1

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```

1 Basic

1.1 Default code

```
#include<bits/stdc++.h>
#define int long long
#define mod 1000000007
#define endl '\n'
#define pii pair<int,int>
using namespace std;

signed main(){
  ios::sync_with_stdio(0),cin.tie(0);
}
```

1.2 Linux 對拍

```
for ((i=0;i<300;i++))
do
    echo "$i"
    python gen.py > input
    ./ac < input > ac.out
    ./wa < input > wa.out
    diff ac.out wa.out || break
done
```

1.3 Windows 對拍

```
@echo off
:loop
    echo %%x
    python gen.py > input
    ./ac.exe < input > ac.out
    ./wa.exe < input > wa.out
    fc ac.out wa.out
if not errorlevel 1 goto loop
```

1.4 builtin 函數

```
// 右邊第一個 1 的位置
int __builtin_ffs(unsigned int);
int __builtin_ffsl(unsigned long);
int __builtin_ffsll(unsigned long long);
// 左邊第一個 1 之前 0 的數量
int __builtin_clz(unsigned int);
int __builtin_clzl(unsigned long);
int __builtin_clzll(unsigned long long);
// 右邊第一個 1 之後 0 的數量
int __builtin_ctz(unsigned int);
int __builtin_ctzl(unsigned long);
int __builtin_ctzll(unsigned long long);
// 1 的數量
int __builtin_popcount(unsigned int);
int __builtin_popcountl(unsigned long);
int __builtin_popcountll(unsigned long long);
// 1 的數量 mod 2
int __builtin_parity(unsigned int);
int __builtin_parityl(unsigned long);
int __builtin_parityll(unsigned long long);
// 二進制表示數字
int a = 0b101101;
```

1.5 輸入輸出

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```
// 開讀檔
fropen("input_file_name","r",stdin);
fropen("output_file_name","w",stdout);
```

1.6 Python 輸入輸出

```
a = list(map(int,input().split()))
# 開讀檔
import sys, os.path
if(os.path.exists('input_file.txt')):
    sys.stdin = open("input_file.txt","r")
    sys.stdout = open("output_file.txt","w")
```

2 Data Structure

2.1 Link-Cut Tree

```
struct Splay {
    static Splay nil, mem[MEM], *pmem;
    Splay *ch[2], *f;
    int val, rev, size;
    Splay (int _val=-1) : val(_val), rev(0), size(1)
    { f = ch[0] = ch[1] = &nil; }
    bool isr()
    { return f->ch[0] != this && f->ch[1] != this; }
    int dir()
    { return f->ch[0] == this ? 0 : 1; }
    void setCh(Splay *c, int d){
        ch[d] = c;
        if (c != &nil) c->f = this;
        pull();
    }
```

```
void push(){
  if( !rev ) return;
    swap(ch[0], ch[1]);
if (ch[0] != &nil) ch[0]->rev ^= 1;
if (ch[1] != &nil) ch[1]->rev ^= 1;
    rev=0;
  void pull(){
    size = ch[0] -> size + ch[1] -> size + 1;
    if (ch[0] != &nil) ch[0]->f = this;
    if (ch[1] != &nil) ch[1]->f = this;
} Splay::nil, Splay::mem[MEM], *Splay::pmem = Splay::
    mem;
Splay *nil = &Splay::nil;
void rotate(Splay *x){
  Splay *p = x->f;
int d = x->dir();
  if (!p->isr()) p->f->setCh(x, p->dir());
  else x->f = p->f
  p->setCh(x->ch[!d], d);
  x->setCh(p, !d);
  p->pull(); x->pull();
vector<Splay*> splayVec;
void splay(Splay *x){
  splayVec.clear();
  for (Splay *q=x;; q=q->f){
    splayVec.push_back(q);
    if (q->isr()) break;
  reverse(begin(splayVec), end(splayVec));
  for (auto it : splayVec) it->push();
  while (!x->isr()) {
    if (x->f->isr()) rotate(x);
    else if (x->dir()==x->f->dir())
      rotate(x->f),rotate(x);
    else rotate(x),rotate(x);
 }
int id(Splay *x) { return x - Splay::mem + 1; }
Splay* access(Splay *x){
  Splay *q = nil;
for (;x!=nil;x=x->f){
    splay(x)
    x - setCh(q, 1);
    q = x;
  }
  return q;
void chroot(Splay *x){
  access(x);
  splay(x);
  x\rightarrow rev ^= 1;
  x->push(); x->pull();
void link(Splay *x, Splay *y){
  access(x);
  splay(x);
  chroot(y);
  x - setCh(y, 1);
void cut_p(Splay *y) {
  access(y);
  splay(y);
  y->push();
  y - ch[0] = y - ch[0] - f = nil;
void cut(Splay *x, Splay *y){
  chroot(x);
  cut_p(y);
Splay* get_root(Splay *x) {
  access(x);
  for(; x \rightarrow ch[0] != nil; x = x \rightarrow ch[0])
    x->push();
  splay(x);
  return x;
bool conn(Splay *x, Splay *y) {
 x = get_root(x);
```

```
y = get_root(y);
  return x == y;
Splay* lca(Splay *x, Splay *y) {
  access(x);
  access(y);
  splay(x);
  if (x->f == nil) return x;
  else return x->f;
```

持久化線段樹 2.2

2.3

```
Treap
struct Treap {
    struct Node {
         int k, p, sz = 1;
        Node *l = 0, *r = 0;
        bool tag = 0;
        Node(int kk) {
             k = kk;
             p = rand();
    Node *root = 0;
    int size(Node *x) {return x ? x->sz : 0;}
    void push(Node *x) {
         if(x->tag) {
             if(x->1) x->1->tag ^= true;
             if(x->r) x->r->tag ^= true;
             x->tag = false;
        }
    void pull(Node* x) {
         x \rightarrow sz = size(x \rightarrow l) + size(x \rightarrow r) + 1;
    Node* merge(Node *a, Node *b) {
         if(!a | | !b) return a ?: b;
         if(a->p > b->p) {
             push(a);
             a \rightarrow r = merge(a \rightarrow r, b);
             pull(a);
             return a;
        else{
             push(b);
             b->1 = merge(a, b->1);
             pull(b);
             return b;
    void splitKey(Node* x, int k, Node *&a, Node *&b) {
         if(!x) \{a = b = 0; return;\}
        push(x);
         if(x->k \ll k) {
             a = x
             splitKey(a->r, k, a->r, b);
             pull(a);
        else{
             splitKey(b->l, k, a, b->l);
             pull(b);
    void splitKth(Node *x, int k, Node *&a, Node *&b) {
         if(!x) \{a = b = 0; return;\}
        push(x)
         if(size(x->1) < k) {
             splitKth(a->r, k - size(x->l) - 1, a->r, b)
             pull(a);
         else{
             splitKth(b->l, k, a, b->l);
             pull(b);
        }
    }
```

3

```
NTOU owo
     void insert(int id) {
   Node *1, *r;
                                                                        int v, f, re;
         splitKey(root, id, l, r);
Node *m = new Node(id);
                                                                      vector<vector<Edge>> E;
                                                                      vector<int> level;
         root = merge(l, merge(m, r));
                                                                      int n, s, t;
                                                                      Dinic(int nn, int ss, int tt) {
    void erase(int x) {
   Node *a, *b, *c;
                                                                        n = nn; s = ss; t = tt;
                                                                        E.resize(n);
         splitKey(root, x, b, c);
splitKey(b, x - 1, a, b);
                                                                        level.resize(n);
                                                                      void addEdge(int u, int v, int w) {
    E[u].push_back({v, w, SZ(E[v])});
         root = merge(a, c);
};
                                                                        E[v].push\_back({u, 0, SZ(E[u]) - 1});
2.4 線段樹
                                                                      bool bfs() {
                                                                        level.assign(n, 0);
                                                                        queue<int> q;
struct Seg{
     vector<int> seg,tag;
                                                                        q.push(s);
     #define cl (i << 1)+1
                                                                        level[s] = 1;
                                                                        while(!q.empty()) {
  int u = q.front(); q.pop();
    #define cr (i<<1)+2
void push(int i,int l,int r){</pre>
         if(tag[i]!=0){
                                                                           for(auto& it : E[u]) {
                                                                             int v = it.v;
if(it.f > 0 && !level[v]) {
              seg[i]+=tag[i]; // update by tag
              if(l!=r){
                   tag[cl]+=tag[i]; // push
                                                                               level[v] = level[u] + 1;
                   tag[cr]+=tag[i]; // push
                                                                               q.push(v);
              tag[i]=0;
                                                                          }
         }
                                                                        return level[t];
     void pull(int i,int l,int r){
         int mid=(l+r)>>1;
                                                                      int dfs(int u, int nf) {
         push(cl,l,mid);push(cr,mid+1,r);
                                                                        if(u == t) return nf;
         seg[i]=max(seg[cl],seg[cr]); // pull
                                                                        int ret = 0:
                                                                        for(auto& it : E[u]) {
     void build(int i,int l,int r,vector<int>&arr){
                                                                           int v = it.v;
                                                                           if(it.f > 0 && level[v] == level[u] + 1) {
         if(l==r){
              seg[i]=arr[l]; // set value
                                                                             int tem = dfs(v, min(nf, it.f));
              return;
                                                                             ret += tem; nf -= tem;
                                                                             it.f -= tem; E[v][it.re].f += tem;
         int mid=(l+r)>>1;
                                                                             if(!nf) return ret;
         build(cl,l,mid,arr);
                                                                          }
         build(cr,mid+1,r,arr);
         pull(i,l,r);
                                                                        if(!ret) level[u] = 0;
                                                                        return ret;
     Seg(vector<int>& arr){
                                                                      int flow() {
         seq.resize(arr.size()*4);
         tag.resize(arr.size()*4)
                                                                        int ret = 0;
         build(0,0,arr.size()-1,arr);
                                                                        while(bfs()) ret += dfs(s, 0x3f3f3f3f);
                                                                        return ret;
     void update(int i,int l,int r,int nl,int nr,int x){
         push(i,l,r);
                                                                   };
         if(nl<=l&&r<=nr){</pre>
                                                                           匈牙利
              tag[i]+=x;
                                                                    3.2
              return;
                                                                   #define NIL -1
                                                                   #define INF 100000000
         int mid=(l+r)>>1;
         if(nl<=mid) update(cl,l,mid,nl,nr,x);</pre>
                                                                   int n,matched;
         if(nr>mid) update(cr,mid+1,r,nl,nr,x);
                                                                    int cost[MAXN][MAXN];
         pull(i,l,r);
                                                                   bool sets[MAXN]; // whether x is in set S
                                                                   bool sets[MAXN]; // whether y is in set S bool sett[MAXN]; // whether y is in set T int xlabel[MAXN], ylabel[MAXN]; int xy[MAXN], ymatched with whom
     int query(int i,int l,int r,int nl,int nr){
         push(i,1,r);
          if(nl \le l\&r \le nr){
                                                                   int slack[MAXN]; // given y: min{xlabel[x]+ylabel[y]-
                                                                   cost[x][y]} | x not in S
int prev[MAXN]; // for augmenting matching
              return seg[i];
         int mid=(l+r)>>1;
                                                                   inline void relabel() {
                                                                      int i,delta=INF
         if(nl<=mid) ans=max(ans,query(cl,l,mid,nl,nr));</pre>
                                                                      for(i=0;i<n;i++) if(!sett[i]) delta=min(slack[i],</pre>
         if(nr>mid) ans=max(ans,query(cr,mid+1,r,nl,nr))
                                                                           delta);
                                                                      for(i=0;i<n;i++) if(sets[i]) xlabel[i]-=delta;</pre>
         return ans;
                                                                      for(i=0;i<n;i++) {</pre>
    }
                                                                        if(sett[i]) ylabel[i]+=delta;
};
                                                                        else slack[i]-=delta;
     Flow
                                                                   inline void add_sets(int x) {
3.1 Dinic
                                                                      int i:
                                                                      sets[x]=1;
struct Dinic {
                                                                      for(i=0;i<n;i++) {</pre>
                                                                        if(xlabel[x]+ylabel[i]-cost[x][i]<slack[i]) {</pre>
  #define SZ(x) (int)(x.size())
```

slack[i]=xlabel[x]+ylabel[i]-cost[x][i];

struct Edge {

