Analysis on the popular vote of the 2020 American federal election

Yena Joo, Woolim Kim, Guemin Kim

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Predictions on the proportions of voters for Donald Trump and Joe Biden in the 2020 US Presidential Election based on the voter survey responses.

Code and data supporting this analysis is available at: https://github.com/Guemin/Problem_Set_3

Model

As the 2020 presidential election of the United States approaches, people across the world are interested in to which candidate the vote of the US citizens will be concentrated, either to Donald Trump or to Joe Biden. Since the election outcome will also affect our community in Canada, we are going to analyze and predict the winner of the popular vote in the 2020 American federal election.

Using the survey and census data obtained from Democracy Fund + UCLA Nationscape and IPUMS USA, we are going to predict the popular vote outcome of the election. To be more specific, we are going to use two logistic regression models, one for each candidate, and employ a post-stratification technique[1] with the models. Then, we will predict the winner of the election in each state, using a post-stratification outcome and compare it with the popular vote prediction.

In the following sub-sections, we will describe the model specifics, the post-stratification calculation, and the result of the analysis.

Model specifics

As already mentioned, we will be using the logistic regression models[2] and post-stratification technique with R software to predict the proportions of voters who will vote for either Donald Trump or Joe Biden. Specifically, we will create two models, each for proportions of voters for Trump or Biden, using 6 different variables(age_group, gender, race, education, household_income , and state)[3].

Since our response variables, vote_Trump and vote_Biden, are binary(either 'vote for' or 'not vote/not sure'), the logistic regression model is a suitable model to be used. Logistic regression is a mathematical

[1] Post-stratification is a technique used in sample survey design to improve the quality of population estimates. In the post-stratification analysis, the population is partitioned into subgroups, and estimates are predicted within the subgroups. Then, the sum of the estimate times the respective population size in each group is calculated, and finally, it is divided by the sum of the total population size. Detailed procedures on post-stratification for our analysis will be shown in the following sub-sections.

[2] glm() function in the "lme4" package is used to make the logistic regression model.

[3] * age_group is divided into 4 different groups: "18-29 year olds", "30-44 year olds", "45-64 year olds", "65 years and older".
* gender indicates either "Male" or "Female".
* race is divided into 5 different categories: "White", "Black", "Native", "Asian", "Other".
* education is divided into 4 different categories: "Didn't graduate from high school", "High school graduate", "Some college or associate degree", "Bachelor's degree or higher".
* household income consists of 9 categories range from "Less than $14,999" to "$150,000 and over".
* state indicates abbreviated names of 52 states in the US.

model used to estimate the probability of an event occurring using binary data.
The logistic regression models we are using are:

$$log(\frac{p_i}{1-p_i}) = \beta_0 + \beta_1 x_{age\ group} + \beta_2 x_{gender} + \beta_3 x_{race} + \beta_4 x_{education} + \beta_5 x_{household\ income} + \beta_6 x_{state}$$

where $log(\frac{p_i}{1-p_i})$ represents log odds in each model, and p_i is the proportion of voters who will vote for Donald trump or Joe Biden. Similarly, β_0 represents the intercept, and $\beta_1, \ldots, \beta_6$ indicate the slope parameters of the model. (Detailed descriptions on the x variables can be found in the footnote[4]).

Model Diagnostics

With the logistic regression models we created above, we are going to study diagnostics of the models. First, we need to keep in mind that logistic regressions are well performed under the following assumptions:

1. Linearity between the log odds and the predictor variables
   (independent variables should be linearly related to the log odds)

2. Binary logistic regression requires the response variable to be binary.

3. Large sample size

4. Multicollinearity among predictors is not too high
   (predictor variables should be independent to each other)

In our models, we do not need to worry about the violation of the first assumption since all of our predictor variables are categorical; hence, the categorization of the independent variables is not necessary.
Similarly, since our response variables, vote_trump and vote_biden are binary, and the size of the survey data is large enough, we can confirm that the second and the third assumptions are also satisfied.

Now, we want to check if the multicollinearity among predictor variables is not too high. This can be done by calculating the variance inflation factor(VIF) for each predictor variable, which measures the amount of multicollinearity in a set of multiple regression variables; the bigger the VIF, the bigger the multicollinearity is. When the variance inflation factor is greater than 5, the corresponding predictor is said to be highly correlated with other predictors. Here are the values of variance inflation factors for predictors in each model:

Table 1: VIF models

model_trump_predictor	VIF	model_biden_predictor	VIF
age_group	1.210003	age_group	1.246368
gender	1.068826	gender	1.072452
race	1.240050	race	1.353103
education	1.477839	education	1.452881
household_income	1.555977	household_income	1.564889
state	1.468859	state	1.461147

As shown above, VIF values do not exceed 2 for both models for Trump and Biden, which suggest that there is no sign of multicollinearity among predictors. Therefore, it is safe to say that the last assumption is also satisfied.

