

AVL trees

AVL Trees

- 1 .These are height balanced binary search trees, We balance height of a BST, because we don't want trees with nodes which have large height
2. This can be attained if both subtrees of each node have roughly the same height.
3. AVL tree is a binary search tree where the height of the two subtrees of a node differs by at most one

Height of a null tree is -1

AVL Tree

Que. How to find out balance of a BST.

Ans: By finding the balance factor of a BST.

Balance factor = height of left subtree – height of right subtree

All node's balance factor should be $\{-1, 0, 1\}$

If any node's balance factor is less than -1 or more than 1 then it is not balanced search tree.

If an insertion cause an imbalance, which nodes can be affected?

Nodes on the path of the inserted node.

Let U be the node nearest to the inserted one which has an imbalance.

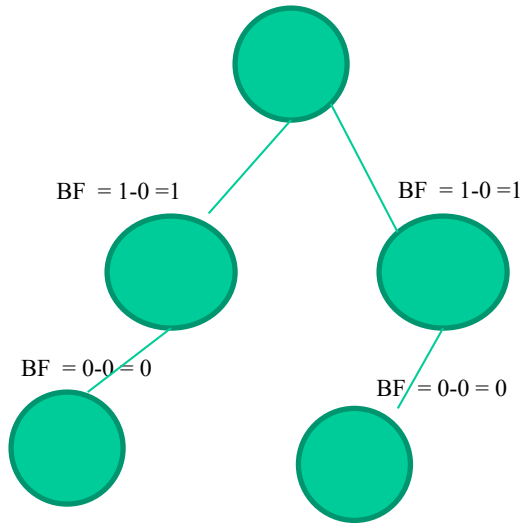
insertion in the left subtree of the left child of U

insertion in the right subtree of the left child of U

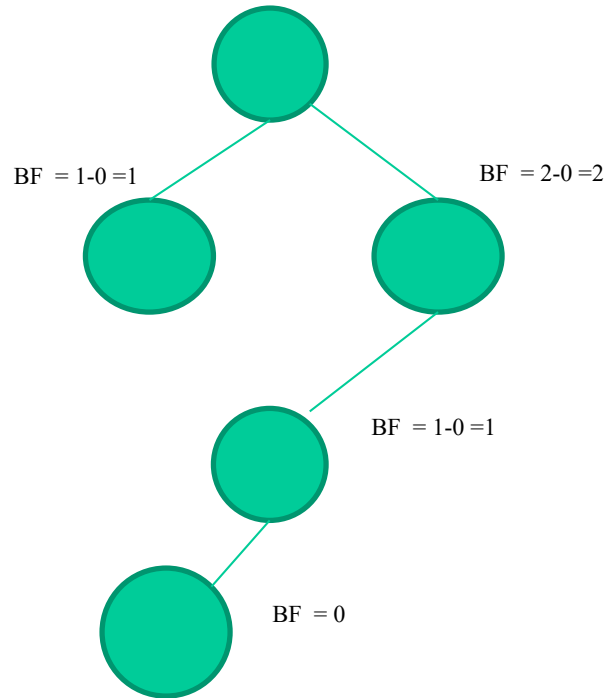
insertion in the left subtree of the right child of U

insertion in the right subtree of the right child of U

$$BF = 2-2 = 0$$



$$BF = 1-3 = -2$$

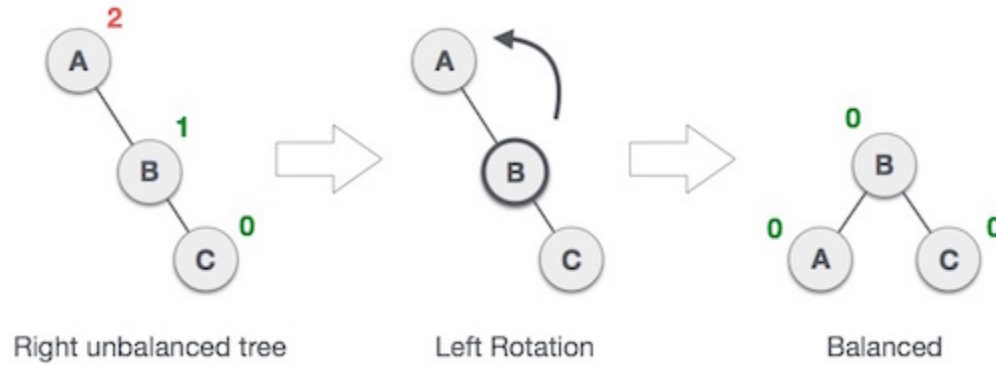


So, at the time of insertion we need to check balance factor of node and if BF is more than 1, then we need to perform rotation.