```
for(int x=1; x<=n; ++x) for(int y=1; y<=n; ++y)
    lx[x] = max(lx[x], g[x][y]);</pre>
       prev[i]=x;
  }
                                                                           for(int x=1; x<=n; ++x) bfs(x);</pre>
                                                                           11 \text{ ans} = 0;
                                                                           for(int y=1; y<=n; ++y) ans += g[my[y]][y];
inline void augment(int final) {
  int x=prev[final],y=final,tmp;
                                                                           return ans;
  matched++;
                                                                     } }graph;
  while(1) {
    tmp=xy[x]; xy[x]=y; yx[y]=x; y=tmp;
if(y==NIL) return;
                                                                      3.4 MCMF
                                                                      struct MCMF {
    x=prev[y];
                                                                           #define SZ(x) (int)(x.size())
                                                                           struct Edge {
inline void phase() {
                                                                                int v, f, re, c;
  int i,y,root;
  for(i=0;i<n;i++) { sets[i]=sett[i]=0; slack[i]=INF; }</pre>
                                                                           vector<vector<Edge>> E;
  for(root=0;root<n&xy[root]!=NIL;root++);</pre>
                                                                           vector<int> dis, x, y;
                                                                           int n, s, t;
  add_sets(root);
  while(1) {
                                                                           MCMF(int nn, int ss, int tt) {
    relabel();
                                                                               n = nn; s = ss; t = tt;
    for(y=0;y<n;y++) if(!sett[y]&&slack[y]==0) break;</pre>
                                                                                E.resize(n);
    if(yx[y]==NIL) { augment(y); return; }
                                                                                x.resize(n);
                                                                               y.resize(n);
    else { add_sets(yx[y]); sett[y]=1; }
                                                                           void addEdge(int u, int v, int w, int c) {
    E[u].push_back({v, w, SZ(E[v]), c});
    E[v].push_back({u, 0, SZ(E[u]) - 1, -c});
inline int hungarian() {
  int i,j,c=0;
  for(i=0;i<n;i++) {</pre>
                                                                           bool spfa() {
    xy[i]=yx[i]=NIL;
    xlabel[i]=ylabel[i]=0;
                                                                                dis.assign(n, 0x3f3f3f3f);
    for(j=0;j<n;j++) xlabel[i]=max(cost[i][j],xlabel[i</pre>
                                                                                x.assign(n, -1);
                                                                                y.assign(n, -1);
                                                                                vector<bool> inq(n, false);
                                                                                queue<int> q;
  for(i=0;i<n;i++) phase();</pre>
  for(i=0;i<n;i++) c+=cost[i][xy[i]];</pre>
                                                                                q.push(s);
                                                                               inq[s] = true;
dis[s] = 0;
  return c;
                                                                                while(q.size()) {
                                                                                    int u = q.front(); q.pop();
3.3 KM
                                                                                    inq[u] = false;
                                                                                     for(int i = 0; i < E[u].size(); i++) {</pre>
struct KM{ // max weight, for min negate the weights
  int n, mx[MXN], my[MXN], pa[MXN];
ll g[MXN][MXN], lx[MXN], ly[MXN], sy[MXN];
                                                                                         auto& it = E[u][i];
                                                                                         int v = it.v;
  bool vx[MXN], vy[MXN];
void init(int _n) { // 1-based
                                                                                         if(it.f > 0 && dis[v] > dis[u] + it.c)
    n = _n;
for(int i=1; i<=n; i++) fill(g[i], g[i]+n+1, 0);</pre>
                                                                                              dis[v] = dis[u] + it.c;
                                                                                              x[v] = u;
y[v] = i;
                                                                                              if(!inq[v]) {
  void addEdge(int x, int y, ll w) \{g[x][y] = w;\}
                                                                                                   q.push(v);
  void augment(int y) {
    for(int x, z; y; y = z)
x=pa[y], z=mx[x], my[y]=x, mx[x]=y;
                                                                                                   inq[v] = true;
                                                                                              }
                                                                                         }
                                                                                    }
  void bfs(int st) {
    for(int i=1; i<=n; ++i) sy[i]=INF, vx[i]=vy[i]=0;</pre>
                                                                                return x[t] != -1;
    queue<int> q; q.push(st);
    for(;;) {
                                                                           pii solve() {
       while(q.size()) {
         int x=q.front(); q.pop(); vx[x]=1;
                                                                                int mf = 0, mc = 0;
                                                                                while(spfa()) {
         for(int y=1; y<=n; ++y) if(!vy[y]){
    ll t = lx[x]+ly[y]-g[x][y];</pre>
                                                                                    int nf = 0x3f3f3f3f;
                                                                                    for(int i = t; i != s; i = x[i]) {
            if(t==0){
                                                                                         nf = min(nf, E[x[i]][y[i]].f);
              pa[y]=x
              if(!my[y]){augment(y);return;}
                                                                                    for(int i = t; i != s; i = x[i]) {
              vy[y]=1, q.push(my[y]);
                                                                                         auto& it = E[x[i]][y[i]];
           }else if(sy[y]>t) pa[y]=x,sy[y]=t;
                                                                                         it.f -= nf;
       ll cut = INF;
for(int y=1; y<=n; ++y)</pre>
                                                                                         E[it.v][it.re].f += nf;
         if(!vy[y]&&cut>sy[y]) cut=sy[y];
                                                                                    mf += nf;
mc += nf * dis[t];
       for(int j=1; j<=n; ++j){
  if(vx[j]) lx[j] -= cut;
  if(vy[j]) ly[j] += cut;</pre>
                                                                                return {mf, mc};
                                                                           }
         else sy[j] -= cut;
                                                                      };
       for(int y=1; y<=n; ++y) if(!vy[y]&&sy[y]==0){</pre>
         if(!my[y]){augment(y);return;}
                                                                      4
         vy[y]=1, q.push(my[y]);
  } } }
                                                                              點宣告
                                                                      4.1
  11 solve(){
    fill(mx, mx+n+1, 0); fill(my, my+n+1, 0); fill(ly, ly+n+1, 0); fill(lx, lx+n+1, -INF);
                                                                      typedef long double ld;
                                                                      const ld eps = 1e-8;
```

