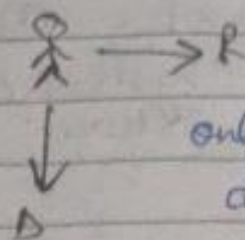
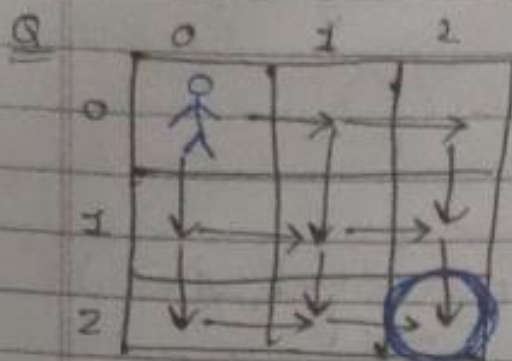


Mazes



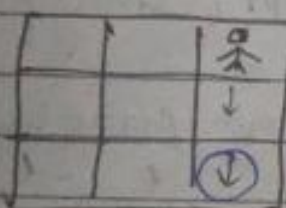
only right & down
allowed

Ans: RRDD, DDRR, RDDR, RDRD...

No. of ways from $(0,0) \rightarrow (2,2)$

BASE CONDITION

⇒ When we are at the last ~~row~~ column

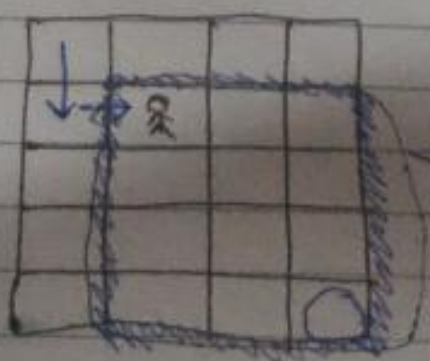


YOU CAN ONLY GO DOWNWARDS

⇒ When we are at the last row



YOU CAN ONLY GO RIGHT

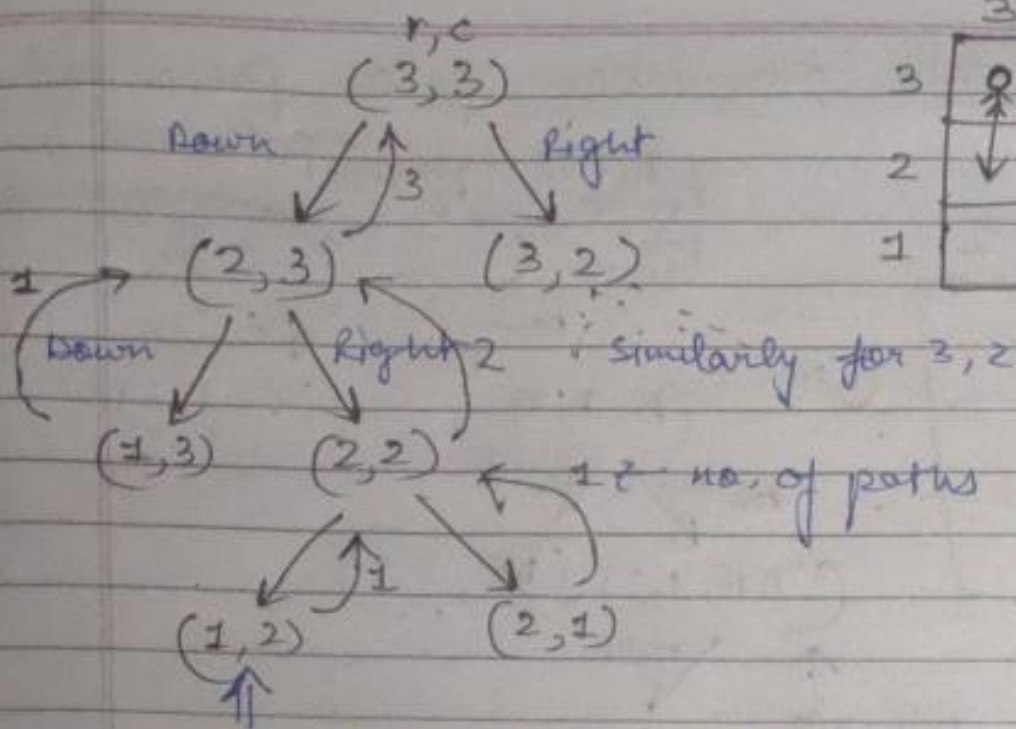


paths till that point

