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Advanced **Programming**

Program Correctness & Property-based Testing





Property-Based Testing

What problem we are solving today?

The Problem

- Scenario testing (unit testing) tries only the situations for which you created test-cases, and which you anticipated
- This **increases the cost** of testing (you need to create many test-cases)
- This **lowers the coverage** of tests (only things you anticipated are tried)

The Solution

- Automate generation of test data
- Use randomized inputs, generated in controlled manner (which we know how to do from the State chapter)
- Generalize tests to properties that should hold on many possible inputs



- Assertions
- Pre-conditions
- Post-conditions
- Contracts
- Invariants
- Property-Based Testing
- Homework & ScalaCheck

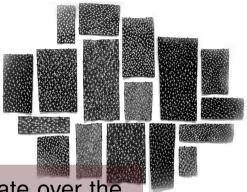


Assertions

```
1 // assertion: an empty list has size zero
2 assert(List().size == 0)
4 def f(l: List[Int]): Unit =
   // A contract for Cons: If I have a list, and add an element to it
   // it will certainly have at least one element in it
   assert(Cons(42, 1).size > 0)
   // A contract for Cons: If length of a list is n, and you add (Cons)
   // an element to the list, it will have size n+1
   assert(1.size + 1 == Cons (42, 1).size)
   // A contract for Cons: If you add (Cons) an element to the list.
   // then this element will be the head of the list.
   assert(Cons(42, 1).headOption == Some (42))
17 def head(l: List[Int]): Int =
   // Precondition for head: 1 is not empty
   assert( ... ) // <---- menti: 7944 0896
```

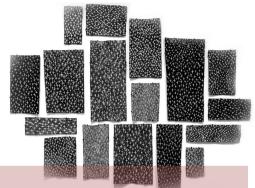
- Analyze examples
- English turned into predicates over program state (variables, values)
- Invariants, pre-conditions, post-conditions, contracts
- In Scala: assert is a method on the Predef object, automatically imported
- 2-argument version: produce an error msg

Definition



Assertion is a Boolean predicate over the program state (variables and values), usually expressed as a logical proposition, that evaluates to true in the correct executions.

Why Assertions?



- Help the programmer read the code
- Facilitate fail-fast programming
- Help compilers compile efficiently
- Support testing and verification

Flavours of Assertions

Scala terminology

- Require: before an action, bug if violated, blame the caller, a pre-condition
- Ensuring: after an action, bug if violated, blame the callee, a post-condition; In Scala it is an expression: (e) ensuring { x =>P(x) }, returns the value of e
- Assert: Must hold, the checker should prove it, a goal, bug if does not hold; A test
- Assume: Consider only satisfying executions; Verifier assumes this; An axiom
- At runtime they all just fail with different exceptions, if violated
- Differences mostly visible in interpreting the failure (and in formal verification)
- Assertions are **not** specific to imperative programming, used in FP too
- Write small assertions if possible, test a single violation at a time. Gives better feedback.

Pre-conditions for Option

```
1 def isEmpty: Boolean = this match { case None => true: case => false }
2 // Get the value held by an option
3 // Precondition for 'get': !this.isEmpty
4 \text{ def qet: } A = \dots
6 // Apply a binary operator to all elements of this iterable collection
7 // Like foldRight, but with an implicit initial element. Examples:
8 // List(1,2,3).reduce[Int] { + } == 6
9 // List(1).reduce[Int] { _+_ } == 1
10 // Some(1).reduce[Int] { + } == 1
11 // Nil.reduce[Int] { _+_ } == 0
12 // precondition for 'reduceRight': true
13 def reduceRight[B >: A](op: (A, B) => B): B
15 // Count the number of elements in a collection that satisfy a predicate
16 // Task: what is the precondition for 'count' in terms of this 'object'?
17 def count(p: A => Boolean): Int // 7944 0896
19 // Always fail with an exception
20 // Task: what is the precondition for this.f to avoid failure?
21 def f = throw Exception()
                                         // 7944 0896
```

- Pre-condition true means always succeeds (no pre-condition)
- Pre-condition false means never succeeds (always fail)

Pre-conditions (require)

Pre-condition: A Boolean predicate such that if it holds before execution of some code then the code behaves correctly.