```
int dcmp(ld x) {
  if(abs(x) < eps) return 0;</pre>
  else return x < 0? -1 : 1;
struct Pt {
  ld x, y;
  Pt(ld _x=0, ld _y=0):x(_x), y(_y) {}
  Pt operator+(const Pt &a) const {
  return Pt(x+a.x, y+a.y); }
Pt operator-(const Pt &a) const {
  return Pt(x-a.x, y-a.y); }
Pt operator*(const ld &a) const {
  return Pt(x*a, y*a); }
Pt operator/(const ld &a) const {
     return Pt(x/a, y/a);
  ld operator*(const Pt &a) const {
  return x*a.x + y*a.y; }
ld operator^(const Pt &a) const {
     return x*a.y - y*a.x;
  bool operator<(const Pt &a) const {</pre>
     return x < a.x | | (x == a.x && y < a.y); }
     //return\ dcmp(x-a.x) < 0 \mid |\ (dcmp(x-a.x) == 0 \&\&
  dcmp(y-a.y) < 0); }
bool operator==(const Pt &a) const {</pre>
     return dcmp(x-a.x) == 0 \&\& dcmp(y-a.y) == 0; }
ld norm2(const Pt &a) {
  return a*a; }
ld norm(const Pt &a)
  return sqrt(norm2(a)); }
Pt perp(const Pt &a) {
  return Pt(-a.y, a.x); }
Pt rotate(const Pt &a, ld ang) {
  return Pt(a.x*cos(ang)-a.y*sin(ang), a.x*sin(ang)+a.y
        *cos(ang)); }
struct Line {
  Pt s, e, v; // start, end, end-start
  Line(Pt _s=Pt(0, 0), Pt _e=Pt(0, 0)):s(_s), e(_e) { v = e-s; ang = atan2(v.y, v.x); }
  bool operator<(const Line &L) const {</pre>
     return ang < L.ang;</pre>
} };
struct Circle {
  Pt o; ld r;
  Circle(Pt _{o}=Pt(0, 0), ld _{r}=0):o(_{o}), r(_{r}) {}
```

4.2 矩形面積

```
struct AreaofRectangles{
#define cl(x) (x<<1)</pre>
#define cr(x) (x<<1|1)
    ll n, id, sid;
    pair<ll, il> tree[MXN<<3]; // count, area</pre>
    vector<ll> ind;
    tuple<ll,ll,ll,ll> scan[MXN<<1];</pre>
    void puli(int i, int l, int r){
   if(tree[i].first) tree[i].second = ind[r+1] -
             ind[l];
         else if(l != r){
             int mid = (l+r)>>1;
             tree[i].second = tree[cl(i)].second + tree[
                  cr(i)].second;
         else
                 tree[i].second = 0;
    void upd(int i, int l, int r, int ql, int qr, int v
         if(ql <= l && r <= qr){
             tree[i].first += v;
             pull(i, l, r); return;
         int mid = (l+r) >> 1;
if(ql <= mid) upd(cl(i), l, mid, ql, qr, v);</pre>
         if(qr > mid) upd(cr(i), mid+1, r, ql, qr, v);
         pull(i, l, r);
    void init(int _n){
         n = _n; id = sid = 0;
         ind.clear(); ind.resize(n<<1);</pre>
         fill(tree, tree+(n<<2), make_pair(0, 0));</pre>
```

```
void addRectangle(int lx, int ly, int rx, int ry){
     ind[id++] = lx; ind[id++] = rx;
     scan[sid++] = make\_tuple(ly, 1, lx, rx);
     scan[sid++] = make_tuple(ry, -1, lx, rx);
ll solve(){
     sort(ind.begin(), ind.end());
     ind.resize(unique(ind.begin(), ind.end()) - ind
           .begin());
     sort(scan, scan + sid);
ll area = 0, pre = get<0>(scan[0]);
     for(int i = 0; i < sid; i++){</pre>
          auto [x, v, l, r] = scan[i];
area += tree[1].second * (x-pre);
          upd(1, 0, ind.size()-1, lower_bound(ind.
  begin(), ind.end(), l)-ind.begin(),
  lower_bound(ind.begin(),ind.end(),r)-
                ind.begin()-1, v);
     }
     return area;
}rect;
```

4.3 最近點對

```
#include<bits/stdc++.h>
#define int long long
using namespace std;
using ld = long double;
const int mod = 1e9+7;
struct pt{
    int x,y;
int id;
    ld dis(const pt& rhs){
         return sqrt((x-rhs.x)*(x-rhs.x)+(y-rhs.y)*(y-
             rhs.y));
    }
};
signed main(){
    int n:
    cin>>n:
    vector<pt> a(n);
    for(int i=0;i<n;i++){</pre>
         cin>>a[i].x>>a[i].y;
         a[i].id=i;
    ld\ ans = 1e19;
    sort(a.begin(),a.end(),[](const pt&a,const pt&b){
         if(a.x==b.y)return a.y<b.y;</pre>
         return a.x<b.x;</pre>
    });
    pt ans2;
    function<void(int,int)> dnq = [&](int l,int r){
         if(r-1<4){
             for(int i=1;i<=r;i++){</pre>
                  for(int j=i+1;j<=r;j++){</pre>
                      ld temans = a[i].dis(a[j]);
                      if(temans<ans){
                          ans=temans
                          ans2 = \{a[i].id,a[j].id\};
             sort(a.begin()+l,a.begin()+r+1,[](const pt&
                  a,const pt&b){return a.y<b.y;});</pre>
         int mid = (1+r)/2;
         int midx = a[mid].x;
         dnq(l,mid);dnq(mid+1,r);
         inplace_merge(a.begin()+l,a.begin()+mid+1,a.
             begin()+r+1, [](const pt&a, const pt&b){}
              return a.y<b.y;});</pre>
         vector<int> c;c.reserve(r-l+1);
for(int i=l;i<=r;i++){</pre>
             if(abs(a[i].x-midx)<ans){</pre>
                  ld temans = a[i].dis(a[c[j]]);
                           if(temans<ans){</pre>
                               ans=temans:
```

4.4 凸包

```
double cross(Pt o, Pt a, Pt b){
 return (a-o) ^ (b-o);
vector<Pt> convex_hull(vector<Pt> pt){
 sort(pt.begin(),pt.end());
  int top=0;
 vector<Pt> stk(2*pt.size());
  for (int i=0; i<(int)pt.size(); i++){</pre>
    while (top >= 2 && cross(stk[top-2],stk[top-1],pt[i
        ]) <= 0)
      top--;
   stk[top++] = pt[i];
  for (int i=pt.size()-2, t=top+1; i>=0; i--){
   while (top >= t && cross(stk[top-2],stk[top-1],pt[i
        ]) <= 0)
      top--;
    stk[top++] = pt[i];
 stk.resize(top-1);
  return stk;
```

4.5 兩直線交點

```
Pt LLIntersect(Line a, Line b) {
  Pt p1 = a.s, p2 = a.e, q1 = b.s, q2 = b.e;
  ld f1 = (p2-p1)^(q1-p1), f2 = (p2-p1)^(p1-q2), f;
  if(dcmp(f=f1+f2) == 0)
    return dcmp(f1)?Pt(NAN,NAN):Pt(INFINITY,INFINITY);
  return q1*(f2/f) + q2*(f1/f);
}
```

4.6 兩線段交點

4.7 李超線段樹

```
struct LiChao_min{
    struct line{
        ll m,c;
        line(ll _m=0,ll _c=0){ m=_m; c=_c; }
        ll eval(ll x){ return m*x+c; } // overflow
    };
    struct node{
        node *l,*r; line f;
        node(line v){ f=v; l=r=NULL; }
    };
    typedef node* pnode;
```

```
pnode root; ll sz,ql,qr;
#define mid ((l+r)>>1)
  void insert(line v,ll l,ll r,pnode &nd){
      * if(!(ql<=l&&r<=qr)){
       if(!nd) nd=new node(line(0,INF));
       if(ql<=mid) insert(v,l,mid,nd->l)
       if(qr>mid) insert(v,mid+1,r,nd->r);
       return;
    } used for adding segment */
     if(!nd){    nd=new node(v);    return;    }
    11 trl=nd->f.eval(l),trr=nd->f.eval(r);
    ll vl=v.eval(l), vr=v.eval(r);
     if(trl<=vl&&trr<=vr) return;</pre>
     if(trl>vl&&trr>vr) { nd->f=v; return; }
     if(trl>vl) swap(nd->f,v)
     if(nd->f.eval(mid)<v.eval(mid))</pre>
       insert(v,mid+1,r,nd->r)
    else swap(nd->f,v),insert(v,l,mid,nd->l);
  ll query(ll x,ll l,ll r,pnode &nd){
    if(!nd) return INF;
     if(l==r) return nd->f.eval(x);
    if(mid >= x)
       return min(nd->f.eval(x),query(x,l,mid,nd->l));
    return min(nd->f.eval(x),query(x,mid+1,r,nd->r));
  /* -sz<=ll query_x<=sz */
  void init(ll _sz){ sz=_sz+1; root=NULL; }
  void add_line(ll m,ll c,ll l=-INF,ll r=INF){
    line v(m,c); ql=l; qr=r; insert(v,-sz,sz,root);
  11 query(ll x) { return query(x,-sz,sz,root); }
};
```

6

4.8 最小包覆圓

```
/* minimum enclosing circle */
int n;
Pt p[ N ];
const Circle circumcircle(Pt a,Pt b,Pt c){
  Circle cir
  double fa,fb,fc,fd,fe,ff,dx,dy,dd;
  if( iszero( ( b - a ) ^ ( c - a ) ) ){
  if( ( b - a ) * ( c - a ) ) <= 0 )
       return Circle((b+c)/2,norm(b-c)/2);
    if(((c-b)*(a-b))<=0)
    return Circle((c+a)/2,norm(c-a)/2);
if( ( ( a - c ) * ( b - c ) ) <= 0 )
      return Circle((a+b)/2,norm(a-b)/2);
  }else{
    fa=\bar{2}*(a.x-b.x);
    fb=2*(a.y-b.y);
    fc=norm2(a)-norm2(b);
    fd=2*(a.x-c.x);
    fe=2*(a.y-c.y);
    ff=norm2(a)-norm2(c);
    dx=fc*fe-ff*fb;
    dy=fa*ff-fd*fc;
    dd=fa*fe-fd*fb;
    cir.o=Pt(dx/dd,dy/dd);
    cir.r=norm(a-cir.o);
    return cir;
inline Circle mec(int fixed,int num){
  int i:
  Circle cir;
  if(fixed==3) return circumcircle(p[0],p[1],p[2]);
  cir=circumcircle(p[0],p[0],p[1]);
  for(i=fixed;i<num;i++) {</pre>
    if(cir.inside(p[i])) continue;
    swap(p[i],p[fixed]);
    cir=mec(fixed+1,i+1);
  return cir;
inline double min_radius() {
  if(n<=1) return 0.0;</pre>
  if(n==2) return norm(p[0]-p[1])/2;
  scramble();
  return mec(0,n).r;
```

4.9 最小包覆球

