

# Supplementary Information for “The relationship between $dN/dS$ and scaled selection coefficients”

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Mutation rate	MG1	F1x4	MG3	CF3x4	F3x4	F61
NP	-0.014	-0.02	-0.007	-0.009	-0.007	0.019
Yeast	0.025	0.007	-0.063	-0.084	-0.076	-0.068
Polio	-0.049	-0.103	-0.088	-0.148	-0.161	-0.136

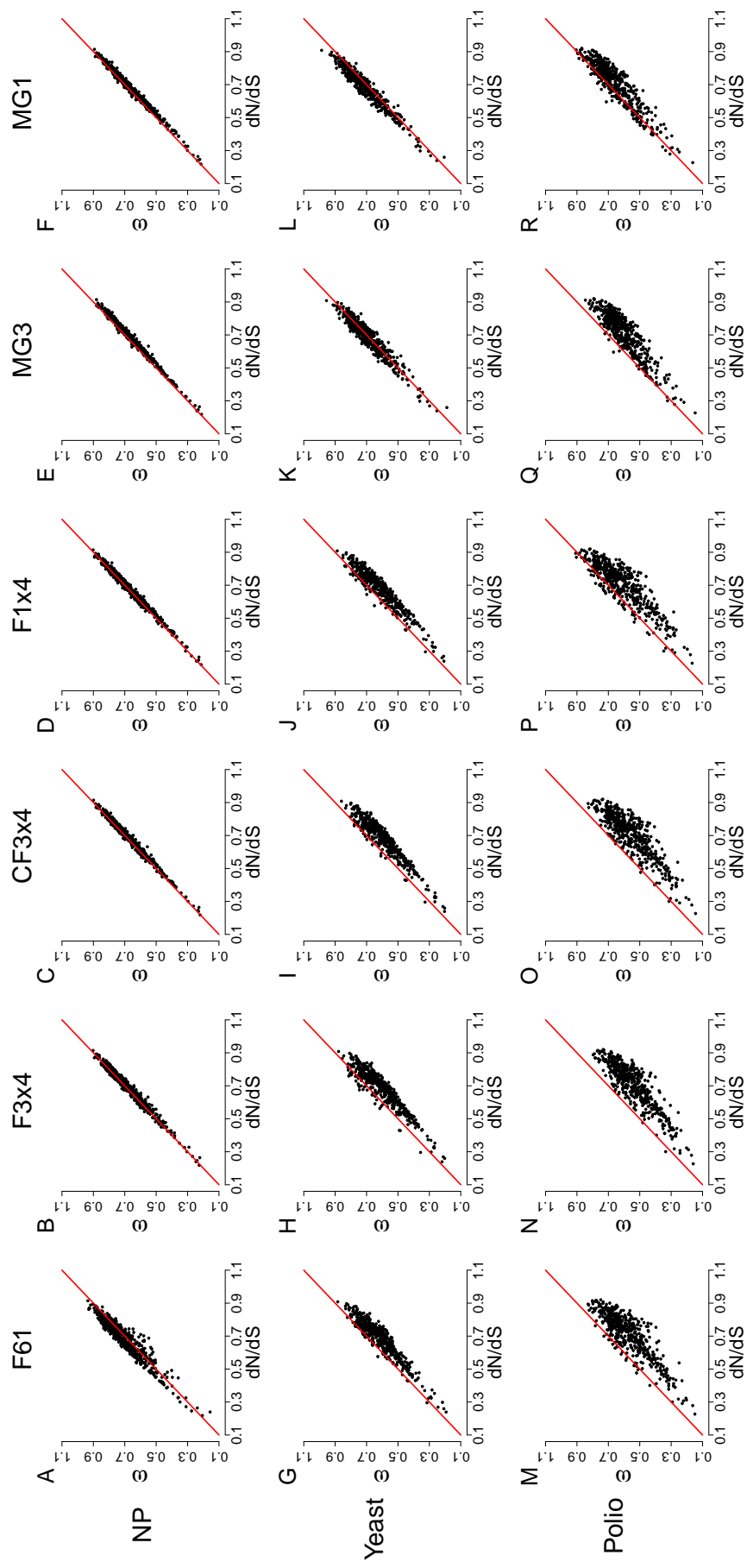
**Table S1.** Estimator bias of  $\omega$  MLEs and the true  $dN/dS$  values, for all nucleotide mutation rates and model frequency parameterizations examined. All biases are statistically significant (different from 0), with all  $P < 2 \times 10^{-16}$  except for the estimator bias associated with yeast mutation rates for MG3, where  $P = 5.4 \times 10^{-5}$ .

Mutation rate	MG1	F1x4	MG3	CF3x4	F3x4	F61
NP	0.988	0.989	0.985	0.986	0.977	0.902
Yeast	0.943	0.917	0.905	0.897	0.864	0.889
Polio	0.842	0.811	0.777	0.754	0.781	0.752

**Table S2.** Precision, measured as the squared correlation coefficient  $r^2$ , of  $\omega$  MLEs relative to the true  $dN/dS$  values, for all nucleotide mutation rates and model frequency parameterizations examined. All values shown are statistically significant, with all  $P < 2 \times 10^{-16}$ .

Frequencies	NP	Yeast	Polio
F61	0	0	0
CF3x4	-8918.92	-7243.16	-7306.7
MG1	-12551.28	-9267.83	-4399.6
F1x4	-12776.56	-12910.5	-14720.32
MG3	-13653.31	-12103.59	-7955.63
F3x4	-14098.61	-16676.69	-18715.34

**Table S3.** Mean  $\Delta\text{BIC}$  for datasets simulated with NP, yeast, or polio virus mutation rates. Note that the order of frequency models shown here corresponds to the model ranking for NP, and the ranking differs somewhat for yeast and polio datasets. BIC is computed as  $\text{BIC} = -2 \ln L + k \ln n$ , where  $k$  is the number of free parameters of the model,  $\ln L$  is the log-likelihood, and  $n$  is the sample size (Burnham and Anderson 2004). For all models,  $n = 500000$ , which corresponds to the number of alignment columns. The number of free parameters for each model is F61, 63; CF3x4, 12; MG1, 6; F1x4, 6; MG3, 12; and F3x4, 12. Note that, for each model, 3 of the parameters are  $\omega$ ,  $\kappa$ , and a global branch-length scaling parameter, and the remaining parameters are either empirical codon or nucleotide frequencies.



**Figure S1.** Regressions of  $\omega$  MLEs on the true  $dN/dS$  values, as calculated from scaled selection coefficients, for datasets simulated using experimental fitnesses and mutation rates. Each point represents an alignment, and each red line is the  $x = y$  line.

## References

Burnham K P, Anderson D R. 2004. Multimodel inference: understanding AIC and BIC in model selection. *Sociol Method Res* 33:261 – 304.