DR +

Answer of this part

Remaining paths



	3	2	1
3	0	→	
2	↓		
1			

When row or column = 1 then only 1 path possible

* Return Count of paths

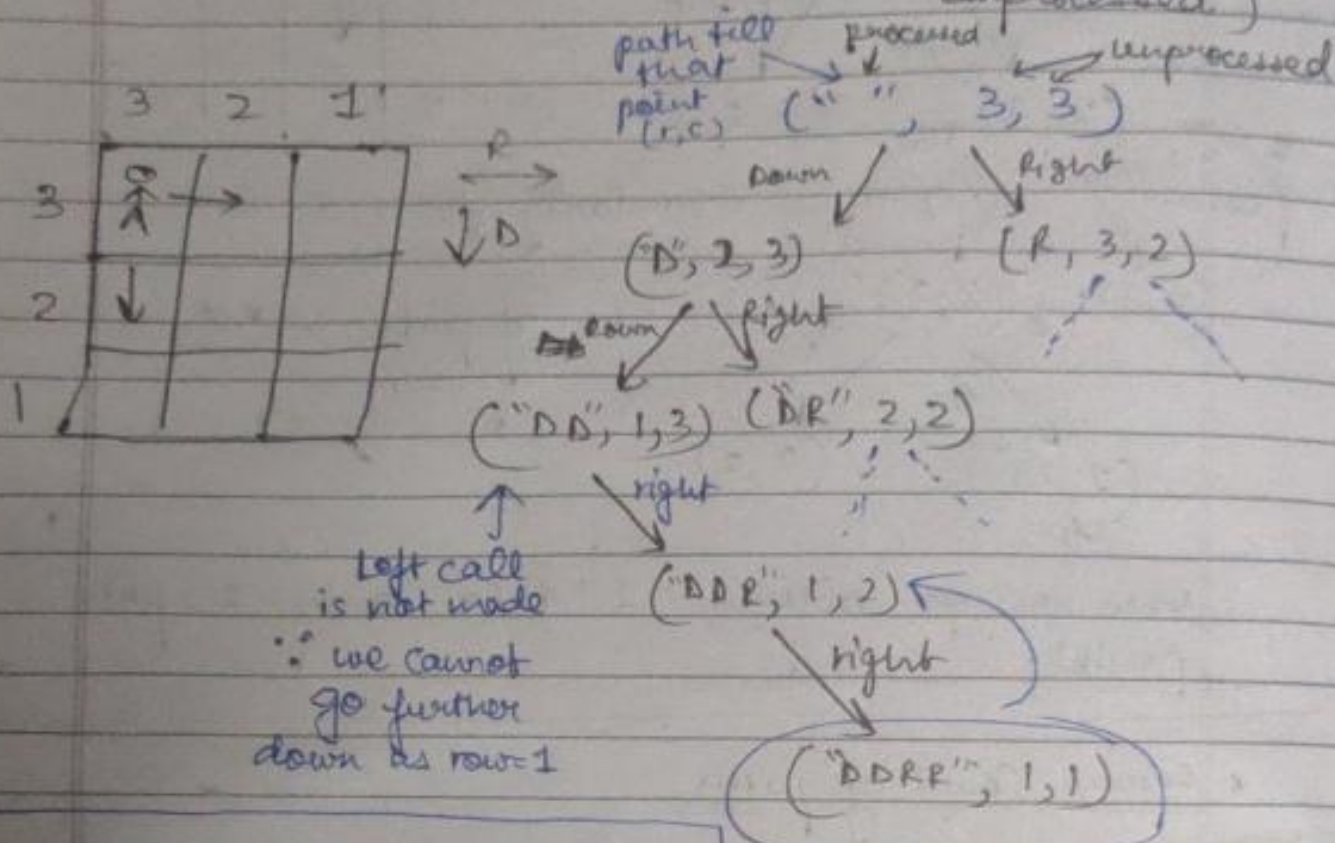
```
static int count(int row, int col) {
    if (row == 1 || col == 1) {
        return 1; // only 1 ans possible
    }
}
```

```
int leftDown = count(row-1, col); // Get count when going downwards
int right = count(row, col-1); // Get count when going right
return leftDown + right;
```

```
}
```