```
// Pt : { x , y , z }
#define N 202020
int n, nouter; Pt pt[ N ], outer[4], res;
double radius, tmp;
void ball() {
  Pt q[3]; double m[3][3], sol[3], L[3], det;
  int i,j; res.x = res.y = res.z = radius = 0;
switch ( nouter ) {
   case 1: res=outer[0]; break;
      case 2: res=(outer[0]+outer[1])/2; radius=norm2(res
              outer[0]); break;
        for (i=0; i<2; ++i) q[i]=outer[i+1]-outer[0];
for (i=0; i<2; ++i) for(j=0; j<2; ++j) m[i][j]=(q
    [i] * q[j])*2;
for (i=0; i<2; ++i) sol[i]=(q[i] * q[i]);
if (fabs(det=m[0][0]*m[1][1]-m[0][1]*m[1][0])<eps</pre>
        L[0]=(sol[0]*m[1][1]-sol[1]*m[0][1])/det;
L[1]=(sol[1]*m[0][0]-sol[0]*m[1][0])/det;
        res=outer[0]+q[0]*L[0]+q[1]*L[1];
        radius=norm2(res, outer[0]);
      case 4:
        for (i=0; i<3; ++i) q[i]=outer[i+1]-outer[0], sol
    [i]=(q[i] * q[i]);</pre>
              (i=0;i<3;++i) for(j=0;j<3;++j) m[i][j]=(q[i]
                q[j])*2:
        det= m[0][0]*m[1][1]*m[2][2]
           + m[0][1]*m[1][2]*m[2][0]
+ m[0][2]*m[2][1]*m[1][0]
+ m[0][2]*m[1][1]*m[1][0]
- m[0][2]*m[1][1]*m[2][0]
           - m[0][1]*m[1][0]*m[2][2]
        - m[0][0]*m[1][2]*m[2][1];
if (fabs(det)<eps) return;
         for (j=0; j<3; ++j) {
           for (i=0; i<3; ++i) m[i][j]=sol[i];
L[j]=( m[0][0]*m[1][1]*m[2][2]
+ m[0][1]*m[1][2]*m[2][0]
                     + m[0][1] :m[1][2] :m[2][0]
+ m[0][2]*m[2][1]*m[1][0]
- m[0][2]*m[1][1]*m[2][0]
- m[0][1]*m[1][0]*m[2][2]
                        m[0][0]*m[1][2]*m[2][1]
                   ) / det;
           for (i=0; i<3; ++i) m[i][j]=(q[i] * q[j])*2;
        } res=outer[0];
         for (i=0; i<3; ++i ) res = res + q[i] * L[i];
        radius=norm2(res, outer[0]);
void minball(int n){ ball();
   if( nouter < 4 ) for( int i = 0 ; i < n ; i ++ )</pre>
      if( norm2(res, pt[i]) - radius > eps )
        outer[ nouter ++ ] = pt[ i ]; minball(i); --
         if(i>0){ Pt Tt = pt[i];
  memmove(&pt[1], &pt[0], sizeof(Pt)*i); pt[0]=Tt
}}}
double solve(){
  // n points in pt
random_shuffle(pt, pt+n); radius=-1;
   for(int i=0;i<n;i++) if(norm2(res,pt[i])-radius>eps)
     nouter=1, outer[0]=pt[i], minball(i);
   return sqrt(radius);
```

旋轉卡尺 4.10

```
int FarthestPair(vector<Pt>& arr){
    int ret=0;
    for(int i = 0, j = i+1; i<arr.size(); i++){</pre>
        while(distance(arr[i], arr[j]) < distance(arr[i</pre>
             ], arr[(j+1)%arr.size()]) ){
             j = (j+1) % arr.size();
        ret = max(ret, distance(arr[i],arr[j]));
    return ret;
}
```

圖論 5

5.1 BCC

```
struct BccVertex {
   int n,nScc,step,dfn[MXN],low[MXN];
   vector<int> E[MXN], sccv[MXN];
   int top,stk[MXN];
   void init(int _n) {
  n = _n;  nScc = step = 0;
  for (int i=0; i<n; i++) E[i].clear();</pre>
   void addEdge(int u, int v)
{ E[u].PB(v); E[v].PB(u); }
   void DFS(int u, int f) {
      dfn[u] = low[u] = step++;
      stk[top++] = u;
for (auto v:E[u]) {
        if (v == f) continue;
        if (dfn[v] == -1) {
          DFS(v,u);
           low[u] = min(low[u], low[v]);
           if (low[v] >= dfn[u]) {
             int z;
             sccv[nScc].clear();
             do {
               z = stk[--top];
               sccv[nScc].PB(z);
             } while (z != v)
             sccv[nScc++].PB(u);
        }else
          low[u] = min(low[u],dfn[v]);
   } }
   vector<vector<int>> solve() {
      vector<vector<int>> res;
      for (int i=0; i<n; i++)</pre>
        dfn[i] = low[i] = -1;
      for (int i=0; i<n; i++)
  if (dfn[i] == -1) {</pre>
          top = 0;
          DFS(i,i);
      REP(i,nScc) res.PB(sccv[i]);
     return res;
}graph;
```

5.2 重心剖分

```
struct CentroidDecomposition {
    int n;
    vector<vector<int>> G, out;
    vector<<mark>int</mark>> sz, v
    CentroidDecomposition(int _n) : n(_n), G(_n), out(
    _n), sz(_n), v(_n) {} int dfs(int x, int par){
         sz[x] = 1;
         for (auto &&i : G[x]) {
              if(i == par | \overline{v}[i]) continue;
              sz[x] += dfs(i, x);
         return sz[x];
    int search_centroid(int x, int p, const int mid){
   for (auto &&i : G[x]) {
              if(i == p || v[i]) continue;
              if(sz[i] > mid) return search_centroid(i, x
         return x;
    void add_edge(int 1, int r){
   G[l].PB(r); G[r].PB(l);
    int get(int x){
         int centroid = search_centroid(x, -1, dfs(x,
              -1)/2);
         v[centroid] = true;
         for (auto &&i : G[centroid]) {
              if(!v[i]) out[centroid].PB(get(i));
```

```
v[centroid] = false;
                                                                     void addEdge(int a , int b)
{ v[a][b] = v[b][a] = 1; }
         return centroid;
} };
                                                                     int ans , stk[N], id[N] , di[N] , deg[N];
                                                                     Int cans:
        歐拉路徑
5.3
                                                                     void dfs(int elem_num, Int candi, Int ex){
                                                                        if(candi.none()&&ex.none()){
#define FOR(i,a,b) for(int i=a;i<=b;i++)</pre>
                                                                          cans.reset();
int dfs_st[10000500],dfn=0;
                                                                          for(int i = 0)
                                                                                            i < elem_num ; i ++)
                                                                          cans[id[stk[i]]] = 1;
ans = elem_num; // cans is a maximal clique
int ans[10000500], cnt=0, num=0;
vector<int>G[1000050];
int cur[1000050];
int ind[1000050],out[1000050];
                                                                        int pivot = (candilex)._Find_first();
void dfs(int x){
    FOR(i,1,n)sort(G[i].begin(),G[i].end());
                                                                        Int smaller_candi = candi & (~lnk[pivot]);
                                                                        while(smaller_candi.count()){
    dfs_st[++dfn]=x;
                                                                          int nxt = smaller_candi._Find_first();
    memset(cur,-1,sizeof(cur));
    while(dfn>0){
                                                                          candi[nxt] = smaller_candi[nxt] = 0;
         int u=dfs_st[dfn];
                                                                          ex[nxt] = 1:
         int complete=1;
                                                                          stk[elem_num] = nxt;
                                                                          dfs(elem_num+1,candi&lnk[nxt],ex&lnk[nxt]);
         for(int i=cur[u]+1;i<G[u].size();i++){</pre>
              int v=G[u][i];
                                                                     int solve(){
              num++;
                                                                       for(int i = 0 ; i < n ; i ++){
  id[i] = i; deg[i] = v[i].count();</pre>
              dfs_st[++dfn]=v;
              cur[u]=i;
              complete=0;
                                                                       sort(id , id + n , [&](int id1, int id2){
    return deg[id1] > deg[id2]; });
for(int i = 0 ; i < n ; i ++) di[id[i]] = i;
for(int i = 0 ; i < n ; i ++) di[id[i]] = i;</pre>
              break:
         if(complete)ans[++cnt]=u,dfn--;
    }
                                                                        for(int i = 0 ; i < n ; i ++)</pre>
                                                                          for(int j = 0 ; j < n ; j ++)
  if(v[i][j]) lnk[di[i]][di[j]] = 1;</pre>
bool check(int &start){
     int l=0,r=0,mid=0;
                                                                        ans = 1; cans.reset(); cans[0] = 1;
    FOR(i,1,n){
                                                                        dfs(0, Int(string(n,'1')), 0);
         if(ind[i]==out[i]+1)l++;
                                                                        return ans;
         if(out[i]==ind[i]+1)r++,start=i;
                                                                  } }solver;
         if(ind[i]==out[i])mid++;
                                                                   5.5 最大團
    if(l==1&&r==1&&mid==n-2)return true;
    l=1;
FOR(i,1,n)if(ind[i]!=out[i])l=0;
                                                                   #define N 111
                                                                   struct MaxClique{ // 0-base
                                                                     typedef bitset<N> Int;
    if(1){
         FOR(i,1,n)if(out[i]>0){
                                                                     Int linkto[N] , v[N];
              start=i;
                                                                     int n;
                                                                     void init(int _n){
              break:
         return true;
                                                                        for(int i = 0; i < n; i ++){
                                                                          linkto[i].reset(); v[i].reset();
    return false;
                                                                     void addEdge(int a , int b)
{ v[a][b] = v[b][a] = 1; }
int main(){
                                                                     int popcount(const Int& val)
    cin>>n>>m;
    FOR(i,1,m){
                                                                     { return val.count();
          int x,y;scanf("%d%d",&x,&y);
                                                                     int lowbit(const Int& val)
         G[x].push_back(y);
                                                                     { return val._Find_first(); }
                                                                     int ans , stk[N];
int id[N] , di[N] , deg[N];
         ind[y]++,out[x]++;
    int start=-1,ok=true;
                                                                     Int cans:
     if(check(start)){
                                                                     void maxclique(int elem_num, Int candi){
         dfs(start);
                                                                       if(elem_num > ans){
                                                                          ans = elem_num; cans.reset();
for(int i = 0; i < elem_num; i ++)</pre>
         if(num!=m){
              puts("What a shame!");
                                                                            cans[id[stk[i]]] = 1;
              return 0:
         for(int i=cnt;i>=1;i--)
                                                                        int potential = elem_num + popcount(candi);
              printf("%d ",ans[i]);
                                                                        if(potential <= ans) return;</pre>
         puts("");
                                                                        int pivot = lowbit(candi);
                                                                        Int smaller_candi = candi & (~linkto[pivot]);
                                                                       while(smaller_candi.count() && potential > ans){
  int next = lowbit(smaller_candi);
    else puts("What a shame!");
}
                                                                          candi[next] = !candi[next];
5.4 極大團
                                                                          smaller_candi[next] = !smaller_candi[next];
                                                                          potential -
#define N 80
                                                                          if(next == pivot || (smaller_candi & linkto[next
struct MaxClique{ // 0-base
                                                                               ]).count()){
  typedef bitset<N> Int;
                                                                            stk[elem_num] = next;
  Int lnk[N] , v[N];
                                                                            maxclique(elem_num + 1, candi & linkto[next]);
  int n;
  void init(int _n){
                                                                     int solve(){
                                                                       for(int i = 0; i < n; i ++){
    n = _n;
     for(int i = 0; i < n; i ++){
                                                                          id[i] = i; deg[i] = v[i].count();
       lnk[i].reset(); v[i].reset();
```

sort(id , id + n , [&](int id1, int id2){

} }