- Typically considered at the entry point to a function or procedure
- Can constrain arguments + other variables and values in scope
- Enforced using assertions in most programming languages
- A function can have **several pre-conditions** (a single example)
 - Consider: def factorial(n: Int): Int
 - \blacksquare n >= 0 is a pre-condition
 - \blacksquare n >= 2 is a pre-condition, too. Why?
 - \blacksquare n >= 0 is weaker, n >= 2 is stronger. Why?
- The weakest pre-condition: the minimal assumption for a block of code (typically a function) to behave correctly, so to satisfy the expected post-condition
- We specify the weakest pre-conditions for functions to achieve complete specifications
- Stronger pre-conditions are used in testing (when testing only one aspect of logics)

Post-conditions

```
1 def size[A](t: Tree[A]): Int
2 // A post-condition: forall t. size(t) >= 1
4 def depth[A](t: Tree[A]): Int
5 // A post-condition: forall t. depth(t) >= 0
7 // A helper function
8 def get(t: Tree[Int]): Int = t match
   case Leaf(n) => n
10    case Branch(1, _) => get(1)
12 // Now we use it
13 def maximum(t: Tree[Int]): Int
14 // A post-condition: forall t: maximum(t) >= get(t)
16 // We previously defined
17 def nextInt: (Int. RNG) = ...
18 // The postcondition: true
19 // Not the strongest post-condition for random,
20 // but it is hard to give a stronger one.
21 // This would require formally defining the pseudo-
22 // random stream (likely not needed)
```

- Are these the strongest post-conditions we could think of? Could we guarantee more?
- Strongest post-conditions may be difficult to write
- The maximum post-condition relates more than one function (we shall return to this)
- A true post-condition means that we cannot say anything useful about the result
- (like a false pre-condition meant that there is no useful conditions in which the function could be called)

Post-conditions (ensuring)

Post-condition A Boolean **predicate** describing a correct result of an execution of a fragment of code.

- Typically applied to functions
- For a function it constraints the return value
- In imperative programs also constraints variables and values in scope
- The **strongest post-condition**: the maximum guarentee for a code fragment given by a correct execution, so an execution that satisfies a pre-condition
- Strongest post-conditions are used to define the **complete behavior** of code
- **Testing:** check post-conditions with assertions after a function call
- Giving strongest post-conditions is often difficult without replicating the code
- Decompose the post-condition and test for several weaker conditions instead

Contracts

```
1 // Returns this scala.Option if it is nonempty, otherwise return
2 // the result of evaluating alternative.
3 def orElse[B >: A](alternative: => Option[B]): Option[B]
4 // pre-condition: true
5 // post-condition:
6 // (!this.isEmpty => orElse(alternative) == this
                                                            ) &&
7 // ( this.isEmptv => orElse(alternative) == alternative)
9 def maximum (t: Tree[Int]): Int
10 // pre-condition: true
11 // post-condition:
12 // (forall a in t: { a <= maximum(t) }) &&</pre>
13 // (exist a in t: { a == maximum(t) })
14 // (forAll/exist could be implemented for trees as static methods)
16 // For partial functions a pre-condition is not true.
17 def get[A](oa: Option[A]): A = ...
18 // pre-condition: !oa.isEmpty
19 // post-condition: Some(get(oa)) == oa
```

- We are using algebraic laws again in all three examples
- A key aspect of correct behavior is that it interacts well with other parts of our API

Contracts

Contract. A contract for a function is a pair of a pre-condition and a post-condition. The caller of the function must ensure that the pre-condition is satisfied at the call time, and the callee has to ensure that the post-condition holds after termination, if the pre-condition was satisfied.

