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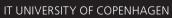
Advanced Programming

Algebraic Data Types





SOFTWARE



- Algebraic Data Types
- Functional lists and trees
- Fold functions
- Style guidelines for functional programming in ADPRO



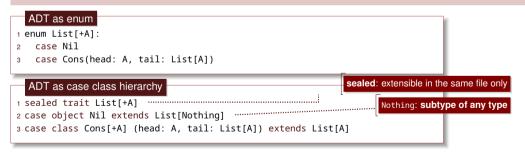
Algebraic Data Types (ADTs) as Enums and Classes

Enums less general, but used more often

Def. Algebraic Data Type

A type generated by one or more constructors, each taking zero or more arguments.

The sets of objects generated by each constructor are **summed** (unioned), each constructor can be seen as a representation of a Cartesian **product** (tuple) of its arguments; thus the name **algebraic**.



Algebraic Data Types (ADTs)

Def. Algebraic Data Type

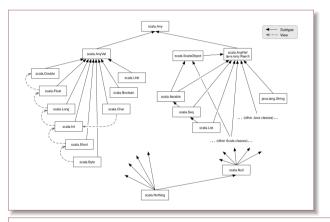
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```
Example: lists
 enum List[+A]:
   case Nil
   case Cons(head: A. tail: List[A])
 operations on lists
                                                                                       companion object of List[+A]
1 object List: .....
   def sum(ints: List[Int]): Int = ints match
                                                                             pattern matching against case constructors
     case Nil \Rightarrow 0
     case Cons(xxs) \Rightarrow x + sum(xs)
   def apply[A] (as: A*): List[A] =
                                                                        overloading function application for the object
     if as.isEmpty then Nil
     else Cons(as.head, apply(as.tail*))
                                                                                                   variadic function
```

Lists are covariant

All share the same tail!



For any type A we have that

Nil <:List[Nothing] <:List[A]</pre>

```
1 sealed trait List[+A]
```

- 2 case object Nil extends List[Nothing]
- 3 case class Cons[+A] (head: A, tail: List[A]) extends List[A]

Poll: How is your recursion?

Mentimeter: 3473 1775

```
1 def f (a: List[Int]): Int = a match
  case Nil => 0
  case Cons(h, t) \Rightarrow h + f(t)
```

What is f(List(42, -1, 1, -1, 1, -1))?



Function Values

- In functional programing functions are values
- Functions can be **passed to other functions**, composed, etc.
- Functions operating on function values are higher order (HOFs)

```
def map(a: List[Int])(f: Int => Int): List[Int] = a match
 case Nil => Nil
 case Cons(h, tail) => Cons(f(h), map(tail)(f))
```

A functional (pure) example

```
val mixed = List(-1, 2, -3, 4)
```

- map(mixed)(abs)
- map(mixed)((factorial) compose (abs))

```
An imperative (impure) example
```

- val mixed = Array(-1, 2, -3, 4)
- for i <- 0 until mixed.length do
- mixed(i) = abs(mixed(i))

```
val mixed1 = Array(-1, 2, -3, 4)
```

- for i <- 0 until mixed1.length do
- mixed1(i) = factorial(abs(mixed1(i)))

Parametric Polymorphism

Monomorphic functions operate on fixed types:

A monomorphic map in Scala def map(a: List[Int])(f: Int => Int): List[Int] = a match case Nil => Nil case Cons(h, tail) => Cons(f(h), map(tail)(f))

There is nothing specific here regarding Int.

```
A polymorphic map in Scala
def map[A, B](a: List[A])(f: A \Rightarrow B): List[B] = a match
  case Nil => Nil
  case Cons(h, tail) => Cons(f(h), map(tail)(f))
```

An example of use:

```
1 map[Int, String] (mixed) {
  (_.toString) compose (factorial) compose (abs) }
```

- A polymorphic function operates on values of (m)anv types
- A polymorphic type constructor defines a parameterized family of types
- Don't confuse with inheritance-based polymorphism AKA "dynamic dispatch"

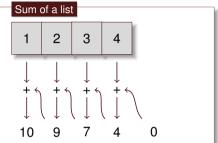
HOFs in the Standard Library

Methods of class List[A], operate on this list, type A is bound in the class

More at https://www.scala-lang.org/api/current/scala/collection/immutable/List.html

```
map[B](f: A => B): List[B]
Translate this list of As into a list of Bs using f to convert the values
filter(p: A =>Boolean): List[A]
A sublist of this containing elements satisfying predicate p
flatMap[B](f: A =>List[B]): List[B]
                                                                *type slightly simplified
Apply f to elements of this and concatenate the produced lists
take(n: Int): List[A]
A list of first n elements of this.
takeWhile(p: A =>Boolean): List[A]
A prefix of this containing elements satisfying p
forall(p: A =>Boolean): Boolean
True iff p holds for all elements of this
exists(p: A =>Boolean): Boolean
True iff p holds for at least one element of this
```

Folds: Functional Loops



```
What characterizes folds?
```

- An input list 1 = List(1,2,3,4)
- An initial value z = 0
- A binary operation f: (Int,Int) => Int = _ + _
- An iteration algorithm

```
def foldRight[A,B](f: (A,B) \Rightarrow B(z: B)(1: List[A]): B =
      1 match
        case Cons(x, xs) \Rightarrow f(x, foldRight(f)(z)(xs))
        case Nil => z
    val 11 = List(1,2,3,4,5,6)
    val sum = foldRight[Int,Int](_+_)(0)(11)
    val product = foldRight[Int,Int](_*_)(1)(11)
    def map[A,B] (f: A \Rightarrow B) (1: List[A]): List[B] =
      foldRight[A,List[B]]((x, z) \Rightarrow Cons(f(x), z))(Nil)(1)
10
```

Many HOFs are special cases of folding

Preferred Programming Style in ADPRO

Always choose the best possible style for an exercise and your abilities

Condemned (fail)	ightarrow Forgivable (medium grade*) $ ightarrow$	Enlightened (top grade)
variables < assignments < return statement < Any/Object type <		< values < value bindings < expression value < parametric polymorphism
loops <	tail recursion* < simple recursion < folds* if conditions < pattern matching*	< compose dedicated HOFs
exceptions <	,	< Option or Either monad

^{*} unless asked for explicitly, or really important for memory use.

Scala: Summarv

- **Basics** (objects, modules, functions, expressions, values, variables, operator overloading, infix methods, interpolated strings.)
- Pure functions (referential transparency, side effects)
- **Loops and recursion** (tail recursion)
- **Functions as values** (higher-order functions)
- Parametric polymorphism (monomorphic functions, dynamic and static dispatch)
- Standard HOFs in Scala's library
- **Anonymous functions** (currying, partial function application)
- Traits (fat interfaces, multiple inheritance, mixins)
- Algebraic Data Types (pattern matching, case classes)
- Folding