Rotation is performed always on 3 nodes

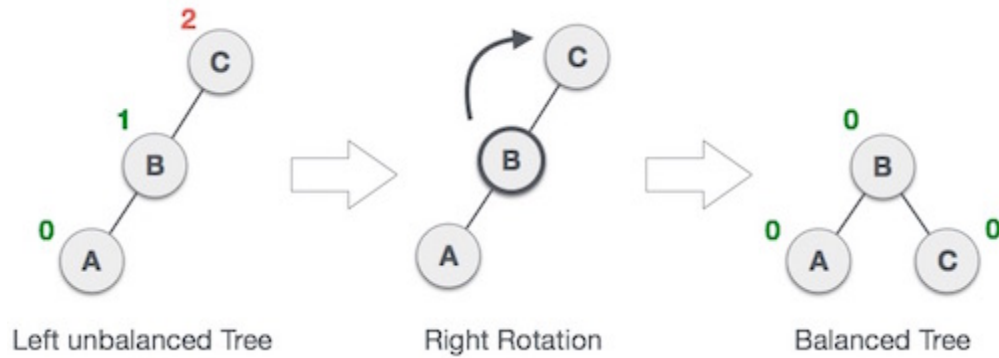
LL rotation

RR imbalance



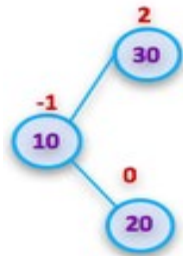
RR rotation

LL imbalance

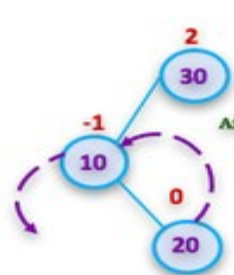


LR rotation

Insert 30, 10 and 20

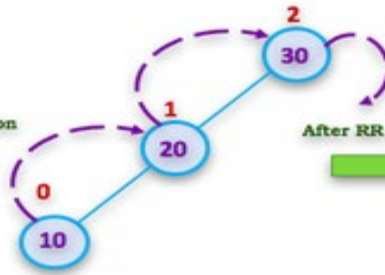


Tree is imbalanced
Because node 30 has balance factor 2



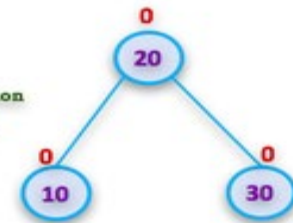
LL Rotation

After LL Rotation