Add both answers & return

* Print the path (permutations, follow processed & unprocessed.)



Code

Initially "" when called from main

When both 1, 1 we got an answer. Hence, return of the processed

```
void path(String p, int r, int c)
{
    if (r == 1 && c == 1) { ← r=1, c=1 means you reached the destination
        System.out.println(p); ← print the path & return
        return;
    }

    if (r > 1) { ← if not at last, then you can go further DOWN i.e. (r-1, c)
        path(p + 'D', r-1, c);
    }

    if (c > 1) { ← if not at last col then you may go further RIGHT i.e. (r, c-1)
        path(p + 'R', r, c-1);
    }
}
```

* Add all paths in ArrayList

```
ArrayList<String> pathlet (String p, int r, int c) {
```

```
    if (r == 1 && c == 1) {
```

```
        ArrayList<String> list = new ArrayList<>();  
        list.add(p);  
        return;
```

```
    }
```

```
    ArrayList<String> list = new ArrayList<>();
```

```
    if (r > 1) {
```

```
        list.addAll(pathlet(p + 'D', r - 1, c));
```

```
    }
```

```
    if (c > 1) {
```

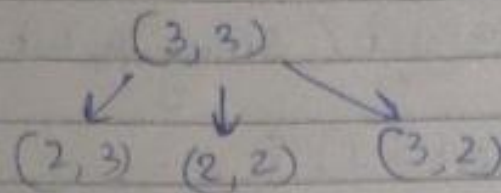
```
        list.addAll(pathlet(p + 'R', r, c - 1));
```

```
    }
```

```
    return list;
```

```
}
```


* With Diagonal, Right, Down allowed



→ Conditions for going:

Down $\Rightarrow (r > 1)$

Diagonal $\Rightarrow (r > 1 \ \&\& \ c > 1)$

Right $\Rightarrow (c > 1)$

```

    ArrayList<String> pathRetDiagonal(String p, int r, int c) {
        if (r == 1 && c == 1) {
            ArrayList<String> list = new ArrayList<>();
            list.add(p);
            return list;
        }
    
```

```

        ArrayList<String> list = new ArrayList<>();
    
```

```

        if (r > 1 && c > 1) { // Diagonal calls
            list.addAll(pathRetDiagonal(p + 'D', r-1, c-1));
        }
    
```

```

        if (r > 1) { // Vertical (Right) calls
            list.addAll(pathRetDiagonal(p + 'V', r-1, c));
        }
    
```

```

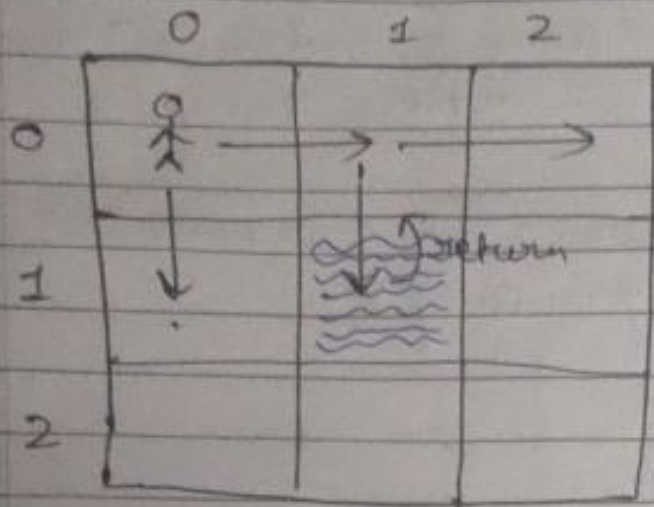
        if (c > 1) { // Horizontal (Down) calls
            list.addAll(pathRetDiagonal(p + 'H', r, c-1));
        }
    
```

```

        return list;
    }

