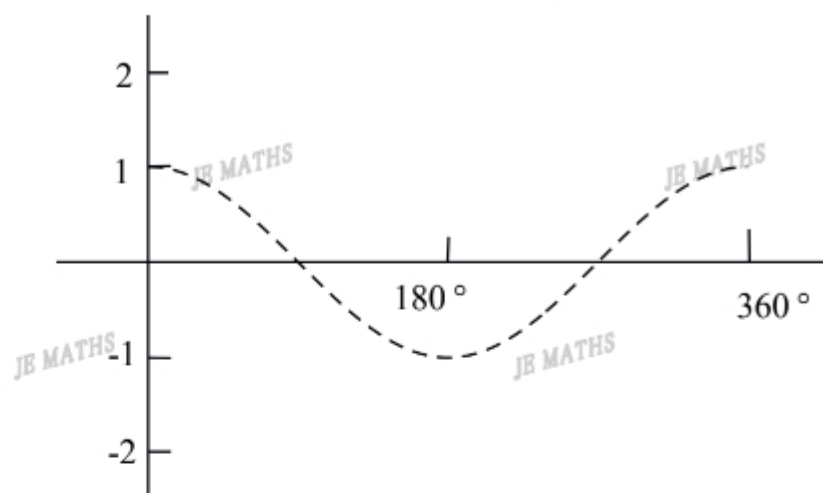


- Dilated in and out vertically:

11. Sketch the following trig graphs from the basic graph and find its **amplitude**, for $0 \leq x \leq 360^\circ$.

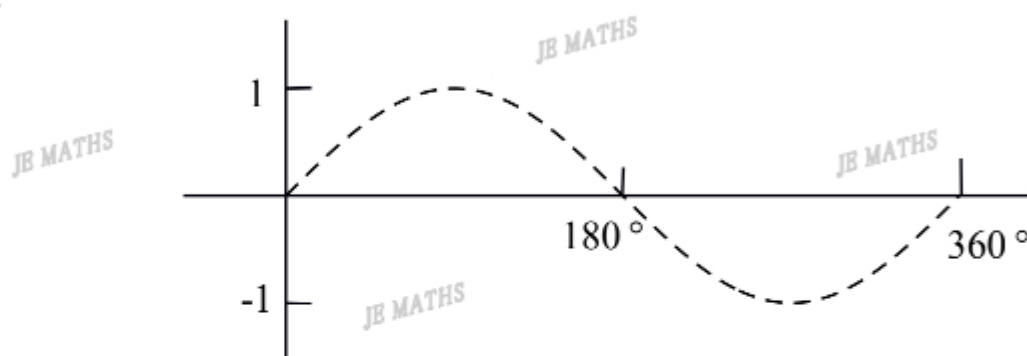
(a) $y = 2 \cos x$

—
—
—



(b) $y = \frac{1}{2} \sin x$

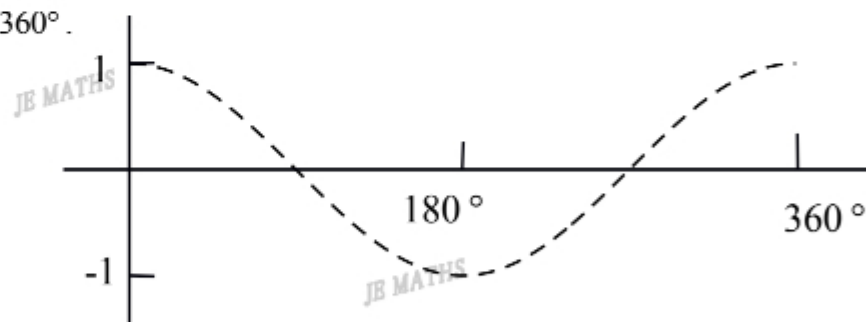
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**- Dilated in and out horizontally:**

