

## Unified Channel Charge Density Expression

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(3.1.1a)

$$Q_{chsub0} = Q_0 \exp\left(\frac{V_{gs} - V_{th}}{n v_t}\right)$$

where  $Q_0$  is

(3.1.1b)

$$Q_0 = \sqrt{\frac{q \epsilon_{si} N_{ch}}{2 \phi_s}} v_t \exp\left(-\frac{V_{off}}{n v_t}\right)$$

(3.1.2)

$$Q_{chs0} = C_{ox}(V_{gs} - V_{th})$$

In both Eqs. (3.1.1a) and (3.1.2), the parameters  $Q_{chsub0}$  and  $Q_{chs0}$  are the channel charge densities at the source for very small  $V_d$ s. To form a unified expression, an effective  $(V_{gs} - V_{th})$  function named  $V_{gsteff}$  is introduced to describe the channel charge characteristics from subthreshold to strong inversion

(3.1.3)

$$V_{gsteff} = \frac{2 n v_t \ln \left[ 1 + \exp\left(\frac{V_{gs} - V_{th}}{2 n v_t}\right) \right]}{1 + 2 n C_{ox} \sqrt{\frac{2 \Phi_s}{q \epsilon_{si} N_{ch}}} \exp\left(-\frac{V_{gs} - V_{th} - 2 V_{off}}{2 n v_t}\right)}$$

The unified channel charge density at the source end for both subthreshold and inversion region can therefore be written as

(3.1.4)

$$Q_{chs0} = C_{ox} V_{gsteff}$$

Figures 3-1 and 3-2 show the smoothness of Eq. (3.1.4) from subthreshold to strong inversion regions. The  $V_{gsteff}$  expression will be used again in subsequent sections of this chapter to model the drain current.