```

Q. Maze With Obstacles

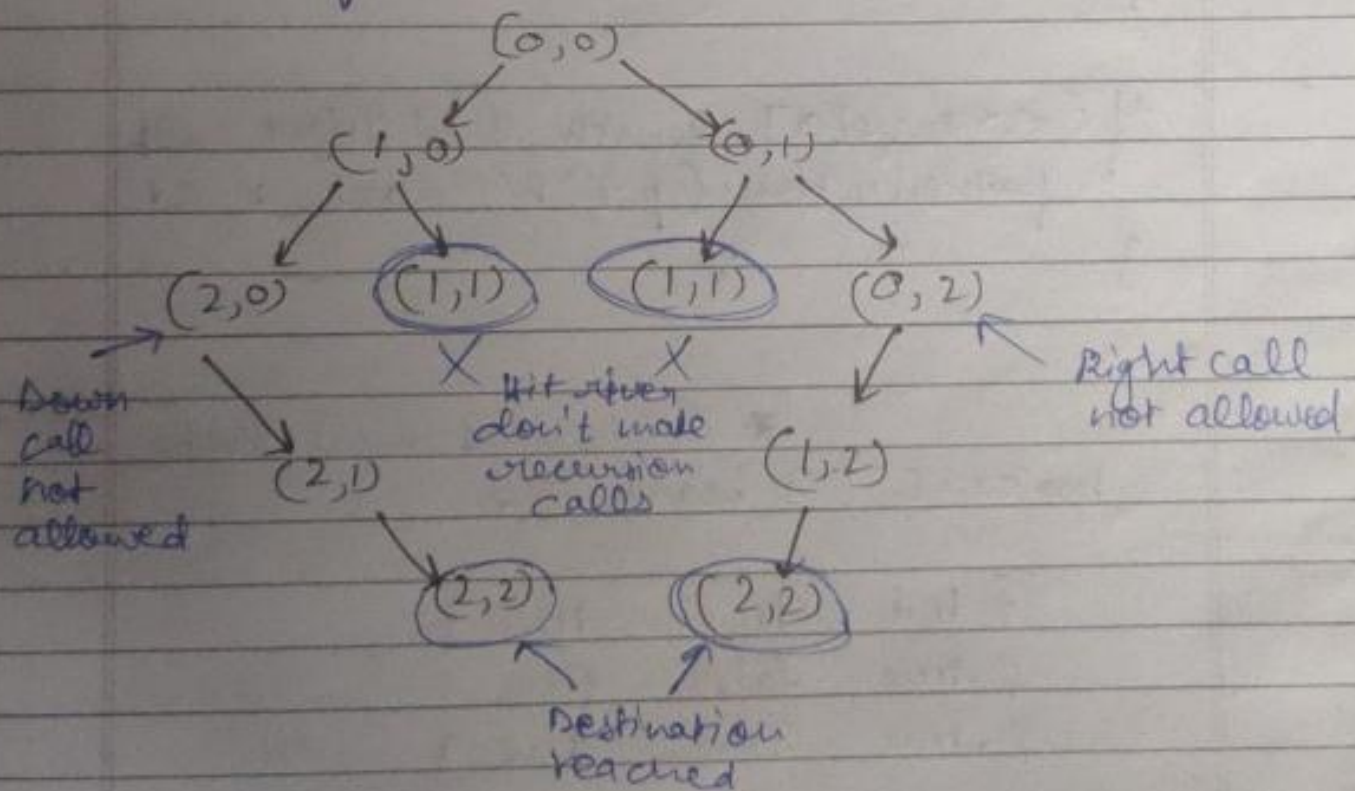


Boolean Matrix
false \Rightarrow river
 \nwarrow can't cross it

Allowed paths
 $\rightarrow R$
 \downarrow
D

NOTE: When you land on a new cell, check whether that is river or not.

