

# CST362-3 Pixel Relationship

Chapter-03  
2016

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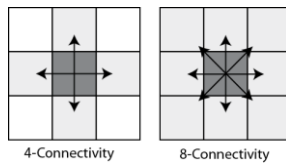
## Digitization

- Sampling
- Quantization
- 2D Matrix with Elements
- Pixels

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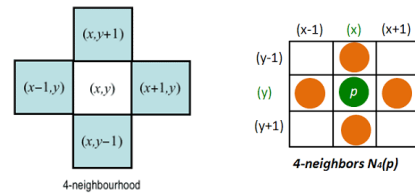
## Pixel Relationship

- Neighborhood
- Connectivity
- Adjacency



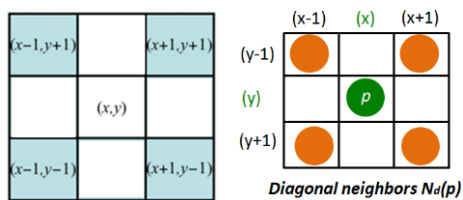
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## Neighborhood $N_4(P)$



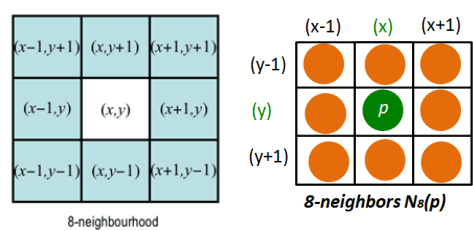
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## Neighborhood $N_D(P)$



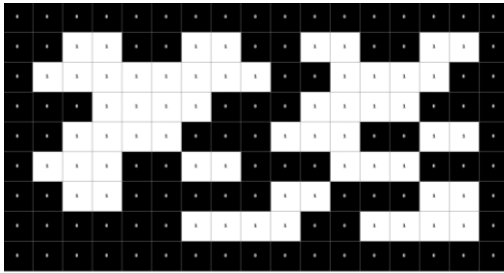
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## Neighborhood $N_8(P)$



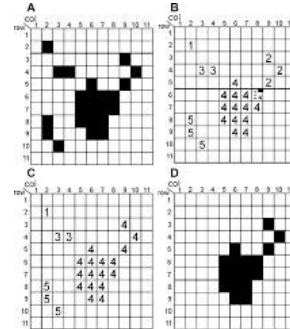
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## Objet and Connection



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## Different Object Count



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## Adjacency and Connectivity

- Let  $V$ : a set of intensity values used to define adjacency and connectivity.
- In a binary image,  $V = \{1\}$ , if we are referring to adjacency of pixels with value 1.
- In a gray-scale image, the idea is the same, but  $V$  typically contains more elements, for example,  $V = \{180, 181, 182, \dots, 200\}$
- If the possible intensity values 0 – 255,  $V$  set can be any subset of these 256 values.

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## Connectivity

- If two pixels are said to be connected if they are adjacent in some sense
  - $N_4(p)$ ,  $N_8(p)$ ,  $N_8(P)$
  - Their intensity values must be similar

	q	
p		

		q
	p	

	p	q

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## Type of Adjacency

- 4-adjacency:** Two pixels  $p$  and  $q$  with values from  $V$  are 4-adjacent if  $q$  is in the set  $N_4(p)$ .
- 8-adjacency:** Two pixels  $p$  and  $q$  with values from  $V$  are 8-adjacent if  $q$  is in the set  $N_8(p)$ .
- m-adjacency=(mixed)**

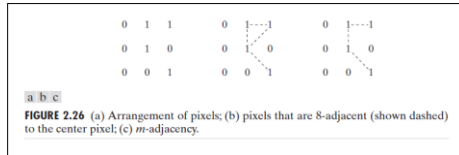
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## Digital Path

- A digital path (or curve) from pixel  $p$  with coordinate  $(x,y)$  to pixel  $q$  with coordinate  $(s,t)$  is a sequence of distinct pixels with
  - coordinates  $(x_0, y_0)$ ,  $(x_1, y_1)$ , ...,  $(x_n, y_n)$  where  $(x_0, y_0) = (x, y)$  and  $(x_n, y_n) = (s, t)$  and pixels  $(x_i, y_i)$  and  $(x_{i-1}, y_{i-1})$  are adjacent for  $1 \leq i \leq n$
  - $n$  is the length of the path
  - If  $(x_0, y_0) = (x_n, y_n)$ , the path is closed.
  - We can specify 4-, 8- or m-paths depending on the type of adjacency specified.

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## Digital Path



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## Region and Boundry

### • Region

Let  $R$  be a subset of pixels in an image, we call  $R$  a region of the image if  $R$  is a connected set.

