

## Plan for this Afternoon

### Character state-dependent diversification

- \* Theory: Speciation, extinction, and trait transitions
- \* Practical: Using BiSSE

### Break

### Biogeography

- \* Theory: Modeling range shifts and geographic mode of speciation
- \* Practical
  - o Using DEC
  - o Using ClaSSE

# Outline

## **Character State-Dependent Diversification**

- Motivating Biological Questions

- Methods History

- How BiSSE Works

- Current State of Methods

## **Biogeography**

# Motivating Biological Questions

## Macroevolutionary processes

- \* Traits that affect speciation or extinction
  - Is this trait a key innovation?
  - Does species-level selection act on this trait?
- \* Trait evolution
  - How quickly does this trait evolve?
  - Is evolution of this trait irreversible?

**Central point:** Questions of trait evolution and diversification are intrinsically linked. . .

# Methods History

## Some methods consider these processes separately

- \* Lineage diversification: sister clades (Mitter et al. 1988)
- \* Trait evolution: models like sequence evol. (Pagel 1999; Lewis 2001)

*[board: sister clades, transition model; unequal freqs]*

# Methods History

## Some methods consider these processes separately

- \* Lineage diversification: sister clades (Mitter et al. 1988)
- \* Trait evolution: models like sequence evol. (Pagel 1999; Lewis 2001)

## But asymmetry in one process can mislead inference of other

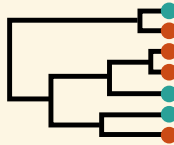
- \* Simulation demonstration (Maddison 2006)
- \* BiSSE model developed as a solution (Maddison et al. 2007)  
“Binary State Speciation and Extinction”

*[board: sister clades, transition model; unequal freqs]*

# How BiSSE Works

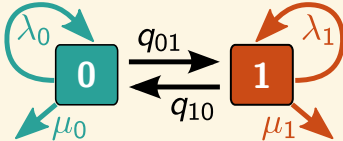
## Input data

- \* “Known” tree
- \* Observed tip states



## Goal

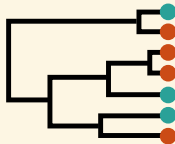
- \* Likelihood of data under 6-parameter model



# How BiSSE Works

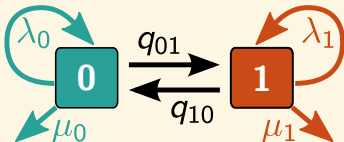
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## Goal

- \* Likelihood of data under 6-parameter model



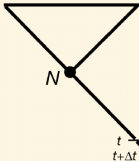
## Approach

- \* Evolve two probability vectors down the tree
  - Clade probabilities,  $D_{Ni}(t)$
  - Extinction probabilities,  $E_i(t)$

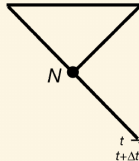
# How BiSSE Works

## Within branches

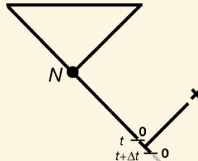
a) No state change,  
No speciation



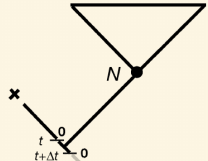
b) State change,  
No speciation



c) No state change,  
Speciation & Extinction



d) No state change,  
Speciation & Extinction



$$\frac{dD_{N0}(t)}{dt} = -(\lambda_0 + \mu_0 + q_{01}) D_{N0}(t) + q_{01} D_{N1}(t) + 2\lambda_0 D_{N0}(t) E_0(t)$$

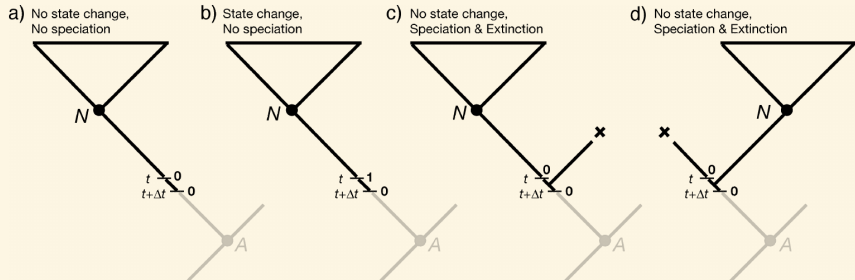
$$\frac{dD_{N1}(t)}{dt} = -(\lambda_1 + \mu_1 + q_{10}) D_{N1}(t) + q_{10} D_{N0}(t) + 2\lambda_1 D_{N1}(t) E_1(t)$$

[board: walk down from tips]



# How BiSSE Works

## Within branches



$$\frac{dD_{N0}(t)}{dt} = -(\lambda_0 + \mu_0 + q_{01}) D_{N0}(t) + q_{01} D_{N1}(t) + 2\lambda_0 D_{N0}(t) E_0(t)$$