RR Rotation

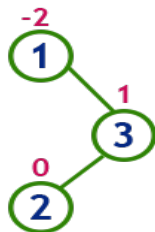
After RR Rotation



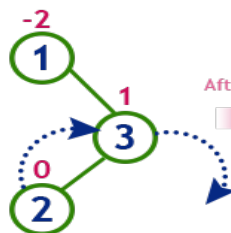
After LR Rotation
Tree is balanced

RL rotation

insert 1, 3 and 2

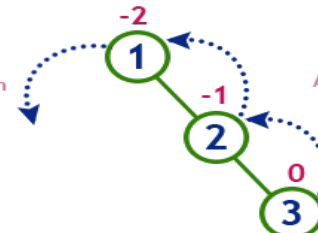


Tree is imbalanced
because node 1 has balance factor -2



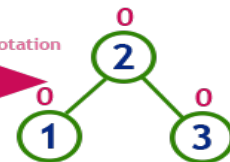
RR Rotation

After RR Rotation

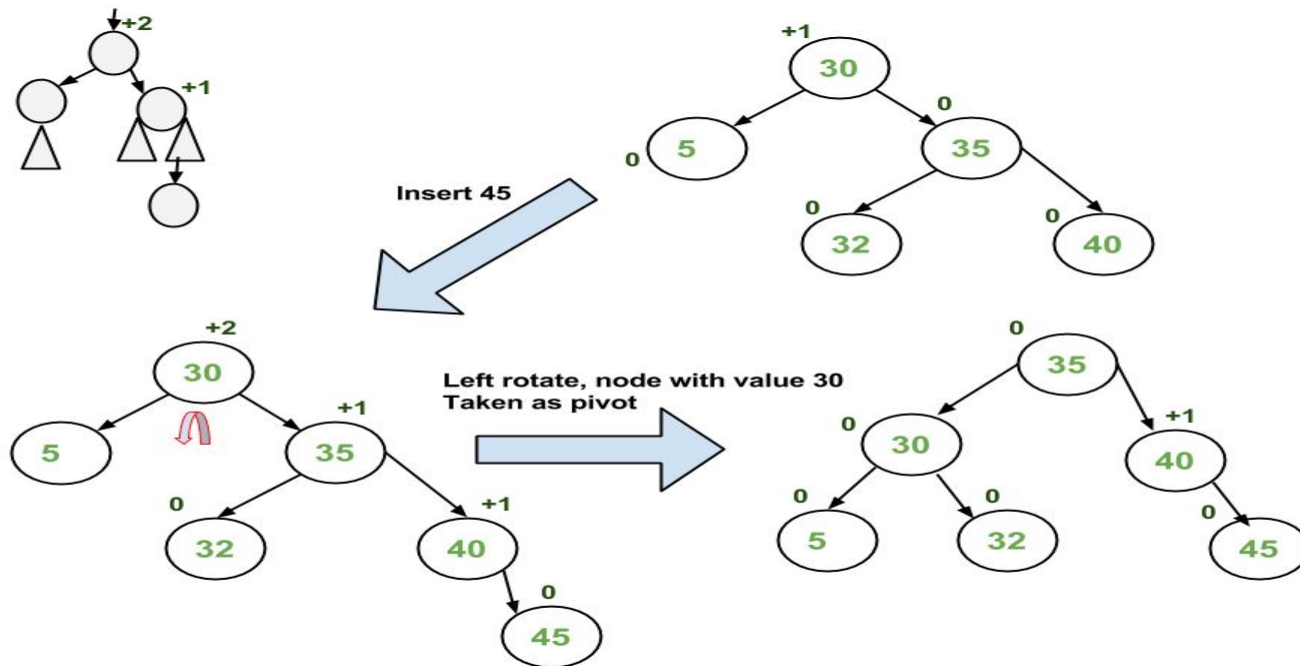
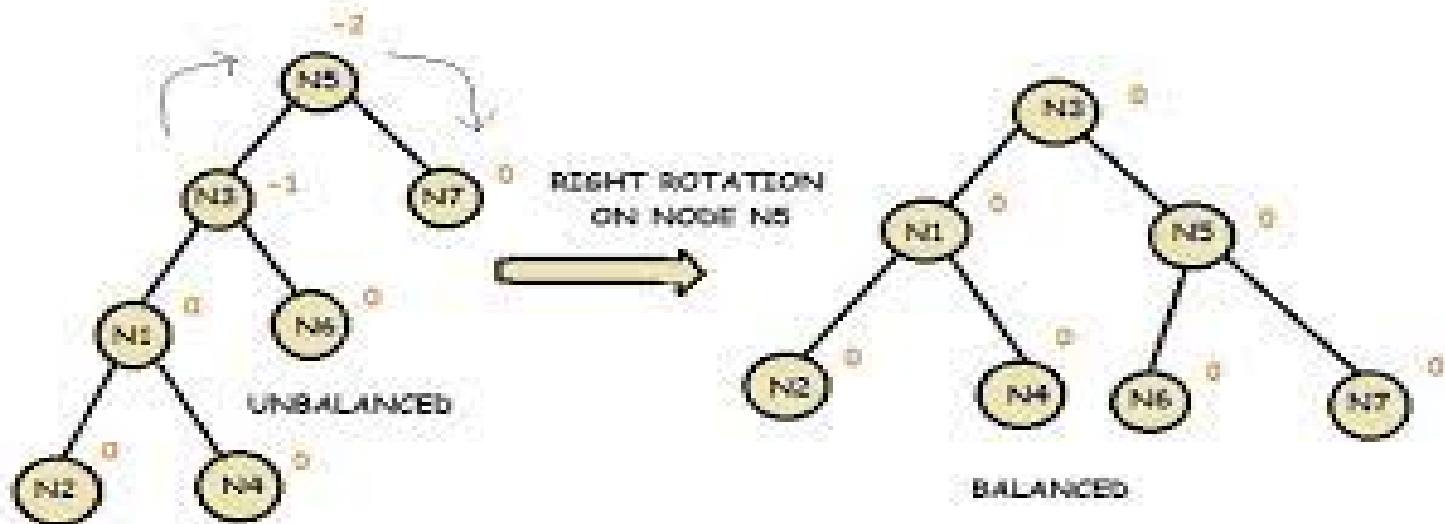


