

$$g) \quad p_r = m \dot{r} = m \frac{d\sqrt{x^2 + y^2}}{dt}$$

$$\vec{r}_0 = (r_0 \cos \phi, r_0 \sin \phi)$$

$$\vec{V}_0 = (\dot{x}, \dot{y}) = (V_0 \cos \theta_0, V_0 \sin \theta_0)$$

$$\tilde{p}_{r_0} = \frac{p_{r_0}}{m d} = \frac{dr_0}{dt} \frac{1}{d} = \frac{x_0 \dot{x}_0 + y_0 \dot{y}_0}{r_0 d}$$

$$= \frac{r_0 (\cos \phi_0 \boxed{V_0} \cos \theta_0 + \sin \phi_0 \boxed{V_0} \sin \theta_0)}{r_0 d}$$

$$= \tilde{V}_0 (\cos(\phi_0) \cos(\theta_0) + \sin(\phi_0) \sin(\theta_0)) = \tilde{V}_0 \cos(\theta_0 - \phi_0)$$

Para ϕ :

$$\frac{d\phi}{dt} = \frac{d(\arctan(x/y))}{dt} \Rightarrow m r^2 \frac{d\phi}{dt} = p_\phi$$

$$p_\phi = m r^2 \frac{d(\arctan(x/y))}{dt}$$

$$\tilde{p}_{\phi_0} = \frac{p_{\phi_0}}{m d^2} = \frac{m r_0^2}{m d^2} \dot{\phi} = \frac{\tilde{r}_0^2}{r_0^2} \frac{1}{1 + \left(\frac{y_0}{x_0}\right)^2} \frac{d\left(\frac{y_0}{x_0}\right)}{dt}$$

$$= \frac{\tilde{r}_0^2}{r_0^2} \frac{1}{x_0^2 + y_0^2} (\dot{y}x - \dot{x}y) = \frac{\tilde{r}_0^2}{r_0^2} (\dot{y}x - \dot{x}y)$$

$$= \frac{1}{d^2} (V_0 r_0 \sin \theta_0 \cos \phi_0 - V_0 r_0 \cos \theta_0 \sin \phi_0)$$

$$= \tilde{V}_0 \tilde{r}_0 (\sin \theta_0 \cos \phi_0 - \cos \theta_0 \sin \phi_0) = \tilde{V}_0 \tilde{r}_0 \sin(\theta_0 - \phi_0)$$