12. Sketch the following trig graphs from the basic graph and find its **period**.

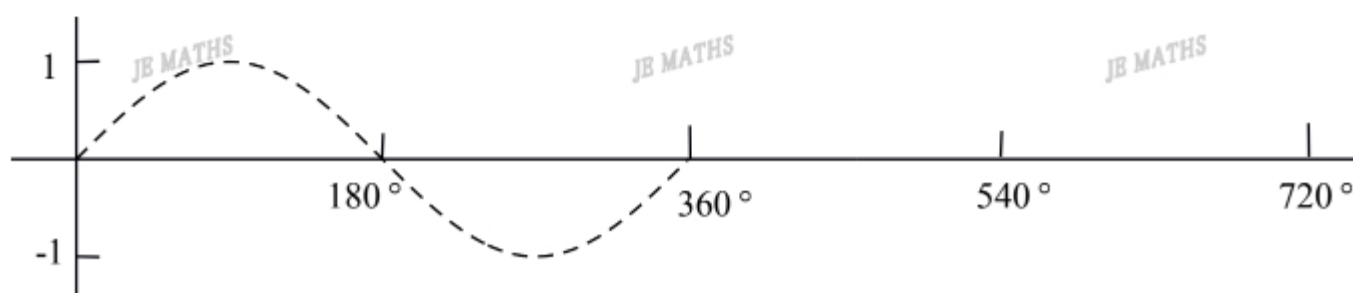
(a) $y = \cos 2x$ for $0 \leq x \leq 360^\circ$.

—
—



(b) $y = \sin \frac{1}{2} x$ for $0 \leq x \leq 720^\circ$.

—
—



- Sketching mixed (2 types) trig functions:

13. Given the following trigonometric functions and find the amplitude and range.

(a) $y = 2 \sin x$

(b) $y = \frac{1}{3} \cos x$

(c) $y = 5 \cos 2x$

(d) $y = \frac{2 \sin 3x}{7}$

14. Given the following trigonometric functions and find the period.

(a) $y = \sin 2x$

(b) $y = \cos \frac{x}{4}$

(c) $y = 2 \cos 4x$

(d) $y = \sin \frac{3x}{2}$

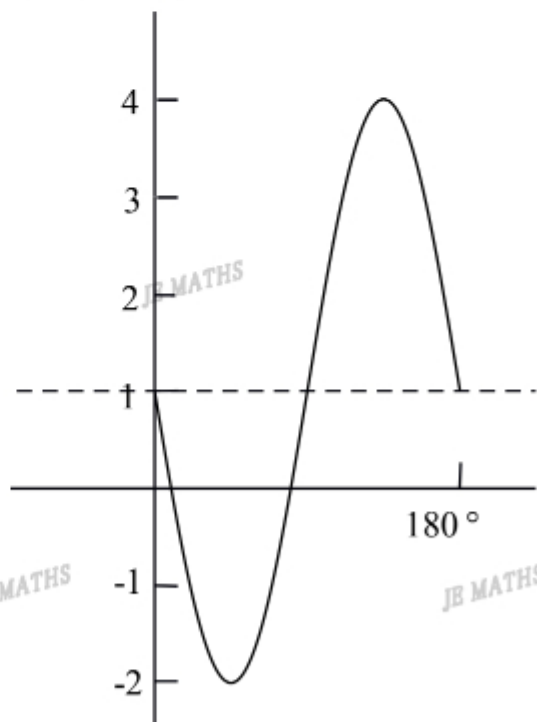
15. From the given graph of $y = -3 \sin 2x + 1$ as shown below,

(a) find:

(i) the amplitude.

(ii) the range.

(iii) the period.



