From Generalized Lotka-Voltera (GLV):

Assuming has linear relationship with all species density:

GLV becomes:

If we assume a higher order dependency of on species density:

GLV becomes: