# Natural Language Processing

CS 3216/UG, AI 5203/PG

Week-5 Language models



#### Recap

- NLP
- Applications
- Regular expressions
- Tokenization
- Stemming
  - o Porter Stemmer
- Lemmatization
- Normalization
- Stopwords
- o Bag-of-Words
- o TF-IDF
- o NER
- o POS tagging
- o Semantics, Distributional semantics, Word2vec

# Language Model

- Classic definition- Probability distribution over sequence of tokens
- Vocabulary V a set of tokens!

• A language model **p** assigns each sequence of tokens  $(x_1, .........x_L) \in V$ , a probability (a number between 0 and 1),

$$P(x_1, x_2, x_3, \dots, x_L)$$

• The probability intuitively tells us how "good" a sequence of tokens is.

### Language Model

- Consider the probability of four strings in English.
- Here Vocabulary,

 $V = \{ate, ball, cheese, mouse, the\}$ 

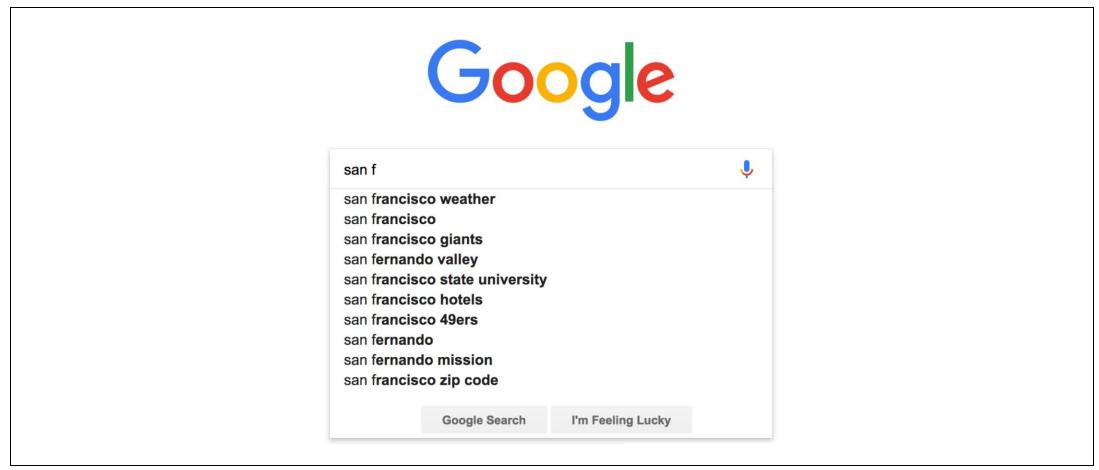
- p(the, mouse, ate, the, cheese)=0.02 ---->  $P_1$
- $p(the, cheese, ate, the, mouse)=0.01 \longrightarrow P_2$
- $p(mouse ,the, the, cheese, ate)=0.0001 ----> P_3$

### Language Model

• LM assigned, "mouse the the cheese ate" a very low probability implicitly because it's ungrammatical (syntactic knowledge).

- The LM should assign the mouse ate the cheese higher probability than the cheese ate the mouse implicitly because of,
  - world knowledge: both sentences are the same syntactically,
  - they differ in semantic plausibility

# Where do you see language models? Google Search system



# Spell correction



- The office is about fifteen minuets from my house
  - P(about fifteen minutes from) > P(about fifteen minuets from)

#### Machine Translation: Important Things To Know



# Machine Translation

P(high winds tonite) > P(large winds tonite)

# Speech recognition



Here, P(I saw a van) >> P(eyes awe of an)

### Types of Language Models

Probabilistic language models (PLMs)

Neural language models (NLMs)

# Probabilistic Language Modeling

• **Goal**: compute the probability of a *sentence* or *sequence of words*:

$$P(W) = P(w_1, w_2, w_3, w_4, w_5, \dots, w_n)$$

Related task: probability of an upcoming word:

$$P(w_5 | w_1, w_2, w_3, w_4)$$

• A model that computes either of these:

$$P(W)$$
 or  $P(w_n | w_1, w_2, \dots, w_{n-1})$  is called a language model.