```
return deg[id1] > deg[id2]; });
for(int i = 0; i < n; i ++) di[id[i]] = i;
for(int i = 0; i < n; i ++)
    for(int j = 0; j < n; j ++)
        if(v[i][j]) linkto[di[i]][di[j]] = 1;
    Int cand; cand.reset();
    for(int i = 0; i < n; i ++) cand[i] = 1;
    ans = 1;
    cans.reset(); cans[0] = 1;
    maxclique(0, cand);
    return ans;
} }solver;</pre>
```

5.6 SCC

```
struct Scc{
  int n, nScc, vst[MXN], bln[MXN];
vector<int> E[MXN], rE[MXN], vec;
  void init(int _n){
    n = _n;
for (int i=0; i<MXN; i++)</pre>
      E[i].clear(), rE[i].clear();
  void addEdge(int u, int v){
    E[u].PB(v); rE[v].PB(u);
  void DFS(int u){
    vst[u]=1;
    for (auto v : E[u]) if (!vst[v]) DFS(v);
    vec.PB(u);
  void rDFS(int u){
    vst[u] = 1; bln[u] = nScc;
for (auto v : rE[u]) if (!vst[v]) rDFS(v);
  void solve(){
    nScc = 0;
    vec.clear();
    FZ(vst);
    for (int i=0; i<n; i++)
      if (!vst[i]) DFS(i);
    reverse(vec.begin(),vec.end());
    FZ(vst);
    for (auto v : vec)
      if (!vst[v]){
         rDFS(v); nScc++;
```

5.7 SPFA

```
#define MXN 200005
struct SPFA{
  int n:
  LL inq[MXN], len[MXN];
 vector<LL> dis;
  vector<pair<int, LL>> edge[MXN];
  void init(int _n){
    n = _n;
    dis.clear(); dis.resize(n, 1e18);
    for(int i = 0; i < n; i++){
  edge[i].clear();</pre>
      inq[i] = len[i] = 0;
  void addEdge(int u, int v, LL w){
    edge[u].push_back({v, w});
  vector<LL> solve(int st = 0){
    deque<int> dq; //return {-1} if has negative cycle
    dq.push_back(st); //otherwise return dis from st
    inq[st] = 1; dis[st] = 0;
    while(!dq.empty()){
      int u = dq.front(); dq.pop_front();
      inq[u] = 0;
      for(auto [to, d] : edge[u]){
  if(dis[to] > d+dis[u]){
           dis[to] = d+dis[u];
len[to] = len[u]+1;
           if(len[to] > n) return {-1};
           if(inq[to]) continue;
           (!dq.empty()&&dis[dq.front()] > dis[to]?
```

```
dq.push_front(to) : dq.push_back(to));
    inq[to] = 1;
    } }
    return dis;
} }spfa;
```

5.8 差分約束

約束條件 $V_j - V_i \leq W$ addEdge(V_i, V_j, W) and run bellman-ford or spfa

6數論

6.1 離散根號

```
void calcH(LL &t, LL &h, const LL p) {
   LL tmp=p-1; for(t=0;(tmp&1)==0;tmp/=2) t++; h=tmp;
\frac{1}{y} solve equation x^2 mod p = a
bool solve(LL a, LL p, LL &x, LL &y) {
   if(p == 2) { x = y = 1; return true; }
int p2 = p / 2, tmp = mypow(a, p2, p);
if (tmp == p - 1) return false;
   if ((p + 1) \% 4 == 0) {
      x=mypow(a,(p+1)/4,p); y=p-x; return true;
   } else {
      LL t, h, b, pb; calcH(t, h, p);
      if (t >= 2) {
         do \{b = rand() \% (p - 2) + 2;
         } while (mypow(b, p / 2, p) != p - 1);
      pb = mypow(b, h, p);
} int s = mypow(a, h / 2, p);
for (int step = 2; step <= t; step++) {
  int ss = (((LL)(s * s) % p) * a) % p;
}</pre>
         for(int i=0;i<t-step;i++) ss=mul(ss,ss,p);</pre>
         if (ss + 1 == p) s = (s * pb) % p;
pb = ((LL)pb * pb) % p;
      x = ((LL)s * a) % p; y = p - x;
   } return true;
}
```

6.2 ex-crt

```
typedef __int128 ll;
void exgcd(ll a,ll b,ll &g,ll &x,ll &y) {
    if (b == 0) {
         g = a;
         x = 1;
         y = 0;
         return;
    exgcd(b,a\%b,g,y,x);
    y = (a/b) *x;
bool flag = false;
ll a1,a2,n1,n2;
ll abs(ll x) {
    return x>0?x:-x;
void china() {
    11 d = a2 - a1;
    11 g,x,y;
    exgcd(n1,n2,g,x,y);
    if (d \% g == 0) {
 x = ((x*d/g)\%(n2/g)+(n2/g))\%(n2/g);
         a1 = x*n1 + a1;
         n1 = (n1*n2)/g;
    else
         flag = true;
long long as[100001]; //算式答案 x
long long ns[100001]; //模數 MOD
ll realchina() {
    a1 = as[0];
    n1 = ns[0];
    for (ll i = 1;i<n;i++) {</pre>
         a2 = as[i];
         n2 = ns[i];
         china();
         if (flag)
              return -1;
```

```
return a1;
                                                                                        if(k \% 2 == 0) return ppow(a * a % GAUSS_MOD .
                                                                                        k \gg 1);
if(k % 2 == 1) return ppow(a * a % GAUSS_MOD ,
int main() {
     cin>>n;
flag = false;
                                                                                             k \gg 1) * a % GAUSS_MOD;
     for (ll i = 0; i < n; i++)
                                                                                   vector<int> solve(){
                                                                                        vector<int> ans(n);
          cin>>ns[i]>>as[i];
                                                                                        cout<<(long long)realchina()<<endl;</pre>
6.3 ex-gcd
                                                                                             int inv = ppow(v[now][now] , GAUSS_MOD - 2)
int exgcd(int a,int b,int&x,int&y){
     if(b==0)return x=1,y=0,a;
                                                                                             REP(i , 0 , n) if(i != now){
   int tmp = v[i][now] * inv % GAUSS_MOD;
     int d = exgcd(b,a\%b,y,x);
     y=a/b*x;
                                                                                                   return d;
                                                                                                        GAUSS_MOD) %= GAUSS_MOD;
6.4 FFT
                                                                                             }
                                                                                             i , 0 , n) ans[i] = v[i][n + 1] * ppow(v[i
][i] , GAUSS_MOD - 2) % GAUSS_MOD;
// const int MAXN = 262144;
// (must be 2^k)
// before any usage, run pre_fft() first
typedef long double ld;
                                                                                        return ans;
typedef complex<ld> cplx; //real() ,imag()
                                                                                   // gs.v.clear() , gs.v.resize(n , vector<int>(n + 1
const ld PI = acosl(-1);
const cplx I(0, 1);
                                                                             } gs;
cplx omega[MAXN+1]
void pre_fft(){
  for(int i=0; i<=MAXN; i++)
    omega[i] = exp(i * 2 * PI / MAXN * I);</pre>
                                                                                      喬瑟夫問題
                                                                             6.6
                                                                             int josephus(int n, int m){ //n人每m次
                                                                                   int ans = 0;
                                                                                   for (int i=1; i<=n; ++i)
// n must be 2^k
                                                                                        ans = (ans + m) \% i;
void fft(int n, cplx a[], bool inv=false){
  int basic = MAXN / n;
                                                                                   return ans;
                                                                            }
  int theta = basic;
  for (int m = n; m >= 2; m >>= 1) {
     int mh = m >> 1;