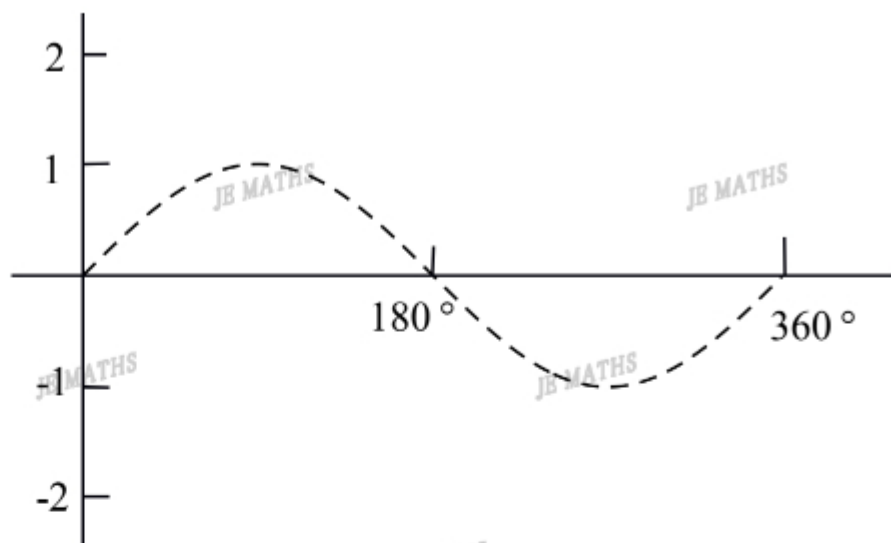
(b) Is that possible to find all questions in part (a) by looking at the function **only**?
(yes)

16. Given that $y = -2\sin x$.

(a) Find the period.

—

(b) Sketch $y = -2\sin x$,
for $0 \leq x \leq 360^\circ$.



(c) Hence, find:

(i) the amplitude.

—

(ii) the range.

—

17. Given that $y = -\cos 2x$.

(a) Find:

(i) the amplitude.

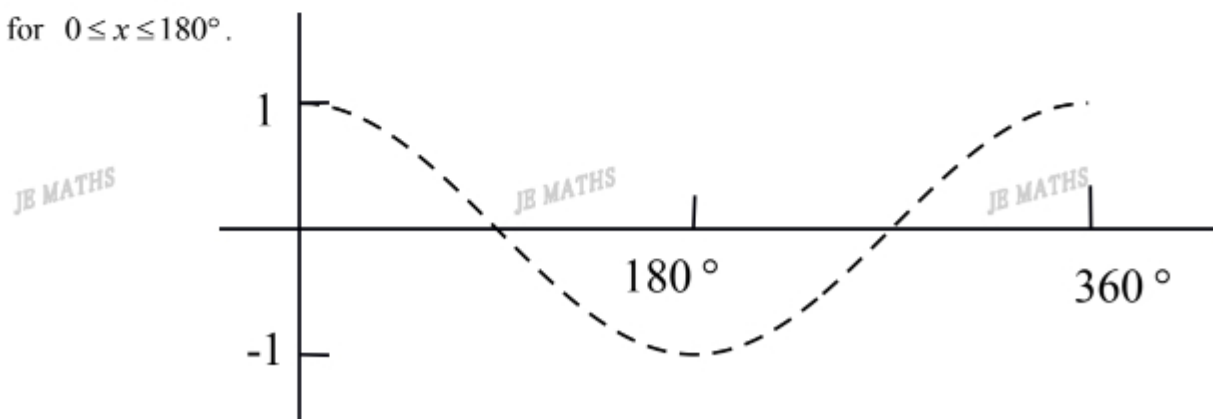
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(ii) the range.

(iii) the period.

—

(b) Hence, sketch $y = -\cos 2x$,
for $0 \leq x \leq 180^\circ$.



18. Given that $y = 3 \cos 2x$.

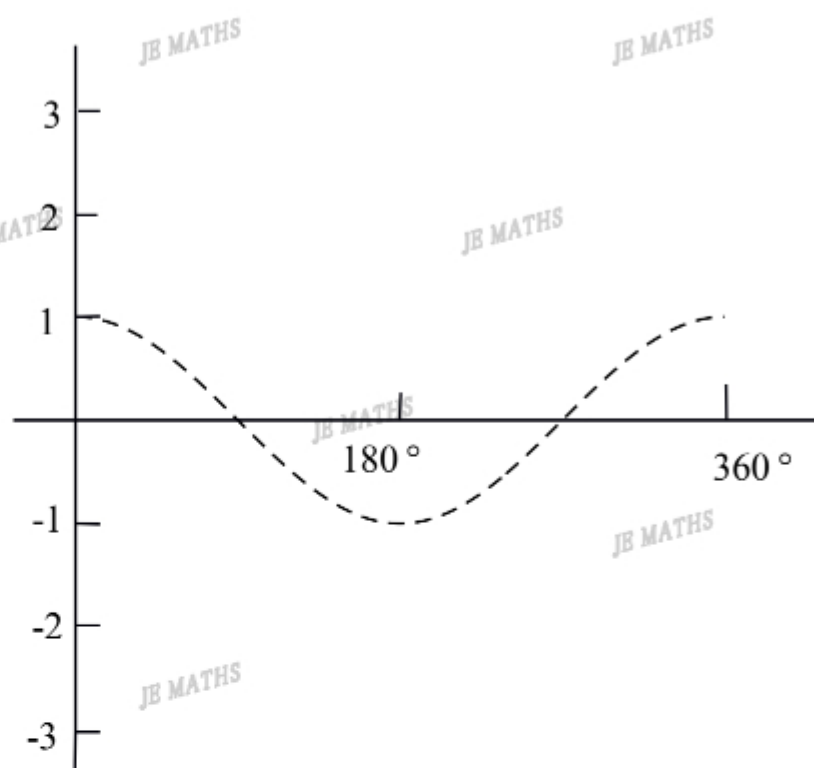
(a) Find:

(i) the amplitude.

(ii) the range.

(iii) the period.

(b) Hence, sketch $y = 3 \cos 2x$,
for $0 \leq x \leq 360^\circ$.



19. Given that $y = \frac{1}{2} \sin \frac{x}{2}$.

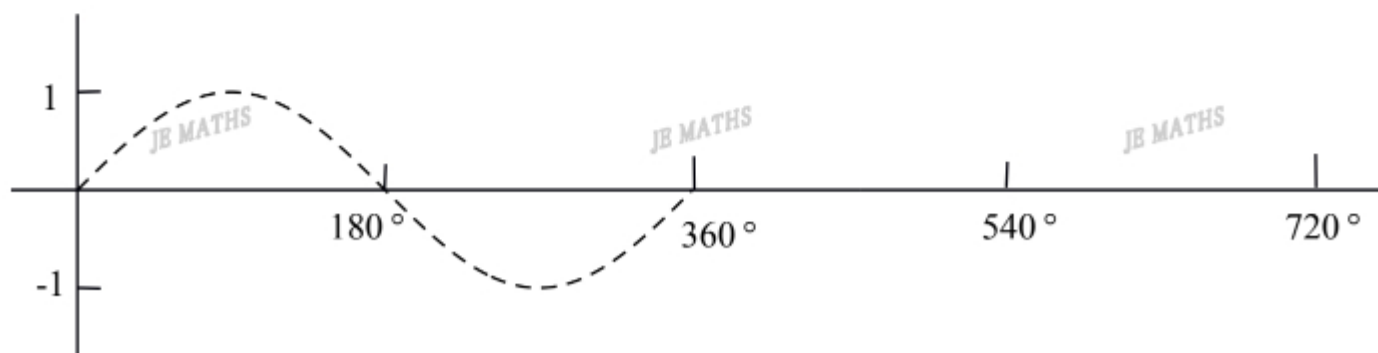
(a) Find:

(i) the amplitude.

(ii) the range.

(iii) the period.

(b) Hence, sketch $y = \frac{1}{2} \sin \frac{x}{2}$, for $0 \leq x \leq 720^\circ$.



20. Given that $y = 3\sin x - 1$.

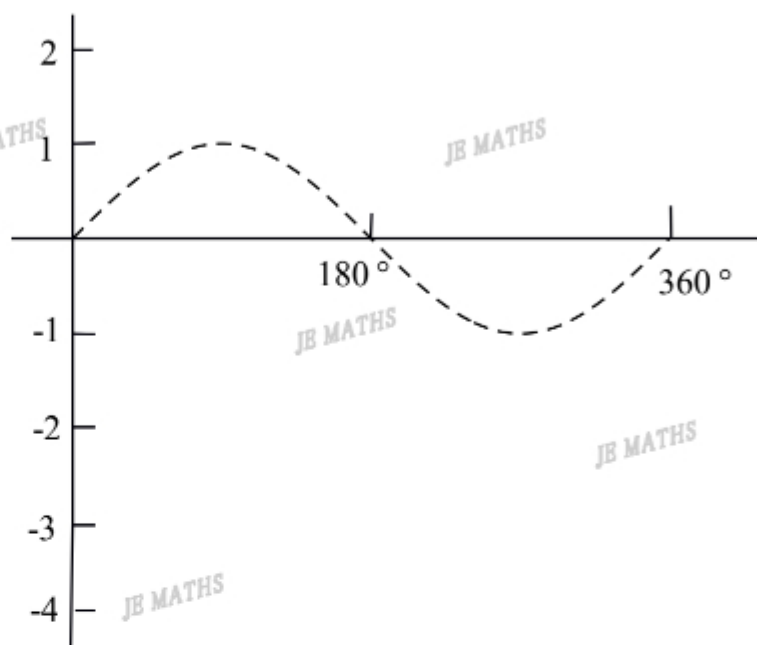
(a) Find:

(i) the amplitude.

(ii) the range.

(iii) the period.

(b) Hence, sketch $y = 3\sin x - 1$,
for $0 \leq x \leq 360^\circ$.



21. Given that $y = 1 + 2\cos x$.

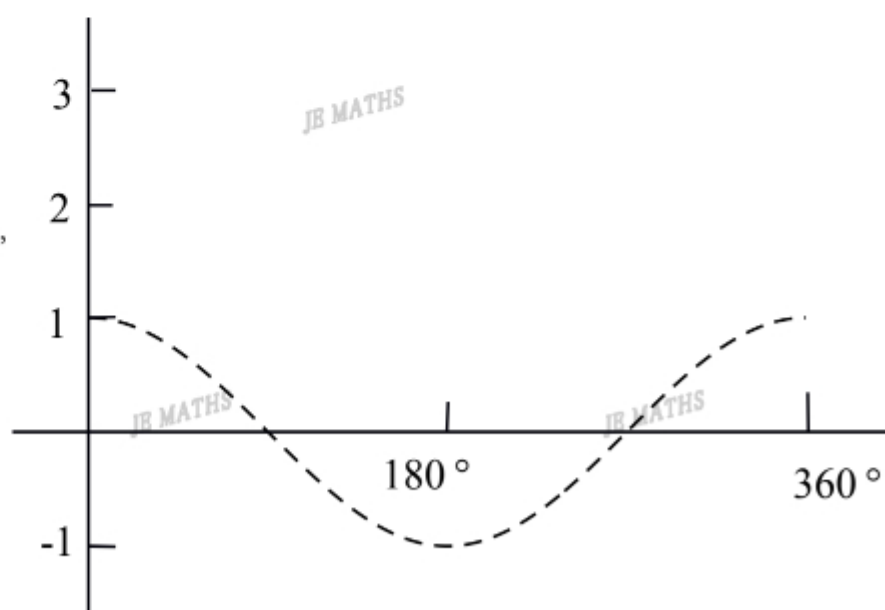
(a) Find:

(i) the amplitude.

(ii) the range.

(iii) the period.

(b) Hence, sketch $y = 1 + 2\cos x$,
for $0 \leq x \leq 360^\circ$.



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