

1 Example test.wls

File content

```
{
(* Upper List *) {
  (* Upper Front List *) {{1, \[Alpha]^(-1)}, {1, 1}},
  (* Upper Rear List *) {{Ceil[\[Beta]], \[Beta]}, {1, 1}}
},
(* Lower List *) {
  (* Lower Front List *) {{1/2, \[Alpha]/2}, {1, 1}, {3, 3}, {2, 2}},
  (* Lower Rear List *) {{1, \[Alpha]/2}}
}
}
```

Fox H-function

$$H_{4,5}^{4,2} \left(\cdot \left| \begin{array}{c} (1, \frac{1}{\alpha}), (1, 1), (\text{Ceil}(\beta), \beta), (1, 1) \\ (\frac{1}{2}, \frac{\alpha}{2}), (1, 1), (3, 3), (2, 2), (1, \frac{\alpha}{2}) \end{array} \right. \right)$$
$$H_{4,5}^{4,2} \left(\cdot \left| \begin{array}{c|c} (1, \frac{1}{\alpha}), (1, 1) & (\text{Ceil}(\beta), \beta), (1, 1) \\ \hline (\frac{1}{2}, \frac{\alpha}{2}), (1, 1), (3, 3), (2, 2) & (1, \frac{\alpha}{2}) \end{array} \right. \right)$$

Summary

$$\begin{aligned} a^* &= \frac{1}{\alpha} - \beta + 6 \\ \Delta &= \alpha - \frac{1}{\alpha} - \beta + 4 \\ \delta &= \frac{2^{-\alpha} \left(2^{\frac{\alpha}{2}+5} \alpha^{\alpha/2} + \alpha^\alpha \right)}{\left(\left(\frac{1}{\alpha} \right)^{\frac{1}{\alpha}} + 1 \right) (\beta^\beta + 1)} \\ \mu &= 4 - \text{Ceil}(\beta) \\ a_1^* &= \frac{\alpha}{2} - \beta + 5 \\ a_2^* &= -\frac{\alpha}{2} + \frac{1}{\alpha} + 1 \\ \xi &= \frac{13}{2} - \text{Ceil}(\beta) \\ c^* &= \frac{3}{2} \end{aligned}$$

Poles 1. First ten poles from upper front list

$$a_{i,k} = \left(\begin{array}{cc} 0 & 0 \\ \alpha & 1 \\ 2\alpha & 2 \\ 3\alpha & 3 \\ 4\alpha & 4 \\ 5\alpha & 5 \\ 6\alpha & 6 \\ 7\alpha & 7 \\ 8\alpha & 8 \\ 9\alpha & 9 \\ 10\alpha & 10 \end{array} \right)$$

2. First ten poles from lower front list

$$b_{j,\ell} = \left(\begin{array}{cccc} -\frac{1}{\alpha} & -1 & -1 & -1 \\ -\frac{3}{\alpha} & -2 & -\frac{4}{3} & -\frac{3}{2} \\ -\frac{5}{\alpha} & -3 & -\frac{5}{3} & -2 \\ -\frac{7}{\alpha} & -4 & -2 & -\frac{5}{2} \\ -\frac{9}{\alpha} & -5 & -\frac{7}{3} & -3 \\ -\frac{11}{\alpha} & -6 & -\frac{8}{3} & -\frac{7}{2} \\ -\frac{13}{\alpha} & -7 & -3 & -4 \\ -\frac{15}{\alpha} & -8 & -\frac{10}{3} & -\frac{9}{2} \\ -\frac{17}{\alpha} & -9 & -\frac{11}{3} & -5 \\ -\frac{19}{\alpha} & -10 & -4 & -\frac{11}{2} \\ -\frac{21}{\alpha} & -11 & -\frac{13}{3} & -6 \end{array} \right)$$