If you land on river, stop recursion of that call



* Print all paths (starts from (0,0), boolean ^{matrix} ~~and~~)

```
void pathrestrictions (String p, boolean[][] maze,
                      int r, int c) {
```

```
    if (r == maze.length - 1 && c == maze[0].length - 1)
    {
        System.out.println(p);
        return;
    }
```

```
    if (!maze[r][c]) { // if (maze[r][c] = false)
        return; // river encountered
    } // return without calling further
```

```
    if (r < maze.length - 1) { // down ward calls
        pathrestrictions (same p + 'D', maze, r+1, c);
    }
```

```
    if (c < maze[0].length - 1) { // right calls
        pathrestrictions (p + 'R', maze, r, c+1);
    }
```

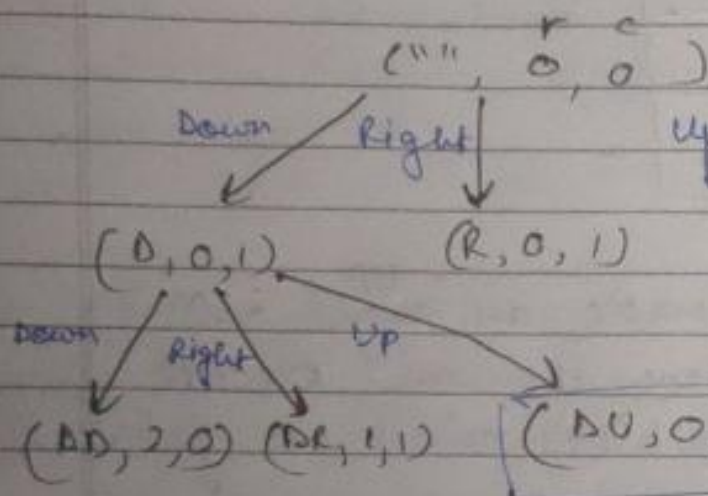
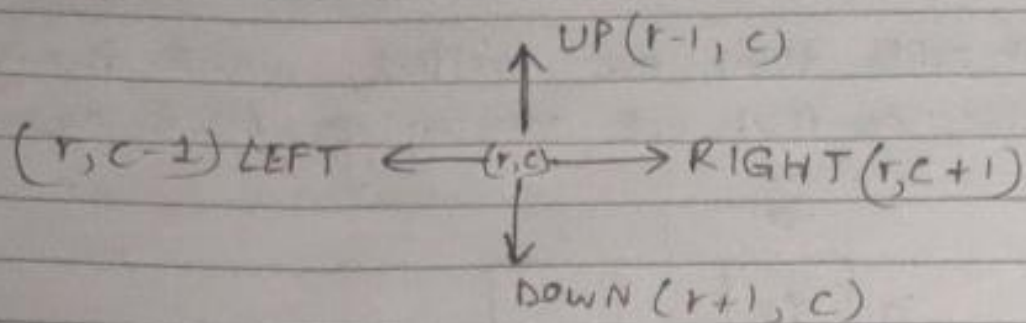
```
}
```

* This is what maze looks like
boolean[][] board = {

```
{ true, true, true },
{ true, false, true },
{ true, true, true }
```

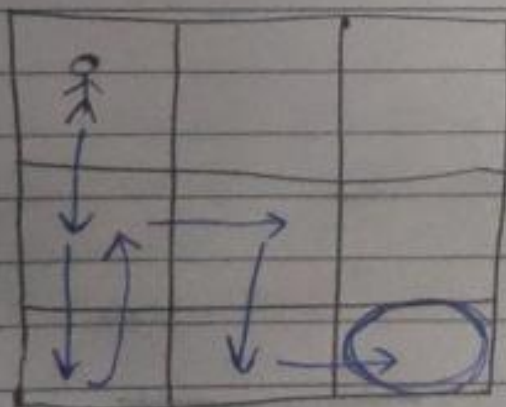
```
};
```

MAZE (All Directions allowed)



up & left calls are not made as it is out of bounds

⚡ We are at the same position as we started this will cause stack-overflow as recursion tree keeps on growing infinitely.



