

# CS422 Robotics and Automation

## Assignment 1

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Due 30th Sept. Late submissions will not be accepted

Read Textbook Chapter 2 and answer the following questions:

1. Use Grübler's formula to verify that the Stewart mechanism (Fig. 1) indeed has six degrees of freedom (10pts)

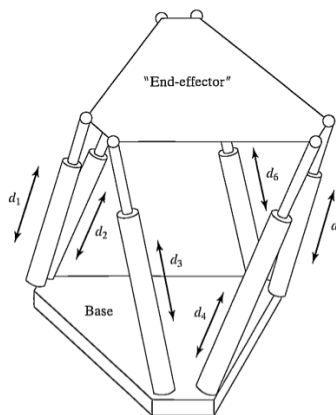


Figure 1: The Stewart mechanism is a six-degree-of-freedom fully parallel manipulator.

2. A vector  $P^A$  is rotated about  $\hat{Z}_A$  by  $\theta$  degrees and is subsequently rotated about  $\hat{X}_A$  by  $\phi$  degrees. Give the rotation matrix that accomplishes these rotations in the given order (5 pts).
3. A frame  $\{B\}$  is located initially coincident with a frame  $\{A\}$ . We rotate  $\{B\}$  about  $\hat{Z}_B$  by  $\theta$  degrees, and then we rotate the resulting frame about  $\hat{X}_B$  by  $\theta$  degrees. Give the rotation matrix that will change the descriptions of vectors from  $P^B$  to  $P^A$  (5pts)
4. Referring to Fig. 2

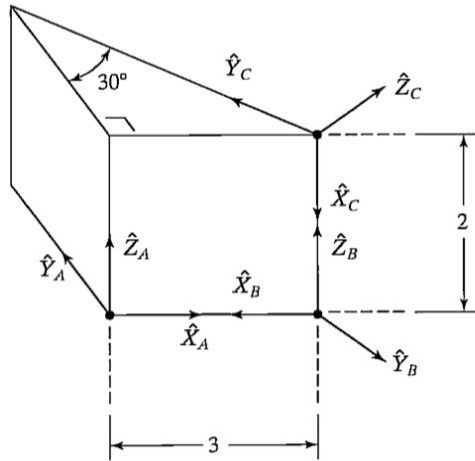


Figure 2: Frames at the corners of a wedge

- (a) give the value of  $H_B^A$
- (b) give the value of  $H_C^A$
- (c) give the value of  $H_C^B$
- (d) give the value of  $H_A^C$
- (e) give the value of  $H_A^B$  (10pts)

5. Given

$$H_B^A = \begin{bmatrix} 0.25 & 0.43 & 0.86 & 5.0 \\ 0.87 & -0.50 & 0.00 & -4.0 \\ 0.43 & 0.75 & -0.50 & 3.0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

find  $H_A^B$  (5pts)

0.2511	0.8638	0.4319	0.9040
0.4369	-0.4970	0.7515	-6.4271
0.8713	-0.0026	-0.5013	-2.8632
0	0	0	1.0000