- Ideally a contract minimizes assumptions and maximizes quarantees (the pre-condition is the weakest, the post-condition is the strongest)
- Writing these ideal complete contracts may be difficult
- In testing, we can use weaker contracts:
 - \blacksquare If ϕ holds before the call then ψ holds after the call
 - Not necessarily the weakest/strongest
 - We decompose the ideal contract into tests and test-cases, or, in other words pairs of stronger preconditions and weaker post-conditions
- NB. The weakest contract is false => true
 - Any terminating function satisfies it vacously

Invariants

- An invariant is a related concept: A property that should always hold (for an object/concept at runtime)
- **Loop invariant** holds at every loop iteration (not useful in FP). Why?
 - Insertion sort: Elements left of the current index form a sorted sequence
- In FP loop invariants are replaced by contracts of recursive functions
- Data structure invariant holds always for instances f the data structure:
 - AVL trees: The difference of height between the left and right subtree is at most 1 for anv AVL tree node

Property-based testing in a nutshell /1

Actual test code from exercises in the prior weeks

Three weak/partial contracts/laws for map on trees (with trivial/true preconditions)

```
property("Ex04.02: identity is a unit with map") =
   forAll { (t: Tree[Int]) => Tree.map(t)(identity[Int]) == t }
4 property("Ex04.03: map does not change size") = // 7944 0896
   forAll { (t: Tree[Int], f: Int => Int) =>
     Tree.size(Tree.map(t)(f)) == Tree.size(t) }
8 property("Ex04.04: map is 'associative'") = // 7944 0896
   forAll { (t: Tree[Int], f: Int => Int, a: Int => Int) =>
     Tree.map (Tree.map(t)(f))(g) == Tree.map(t)(g compose f) }
10
```

- forAll generates random Tree[Int]
- forAll checks if the predicate (lambda) holds for all random data. Fail if false
- This code uses the ScalaCheck library
- We implement a similar lib next week

Property-based testing in a nutshell /2

Test-data generators

```
1 def genTree[A](using arbA: Arbitrary[A]): Gen[Tree[A]] =
   for
     coin <- Gen.frequency(7 -> true, 1 -> false)
     tree <- if coin
       then arbA.arbitrary.map(Leaf.apply)
       else genTree.flatMap { l => genTree.map { Branch(l, _) } }
   vield tree
9 given arbitraryTree[A: Arbitrary]: Arbitrary[Tree[A]] =
   Arbitrary[Tree[A]](genTree)
```

- This week we learn how to use the API
- Next we build such API, incl. givens + Gen monad
- When you test a new data type: create a generator for it
- Normally you write much more tests than generators
- genTree generates a random tree of A, if it can find a given generator of arbitrary A
- Gen.frequency is a Gen[Boolean], returns true/false with relative frequencies 7/1 (polymorphic)
- arbA.arbitrary is a Gen[A], mapped into a leaf containing the A (Gen[Leaf[A]])
- Last 2 lines expose a given generator of arbitrary trees of As, so forAll and other Gens can find it

Scenario tests vs Property tests

- Most traditional unit-level and integration-level testing uses scenarios
- Examples, test cases, one path through a system per test
- Scenarios are obtained from requirements
- Good for **covering requirements**.
- Good for testing special corner cases
- Good for recording **regression tests**
- Automation key for success
- Test libraries are more important than debuggers, in the sense that if you automate tests, you reuse the effort
- BDD, TDD, JUnit (XUnit), Cucamber/RSpec, scalatest

- Property-based testing (PBT) tests algebraic laws that should hold for an API
- The process is:
 - 1 Formulate laws (pre/post/invariant thinking helps)
 - 2 Generate random data
 - 3 Test the laws on this data
- Gives better (? rather alternative)
 coverage than scenario testing
- It may catch things that you did not predict, due to randomness
- Gets closer to verification but remains easy
- You use formal specifications to test

PBT and Contracts

```
1 // Recall the specification // pre-condition: !oa.isEmpty
2 def get[A](oa: Option[A]): A
                              // post-condition: Some(get(oa)) == oa
4 // When testing in the classical way, create a value 'oa', run get, inspect the result
5 property ("test get contract") = // Example with ScalaCheck simple Boolean property
   get (oa) == 1
                               // Any Boolean function (predicate) is treated like an assert
9 // Two weaknesses:
10 // 1. For another integer, write another test; create repetive code (or iterate a collection)
11 // 2. The contract specification is not explicit in the test.
12 // A property-based test does the iteration implicitly and solves these problems:
14 property ("test get contract (PBT)") =
   forAll { (oa: Option[Int]) => // <-- quantifier</pre>
     !oa.isEmpty ==>
                                  // <-- pre-condition (implication)</pre>
16
       Some(get(oa)) == oa }
// <-- post-condition</pre>
17
19 // An explicit contract; 100 different tests without test case tables and iterations
```