LL Rotation

After LL Rotation

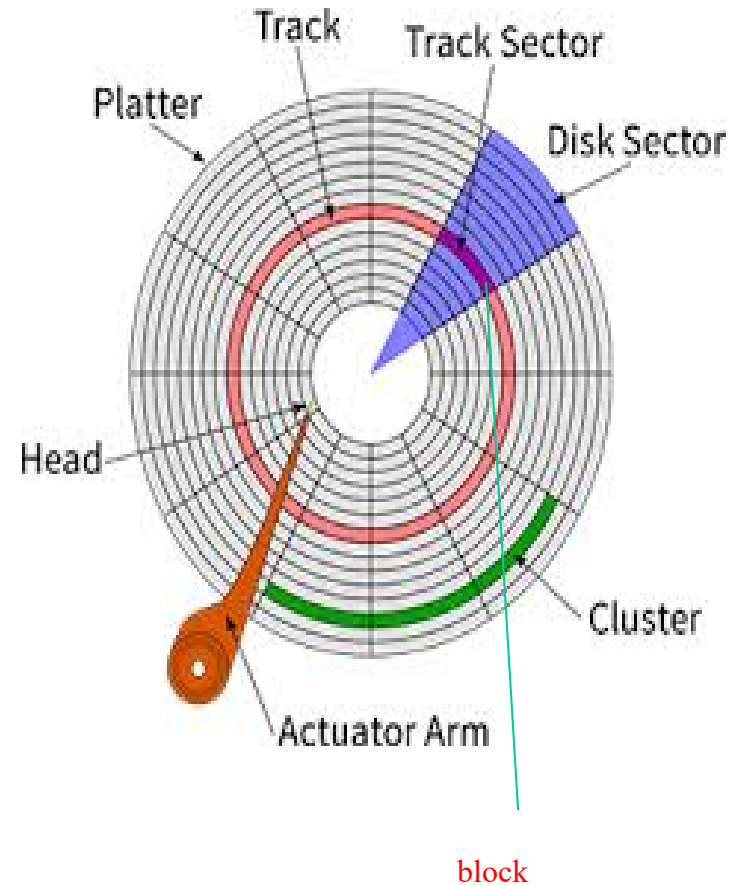
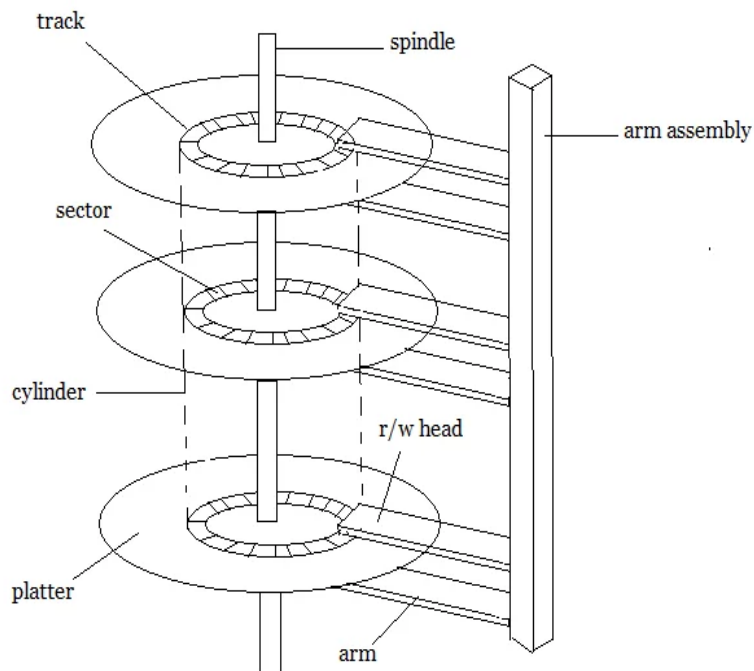


After RL Rotation
Tree is Balanced



Multiway Search Tree:

1. Disk structure
2. How data is stored
3. What is indexing
4. Multilevel indexing
5. M-Way tree
6. B tree
7. B+ tree



Block: block address means track number + sector number

Typical block size is 512 bytes.

