

3. (a) linear 2 order  
 (b) nonlinear 3 order  
 (c) nonlinear 1. order  
 (d) nonlinear 2 order

4. (a)  $y' = -\sin \ln \frac{1}{x}$   
 sol  $y'' = -\cos \ln \frac{1}{x^2} + \sin \ln \frac{1}{x^2}$   
 and  $x^2 (-\cos \ln x \cdot \frac{1}{x^2} + \sin \ln x \cdot \frac{1}{x^2})$   
 $+ x (-\sin \ln x \cdot \frac{1}{x}) + \cos \ln x$   
 $= 0$

So verify  $y$  is the solution  
 $\therefore$  explicit.

(b)  $-2x^2y + y^2 = 1$   
 sol  $\begin{cases} -4xy dx + 2x^2 dy + 2y dy = 0 \\ 2xy dx + (x^2 - y) dy = 0 \end{cases}$   
 $\therefore$  verify implicit

5. (a)  $(1-x^2) \frac{dy}{dx} + x(3y-3) = 0$

sol  $\frac{dy}{3-y} = \frac{1+x-1}{1-x^2} dx$

$C - \ln(3-y) = -\ln(1-x) + \frac{1}{2} \ln \frac{1+x}{1-x}$

$\therefore C \sqrt{1-x^2} = 3-y$

$\therefore y = 3 - C \sqrt{1-x^2}$

(b)  $e^x y \frac{dy}{dx} = e^{-2x} + e^{-2x-y} \quad y(0) = 0$

$y \cdot e^y dy = \frac{1+e^x}{e^x} dx$

$\int y e^y dy = \int (e^{-x} + e^{-3x}) dx$

$(y-1)e^y = -e^{-x} - \frac{e^{-3x}}{3} + C$

$\therefore y(0) = 0$

$\therefore (0-1)1 = -1 - \frac{1}{3} + C$

So  $C = \frac{1}{3}$

$\therefore (y-1)e^y = -e^{-x} - \frac{1}{3}e^{-3x} + \frac{1}{3}$