for (int i = 0; i < mh; i++) {

    cplx w = omega[inv ? MAXN-(i*theta%MAXN)
                                                                             6.7 定理
                                                                                 Lucas's Theorem :
                                                                                   For n,m\in\mathbb{Z}^* and prime P, C(m,n)\mod P=\Pi(C(m_i,n_i)) where
                                                                                   m_i is the i\text{-th} digit of m in base P.
                                 : i*theta%MAXN];
        for (int j = i; j < n; j += m) {
                                                                                • Stirling approximation :
          int k = j + mh;
                                                                                   n! \approx \sqrt{2\pi n} (\frac{n}{e})^n e^{\frac{1}{12n}}
          cplx x = a[j] - a[k];
          a[j] += a[k];

a[k] = w * x;
                                                                                • Stirling Numbers(permutation |P|=n with k cycles): S(n,k)= coefficient of x^k in \Pi_{i=0}^{n-1}(x+i)
     } }
                                                                                - Stirling Numbers(Partition \boldsymbol{n} elements into \boldsymbol{k} non-empty set):
     theta = (theta * 2) % MAXN;
                                                                                   S(n,k) = \frac{1}{k!} \sum_{j=0}^{k} (-1)^{k-j} {k \choose j} j^n
  for (int j = 1; j < n - 1; j++) {
  for (int k = n >> 1; k > (i ^= k); k >>= 1);
                                                                                 • Pick's Theorem : A=i+b/2-1
                                                                                   A\colon Area i\colon grid number in the inner b\colon grid number on the side
     if (j < i) swap(a[i], a[j]);</pre>
                                                                                 • Catalan number : C_n = {2n \choose n}/(n+1)
                                                                                   C_n^{n+m} - C_{n+1}^{n+m} = (m+n)! \frac{n-m+1}{n+1} \quad for \quad n \ge m
C_n = \frac{1}{n+1} \binom{2n}{n} = \frac{(2n)!}{(n+1)!n!}
  if(inv) for (i = 0; i < n; i++) a[i] /= n;
cplx arr[MAXN+1];
                                                                                   \begin{array}{lll} C_0 = 1 & and & C_{n+1} = 2(\frac{2n+1}{n+2})C_n \\ C_0 = 1 & and & C_{n+1} = \sum_{i=0}^n C_i C_{n-i} & for & n \geq 0 \end{array}
inline void mul(int _n,ll a[],int _m,ll b[],ll ans[]){
  int n=1, sum=_n+_m-1;
  while(n<sum)</pre>
                                                                                 • Euler Characteristic:
  n<<=1;
for(int i=0;i<n;i++) {
                                                                                   planar graph: V-E+F-C=1 convex polyhedron: V-E+F=2
                                                                                   V,E,F,C : number of vertices, edges, faces(regions), and compo-
     double x=(i<_n?a[i]:0), y=(i<_m?b[i]:0);
                                                                                   nents
     arr[i]=complex<double>(x+y,x-y);
                                                                                • Kirchhoff's theorem :
                                                                                   A_{ii}=deg(i), A_{ij}=(i,j)\in E ?-1:0, Deleting any one row, one column, and call the det(A)
  fft(n,arr);
  for(int i=0;i<n;i++)
    arr[i]=arr[i]*arr[i];</pre>
                                                                                 ullet Polya' theorem (c is number of color \cdot m is the number of cycle
  fft(n,arr,true);
  for(int i=0;i<sum;i++)</pre>
                                                                                   (\sum_{i=1}^m c^{\gcd(i,m)})/m
     ans[i]=(long long int)(arr[i].real()/4+0.5);
                                                                                • Burnside lemma:
                                                                                  |X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|
6.5 高斯消去法
                                                                                • 錯排公式: (n 個人中 每個人皆不再原來位置的組合數):
                                                                                   dp[0] = 1; dp[1] = 0;
const int GAUSS_MOD = 100000007LL;
                                                                                   dp[i] = (i-1) * (dp[i-1] + dp[i-2]);
```

• Bell 數 (有 n 個人, 把他們拆組的方法總數):

 $B_n = \sum_{k=0}^{n} s(n,k) \quad (second - stirling)$ $B_{n+1} = \sum_{k=0}^{n} {n \choose k} B_k$

struct GAUSS{
 int n;

vector<vector<int>>> v;
int ppow(int a , int k){
 if(k == 0) return 1;

```
    Wilson's theorem

  (p-1)! \equiv -1 \pmod{p}
• Fermat's little theorem :
  a^p \equiv a \pmod{p}
• Euler's totient function:
  A^{B^C} mod \ p = pow(A, pow(B, C, p-1)) mod \ p
• 歐拉函數降幂公式: A^B \mod C = A^B \mod \phi(c) + \phi(c) \mod C
• 6 的倍數:
  (a-1)^3 + (a+1)^3 + (-a)^3 + (-a)^3 = 6a
```

6.8 Miller Rabin

```
// n < 4,759,123,141
                             3: 2, 7, 61
                                   2, 13, 23, 1662803
// n < 1,122,004,669,633
// n < 3,474,749,660,383
                                         pirmes <= 13
// n < 2^64
// 2, 325, 9375, 28178, 450775, 9780504, 1795265022
// Make sure testing integer is in range [2, n-2] if
// you want to use magic.
LL magic[]={}
bool witness(LL a, LL n, LL u, int t){
  if(!a) return 0;
  LL x=mypow(a,u,n);
  for(int i=0;i<t;i++) {</pre>
    LL nx=mul(x,x,n);
    if(nx==1&&x!=1&&x!=n-1) return 1;
    x=nx;
  return x!=1;
bool miller_rabin(LL n) {
  int s=(magic number size)
  // iterate s times of witness on n
  if(n<2) return 0;</pre>
  if(!(n\&1)) return n == 2;
 ll u=n-1; int t=0;
// n-1 = u*2^t
  while(!(u&1)) u>>=1, t++;
  while(s--){
    LL a=magic[s]%n;
    if(witness(a,n,u,t)) return 0;
  return 1;
```

6.9 NTT

```
// Remember coefficient are mod P
/* p=a*2^n+1
         2^n
                                          root
         65536
                       65537
                                          3 */
         1048576
                       7340033
   20
// (must be 2^k)
template<LL P, LL root, int MAXN>
struct NTT{
  static LL bigmod(LL a, LL b) {
    LL res = 1;
    for (LL bs = a; b; b >>= 1, bs = (bs * bs) % P)
       if(b&1) res=(res*bs)%P;
    return res:
  static LL inv(LL a, LL b) {
    if(a==1)return 1;
    return (((LL)(a-inv(b%a,a))*b+1)/a)%b;
  LL omega[MAXN+1];
  NTT() {
    omega[0] = 1;
    LL r = bigmod(root, (P-1)/MAXN);
    for (int i=1; i<=MAXN; i++)</pre>
      omega[i] = (omega[i-1]*r)%P;
  // n must be 2^k
  void tran(int n, LL a[], bool inv_ntt=false){
    int basic = MAXN / n , theta = basic;
for (int m = n; m >= 2; m >>= 1) {
      int mh = m >> 1;
for (int i = 0; i < mh; i++) {
  LL w = omega[i*theta%MAXN];</pre>
```

```
for (int j = i; j < n; j += m) {
  int k = j + mh;
  LL x = a[j] - a[k];</pre>
            if(x < 0) x += P;
            a[j] += a[k];
            if (a[j] > P) a[j] -= P;
a[k] = (w * x) % P;
       theta = (theta * 2) % MAXN;
     int i = 0;
     if (j < i) swap(a[i], a[j]);
     if (inv_ntt) {
       LL ni = inv(n,P);
       reverse( a+1 , a+n );
for (i = 0; i < n; i++)
a[i] = (a[i] * ni) % P;
} } };
const LL P=2013265921,root=31;
const int MAXN=4194304;
NTT<P, root, MAXN> ntt;
```

6.10 Pollard's Rho

```
// does not work when n is prime 0(n^{1/4})
LL f(LL x, LL mod){ return add(mul(x,x,mod),1,mod); }
LL pollard_rho(LL n) {
  if(!(n&1)) return 2;
  while(true){
     LL y=2, x=rand()%(n-1)+1, res=1;
for(int sz=2; res==1; sz*=2) {
       for(int i=0; i<sz && res<=1; i++) {</pre>
         x = f(x, n)
         res = \_gcd(abs(x-y), n);
       }
       y = x;
     if (res!=0 && res!=n) return res;
} }
```

6.11 質數

```
'* 12721, 13331, 14341, 75577, 123457, 222557, 556679
* 999983, 1097774749, 1076767633, 100102021, 999997771
* 1001010013, 1000512343, 987654361, 999991231
* 999888733, 98789101, 987777733, 999991921, 1010101333
* 1010102101, 1000000000039, 100000000000037
* 2305843009213693951, 4611686018427387847
* 9223372036854775783, 18446744073709551557 */
```

矩陣快速冪 6.12

