based clustering?

A. the entropy function

B. the squared error function



| Course    | Name:     | Mach  | ine Lea     | rning (H   | <del>1</del> ) | Exam        | Duratio       | n:        | 2 hou      | rs     |
|-----------|-----------|---|-------------|------------|----------------|-------------|---------------|-----------|------------|--------|
| Dept.:    | Depar     | tment o   | f Comp      | uter Sc    | ience aı       | nd Engi     | neering       |           |            |        |
| Exam Pa   | aner Se   | tter/Sig  | nature).    | •          |                |             |               |           |            |        |
| LX        | арсі Ос   | itor (Oig   | ilatai o).  |            |                |             |               |           |            |        |
| Question  |           |   | _           | 4          | _              |             | 7             | 0         | 0          | 10     |
| No.       | 1         | 2   | 3           | 4          | 5              | 6           | 7             | 8         | 9          | 10     |
| Score     | 20        | 40  | 40          | 10         |                |             |               |           |            |        |
| This exar | n paper   | contains  | _4_ que     | estions a  | nd the s       | core is _   | <u>110</u> ir | total. (F | lease ha   | and in |
| your exar | n paper.  | answer s  | sheet, an   | d vour so  | rap pape       | er to the r | proctor w     | hen the e | exam end   | ls.)   |
| you. ona. | раро.,    |   |             | a          | . op popo      |             |               |           |            | ,      |
| Proble    | m I Mı    | ultiple   | Choice      | e (20 Pc   | oints)         |             |               |           |            |        |
| (only one |           | _   |             | -          | ,              |             |               |           |            |        |
| 1. (2 pc  | oints) Th | ree essen   | tial comp   | ponents o  | of a learn     | ing syste   | m are         | ·         |            |        |
|           | A. mod    | el, gradie  | ent desce   | nt, learni | ng algori      | thm         |               |           |            |        |
|           | B. erro   | r function  | , model,    | learning   | algorith       | n           |               |           |            |        |
|           | C. accu   | racy, sen   | sitivity, s | pecificity | y              |             |               |           |            |        |
|           | D. mod    | el, error f   | function,   | cost fund  | ction          |             |               |           |            |        |
| 2. (2 pc  | oints) Th | e objecti   | ve of ma    | chine lea  | rning is t     | o minimi    | ze            | _•        |            |        |
|           | A. the l  | KL diverg   | gence bet   | ween rea   | l-world d      | lata and t  | he traine     | d probab  | ilistic mo | odel   |
|           | B. the l  | the KL divergence between training data and the trained probabilistic model |             |            |                |             |               |           |            |        |
|           | C. the l  | the KL divergence between real-world data and training data                 |             |            |                |             |               |           |            |        |
|           | D. the I  | KL diverg   | gence bet   | ween trai  | ning data      | a and pre   | diction d     | ata       |            |        |
| 3. (2 pc  | oints) W  | hat is the  | loss fund   | ction mos  | st suited t    | or linear   | regressi      | on?       |            |        |
| _         |           | entropy fu  |             |            | ot Builder     | or inicar   | regressi      | on.       |            |        |
|           |           | squared e   |             | tion       |                |             |               |           |            |        |
|           |           | cross-entr  |             |            |                |             |               |           |            |        |
|           |           | number of   |             |            |                |             |               |           |            |        |
|           |           |   |             |            |                |             |               |           |            |        |
| 4. (2 pc  | oints) W  | hat is the  | loss fund   | ction mos  | st suited f    | for proba   | bilistic d    | ensity mi | xture mo   | odel   |