# How to compute P(W)

- How to compute this joint probability:
  - P(its, water, is, so, transparent, that)
- Intuition: let's rely on the Chain Rule of Probability

#### Reminder: The Chain Rule

• Recall the definition of conditional probabilities

$$P(B|A) = P(A,B)/P(A)$$

Rewriting: 
$$P(A,B) = P(A)P(B|A)$$

More variables:

$$P(A,B,C,D) = P(A)P(B | A)P(C | A,B)P(D | A,B,C)$$

The Chain Rule in General

$$P(x_1,x_2,x_3,...,x_n) = P(x_1)P(x_2 | x_1)P(x_3 | x_1,x_2)...P(x_n | x_1,...,x_{n-1})$$

#### Chain Rule

To Compute joint probability of words in a sentence "its water is so transparent"

$$P(w_1 w_2 ... w_n) = \prod_{i} P(w_i | w_1 w_2 ... w_{i-1})$$

```
P("its water is so transparent") =
  P(its) × P(water|its) × P(is|its water)
  × P(so|its water is) × P(transparent|its water is so)
```

#### How to estimate these probabilities

Could we just count and divide?

P(the | its water is so transparent that) = Count(its water is so transparent that the) Count(its water is so transparent that)

Why Not?

No!!!! Too many possible sentences! We will never see enough data to estimate these



# Markov Assumption:

Simplifying assumption:

 $P(\text{the }|\text{ its water is so transparent that}) \approx P(\text{the }|\text{ that})$ 

Or maybe

 $P(\text{the }|\text{its water is so transparent that}) \approx P(\text{the }|\text{transparent that})$ 

# Markov Assumption

$$P(w_1 w_2 ... w_n) \approx \prod_i P(w_i | w_{i-k} ... w_{i-1})$$

 In other words, we approximate each component in the product

$$P(w_i | w_1 w_2 ... w_{i-1}) \approx P(w_i | w_{i-k} ... w_{i-1})$$

# Simplest case: Unigram model

$$P(w_1 w_2 \dots w_n) \approx \prod_i P(w_i)$$

Some automatically generated sentences from a unigram model

fifth, an, of, futures, the, an, incorporated, a, a, the, inflation, most, dollars, quarter, in, is, mass

thrift, did, eighty, said, hard, 'm, july, bullish

that, or, limited, the

# Bigram model

Condition on the previous word:

$$P(w_i | w_1 w_2 ... w_{i-1}) \approx P(w_i | w_{i-1})$$

texaco, rose, one, in, this, issue, is, pursuing, growth, in, a, boiler, house, said, mr., gurria, mexico, 's, motion, control, proposal, without, permission, from, five, hundred, fifty, five, yen

outside, new, car, parking, lot, of, the, agreement, reached

this, would, be, a, record, november

# Estimating bigram probabilities

#### The Maximum Likelihood Estimate

$$P(w_{i} | w_{i-1}) = \frac{count(w_{i-1}, w_{i})}{count(w_{i-1})}$$

$$P(w_i \mid w_{i-1}) = \frac{c(w_{i-1}, w_i)}{c(w_{i-1})}$$

# An example

$$P(w_i \mid w_{i-1}) = \frac{c(w_{i-1}, w_i)}{c(w_{i-1})}$$
  ~~I am Sam~~   ~~Sam I am~~   ~~I do not like green eggs and ham~~ 