Homework / Exercises

- The goal is to **test our lazy list library**
- We invert the situation from previous weeks: assume that the type (LazyList) is implemented, you write the test file
- The build system is set up with the testing library, and 3 example tests
- There is even an **example generator** of lazy lists
- Add more tests, and possibly more generators
- There must be **several property-based tests** (PBT) in your solution to pass. The rules are explained in the Exercise file (slightly different than other weeks)

Resources on ScalaCheck

- ScalaCheck: https://github.com/typelevel/scalacheck/blob/main/doc/UserGuide.md
- Gen, a key type: https: //javadoc.io/doc/org.scalacheck/scalacheck_3/1.17.0/org/scalacheck/Gen.html
- Arbitrary, a key type: https://javadoc.io/doc/org.scalacheck/scalacheck_3/1.17.0/ org/scalacheck/Arbitrary.html.
- I also find source code at https://github.com/typelevel/scalasheck/blob/v1.17.0/core/shared/src/main/scala/org/scalacheck/Gen.scala useful to read (actually I read it more often than the docs).
- Additionally, next week we study the design of Prop and Gen, to deepen understanding (you can start reading Ch. 8)

Further reading: Blogs! (Read one for context)

- C++: couldn't find a nice blog post; read the user guide of rapidcheck if C++ is your fare: https://github.com/emil-e/rapidcheck/blob/master/doc/user_guide.md
- C#: https://www.codit.eu/blog/property-based-testing-with-c/ with https://fscheck.github.io/FsCheck/
- **F#**: https://www.codit.eu/blog/practically-property-based-testing-your-strict-domain-model-in-f-c/using https://fscheck.github.io/FsCheck/
- Go: https://earthly.dev/blog/property-based-testing/ uses a small CSV file manipulation tool as an example
- Haskell: https://www.fpcomplete.com/blog/2017/01/quickcheck/ with Quickcheck, of course!
- Java: https://yoan-thirion.medium.com/improve-your-software-quality-with-property-based-testing-70bd5ad9a09a with junit-quickcheck. There is also https://jqwik.net which seems to be a rich library used also in Kotlin and Groovy
- JavaScript/TypeScript:

 $https://mokkapps.de/blog/property-based-testing-with-type-script \\ using \\ https://github.com/dubzzz/fast-checkapps.de/blog/property-based-testing-with-type-script \\ using \\ https://github.com/dubzz/fast-checkapps.de/blog/property-based-testing-with-type-script \\ using \\ https://github.com/dubzz/fast-checkapps.de/blog/property-based-testing-with-type-script \\ https://github.com/dubzz/fast-checkapps.de/blog/property-based-testing-with-type-script \\ https://github.com/dubzz/fast-checkapps.de/blog/property-based-testing-test$

- Kotlin: https://instil.co/blog/from-tdd-to-pbt-via-kotest/
 Uses https://kotest.io which apparently also runs on non-jvm tool chains of Kotlin.
- Python: https://medium.com/clarityai-engineering/ property-based-testing-a-practical-approach-in-python-with-hypothesis-and-pandas-6082d737c3ee and https://datascience.blog.wzb.eu/2019/11/08/property-based-testing-for-scientific-code-in-python/, the latter with more data-science angle, both using Hypothesis.
- Rust: with https://blog.auxon.io/2021/02/01/effective-property-based-testing/ with proptest, and https://dev.to/itminds/introduction-to-property-based-testing-via-rust-3h6f with quickcheck
- Scala: https://medium.com/analytics-vidhya/property-based-testing-scalatest-scalacheck-52261a2b5c2c, shows how to PBT within ScalaTest (the unit testing framework for Scala)