|     | C.       | the likelihood function of complete data   |
|-----|----------|--|
|     | D.       | the likelihood function of incomplete data                                       |
| 5.  | (2 point | ts) The differences between the generative and discriminative approaches include |
|     | A.       | that the former has less parameters  |
|     | B.       | that the former cannot add a new class   |
|     | C.       | that the latter emphasizes the boundary among classes                            |
|     | D.       | that the latter can be trained faster  |
| 6.  | (2 poin  | ts) Neural networks can NOT be regularized by using                              |
|     | A.       | using a prior on model parameters  |
|     | B.       | data augmentation  |
|     | C.       | node dropping out  |
|     | D.       | ReLU activation  |
| 7.  | (2 point | ts) The advantages of the hidden Markov model DO NOT include                     |
|     | A.       | global convergence   |
|     | B.       | fast estimation algorithm  |
|     | C.       | unsupervised learning  |
|     | D.       | capability of modeling both continuous and discrete data                         |
| 8.  | (2 poin  | ts) The advantages of using ReLU as activation functions DO NOT include          |
|     | A.       | reducing gradient vanishing  |
|     | В.       | reducing gradient explosion  |
|     | C.       | encouraging model sparsity   |
|     | D.       | increasing computational efficiency  |
| 9.  | (2 point | ts) Which of the following is NOT a way to reduce the model overfitting?         |
|     | A.       | increase the amount of training data   |
|     | B.       | improve the optimization algorithm being used for error minimization             |
|     | C.       | decrease the model complexity  |
|     | D.       | reduce the noise in the training data  |
| 10. | (2 point | ts) Which of the following statements is NOT true for Bellman equations?         |
|     | A.       | it can be used to estimate state value functions                                 |
|     | B.       | it is can be solved by using dynamic programing, Monti Carlo, and temporal       |
|     |          | difference approaches  |
|     | C.       | solving Bellman equation requires environment models                             |
|     | D.       | its fixed point is the optimal policy  |

## **Problem II Numerical Calculation (40 Points)**

- (1) **Linear Regression (5 points)**. For three points  $\{(1, 4), (2, 8), (3, 14)\}$ , what is the linear regression function for the least squared errors (assuming  $y = a_2x^2 + a_1x + a_0$ )?
- (2) **Supervised Classification (5 points)**. For class A of two points  $\{(1, 2) (2, 1)\}$  and class B of two points  $\{(4, 1) (3, 4)\}$ , what are the labels for points  $\{(2,2) (3,3)\}$  using the K-NN algorithm (*where K*=3)?
- (3) **Maximum margin classifier (5 points)**. For one class of two points {(1, 2) (2, 2)} and another class of two points {(4, 4) (5, 6)}, what are the support vectors and what is the decision boundary's function (*plot your answer*)?
- (4) **Clustering** (**5 points**). For four points with two classes, {(1, 2) (2, 2) (4, 4) (5, 6)}, how to achieve two cluster centers using the K-means algorithm (*outline the algorithm and show the details of one iteration*)?
- (5) **Factor Graph** (10 points). How to design a factor graph to solve the following linear Gaussian system:  $[3\ 3]^T = [1\ 1\ 1;\ 0\ 2\ 1][x_1\ x_2\ x_3]^T$ ? Assuming the initial Gaussian distributions of X is  $\{[m_1,\ \sigma_1],\ [m_2,\ \sigma_2],\ [m_3,\ \sigma_3]\}$ , outline the whole computation procedure and show the details of one iteration.
- (6) **Hidden Markov Model (10 points)**. For a HMM, the states of latent variables are {bull, bear}, the states of observation variables are {rise, fall}, the initial state probability distribution  $\pi$  is  $[0.5 \ 0.5]^T$ , the transition probability distribution A is  $[0.4 \ 0.7; \ 0.6 \ 0.3]$ , and the observation probability distribution B is  $[0.8 \ 0.1; 0.2 \ 0.9]$ . If the observation sequence X is {fall fall rise}, please show the computation procedure for  $p(z_1|X, \theta)$  and  $p(z_1, z_2|X, \theta)$  using the forward-backward algorithm, where  $z_n$  is the latent variable at time n and  $\theta = {\pi, A, B}$ ?

## **Problem III Theoretical Analysis (40 Points)**

- (1) What is the EM procedure? When do we need the EM procedure for machine learning? Please give a specific example.
- (2) What is the EM procedure in terms of the Q function? Please give the detailed equations assuming that X is the observed variable, Z is the latent variable and  $\theta$  is the model parameter.
- (3) What is the EM procedure in terms of likelihood and KL divergence? Please give the detailed equations and plots to illustrate the procedure.
- (4) What is the EM procedure in terms of optimization of non-convex function? Please give a plot to illustrate the procedure.
- (5) What is the EM procedure for the factor graph network model? Please give an example.

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## **Problem IV Reinforcement Learning (Bonus 10 Points)**

- (1) What is the Bellman equation? How to solve the Bellman equation?
- (2) What are the differences between policy iteration and value iteration? What are their advantages and disadvantages respectively?
- (3) What is the model-free reinforcement learning? How to achieve the mode-free reinforcement learning? Please use specific examples to illustrate your points.
- (4) What are the differences between on-line and off-line RL? What are their advantages and disadvantages respectively? Please use specific examples to illustrate your points.
- (5) What are the differences between on-policy and off-policy RL? What are their advantages and disadvantages respectively? Please use specific examples to illustrate your points.