#### Solution?

#### Solution

$$P(w_i \mid w_{i-1}) = \frac{c(w_{i-1}, w_i)}{c(w_{i-1})} \quad \begin{array}{l} < > 1 \text{ am Sam } < / > > \\ < > 5 \text{ Sam I am } < / > > \\ < > 5 \text{ I do not like green eggs and ham } < / > > \\ < > 6 \text{ Sam I am } < / > > \\ < > 7 \text{ Sam I am } < / > > \\ < > 8 \text{ I do not like green eggs and ham } < / > > \\ < > 8 \text{ I do not like green eggs and ham } < / > > \\ < > 8 \text{ I do not like green eggs and ham } < / > > \\ < 8 \text{ I do not like green eggs and ham } < / > > \\ < 8 \text{ I do not like green eggs and ham } < / > > \\ < 8 \text{ I do not like green eggs and ham } < / > > \\ < 8 \text{ I do not like green eggs and ham } < / > > \\ < 8 \text{ I do not like green eggs and ham } < / > > \\ < 8 \text{ I do not like green eggs and ham } < / > < 8 \text{ I do not like green eggs and ham } < / > < 8 \text{ I do not like green eggs and ham } < / > < 8 \text{ I do not like green eggs and ham } < / > < 8 \text{ I do not like green eggs and ham } < / > < 8 \text{ I do not like green eggs and ham } < / > < 8 \text{ I do not like green eggs and ham } < / > < 8 \text{ I do not like green eggs and ham } < / > < 8 \text{ I do not like green eggs and ham } < / > < 8 \text{ I do not like green eggs and ham } < / > < 8 \text{ I do not like green eggs and ham } < / > < 8 \text{ I do not like green eggs and ham } < / > < 8 \text{ I do not like green eggs and ham } < / > < 8 \text{ I do not like green eggs and ham } < / > < 8 \text{ I do not like green eggs and ham } < / > < 8 \text{ I do not like green eggs and ham } < / > < 8 \text{ I do not like green eggs and ham } < / > < 8 \text{ I do not like green eggs and ham } < / > < 8 \text{ I do not like green eggs and ham } < / > < 8 \text{ I do not like green eggs and ham } < / > < 8 \text{ I do not like green eggs and ham } < / > < 8 \text{ I do not like green eggs and ham } < / > < 8 \text{ I do not like green eggs and ham } < / > < 8 \text{ I do not like green eggs and ham } < / > < 8 \text{ I do not like green eggs and ham } < / > < 8 \text{ I do not like green eggs and ham } < / > < 8 \text{ I do not like green eggs and ham } < / > < 8 \text{ I do not like green eggs and ham } < / > < 8 \text{ I do not like green eggs and ham } < / > <$$

$$P({
m I}|{
m <} {
m >}) = {2\over 3} = .67$$
  $P({
m Sam}|{
m <} {
m >}) = {1\over 3} = .33$   $P({
m am}|{
m I}) = {2\over 3} = .67$   $P({
m <} {
m /s} {
m >} |{
m Sam}) = {1\over 2} = 0.5$   $P({
m Sam}|{
m am}) = {1\over 2} = .5$   $P({
m do}|{
m I}) = {1\over 3} = .33$ 

#### Raw bigram counts

• Total- 9333 sentences

	i	want	to	eat	chinese	food	lunch	spend
i	5	827	0	9	0	0	0	2
want	2	0	608	1	6	6	5	1
to	2	0	4	686	2	0	6	211
eat	0	0	2	0	16	2	42	0
chinese	1	0	0	0	0	82	1	0
food	15	0	15	0	1	4	0	0
lunch	2	0	0	0	0	1	0	0
spend	1	0	1	0	0	0	0	0

#### Normalize by unigrams:

i	want	to	eat	chinese	food	lunch	spend
2533	927	2417	746	158	1093	341	278

#### Result:

	i	want	to	eat	chinese	food	lunch	spend
i	0.002	0.33	0	0.0036	0	0	0	0.00079
want	0.0022	0	0.66	0.0011	0.0065	0.0065	0.0054	0.0011
to	0.00083	0	0.0017	0.28	0.00083	0	0.0025	0.087
eat	0	0	0.0027	0	0.021	0.0027	0.056	0
chinese	0.0063	0	0	0	0	0.52	0.0063	0
food	0.014	0	0.014	0	0.00092	0.0037	0	0
lunch	0.0059	0	0	0	0	0.0029	0	0
spend	0.0036	0	0.0036	0	0	0	0	0

Credits: Slide adapted from [2]

#### Bigram estimates of sentence probabilities

```
P(<s> I want english food </s>) =
  P(1|<s>)
  \times P(want|I)
  × P(english|want)
  × P(food|english)
  \times P(</s>|food)
    = .000031
```

#### What kinds of knowledge?

- P(english|want) = .0011
- P(chinese|want) = .0065
- P(to|want) = .66
- P(eat | to) = .28
- P(food | to) = 0
- P(want | spend) = 0
   P(i | <s>) = .25

#### Practical Issues

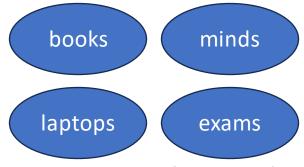
- We do everything in log space
  - Avoid underflow
  - (also adding is faster than multiplying)

$$\log(p_1 \times p_2 \times p_3 \times p_4) = \log p_1 + \log p_2 + \log p_3 + \log p_4$$

