@AndrzejWasowski@scholar.social

Andrzej Wąsowski Florian Biermann

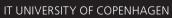
Advanced Programming

Algebraic Data Types





SOFTWARE



- Algebraic Data Types
- Functional lists and trees
- Fold functions
- Style guidelines for functional programming in ADPRO



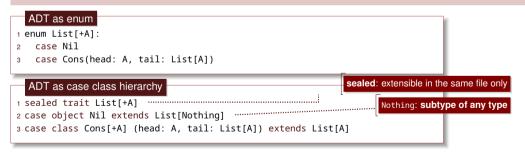
Algebraic Data Types (ADTs) as Enums and Classes

Enums less general, but used more often

Def. Algebraic Data Type

A type generated by one or more constructors, each taking zero or more arguments.

The sets of objects generated by each constructor are **summed** (unioned), each constructor can be seen as a representation of a Cartesian **product** (tuple) of its arguments; thus the name **algebraic**.



Algebraic Data Types (ADTs)

Def. Algebraic Data Type

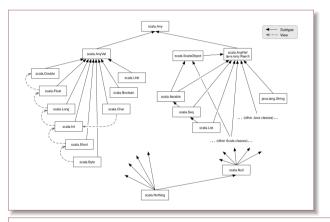
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```
Example: lists
enum List[+A]:
   case Nil
   case Cons(head: A. tail: List[A])
 operations on lists
                                                                                  companion object of List[+A]
1 object List: .....
   def sum(ints: List[Int]): Int = ints match
                                                                         pattern matching against case constructors
     case Nil => 0
     case Cons(x, xs) => x + sum(xs)
   def apply[A] (as: A*): List[A] =
                                                                     overloading function application for the object
     if as.isEmpty then Nil
     else Cons(as.head, apply(as.tail*))
                                                                                              variadic function
```

Lists are covariant

All share the same tail!



For any type A we have that

Nil <:List[Nothing] <:List[A]</pre>

```
1 sealed trait List[+A]
```

- 2 case object Nil extends List[Nothing]
- 3 case class Cons[+A] (head: A, tail: List[A]) extends List[A]

Poll: How is your recursion?

Mentimeter: 3473 1775

```
1 def f (a: List[Int]): Int = a match
  case Nil => 0
  case Cons(h, t) \Rightarrow h + f(t)
```

What is f(List(42, -1, 1, -1, 1, -1))?



Function Values

- In functional programing functions are values
- Functions can be **passed to other functions**, composed, etc.
- Nothing special: just functions (called "higher order" or HOF)

```
def map(a: List[Int])(f: Int => Int): List[Int] = a match
 case Nil => Nil
 case Cons(h, tail) => Cons(f(h), map(tail)(f))
```

A functional (pure) example

```
val mixed = List(-1, 2, -3, 4)
```

map(mixed)(abs)

```
map(mixed)((factorial) compose (abs))
```

An imperative (impure) example

```
val mixed = Array(-1, 2, -3, 4)
```

- for i <- 0 until mixed.length do
- mixed(i) = abs(mixed(i))

```
val mixed1 = Array(-1, 2, -3, 4)
```

- for i <- 0 until mixed1.length do
- mixed1(i) = factorial(abs(mixed1(i)))

Parametric Polymorphism

Monomorphic functions operate on fixed types:

A monomorphic map in Scala def map(a: List[Int])(f: Int => Int): List[Int] = a match case Nil => Nil case Cons(h, tail) => Cons(f(h), map(tail)(f))

There is nothing specific here regarding Int.

```
A polymorphic map in Scala
def map[A, B](a: List[A])(f: A \Rightarrow B): List[B] = a match
  case Nil => Nil
  case Cons(h, tail) => Cons(f(h), map(tail)(f))
```

An example of use:

```
1 map[Int, String] (mixed) {
  (_.toString) compose (factorial) compose (abs) }
```

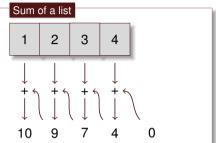
- A polymorphic function operates on values of (m)anv types
- A polymorphic type constructor defines a parameterized family of types
- Don't confuse with inheritance-based polymorphism AKA "dynamic dispatch"

Useful Functions from the Standard Library

Methods of class List[A], operate on this list, type A is bound in the class

```
map[B](f: A => B): List[B]
Translate this list of As into a list of Bs using f to convert the values
filter(p: A =>Boolean): List[A]
A sublist of this containing elements satisfying predicate p
flatMap[B](f: A =>List[B]): List[B]
                                                                 *type slightly simplified
Apply f to elements of this and concatenate the produced lists
take(n: Int): List[A]
A list of first n elements of this.
takeWhile(p: A =>Boolean): List[A]
A prefix of this containing elements satisfying p
forall(p: A =>Boolean): Boolean
True iff p holds for all elements of this
exists(p: A =>Boolean): Boolean
True iff p holds for at least one element of this
More at https://www.scala-lang.org/api/current/scala/collection/immutable/List.html
```

Folds: Functional Loops



```
What characterizes folds?
```

- An input list 1 = List(1,2,3,4)
- An initial value z = 0
- A binary operation f: (Int,Int) => Int = _ + _
- An iteration algorithm

Many HOFs are special cases of folding

Preferred Programming Style in ADPRO

Always choose the best possible style for an exercise and your abilities

Condemned (fail)	ightarrow Forgivable (medium grade*) $ ightarrow$	Enlightened (top grade)
variables < assignments < return statement < Any/Object type <		< values < value bindings < expression value < parametric polymorphism
loops <	tail recursion* < simple re- cursion < folds* if conditions < pattern	< compose dedicated (higher order) functions < use dedicated API
exceptions <	matching*	< Option or Either monad

^{*} unless asked for explicitly, or really important for memory use.

Scala: Summarv

- **Basics** (objects, modules, functions, expressions, values, variables, operator overloading, infix methods, interpolated strings.)
- Pure functions (referential transparency, side effects)
- **Loops and recursion** (tail recursion)
- **Functions as values** (higher-order functions)
- Parametric polymorphism (monomorphic functions, dynamic and static dispatch)
- Standard functions in Scala's library
- **Anonymous functions** (currying, partial function application)
- Traits (fat interfaces, multiple inheritance, mixins)
- Algebraic Data Types (pattern matching, case classes)
- Folding