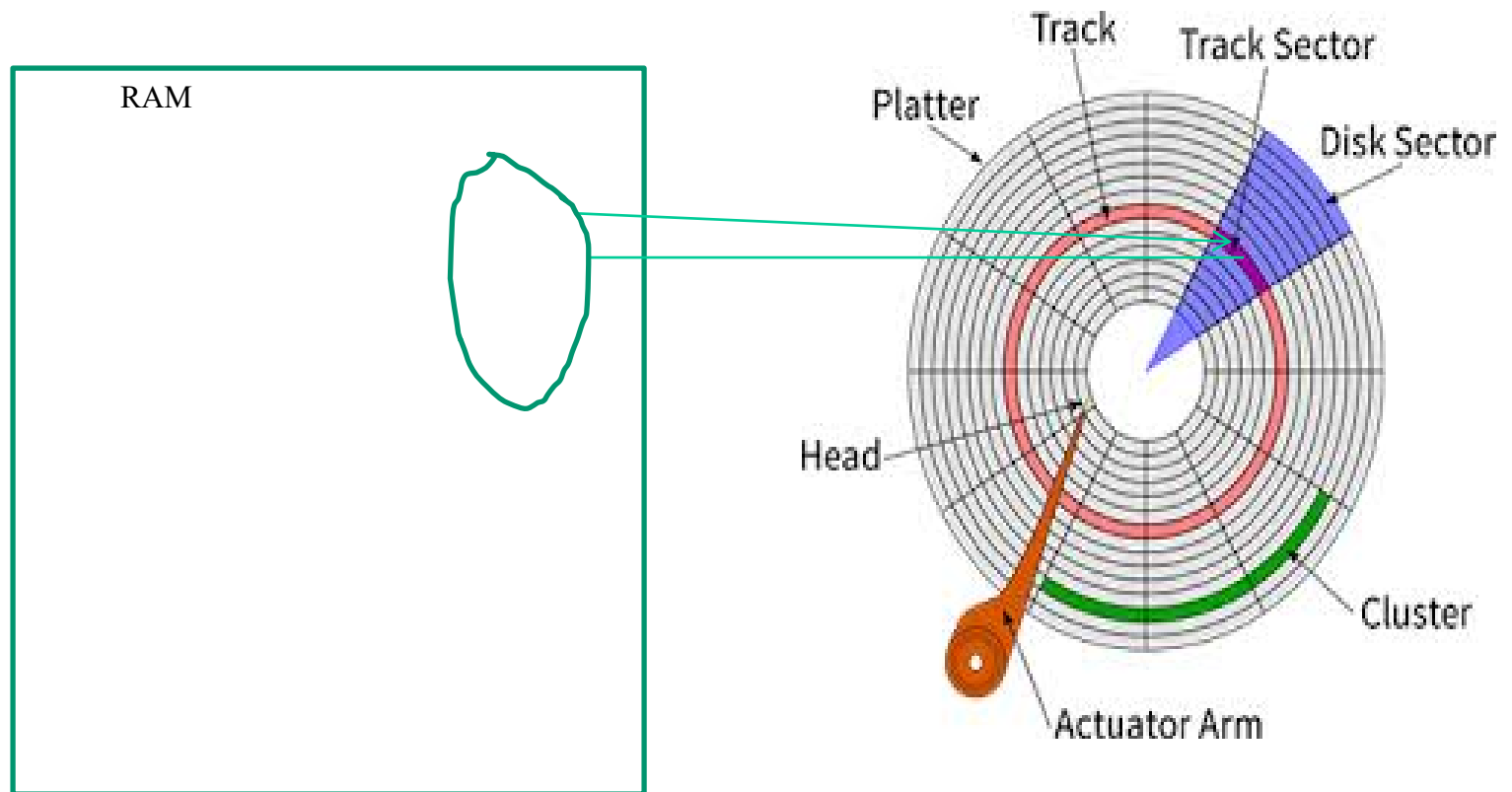
We always Read and write in terms of block



0 1

511

Each byte can be accessed by offset.



Data has to be brought into RAM, now how is stored in HDD is DBMS and how it is placed in RAM is DS.

