

# trace of $\Gamma$ -matrices

$$\text{tr}(\Gamma^1 \Gamma^2 \Gamma^3 \Gamma^4 \Gamma^5 \Gamma^6 \Gamma^7 \Gamma^8) \quad \text{tr}(A^1 a^2 A^3 a^4 A^5 a^6 A^7 a^8)$$

possible terms from contractions

$$\text{I. } a^4 \text{tr}(A_\mu A^\mu A_\nu A^\nu)$$

$$\text{II. } a^4 \text{tr}(A_\mu A_\nu A^\mu A^\nu)$$

$$\text{III. } a^2 \text{tr}(A_\mu a \cdot A A^\mu a \cdot A)$$

$$\text{IV. } a^2 \text{tr}(A_\mu A^\mu a \cdot A a \cdot A)$$

$$\text{V. } \text{tr}(a \cdot A a \cdot A a \cdot A a \cdot A)$$

look at III.

all possible  
contractions

$$+ \begin{array}{c} A a A a A a A a \\ \underbrace{\hspace{1.5cm}} \end{array} + \begin{array}{c} A a A a A a A a \\ \underbrace{\hspace{1.5cm}} \end{array}$$

$$- \begin{array}{c} A a A a A a A a \\ \underbrace{\hspace{1.5cm}} \end{array} - \begin{array}{c} A a A a A a A a \\ \underbrace{\hspace{1.5cm}} \end{array}$$

$$- \begin{array}{c} A a A a A a A a \\ \underbrace{\hspace{1.5cm}} \end{array} - \begin{array}{c} A a A a A a A a \\ \underbrace{\hspace{1.5cm}} \end{array}$$

$$+ \begin{array}{c} A a A a A a A a \\ \underbrace{\hspace{1.5cm}} \end{array} + \begin{array}{c} A a A a A a A a \\ \underbrace{\hspace{1.5cm}} \end{array}$$

$$+ \begin{array}{c} A a A a A a A a \\ \underbrace{\hspace{1.5cm}} \end{array} - \begin{array}{c} A a A a A a A a \\ \underbrace{\hspace{1.5cm}} \end{array}$$

$$+ \begin{array}{c} A a A a A a A a \\ \underbrace{\hspace{1.5cm}} \end{array} - \begin{array}{c} A a A a A a A a \\ \underbrace{\hspace{1.5cm}} \end{array}$$

$$A a A a A a A a$$

same as above