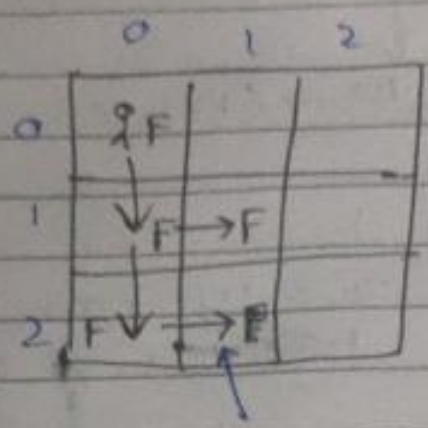
THIS **CANNOT** BE AN ANSWER

* Do not move back the same path

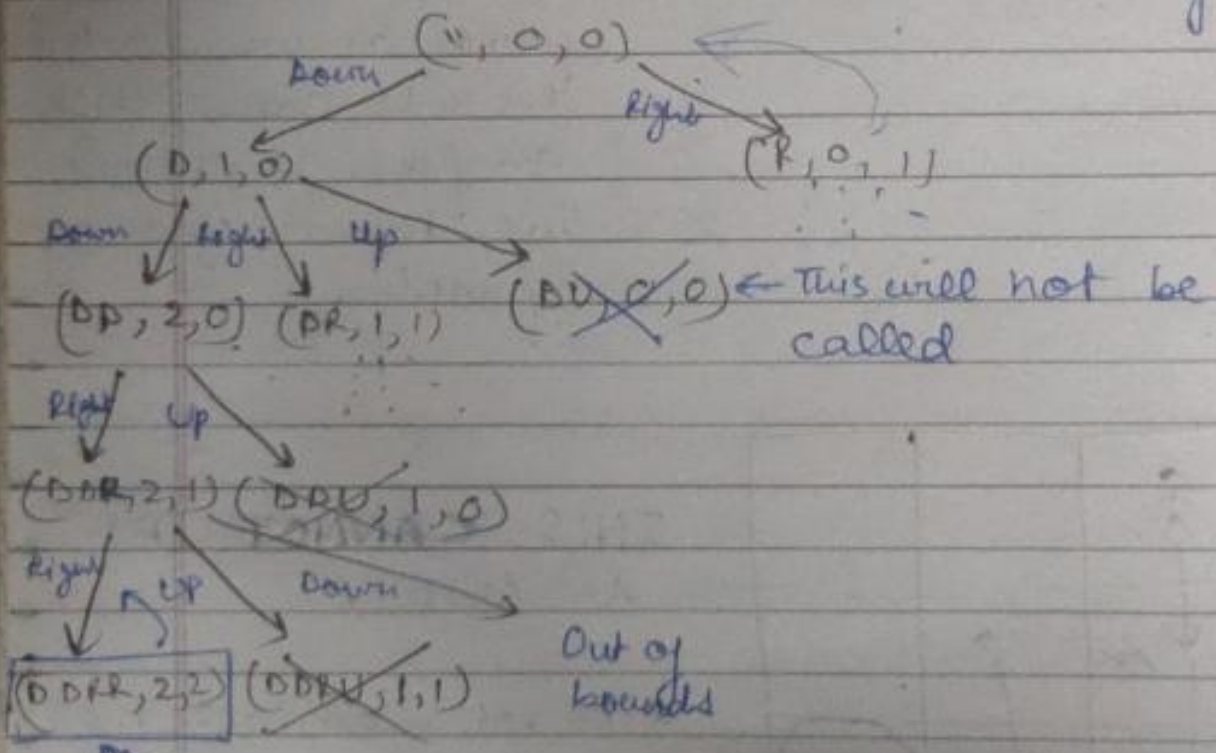
* This is Backtracking problem

* How to solve this problem

All calls that are visited, mark those as false, so that we cannot go back again.