# Summary- Language Modeling Task

Language Modeling is the task of predicting what word comes next

the students opened their



- More formally: given a sequence of words, compute the probability distribution of the next word
- A system that does this is called a Language Model

# Summary: N-gram Language Models

the students opened their \_\_\_\_\_

- Question: How to learn a Language Model?
- Answer (pre- Deep Learning): learn an n-gram Language Model!
  - o Definition: An n-gram is a chunk of n consecutive words.
  - o *unigrams*: "the", "students", "opened", "their"
  - o bigrams: "the students", "students opened", "opened their"
  - o *trigrams*: "the students opened", "students opened their"
  - o four-grams: "the students opened their"
- Idea: Collect statistics about how frequent different n-grams are and use these to predict next word.

#### n-gram Language Models

• First we make a Markov assumption:  $x^{(t+1)}$  depends only on the preceding n-1 words

$$P(oldsymbol{x}^{(t+1)}|oldsymbol{x}^{(t)},\ldots,oldsymbol{x}^{(1)}) = P(oldsymbol{x}^{(t+1)}|oldsymbol{x}^{(t)},\ldots,oldsymbol{x}^{(t-n+2)})$$
 (assumption)

prob of a n-gram 
$$= P(\boldsymbol{x}^{(t+1)}, \boldsymbol{x}^{(t)}, \dots, \boldsymbol{x}^{(t-n+2)})$$
 prob of a (n-1)-gram 
$$= P(\boldsymbol{x}^{(t+1)}, \boldsymbol{x}^{(t)}, \dots, \boldsymbol{x}^{(t-n+2)})$$

(definition of conditional prob)

- Question: How do we get these n-gram and (n-1)-gram probabilities?
- Answer: By counting them in some large corpus of text!

$$pprox rac{ ext{count}(oldsymbol{x}^{(t+1)},oldsymbol{x}^{(t)},\ldots,oldsymbol{x}^{(t-n+2)})}{ ext{count}(oldsymbol{x}^{(t)},\ldots,oldsymbol{x}^{(t-n+2)})}$$
 (statistical approximation)



#### n-gram Language Models: Example

Suppose we are learning a 4-gram Language Model.

$$P(\boldsymbol{w}|\text{students opened their}) = \frac{\text{count}(\text{students opened their }\boldsymbol{w})}{\text{count}(\text{students opened their})}$$

For example, suppose that in the corpus:

- "students opened their" occurred 1000 times
- "students opened their books" occurred 400 times
  - $\rightarrow$  P(books | students opened their) = 0.4
- "students opened their exams" occurred 100 times
  - → P(exams | students opened their) = 0.1

Should we have discarded the "proctor" context?



#### **Sparsity Problems with n-gram Language Models**

**Sparsity Problem 1 Problem:** What if "students (Partial) Solution: Add small  $\delta$ opened their w" never to the count for every  $w \in V$ . occurred in data? Then w has This is called *smoothing*. probability 0! count(students opened their w) $P(\boldsymbol{w}|\text{students opened their}) =$ count(students opened their) Sparsity Problem 2 **Problem:** What if "students (Partial) Solution: Just condition opened their" never occurred in on "opened their" instead. data? Then we can't calculate This is called *backoff*. probability for any w!

**Note:** Increasing *n* makes sparsity problems *worse*. Typically, we can't have *n* bigger than 5.



#### **Storage Problems with n-gram Language Models**

**Storage**: Need to store count for all *n*-grams you saw in the corpus.

$$P(\boldsymbol{w}|\text{students opened their}) = \frac{\text{count}(\text{students opened their }\boldsymbol{w})}{\text{count}(\text{students opened their})}$$

Increasing *n* or increasing corpus increases model size!



#### n-gram Language Models in practice

You can build a simple trigram Language Model over a
 1.7 million word corpus (Reuters) in a few seconds on your laptop\*

today the

Business and financial news

get probability distribution



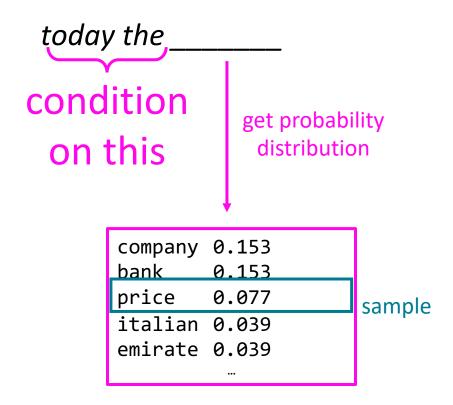
#### **Sparsity problem**:

not much granularity in the probability distribution

Otherwise, seems reasonable!