[4]* $x_{age\ group}$ represents one of the four age groups that the respondent is in.
* x_{gender} indicates the gender of the respondent(either "Male" or "Female").
* x_{race} indicates the race ethnicity of the respondent.
* $x_{education}$ indicates the education attainment of the respondent.
* $x_{household\ income}$ indicates the total pre-tax income of the respondent's household.
* x_{state} indicates the state in which the respondent is located.

Model content

Prior to the modelings, we mutated variables in the survey data to create new variables that could be used in the analysis. Our response variables, vote_trump and vote_biden are also mutated from a variable named "vote_2020", which provides a name of a candidate that the respondent supports[5]. Also, the predictor variables, age_group, gender, race, education, household_income, and state are mutated in the data cleaning process so that the categories in each variable in the survey data match with those in the census data.
Since only those who are 18 years old or older are eligible to vote, we removed the observations obtained from the respondents who are younger than 18 years old in the data cleaning process. Similarly, we removed the observations of respondents who answered "No, I am not eligible to vote" as vote_intention, since their responses to vote_trump and vote_biden will not count in the actual election. Also, we removed people who are "less than 1 year old" or "90 (90+ in 1980 and 1990)" since their responses are unrealistic or not necessary in our analysis.

Post-Stratification

Using the log odds estimates, we are going to find vote_Trump and vote_Biden (the proportions of voters each for Donald Trump and Joe Biden) in every possible combination of categories in our predictor variables, age_group, gender, race, education, household income, and state.

In order to estimate the proportions of voters for both Donald Trump and Joe Biden, we are going to perform a post-stratification analysis. In order to use this technique, we need to subdivide the population having similar characteristics into cells. Hence, we are going to create a total of 55,325 cells based on different age groups, gender, race-ethnicity, education attainment, household income, and state.
Using the logistic regression models presented in the previous sub-section, we will estimate the proportions of voters in each cell for each candidate. Then, we will weight each estimate within each cell by the respective population size of the cell, and sum those values, and divide that by the entire population size. This process can also be described by the expression:

$$\hat{y}^{ps} \;=\; \frac{\sum N_j * \hat{y_j}}{\sum N_j}$$

where $\hat{y_j}$ is the estimate of the probability of voting for either Trump or Biden in each cell, and N_j is the population size of the j^{th} cell based off demographics.

reason for Choice of the variables…

Results

In the previous sub-sections, we have created the logistic Regression models on proportions of voters voting for Donald Trump and Joe Biden using 6 different variables: age_group, gender, race, education, household_income, and state. Based on the post-stratification analysis we made, our estimation of the proportion of voters voting for Donald Trump is 0.433 (43.3%) and Joe Biden to be 0.394(39.4%). From the result of our estimations, We can predict that Donald Trump is more likely to win the popular vote in the 2020 American federal election.

```
## # A tibble: 70 x 5
##    term                                  estimate std.error statistic  p.value
##    <chr>                                    <dbl>     <dbl>     <dbl>    <dbl>
##  1 (Intercept)                             -0.707    0.741     -0.954 3.40e- 1
##  2 as.factor(age_group)30-44 year olds      0.575    0.0950     6.05  1.43e- 9
##  3 as.factor(age_group)45-64 year olds      0.743    0.0940     7.91  2.59e-15
```