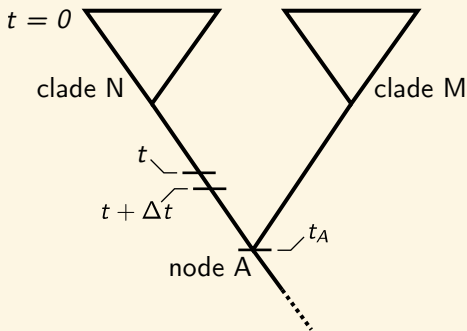
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$$\frac{dE_0(t)}{dt} = \mu_0 - (\lambda_0 + \mu_0 + q_{01}) E_0(t) + q_{01} E_1(t) + \lambda_0 E_0(t)^2$$

$$\frac{dE_1(t)}{dt} = \mu_1 - (\lambda_1 + \mu_1 + q_{10}) E_1(t) + q_{10} E_0(t) + \lambda_1 E_1(t)^2$$

# How BiSSE Works

## At nodes



$$D_{A0}(t_A) = D_{N0}(t_A)D_{M0}(t_A)\lambda_0$$

$$D_{A1}(t_A) = D_{N1}(t_A)D_{M1}(t_A)\lambda_1$$

[board: walk through node]

# How BiSSE Works

## At the root

- \* Have  $D_{R0}(t_R)$  and  $D_{R1}(t_R)$
- \* Combine them to get the overall likelihood of the data

## The result

- \* Likelihood of the data given the model
  - Data = tree shape and tip states
  - Model = BiSSE with 6 parameter values

Then Bayesian inference, etc...

*[board: root weightings]*

# Current State of Methods

## BiSSE is a smart approach

- \* Processes suited to biological questions
- \* Correct algorithm and implementations

## Caution 1: Correlation, not causation

- \* Could be other, related trait
- (Maddison et al. 2007)

## Current State of Methods

### BiSSE is a smart approach

- \* Processes suited to biological questions
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### Caution 1: Correlation, not causation

- \* Could be other, related trait
- (Maddison et al. 2007)

### Caution 2: Correlations reported when not appropriate

- \* Phylogenetic pseudoreplication
  - \* Other diversification rate heterogeneity
- (Maddison & FitzJohn 2015; Rabosky & Goldberg 2015)

## Current State of Methods

### Caution 2: Correlations often reported when not appropriate

What do we do?

- \* Less-model-based approaches  
(Rabosky & Huang 2016; Rabosky & Goldberg 2017)
- \* Add other processes to BiSSE  
e.g., hidden state (Beaulieu & O'Meara 2016)
- \* Ongoing research on other approaches. . .

# Outline

## Character State-Dependent Diversification

### **Biogeography**

- Trait Coding

- Range Shifts

- Geographic Mode of Speciation

- Methods

# Biogeography

## Why is “biogeography” a topic this week?

- \* Geographic range trait applies to all organisms
- \* Modeling it raises interesting methodological considerations
  - How to code the trait
  - Anagenetic and cladogenetic trait change
  - Geology informs time-stratified rate matrices



# Trait Coding

**Usual traits:** discrete values, maybe some uncertainty

**Geographic range:** often multiple values simultaneously

**Approach:** model states are all combinations of areas

## Trait Coding

For 3 areas...











absent:



present:



... these states are possible:

<i>picture</i>	<i>bits</i>	<i>index</i>
	0 0 0	0
	0 0 1	1
	0 1 0	2
	0 1 1	3
	1 0 0	4
	1 0 1	5
	1 1 0	6
	1 1 1	7

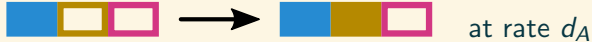
# Range Shifts

## Range expansion or contraction

- \* State transition for one species

Anagenetic change

- \* **Dispersal:** range expansion



















- \* **Extirpation** (a.k.a. local extinction): range contraction



*[board: more examples]*

## Range Shifts

Which transitions to allow is *your* design decision. For example:

	to:							
								
from:								
	—	0	0	0	0	0	0	0
	<i>e</i>	—	0	<i>d</i>	0	<i>d</i>	0	0
	<i>e</i>	0	—	<i>d</i>	0	0	<i>d</i>	0
	0	<i>e</i>	<i>e</i>	—	0	0	0	$2 d$
	<i>e</i>	0	0	0	—	<i>d</i>	<i>d</i>	0
	0	<i>e</i>	0	0	<i>e</i>	—	0	$2 d$
	0	0	<i>e</i>	0	<i>e</i>	0	—	$2 d$
	0	0	0	<i>e</i>	0	<i>e</i>	<i>e</i>	—

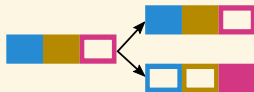
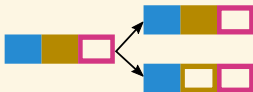
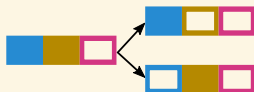
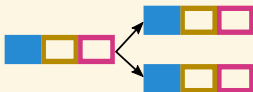
# Geographic Mode of Speciation

## Range changes “during” speciation

- \* State change as one species splits into two

### Cladogenetic change

- Speciation within one region
- Speciation between regions
- Speciation with dispersal



Many possibilities. Which ones to allow is *your* design decision.