#### **Generating text with a n-gram Language Model**

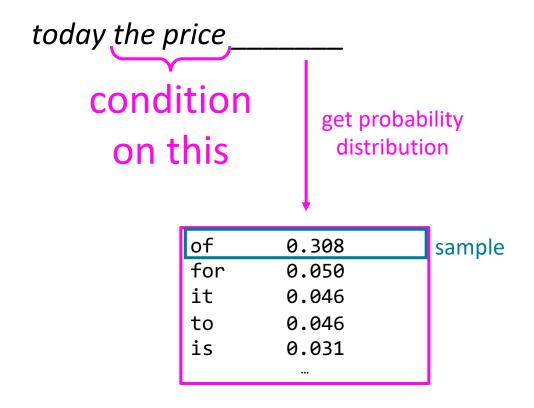
You can also use a Language Model to generate text





#### **Generating text with a n-gram Language Model**

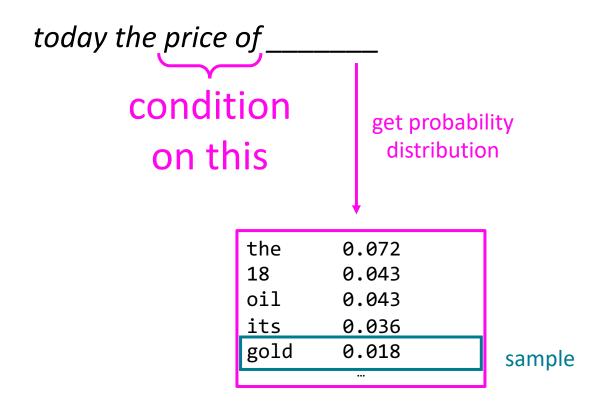
You can also use a Language Model to generate text





#### **Generating text with a n-gram Language Model**

You can also use a Language Model to generate text





#### N-gram models

- Extend to trigrams, 4-grams, 5-grams
- In general, this is an insufficient model of language because language has long-distance dependencies:

"The computer which I had just put into the machine room on the fifth floor crashed."

But we can often get away with N-gram models



#### **Evaluating Language Models**

The standard evaluation metric for Language Models is perplexity.

$$\text{perplexity} = \prod_{t=1}^T \left( \frac{1}{P_{\text{LM}}(\boldsymbol{x}^{(t+1)}|\ \boldsymbol{x}^{(t)},\dots,\boldsymbol{x}^{(1)})} \right)^{1/T}$$
 Normalized by number of words

Inverse probability of corpus, according to Language Model

• This is equal to the exponential of the cross-entropy loss  $J(\theta)$ :

$$= \prod_{t=1}^{T} \left( \frac{1}{\hat{\boldsymbol{y}}_{\boldsymbol{x}_{t+1}}^{(t)}} \right)^{1/T} = \exp \left( \frac{1}{T} \sum_{t=1}^{T} -\log \hat{\boldsymbol{y}}_{\boldsymbol{x}_{t+1}}^{(t)} \right) = \exp(J(\theta))$$

Lower perplexity is better!



#### References

- [1] <a href="https://stanford-cs324.github.io/winter2022/lectures/introduction/">https://stanford-cs324.github.io/winter2022/lectures/introduction/</a>
- [2] <a href="https://web.stanford.edu/~jurafsky/slp3/slides/LM\_4.pdf">https://web.stanford.edu/~jurafsky/slp3/slides/LM\_4.pdf</a>



#### Acknowledgments

- These slides were adapted from the book SPEECH and LANGUAGE PROCESSING: An Introduction to Natural Language Processing, Computational Linguistics, and Speech Recognition
- Practical Natural Language Processing (A Comprehensive Guide to Building Real-World NLP Systems) O'reilly and some modifications from presentations and resources found in the WEB by several scholars.



#### Reference materials

- https://vlanc-lab.github.io/mu-nlpcourse/
- Lecture notes
- (A) Speech and Language Processing by Daniel Jurafsky and James H. Martin
- (B) Natural Language Processing with Python. (updated edition based on Python 3 and NLTK 3) Steven Bird et al. O'Reilly Media