[5] vote_trump is 1 when vote_2020 is "Donald Trump", and 0 otherwise; vote_biden is 1 when vote_2020 is "Joe Biden", and 0 otherwise.

```
##   4 as.factor(age_group)65 years and older     0.782    0.108      7.25  4.10e-13
##   5 as.factor(gender)Male                      0.422    0.0612     6.90  5.25e-12
##   6 as.factor(race)Black                      -1.42     0.209     -6.79  1.12e-11
##   7 as.factor(race)Native                      0.483    0.285      1.70  8.99e- 2
##   8 as.factor(race)Other                      -0.132    0.200     -0.661 5.08e- 1
##   9 as.factor(race)White                       0.589    0.160      3.68  2.37e- 4
##  10 as.factor(education)Didn't graduate fr~    0.357    0.119      3.01  2.61e- 3
## # ... with 60 more rows
```

```
## # A tibble: 70 x 5
##    term                                 estimate std.error statistic    p.value
##    <chr>                                   <dbl>     <dbl>     <dbl>      <dbl>
##  1 (Intercept)                          -0.418      0.839    -0.498      6.18e-1
##  2 as.factor(age_group)30-44 year olds  -0.200      0.0856   -2.34       1.93e-2
##  3 as.factor(age_group)45-64 year olds  -0.287      0.0855   -3.35       8.01e-4
##  4 as.factor(age_group)65 years and old~ -0.125     0.101    -1.24       2.14e-1
##  5 as.factor(gender)Male                -0.302      0.0592   -5.11       3.27e-7
##  6 as.factor(race)Black                  0.999      0.166     6.03       1.67e-9
##  7 as.factor(race)Native                -0.442      0.278    -1.59       1.12e-1
##  8 as.factor(race)Other                  0.00339    0.173     0.0196     9.84e-1
##  9 as.factor(race)White                 -0.449      0.143    -3.14       1.66e-3
## 10 as.factor(education)Didn't graduate ~ -0.667     0.114    -5.86       4.61e-9
## # ... with 60 more rows
```

Table 2: Comparison of predicted estimate between Trump and Biden

total_predict_trump	total_predict_biden
0.4334444	0.3944298

In the summary model for Trump(Figure n), "45-64 year-olds" and "65 years and older" have relatively higher estimates(0.743 and 0.782) which mean for every one-unit increase in the predictor variable, we expect an increase in the log odds, which makes Trump more likely to get voted. Similarly, estimates in household_income show that log-odds get lower for people who have relatively low household income ($15,000 to $24,999). Black race significantly shows low estimates, -1.42192, which lowers the log odds by a significant amount.

(Figure n) For Biden, as opposed to Trump, shows a high estimate in the black race (0.999153), but has a low estimate in a native race(-0.441602). Also, younger people are more likely to vote, individuals with high income ($150,000 or more) lowers the log odds(-0.046616), but overall well distributed.

- individuals with household_income "less than $14,999" are more likely to vote for Biden over Trump (due to Biden's election promises for lower-income people?)

- Individuals with a household income " $100,000 to $149,999" or "$150,000 or more" show a higher probability of voting for Trump over Biden.

Discussion

Here you will summarize the previous sections and discuss conclusions drawn from the results. Make sure to elaborate and connect your analysis to the goal of the study.

Using the 2020 survey data and 2018 census data obtained from Democracy Fund + UCLA Nationscape and IPUMS USA, we have predicted the popular vote outcome of the 2020 presidential election in the USA. In the "Model Specifics" section, logistic regression models are used to predict the candidate who is more likely to win the popular vote in the election. Explanatory variables used for the logistic regression models are age_group, gender, race, education, household_income, and state. There is a possibility of having omitted variable bias[6] and measurement error bias, because people tend to hide their political orientation.

Then, by using the post stratification technique, the census data is partitioned into 55,325 cells - based on the 6 variables used in the logistic Regression models - and the proportions of voters for each candidate are estimated for each cell. Using the estimates in each cell, the total proportions of voters for both Donald Trump and Joe Biden, $\hat{y}^{ps}$ are measured to predict the winner of the popular vote.

Furthermore, we grouped the cell estimates by states and predicted the candidate who is expected to win in each state. The result shows that Trump has greater probabilities to win in 31 states, whereas Biden has higher probabilities to win in 20 states; Trump is ahead of Biden by 11 states.

The result of the popular vote shows that the estimated value $\hat{y}^{ps}$ for the proportion of voters voting for Joe Biden is 39.4% and for Donald Trump is 43.34%.

To sum up, the overall results from the post-stratification analysis suggest that Donald Trump is more likely to win the popular vote in the 2020 US presidential election. However, this is just an estimation based on the provided data sets which do not provide enough information required for predicting the winner of the electoral vote. Historically, in 2016, Hillary Clinton won in the popular vote but lost the election, because Trump won the electoral College. Therefore, winning the popular vote does not determine the next president of USA.

Weaknesses

improvement

One of the weaknesses in our analysis is regarding the omitted variables. In the data cleaning process, some of the variables were removed from the data sets prior to the modeling, because either the census data or the survey data did not include the particular variables. If there were any important variables among the omitted ones, that could affect the vote outcome and there might also exist an omitted variable bias in our models. (The omitted variables should be correlated with the dependent variable and with the explanatory variables included in the model).