### • Boundary

The *boundary* (also called *border* or *contour*) of a region  $R$  is the set of pixels in the region that have one or more neighbors that are not in  $R$ .

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## Region and Boundry

If  $R$  happens to be an entire image, then its boundary is defined as the set of pixels in the first and last rows and columns in the image.

This extra definition is required because an image has no neighbors beyond its borders

Normally, when we refer to a region, we are referring to subset of an image, and any pixels in the boundary of the region that happen to coincide with the border of the image are included implicitly as part of the region boundary.

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## Distance Measures

- For pixels  $p$ ,  $q$  and  $z$ , with coordinates  $(x,y)$ ,  $(s,t)$  and  $(v,w)$ , respectively,  $D$  is a distance function if:

- (a)  $D(p,q) \geq 0$  ( $D(p,q) = 0$  iff  $p = q$ ),
- (b)  $D(p,q) = D(q,p)$ , and
- (c)  $D(p,z) \leq D(p,q) + D(q,z)$ .

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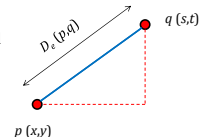
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## Distance Measures

- The *Euclidean Distance* between  $p$  and  $q$  is defined as:

$$D_e(p,q) = [(x-s)^2 + (y-t)^2]^{1/2}$$

Pixels having a distance less than or equal to some value  $r$  from  $(x,y)$  are the points contained in a disk of radius  $r$  centered at  $(x,y)$



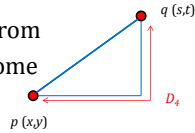
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## Distance Measures

- The  $D_4$  distance (also called *city-block distance*) between  $p$  and  $q$  is defined as:

$$D_4(p, q) = |x - s| + |y - t|$$

Pixels having a  $D_4$  distance from  $(x, y)$ , less than or equal to some value  $r$  form a Diamond centered at  $(x, y)$



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## Distance Measures

Example:

The pixels with distance  $D_4 \leq 2$  from  $(x, y)$  form the following contours of constant distance.

The pixels with  $D_4 = 1$  are the 4-neighbors of  $(x, y)$

		2		
	2	1	2	
2	1	0	1	2
	2	1	2	
		2		

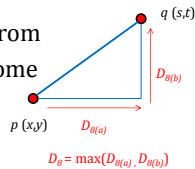
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## Distance Measures

- The  $D_8$  distance (also called *chessboard distance*) between  $p$  and  $q$  is defined as:

$$D_8(p, q) = \max(|x - s|, |y - t|)$$

Pixels having a  $D_8$  distance from  $(x, y)$ , less than or equal to some value  $r$  form a square centered at  $(x, y)$



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## Distance Measures

Example:

$D_8$  distance  $\leq 2$  from  $(x, y)$  form the following contours of constant distance.

2	2	2	2	2
2	1	1	1	2
2	1	0	1	2
2	1	1	1	2
2	2	2	2	2

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## Distance Measures

- Dm distance:**

is defined as the shortest m-path between the points.

In this case, the distance between two pixels will depend on the values of the pixels along the path, as well as the values of their neighbors.

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## Distance Measures

- Example:

Consider the following arrangement of pixels and assume that  $p, p_2$ , and  $p_4$  have value 1 and that  $p_1$  and  $p_3$  can have a value of 0 or 1

Suppose that we consider the adjacency of pixels values 1 (i.e.  $V = \{1\}$ )

	$p_3$	$p_4$
$p_1$	$p_2$	
$p$		

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## Distance Measures

- Cont. Example:

Now, to compute the  $D_m$  between points  $p$  and  $p_4$

Here we have 4 cases:

**Case1:** If  $p_1=0$  and  $p_3=0$

The length of the shortest m-path  
(the  $D_m$  distance) is 2 ( $p, p_2, p_4$ )

	0	1
0	1	
1		

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## Distance Measures

- Cont. Example:

**Case2:** If  $p_1=1$  and  $p_3=0$

now,  $p_1$  and  $p$  will no longer be adjacent (see *m-adjacency definition*)

then, the length of the shortest  
path will be 3 ( $p, p_1, p_2, p_4$ )

	0	1
1	1	
1		

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## Distance Measures

- Cont. Example:

**Case3:** If  $p_1=0$  and  $p_3=1$

The same applies here, and the shortest m-path will be 3 ( $p, p_2, p_3, p_4$ )

	1	1
0	1	
1		

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## Distance Measures

- Cont. Example:

**Case4:** If  $p_1=1$  and  $p_3=1$

The length of the shortest m-path will be 4  
( $p, p_1, p_2, p_3, p_4$ )

	1	1
1	1	
1		

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