```
LL len, mod;
vector<vector<LL>> operator*(vector<vector<LL>> x,
    vector<vector<LL>> y){
    vector<vector<LL>> ret(len,vector<LL>(len,0));
    for(int i=0;i<len;i++){</pre>
         for(int j=0;j<len;j++){
    for(int k=0;k<len;k++){</pre>
                 ret[i][j]=(ret[i][j]+x[i][k]*y[k][j])%
        }
    return ret;
struct Martix_fast_pow{ //O(len^3 lg k)
    LL init(int _len,LL m=9223372036854775783LL){
        len=_len, mod=m;
         // mfp.solve(k,{0, 1}, {1, 1}) k'th fib {值,係
         數} // 0-base
    LL solve(LL n,vector<vector<LL>> poly){
                     return poly[n][0];
         vector<vector<LL>> mar(len,vector<LL>(len,0)),x
             (len,vector<LL>(len,0));
         for(int i=0;i<len;i++)</pre>
                                    mar[i][i]=1;
         for(int i=0;i+1<len;i++) x[i][i+1]=1;
         for(int i=0;i<len;i++)</pre>
                                    x[len-1][i]=poly[i
             ][1];
        while(n){
```

7 字串

7.1 KMP

```
* len-failure[k]:
在k結尾的情況下,這個子字串可以由開頭
長度為(len-failure[k])的部分重複出現來表達
failure[k]為次長相同前綴後綴如果我們不只想求最多,而且以0-base做為考量
  那可能的長度由大到小會是
failuer[k] \ failure[failuer[k]-1]
  failure[failure[failuer[k]-1]-1]..
直到有值為0為止 */
int failure[MXN];
vector<int> KMP(string& t, string& p){
    vector<int> ret;
if (p.size() > t.size()) return;
     for (int i=1, j=failure[0]=-1; i<p.size(); ++i){</pre>
         while (j \ge 0 \&\& p[j+1] != p[i])
              j = failure[j];
         if (p[j+1] == p[i]) j++;
failure[i] = j;
     for (int i=0, j=-1; i<t.size(); ++i){
   while (j >= 0 && p[j+1] != t[i])
         j = failure[j];
if (p[j+1] == t[i]) j++;
         if (j == p.size()-1){
   ret.push_bck( i - p.size() + 1 );
              j = failure[j];
}
   }
         }
```

7.2 馬拉車

7.3 回文樹

```
// len[s]是對應的回文長度
// num[s]是有幾個回文後綴
// cnt[s]是這個回文子字串在整個字串中的出現次數
// fail[s]是他長度次長的回文後綴·aba的fail是a
const int MXN = 1000010;
struct PalT{
  int nxt[MXN][26],fail[MXN],len[MXN];
  int tot,lst,n,state[MXN],cnt[MXN],num[MXN];
  int diff[MXN],sfail[MXN],fac[MXN],dp[MXN];
  char s[MXN] = \{-1\};
  int newNode(int 1,int f){
    len[tot]=1,fail[tot]=f,cnt[tot]=num[tot]=0;
    memset(nxt[tot],0,sizeof(nxt[tot]));
    diff[tot]=(1>0?1-len[f]:0);
    sfail[tot]=(l>0&&diff[tot]==diff[f]?sfail[f]:f);
    return tot++;
  int getfail(int x){
    while(s[n-len[x]-1]!=s[n]) x=fail[x];
    return x:
  int getmin(int v){
    dp[v]=fac[n-len[sfail[v]]-diff[v]];
```

```
if(diff[v]==diff[fail[v]])
        dp[v]=min(dp[v],dp[fail[v]]);
    return dp[v]+1;
  int push(){
    int c=s[n]-'a',np=getfail(lst);
    if(!(lst=nxt[np][c])){
      lst=newNode(len[np]+2,nxt[getfail(fail[np])][c]);
      nxt[np][c]=lst; num[lst]=num[fail[lst]]+1;
    fac[n]=n;
    for(int v=lst;len[v]>0;v=sfail[v])
        fac[n]=min(fac[n],getmin(v));
    return ++cnt[lst], lst;
  void init(const char *_s){
    tot=lst=n=0;
    newNode(0,1), newNode(-1,1);
    for(;_s[n];) s[n+1]=_s[n],++n,state[n-1]=push();
    for(int i=tot-1;i>1;i--) cnt[fail[i]]+=cnt[i];
}palt;
7.4 SA
const int N = 300010;
```

```
struct SA{
#define REP(i,n) for ( int i=0; i<int(n); i++ )</pre>
#define REP1(i,a,b) for ( int i=(a); i <= int(b); i++)
  bool _t[N*2];
  int _s[N*2], _sa[N*2], _c[N*2], x[N], _p[N], _q[N*2],
         hei[N], r[N];
  int operator [] (int i){ return _sa[i]; }
void build(int *s, int n, int m){
     memcpy(_s, s, sizeof(int) * n);
     sais(_s, _sa, _p, _q, _t, _c, n, m);
     mkhei(n);
  void mkhei(int n){
     REP(i,n) r[_sa[i]] = i;
     hei[0] = 0;
     REP(i,n) if(r[i]) {
        int ans = i>0 ? max(hei[r[i-1]] - 1, 0) : 0;
        while(_s[i+ans] == _s[_sa[r[i]-1]+ans]) ans++;
        hei[r[i]] = ans;
     }
  }
  void sais(int *s, int *sa, int *p, int *q, bool *t,
     int *c, int n, int z){
bool uniq = t[n-1] = true, neq;
     int nn = 0, nmxz = -1, *nsa = sa + n, *ns = s + n,
          lst = -1;
#define MSO(x,n) memset((x),0,n*sizeof(*(x)))
#define MAGIC(XD) MS0(sa, n); \
    memcpy(x, c, sizeof(int) * z); \
     \label{eq:memcpy} \begin{array}{ll} \text{memcpy}(x + 1, \ c, \ sizeof(int) * (z - 1)); \\ \text{REP}(i,n) \ if(sa[i] \&\& \ !t[sa[i]-1]) \ sa[x[s[sa[i]-1]]) \end{array}
          ]-1]]++] = sa[i]-1; \setminus
     memcpy(x, c, sizeof(int) * z); \
for(int i = n - 1; i >= 0; i--) if(sa[i] && t[sa[i
           ]-1]) sa[--x[s[sa[i]-1]]] = sa[i]-1;
     MS0(c, z);
     REP(i,n) uniq \&= ++c[s[i]] < 2;
     REP(i,z-1) c[i+1] += c[i];
if (uniq) { REP(i,n) sa[--c[s[i]]] = i; return; }
     for(int i = n - 2; i >= 0; i--) t[i] = (s[i]==s[i +1] ? t[i+1] : s[i]<s[i+1]);

MAGIC(REP1(i,1,n-1) if(t[i] && !t[i-1]) sa[--x[s[i
     ]]]=p[q[i]=nn++]=i);
REP(i, n) if (sa[i] && t[sa[i]] && !t[sa[i]-1]) {
        neq=lst<0|lmemcmp(s+sa[i],s+lst,(p[q[sa[i]]+1]-sa
              [i])*sizeof(int));
        ns[q[lst=sa[i]]]=nmxz+=neq;
     sais(ns, nsa, p + nn, q + n, t + n, c + z, nn, nmxz
            + 1);
     MAGIC(for(int i = nn - 1; i \ge 0; i--) sa[--x[s[p[
          nsa[i]]]] = p[nsa[i]]);
}sa;
int H[ N ], SA[ N ];
```