Since the Census data used in the analysis is the 2018 data, it might not reflect the population in 2020 or to predict the election outcome most accurately. For example, in our analysis, those who are not eligible to vote(back in 2018) were omitted from the data set, however, they could be eligible to vote in the 2020 election. Hence, if the 2020 census data was available, it should be more suitable for our analysis.

Another weakness we should note is that our prediction on the winner of the popular vote could not match with the winner of the electoral college. Even if a candidate wins in the public vote, it is the result of the electoral college that determines the next president of USA. Therefore, analyzing the winner of the popular vote is not the most accurate way to predict the winner of the presidential election.

Next Steps

The analysis does not include the possible effect of other factors - such as an individual's Health insurance state - on the vote result. Analyzing the vote outcome focusing on the election promise would be a more realistic and reasonable prediction of the election. Also, 2016 census data is used for the analysis so it does not reflect the most accurate population. With the 2020 census data, we could estimate the proportion of voting for each candidate by the factors that are closely related to the election promises such as health care, market industry, etc.

Also, throughout the analysis, popular vote and a brief idea of the electoral vote (group the estimate by states, and compare the probability to determine who wins for each state), but did not use the actual election

[6]* explanation of omitted variable bias is described in "Weakness section"

method that is used in the states. Following the procedure of the proper electoral vote, using more accurate data of the electoral colleges would make a huge difference in the analysis.

- Create a visualization of the results to view the groups of the voting estimates at once.

- In our future analysis, we can try to analyze the multilevel regression models using Bayes coding techniques.

- We can compare our prediction and the result of the actual 2020 presidential election.
  (something about comparing with the actual election results and do a post-hoc analysis (or at least a survey) of how to better improve estimation in future elections.)

References (MLA8)

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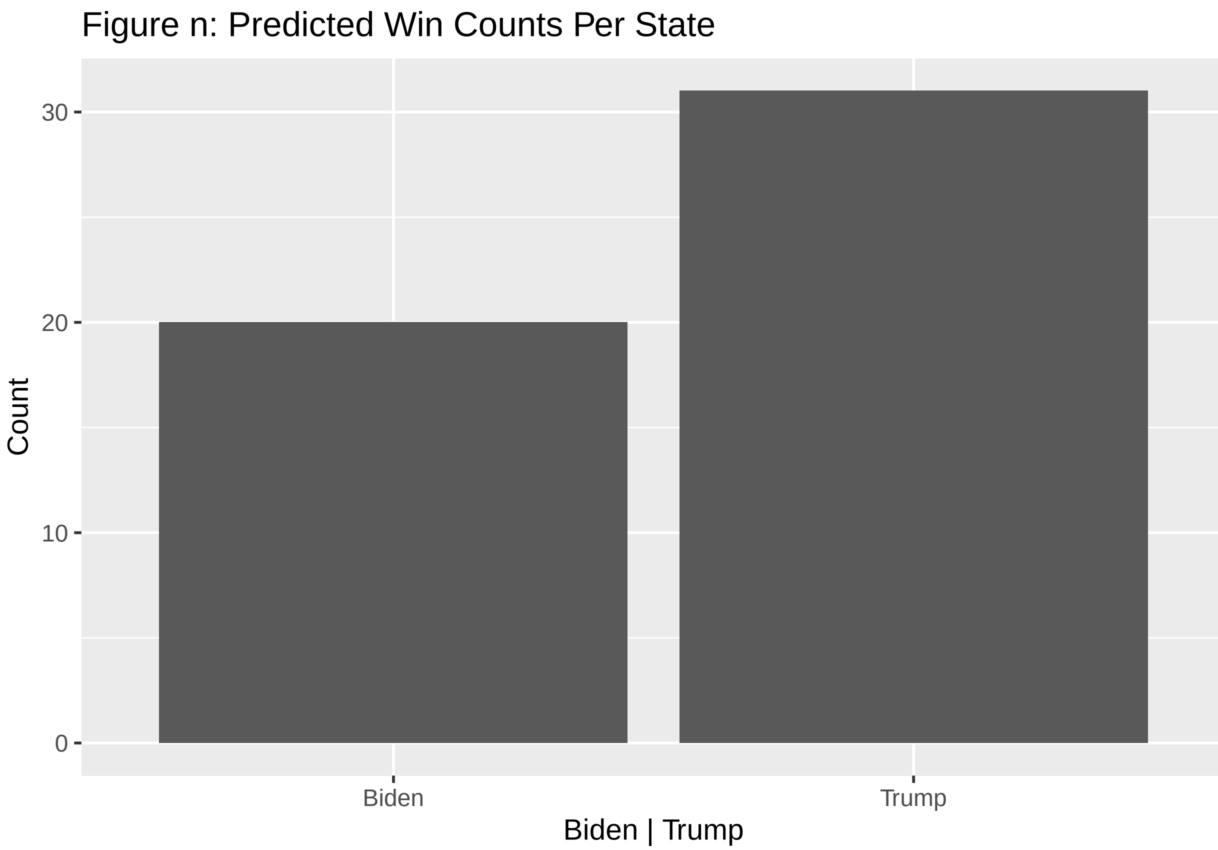
Electoral vote kinda stuff