If we make an ^{UP} ~~above~~ call from here, it won't execute as the block above is false.



∴ we are at last ∴ this is 1 of the answers

NOTE: Here is a problem is that original array is being modified

* While going back the ^{cell} ~~path~~ is marked visited which don't allow future answers to be formed.

Common Sense: Marking false == I have that cell in my current path.

So, when that path is over, e.g.:
You are in another recursion call,
those cells should not be false

Important

While you are moving back you restore the maze as it was.

* When do we go back?

When the function ~~returns~~ is returned.

⇒ When you come out of the recursive fn → you are in above recursive call.

Hence, remark the cell as true.

⇒
This is known as backtracking

Backtracking

We are making some changes while going to ahead recursive calls.

What would the ~~if~~^{if} scenario be, hadn't those changes be made?

Undoing changes made in current recursive call for restoring the state in previous recursive call is called BACKTRACKING.

Code (All 4 directions MAZE)

```
void allPath (String p, boolean[][] maze, int r, int c)
{
    if (r == maze.length - 1 && c == maze[0].length - 1) {
        System.out.println(p);
        return;
    }

    if (!maze[r][c]) {
        return;
    }

    // I am considering this block in my path
    maze[r][c] = false;

    if (r < maze.length - 1) { // Down call
        allPath(p + 'D', maze, r + 1, c);
    }
}
```

```

if (c < maze[0].length - 1) { // Right call
    allpath(p + 'R', maze, r + 1, c);
}
if (r > 0) { // Up call
    allpath(p + 'U', maze, r - 1, c);
}
if (c > 0) { // Left call
    allpath(p + 'L', maze, r, c - 1);
}

```

// this line is where the fⁿ will be over

// so before the fⁿ gets removed, also remove the changes that were made by that fⁿ

maze[r][c] = true;

}

}

boolean ~~[]~~ maze = {

{ true, true, true },

{ true, true, true },

{ true, true, true }

};

GIVEN
MAZE
MATRIX

* Print the paths with matrix

1		
2		
3	4	5

DDR

1		
2	5	6
3	4	7

DDRURD

- Take a step variable
- update the path array
- print it in base condition
- BACKTRACK (∵ All reference variables in diff fn arguments point to same object)

Code

~~void allpathprint (~~

void main() {

boolean[][] board = {

{true, true, true},

{true, true, true},

{true, true, true}

};

int[][] path = new int[board.length][board[0].length];

allpathprint("", board, 0, 0, path, 1);

}

```
void allpathprint(String p, boolean[][] maze, int r, int c,
int[][] path, int step) {
```

```
if (r == maze.length-1 && c == maze[0].length-1) {
    path[r][c] = step; // the destination block is also a stop
```

```
    for (int[] arr: path) {
        System.out.println(Arrays.toString(arr));
```

```
    }
    System.out.println(p);
```

```
    System.out.println();
    return;
}
```

```
if (!maze[r][c]) {
    return;
}
```

```
// Considering this block in my path
maze[r][c] = false;
```

```
// marking the step
path[r][c] = step;
```

```
if (r < maze.length-1) { // Down call
    allpathprint(p+'D', maze, r+1, c, path, step+1);
}
```

```
if (c < maze[0].length-1) { // Right call
    allpathprint(p+'R', maze, r, c+1, path, step+1);
}
```



```

if(r > 0) { // Up call
    allpathprint(p + 'U', maze, r-1, c, path, step+1);
}

```

```

if(c > 0) { // Left call
    allpathprint(p + 'L', maze, r, c-1, path, step+1);
}

```

// this line is where fⁿ will be over

// so before the fⁿ gets removed, also remove the
 // changes that were made by that fⁿ

```

    maze[r][c] = true;
    path[r][c] = 0;
}

```