Size of row is 128 bytes

First name – 25

Last name – 25

Address – 50

City – 18

Id - 10

First Name	Last Name	Address	City	Age
Mickey	Mouse	123 Fantasy Way	Anaheim	73
Bat	Man	321 Cavern Ave	Gotham	54
Wonder	Woman	987 Truth Way	Paradise	39
Donald	Duck	555 Quack Street	Mallard	65
Bugs	Bunny	567 Carrot Street	Rascal	58
Wiley	Coyote	999 Acme Way	Canyon	61
Cat	Woman	234 Purrfect Street	Hairball	32
Tweety	Bird	543	Ittittaw	28

No. of records per block = $512/128 = 4$

For 100 records = $100/4 = 25$ blocks for
100 records

In case u perform search for an employee,
we need no. of blocks, we need to access
25 blocks. **Can we do it faster???**

Yes, create index and keep it on disk say
on a block.. How many blocks will be
needed??

Index: 10 for id and 6 for
pointer = 16 bytes

Id pointer

1 Address

2 Address

3 address

For index

No of entries per block
 $512/16 = 32$

Total 100 records

$100/32 = 3.2$ say 4 blocks
are needed for index

1000 records : 250 blocks

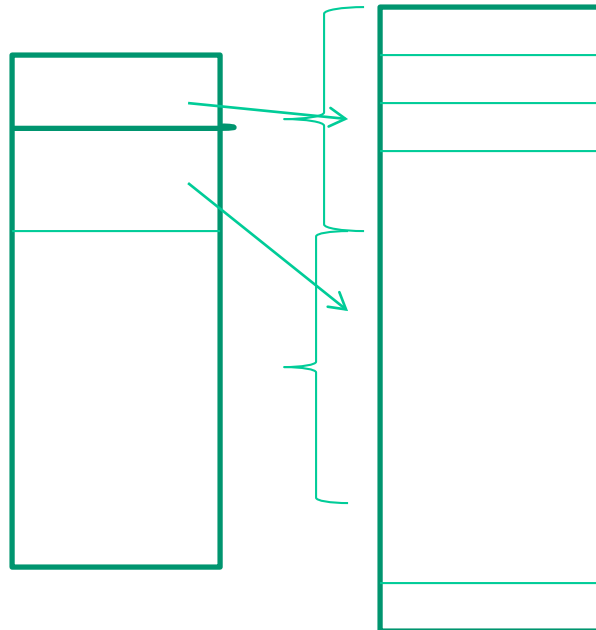
After indexing : 40 blocks

so for 100 records 4 blocks

for 1000 – 40 blocks

Create index above an index is possible:

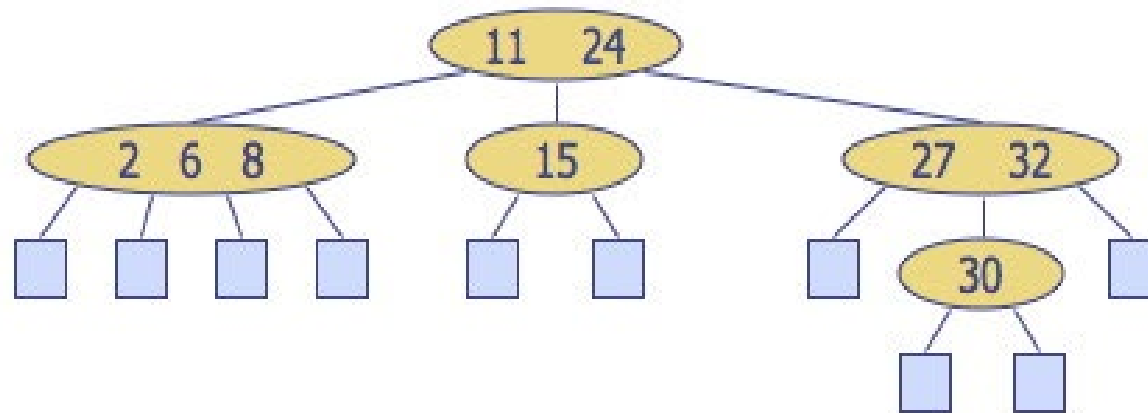
So now per block we can have 32 entries



M-way search tree: each node can have m children, and $m-1$ keys

Keys – 2 keys

Children – maximum 3, so this is 3-way search tree



Height balanced m -way search tree is B tree.

B-Tree:

1. Root can have min 2 children
2. All leaf nodes are at same level
3. All non leaf nodes should have at least $m/2$ children
4. The creation process is bottom up.