The presidential election actually uses the electoral college vote. There are 538 electors in the electoral college, divided among each state. Electors vote based on the results of the popular vote in their respective states. Since there is no information given about the electoral colleges, we are instead going to see how we can predict using a similar method. For each state, we will compare Trump and Biden's $\hat{y}^{ps}$ value, and whoever has the bigger value wins in the state. This way, we would have a better idea who would win, rather than predict using just a popular vote.



The histogram above shows the predicted win counts per state. Trump is expected to have a higher proportion of being elected in 31 states, and Biden has a higher proportion of voters voting for him in 20 states, which makes Trump the winner of the presidential election. Both popular vote and electoral vote shows same prediction where Trump wins the election.

Appendix

state	predict_trump2
AK	0.6178175
AL	0.5294578
AR	0.5690489
AZ	0.4970620
CA	0.3500102
CO	0.4748248
CT	0.2840064
DC	0.2715509
DE	0.3901171
FL	0.4677497
GA	0.4716816
HI	0.3371692
IA	0.4501696
ID	0.6617140
IL	0.4152228
IN	0.4497127
KS	0.5724607
KY	0.4997506
LA	0.4574786
MA	0.2894075
MD	0.3519287
ME	0.4062306
MI	0.4074363
MN	0.4807777
MO	0.4489350
MS	0.4849136
MT	0.5407824
NC	0.4647314
ND	0.5234047
NE	0.4228730
NH	0.4164238
NJ	0.4045109
NM	0.2288712
NV	0.5159548
NY	0.3888962
OH	0.4457807
OK	0.4921180
OR	0.4084833
PA	0.4706141
RI	0.3574909
SC	0.5061444
SD	0.5185028
TN	0.5126872
TX	0.5087421
UT	0.4055765
VA	0.3846518
VT	0.1026603
WA	0.3766525
WI	0.3970139
WV	0.5386586
WY	0.1878584

state	predict_biden2
AK	0.2121776
AL	0.3429311
AR	0.2163157
AZ	0.3532261
CA	0.4605909
CO	0.3723088
CT	0.5343268
DC	0.7314580
DE	0.5308874
FL	0.3841190
GA	0.3827232
HI	0.5260513
IA	0.3894466
ID	0.2276048
IL	0.3984838
IN	0.3483643
KS	0.2903427
KY	0.4122667
LA	0.4197140
MA	0.5138926
MD	0.4938823
ME	0.4861133
MI	0.4562030
MN	0.4625594
MO	0.3787824
MS	0.3758363
MT	0.3513251
NC	0.4126773
ND	0.1747900
NE	0.3367801
NH	0.4753414
NJ	0.4240766
NM	0.5074545
NV	0.3375036
NY	0.4355101
OH	0.3743578
OK	0.2217403
OR	0.4259771
PA	0.3096477
RI	0.4515775
SC	0.2786692
SD	0.3387865
TN	0.2784533
TX	0.3048833
UT	0.2632457
VA	0.4476426
VT	0.7455384
WA	0.4615358
WI	0.4124047
WV	0.3194931
WY	0.2659662

Table 3: Figure n

household_income	predict_trump	household_income	predict_biden
$100,000 to $149,999	0.4788905	$100,000 to $149,999	0.3644576
$15,000 to $24,999	0.3819243	$15,000 to $24,999	0.4089684
$150,000 and over	0.5013108	$150,000 and over	0.3746106
$25,000 to $34,999	0.3917869	$25,000 to $34,999	0.3918452
$35,000 to $44,999	0.4036812	$35,000 to $44,999	0.4117412
$45,000 to $54,999	0.4363749	$45,000 to $54,999	0.3898337
$55,000 to $74,999	0.4219549	$55,000 to $74,999	0.4162607
$75,000 to $99,999	0.4191757	$75,000 to $99,999	0.4305907
Less than $14,999	0.3219549	Less than $14,999	0.3930797