[board: more examples]

# Methods

## DEC

- \* Dispersal-Extinction-Cladogenesis  
(Ree et al. 2005; Ree & Smith 2008; Landis et al. 2013; Matzke 2014)
- \* Range evolution on a fixed tree

## ClaSSE (GeoSSE)

- \* Cladogenetic (Geographic) State Speciation and Extinction  
(Goldberg et al. 2011; Goldberg & Igić 2012)
- \* Range evolution during a birth-death process

## Methods: DEC

### Anagenetic range change

- \* Along branches
- \* Rates of dispersal and local extinction

### Cladogenetic range change

- \* At nodes
- \* Probabilities of the various modes
- \* A logical problem: nodes “hidden” by extinction

*[board: hidden nodes]*

## Methods: ClaSSE

### Anagenetic range change

- \* Along branches
- \* Rates of dispersal and local extinction

### Cladogenetic range change

- \* At all speciation events
- \* Rates of speciation, via the various modes

### Global extinction

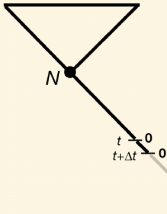
- \* Branches pruned from the tree
- \* Allows for hidden nodes



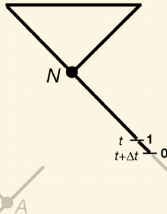
# Methods: BiSSE (MuSSE)

## Within branches

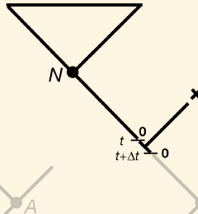
a) No state change,  
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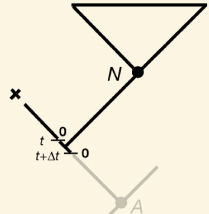
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Speciation & Extinction



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Speciation & Extinction



$$\frac{dD_{Ni}(t)}{dt} = - \left( \lambda_i + \mu_i + \sum_{j \neq i}^k q_{ij} \right) D_{Ni}(t) + \sum_{j \neq i}^k q_{ij} D_{Nj}(t) + 2\lambda_i E_i(t) D_{Ni}(t)$$

$$\frac{dE_i(t)}{dt} = \mu_i - \left( \lambda_i + \mu_i + \sum_{j \neq i}^k q_{ij} \right) E_i(t) + \sum_{j \neq i}^k q_{ij} E_j(t) + \lambda_i E_i(t)^2$$

## At nodes

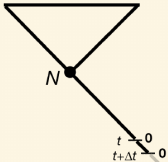
$$D_{Ai}(t_A) = \lambda_i D_{Ni}(t_A) D_{Mi}(t_A)$$

[board: N, M reminder]

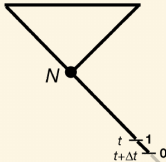
# Methods: ClaSSE

## Within branches

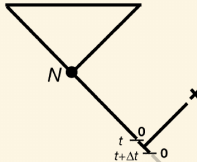
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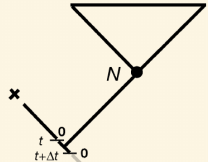
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## At nodes

$$D_{Ai}(t_A) = \frac{1}{2} \sum_{j,k} \lambda_{ijk} [D_{Nj}(t_A) D_{Mk}(t_A) + D_{Nk}(t_A) D_{Mj}(t_A)]$$

## Methods: ClaSSE

*One example of parameterizing ClaSSE for biogeography:*

Two areas:



Three states:



Dispersal:

$$q_{13} = d_B$$

$$q_{23} = d_A$$

Local extinction:

$$q_{31} = e_A$$

$$q_{32} = e_B$$

Global extinction:

$$\mu_1 = e_B$$

$$\mu_2 = e_A$$

Speciation:

$$\lambda_{111} = s_B$$

$$\lambda_{222} = s_A$$

$$\lambda_{312} = \lambda_{321} = s_{AB}$$

$$\lambda_{313} = \lambda_{331} = s_B$$

$$\lambda_{323} = \lambda_{332} = s_A$$

(all other rates are 0)