```
void suffix_array(int* ip, int len) {
  // should padding a zero in the back
                                                                    } sam;
  // ip is int array, len is array length
// ip[0..n-1] != 0, and ip[len] = 0
                                                                            樹哈希
                                                                     7.6
  ip[len++] = 0
  sa.build(ip, len, 128);
for (int i=0; i<len; i++) {</pre>
                                                                    11 dfs(int u){
                                                                         vector<ll> h;
    H[i] = sa.hei[i + 1];
                                                                         subtree_sz[u] = 1;
for(ll child : edge[u]){
     SA[i] = sa.\_sa[i + 1];
                                                                              h.push_back(dfs(child));
  // resulting height, sa array \in [0,len)
                                                                              subtree_sz[u] += subtree_sz[child];
}
                                                                         sort(h.begin(), h.end());
7.5
        SAM
                                                                         11 ret = subtree_sz[u];
                                                                         for(ll v : h){
// any path start from root forms a substring of S
                                                                              ret = (ret * base + v) % MOD;
  occurrence of P : iff SAM can run on input word P
// number of different substring : ds[1]-1
                                                                         return ret;
// total length of all different substring : dsl[1]
                                                                    }
// max/min length of state i : mx[i]/mx[mom[i]]+1
// assume a run on input word P end at state i:
                                                                     7.7
                                                                            trie
// number of occurrences of P : cnt[i]
// first occurrence position of P : fp[i]-|P|+1
// all position of P : fp of "dfs from i through rmom"
                                                                    //01 bitwise trie
                                                                     struct trie{
const int MXM = 1000010;
                                                                         trie *nxt[2];
                                                                                          // 差別
struct SAM{
                                                                                       //紀錄有多少個數字以此節點結尾
                                                                         int cnt;
  int tot, root, lst, mom[MXM], mx[MXM]; //ind[MXM]
int nxt[MXM][33]; //cnt[MXM],ds[MXM],dsl[MXM],fp[MXM]
                                                                                        //有多少數字的前綴包括此節點
                                                                          int sz;
                                                                         trie():cnt(0),sz(0){
  // bool v[MXM]
                                                                              memset(nxt,0,sizeof(nxt));
  int newNode(){
     int res = ++tot;
                                                                    };
|//創建新的字典樹
     fill(nxt[res], nxt[res]+33, 0);
    mom[res] = mx[res] = 0; //cnt=ds=dsl=fp=v=0
     return res;
                                                                     void insert(int x){
                                                                          trie *now = root; // 每次從根節點開始
  void init(){
                                                                          for(int i=22;i>=0;i--){ // 從最高位元開始往低位元走
     tot = 0;
                                                                              now->sz++;
     root = newNode();
                                                                              //cout<<(x>>i&1)<<endl;
     lst = root;
                                                                              if(now->nxt[x>>i&1] == NULL){ //判斷當前第 i 個
                                                                                   位元是 0 還是 1
  void push(int c){
                                                                                   now->nxt[x>>i&1] = new trie();
     int p = lst;
    int np = newNode(); //cnt[np]=1
mx[np] = mx[p]+1; //fp[np]=mx[np]-1
for(; p && nxt[p][c] == 0; p = mom[p])
                                                                              now = now->nxt[x>>i&1]; //走到下一個位元
                                                                         now->cnt++;
     nxt[p][c] = np;
if(p == 0) mom[np] = root;
                                                                         now->sz++;
     else{
       int q = nxt[p][c];
                                                                     7.8 Z-value
       if(mx[p]+1 == mx[q]) mom[np] = q;
                                                                    int z[MAXN];
         int nq = newNode(); //fp[nq]=fp[q]
                                                                     void Z_value(const string& s) { //z[i] = lcp(s[1...],s[
         mx[nq] = mx[p]+1;
for(int i = 0; i < 33; i++)
  nxt[nq][i] = nxt[q][i];</pre>
                                                                         i...])
                                                                       int i, j, left, right, len = s.size();
                                                                       left=right=0; z[0]=len;
for(i=1;i<len;i++) {</pre>
         mom[nq] = mom[q];
         mom[q] = nq;
                                                                          j=max(min(z[i-left],right-i),0);
         mom[np] = nq;
                                                                          for(;i+j<len&&s[i+j]==s[j];j++);</pre>
         for(; p && nxt[p][c] == q; p = mom[p])
                                                                         z[i]=j
           nxt[p][c] = nq;
                                                                          if(i+z[i]>right) {
     } }
                                                                            right=i+z[i];
     lst = np;
                                                                            left=i;
  void calc(){
     calc(root);
                                                                            minRotation
     iota(ind,ind+tot,1);
     sort(ind,ind+tot,[&](int i,int j){return mx[i]<mx[j</pre>
                                                                     //rotate(begin(s),begin(s)+minRotation(s),end(s))
     ];});
for(int_i=tot-1;i>=0;i--)
                                                                     int minRotation(string s) {
                                                                       int a = 0, N = s.size(); s += s;
     cnt[mom[ind[i]]]+=cnt[ind[i]];
                                                                       rep(b,0,N) rep(k,0,N) {
                                                                          if(a+k == b \mid \mid s[a+k] < s[b+k])
  void calc(int x){
                                                                         {b += max(0, k-1); break;}
if(s[a+k] > s[b+k]) {a = b; break;}
    v[x]=ds[x]=1;dsl[x]=0; //rmom[mom[x]].push_back(x);
for(int i=1;i<=26;i++){
                                                                       } return a;
       if(nxt[x][i]){
         if(!v[nxt[x][i]]) calc(nxt[x][i]);
ds[x]+=ds[nxt[x][i]];
         dsl[x]+=ds[nxt[x][i]]+dsl[nxt[x][i]];
                                                                     8
                                                                          DP
  } } }
                                                                     8.1 數位 dp
  void push(const string& str){
    for(int i = 0; i < str.size(); i++)
push(str[i]-'a'+1);</pre>
```

|ll dp[MXN_BIT][PRE_NUM][LIMIT][F0];

```
ll dfs(int i,int pre, bool lim, bool f0, const string&
                                                                       string t = "abc"
                                                                       r[1].insert(0, t.c_str());
r[1].erase(1,1);
    if(v[i][pre][f0][lim]) return dp[i][pre][f0][lim];
    v[i][pre][f0][lim] = true;
                                                                       cout << r[ 1 ].substr( 0 , 2 );</pre>
                                                                  }
    if(i == str.size())
         return dp[i][pre][f0][lim] = 1;
                                                                   9.2 DLX
    ll ret = 0, h = \lim ? str[i] : '9';
                                                                  // given n*m 0-1 matrix
                                                                      find a set of rows s.t.
    for(int j='0'; j<=h; j++){
   if(abs(j-pre)>=2 || f0){
                                                                   // for each column, there's exactly one 1
                                                                   #define N 1024 //row
              ret += dfs(i+1, j, j==h && lim, f0 && j=='0
                                                                   #define M 1024 //column
                   ', str);
                                                                   #define NM ((N+2)*(M+2))
    }}
                                                                  char A[N][M]; //n*m 0-1 matrix
int used[N]; //answer: the row used
    return dp[i][pre][f0][lim] = ret;
}
                                                                   int id[N][M]
                                                                   int L[NM],R[NM],D[NM],U[NM],C[NM],S[NM],ROW[NM];
8.2 SOS dp
                                                                  void remove(int c){
  L[R[c]]=L[c]; R[L[c]]=R[c];
for(int i = 0; i<(1<<N); ++i)</pre>
                                                                     for( int i=D[c]; i!=c; i=D[i] )
  for( int j=R[i]; j!=i; j=R[j] )
F[i] = A[i];
for(int i = 0;i < N; ++i) for(int mask = 0; mask < (1<</pre>
                                                                         U[D[j]]=U[j]; D[U[j]]=D[j]; S[C[j]]--;
    N); ++mask){
                                                                       }
  if(mask & (1<<i))
                                                                  void resume(int c){
    F[mask] += F[mask^{(1<<i)}];
                                                                     for( int i=D[c]; i!=c; i=D[i] )
  for( int j=L[i]; j!=i; j=L[j] ){
    U[D[j]]=D[U[j]]=j; S[C[j]]++;
8.3 p-median
                                                                     L[R[c]]=R[L[c]]=c;
void p_Median(){
    int dfs(){
                                                                     if(R[0]==0) return 1;
                                                  // m是中位
                                                                     int md=100000000,c;
                   數·d[i][j]為距離的總和
                                                                     for( int i=R[0]; i!=0; i=R[i] )
  if(S[i]<md){ md=S[i]; c=i; }</pre>
              for (int k=i; k<=j; ++k) d[i][j] += abs(arr
                  [k] - arr[m]);
                                                                     if(md==0) return 0;
                                                                     remove(c);
        (int p=1; p<=P; ++p)
for (int n=1; n<=N; ++n){
                                                                     for( int i=D[c]; i!=c; i=D[i] ){
                                                                       used[ROW[i]]=1
              dp[p][n] = 1e9;
                                                                        for( int j=R[i]; j!=i; j=R[j] ) remove(C[j]);
              for (int k=p; k<=n; ++k)
    if (dp[p-1][k-1] + d[k][n] < dp[p][n]){
                                                                        if(dfs()) return 1
                                                                       for( int j=L[i]; j!=i; j=L[j] ) resume(C[j]);
                       dp[p][n] = dp[p-1][k-1] + d[k][n];
                                                                       used[ROW[i]]=0;
                       r[p][n] = k;
                                         // 從第k個位置往右
                            到第j個位置
                                                                     resume(c);
                  }
                                                                     return 0;
         }
                                                                   int exact_cover(int n,int m){
                                                                     for( int i=0; i<=m; i++ ){</pre>
9
     Other
                                                                       R[i]=i+1; L[i]=i-1; U[i]=D[i]=i;
                                                                       S[i]=0; C[i]=i;
      黑魔法
9.1
                                                                     R[m]=0; L[0]=m;
#include <bits/extc++.h>
                                                                     int t=m+1;
using namespace __gnu_pbds;
typedef tree<int,null_type,less<int>,rb_tree_tag,
                                                                     for( int i=0; i<n; i++ ){
                                                                       int k=-1;
for( int j=0; j<m; j++ ){
  if(!A[i][j]) continue;
    tree_order_statistics_node_update> set_t;
#include <ext/pb_ds/assoc_container.hpp>
typedef cc_hash_table<int,int> umap_t;
                                                                          if(k==-1) L[t]=R[t]=t
typedef priority_queue<int> heap;
                                                                          else{ L[t]=k; R[t]=R[k]; }
k=t; D[t]=j+1; U[t]=U[j+1];
#include<ext/rope>
using namespace __gnu_cxx;
                                                                          L[R[t]]=R[L[t]]=U[D[t]]=D[U[t]]=t;
int main(){
                                                                          C[t]=j+1; S[C[t]]++; ROW[t]=i; id[i][j]=t++;
    // Insert some entries into s.
    set_t s; s.insert(12); s.insert(505);
                                                                     for( int i=0; i<n; i++ ) used[i]=0;</pre>
    // The order of the keys should be: 12, 505.
                                                                     return dfs();
    assert(*s.find_by_order(0) == 12);
assert(*s.find_by_order(3) == 505);
    // The order of the keys should be: 12, 505.
                                                                  9.3 Hiber Curve
    assert(s.order_of_key(12) == 0);
assert(s.order_of_key(505) == 1);
    // Erase an entry.
                                                                  long long hilbert(int n,int x,int y){
                                                                     long long res=0;
    s.erase(12);
                                                                     for(int s=n/2;s;s>>=1){
    // The order of the keys should be: 505.
    assert(*s.find_by_order(0) == 505);
                                                                        int rx=(x&s)>0,ry=(y&s)>0; res+=s*1ll*s*((3*rx)^ry)
    // The order of the keys should be: 505.
                                                                       if(ry==0){ if(rx==1) x=s-1-x, y=s-1-y; swap(x,y); }
    assert(s.order_of_key(505) == 0);
                                                                     }
```

return res:

}

heap h1 , h2; h1.join(h2); rope<char> r[2]; r[1] = r[0]; // persistenet

9.4 模擬退火

