From Generalized Lotka-Voltera (GLV):

Assuming has linear relationship with all species density:

GLV becomes: